

**Ferroelectric and strain-tuned MoSe₂/Bi₂O₂Se van der Waals
heterostructure with band alignment evolution**

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Supporting Information

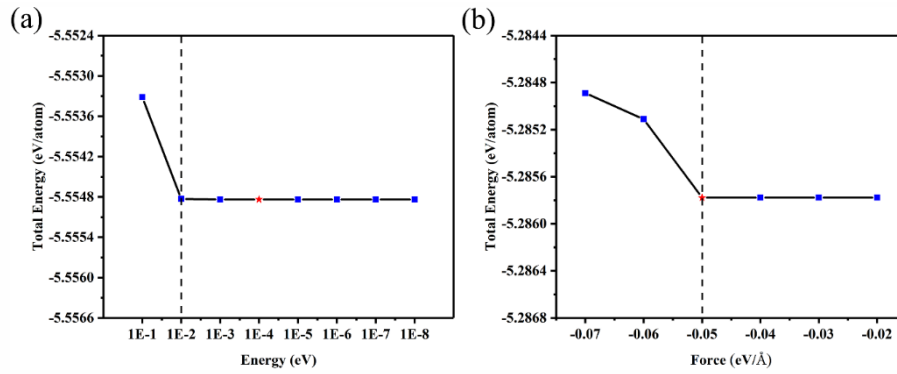


Fig. S1. Convergence tests for energy (a) and force (b), respectively.

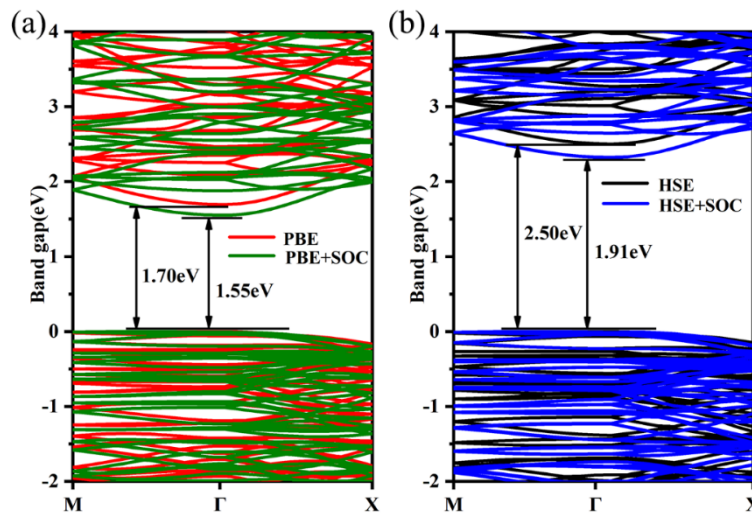


Fig.S2. Band structures of the $\text{Bi}_2\text{O}_2\text{Se}$ monolayer (zipper surface model with 3×4 supercell) with (a) PBE, PBE+SOC and (b) HSE, HSE+SOC approaches.

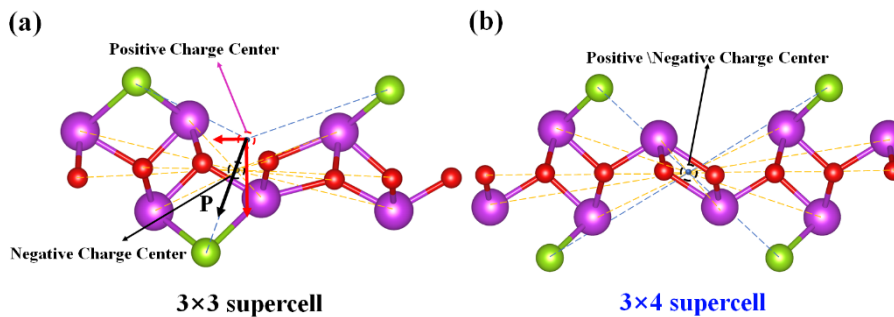


Fig.S3. Positive and negative charge centers of 3×3 (a) and 3×4 (b) $\text{Bi}_2\text{O}_2\text{Se}$ monolayers.

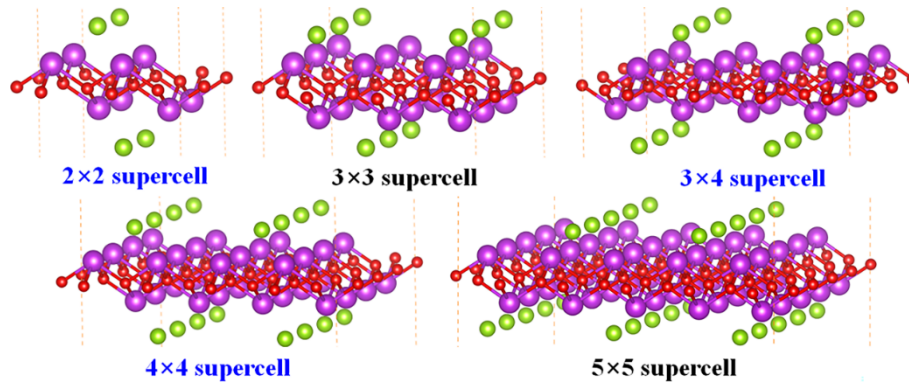


Fig.S4. Crystal structures of the $\text{Bi}_2\text{O}_2\text{Se}$ monolayer with 2×2 , 3×3 , 3×4 , 4×4 and 5×5 supercells.

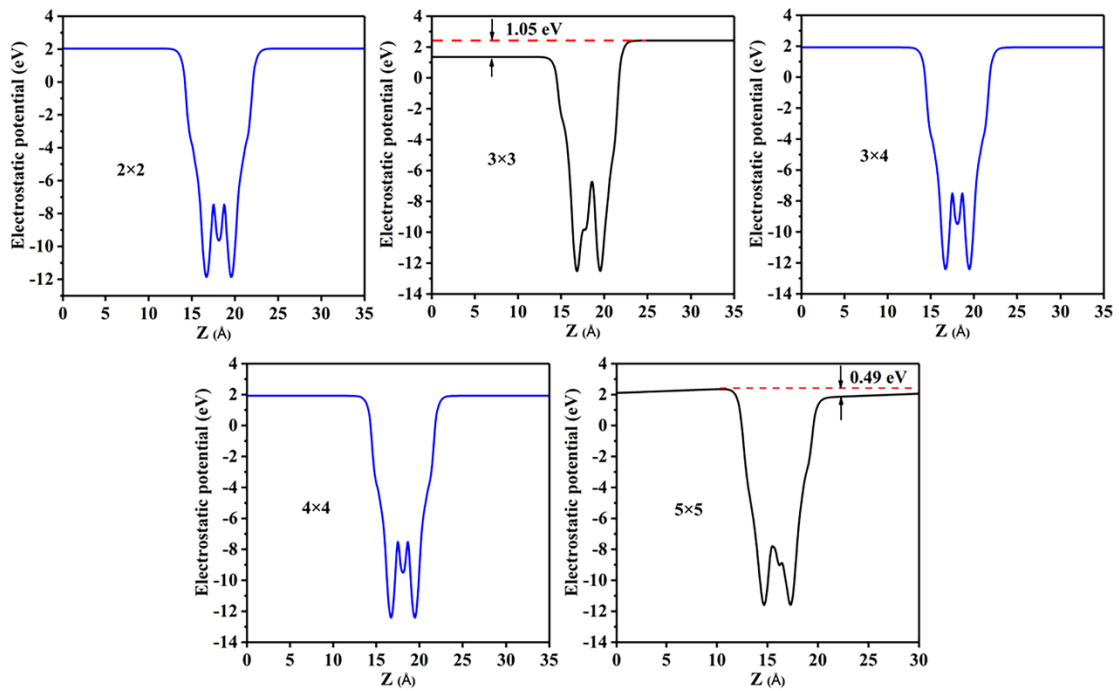


Fig.S5. Electrostatic potentials of the $\text{Bi}_2\text{O}_2\text{Se}$ monolayer with 2×2 , 3×3 , 3×4 , 4×4 and 5×5 supercells.

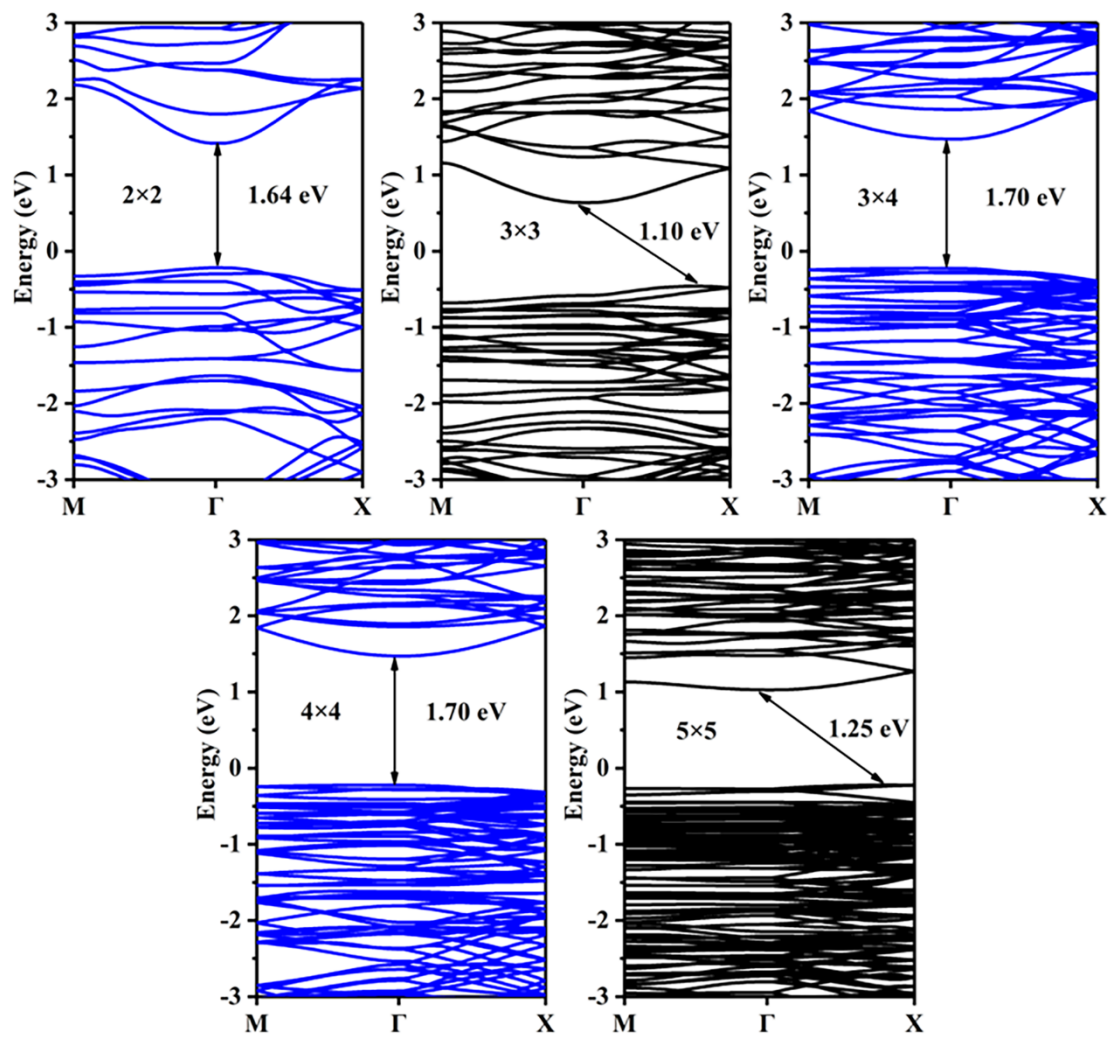


Fig.S6. Band structures of the $\text{Bi}_2\text{O}_2\text{Se}$ monolayer with 2×2 , 3×3 , 3×4 , 4×4 and 5×5 supercells. The Fermi level is set to zero.

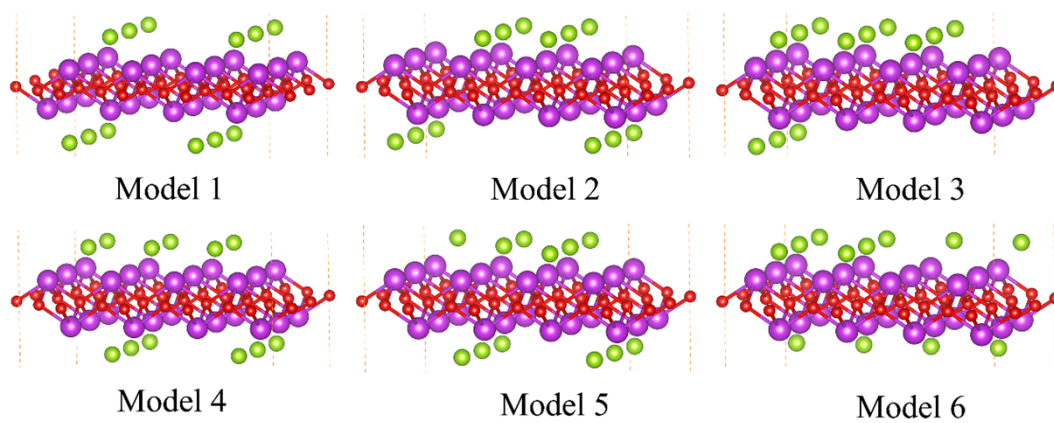


Fig.S7. Crystal structures of the considered $\text{Bi}_2\text{O}_2\text{Se}$ monolayer models.

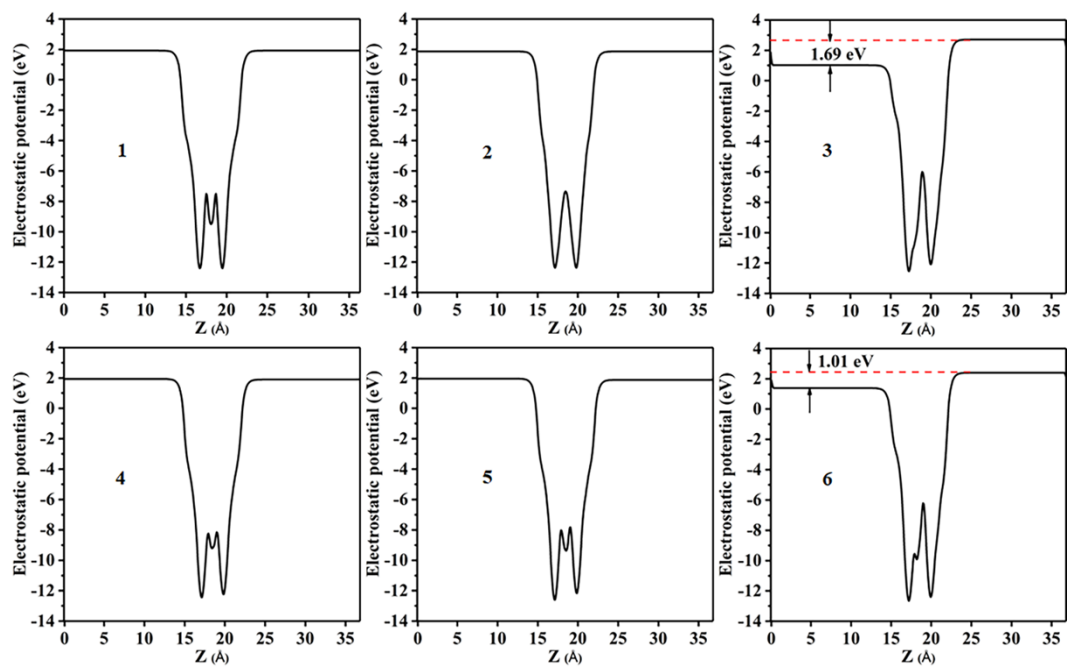


Fig.S8. Electrostatic potentials of the considered $\text{Bi}_2\text{O}_2\text{Se}$ monolayer models.

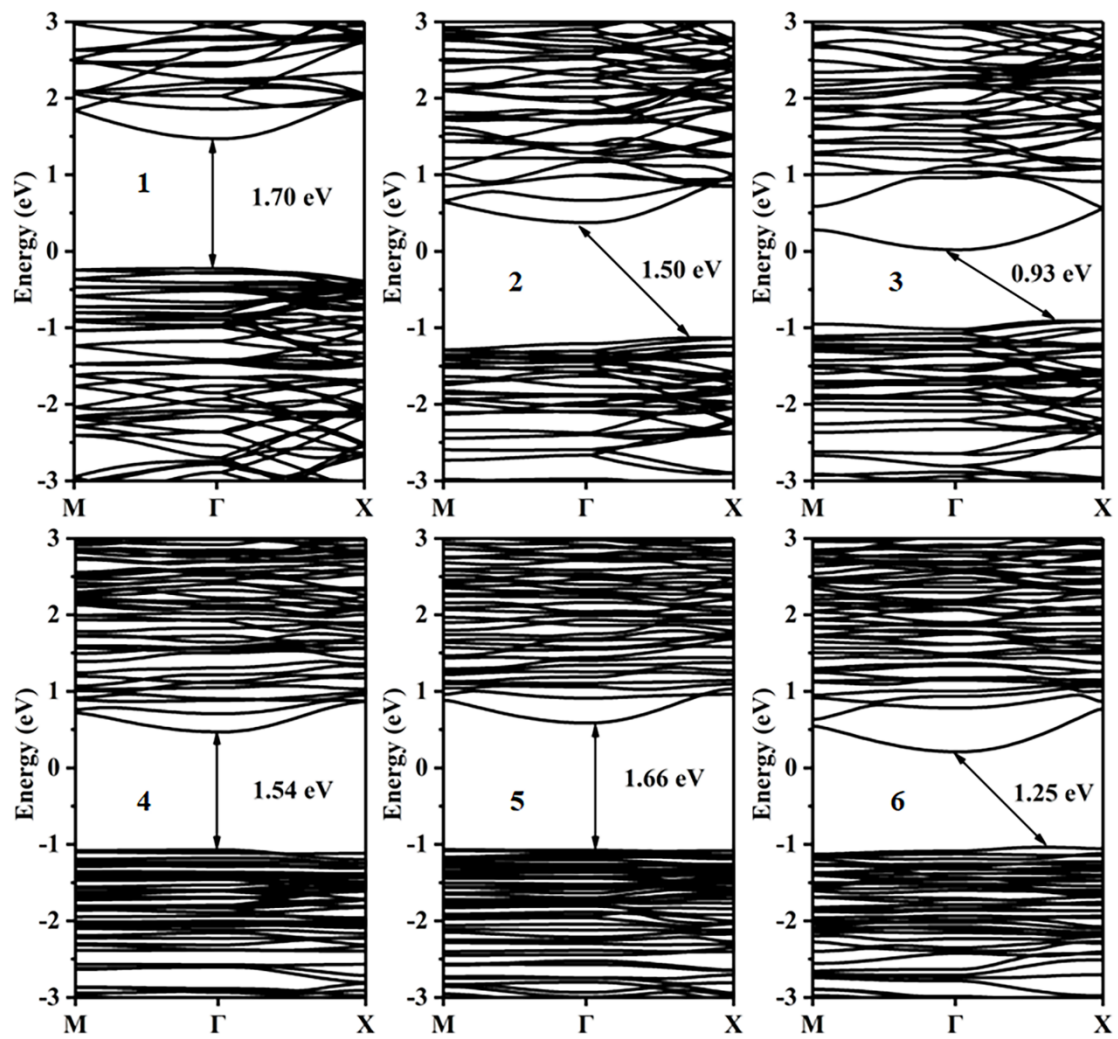


Fig.S9. Band structures of the considered Bi₂O₂Se monolayer models. The Fermi level is set to zero.

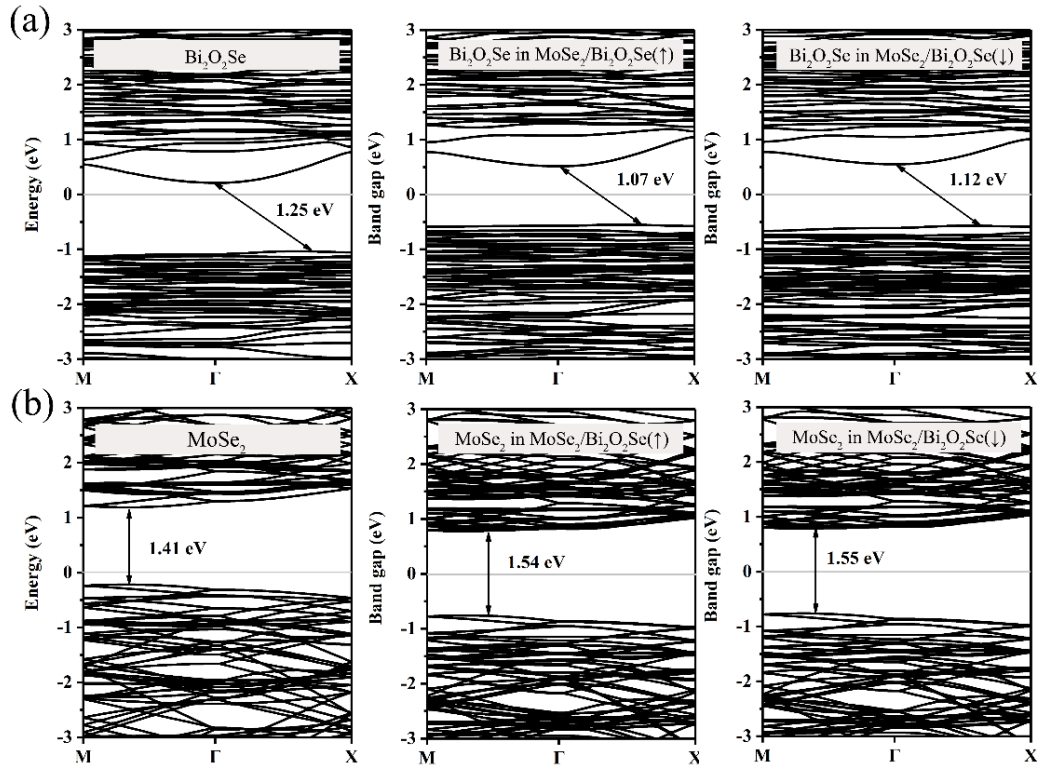


Fig. S10. Band structures of $\text{Bi}_2\text{O}_2\text{Se}$ and those in $\text{MoSe}_2/\text{Bi}_2\text{O}_2\text{Se}(\uparrow)$ and $\text{MoSe}_2/\text{Bi}_2\text{O}_2\text{Se}(\downarrow)$ (a), as well as MoSe_2 and those in $\text{MoSe}_2/\text{Bi}_2\text{O}_2\text{Se}(\uparrow)$ and $\text{MoSe}_2/\text{Bi}_2\text{O}_2\text{Se}(\downarrow)$ (b).

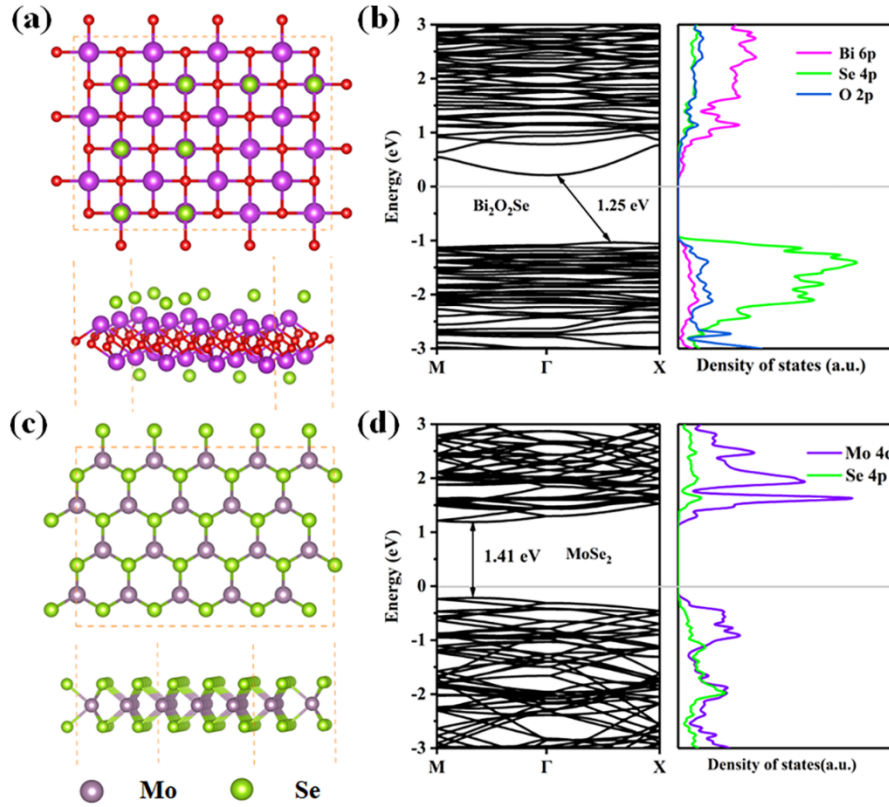


Fig.S11. Top- and side-view of the crystal structures, band structures and projected density of states of (a, b) $\text{Bi}_2\text{O}_2\text{Se}$ and (c, d) MoSe_2 . The Fermi level is set to zero.

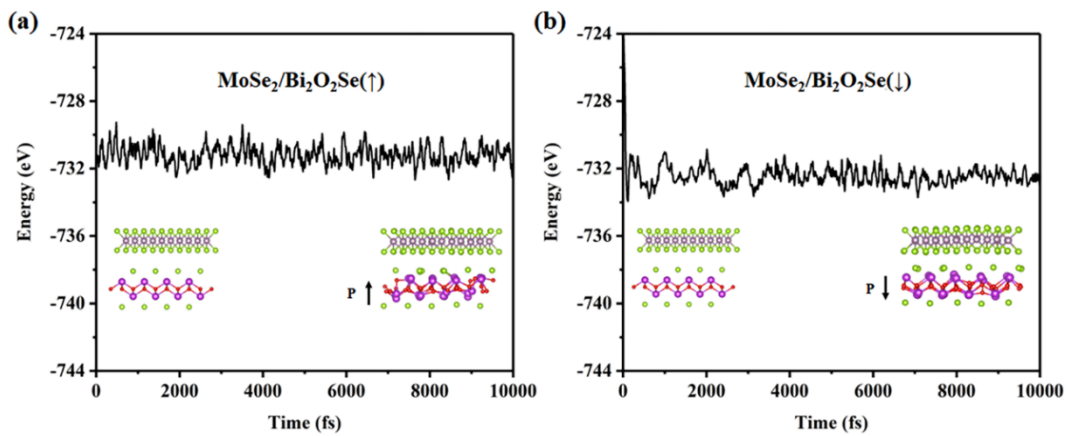


Fig.S12. Variation of the total energies of (a) $\text{MoSe}_2/\text{Bi}_2\text{O}_2\text{Se}(\uparrow)$ and (b) $\text{MoSe}_2/\text{Bi}_2\text{O}_2\text{Se}(\downarrow)$ at 300 K. The structures before and after the evolution of 10 ps are also shown.

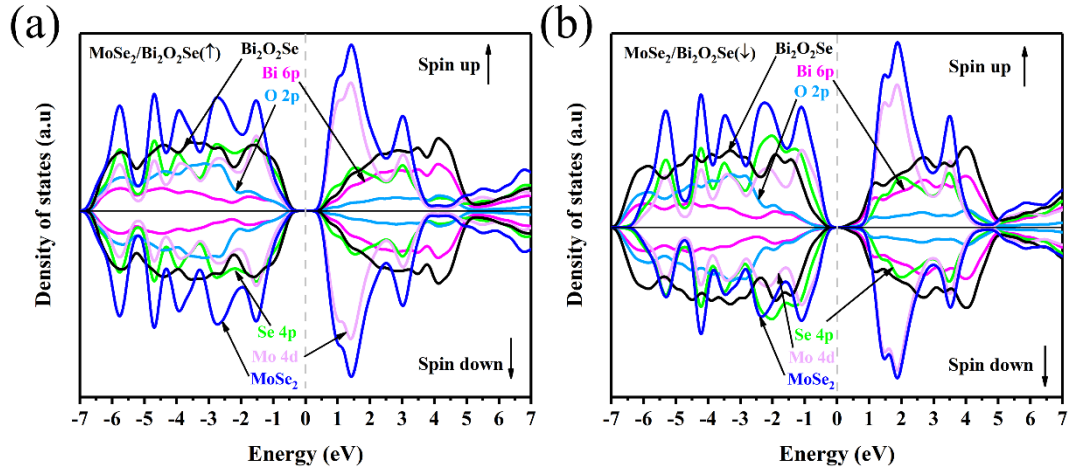


Fig. S13. Spin density of states of MoSe₂/Bi₂O₂Se (↑) and MoSe₂/Bi₂O₂Se (↓).

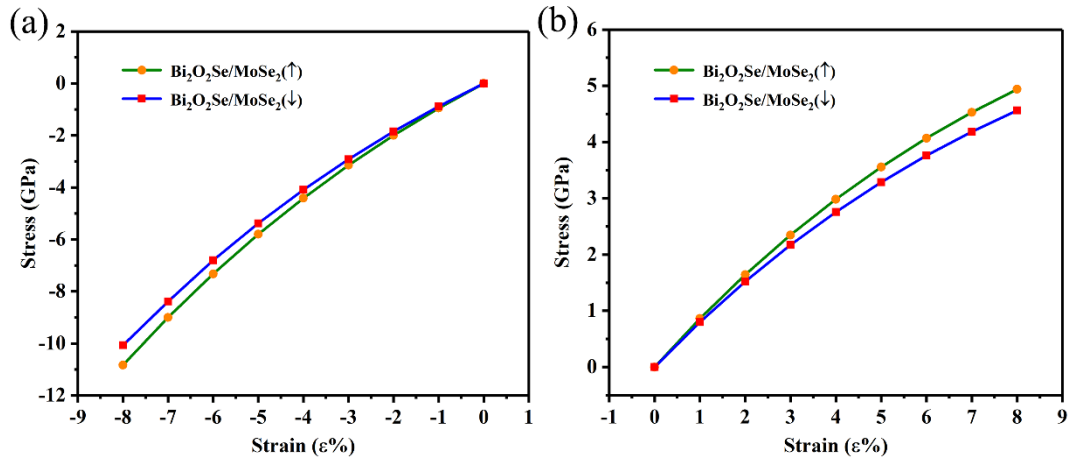


Fig. S14. The curve of stress vs. strain of the heterostructure under tensile strain (a) and compressive strain (b).

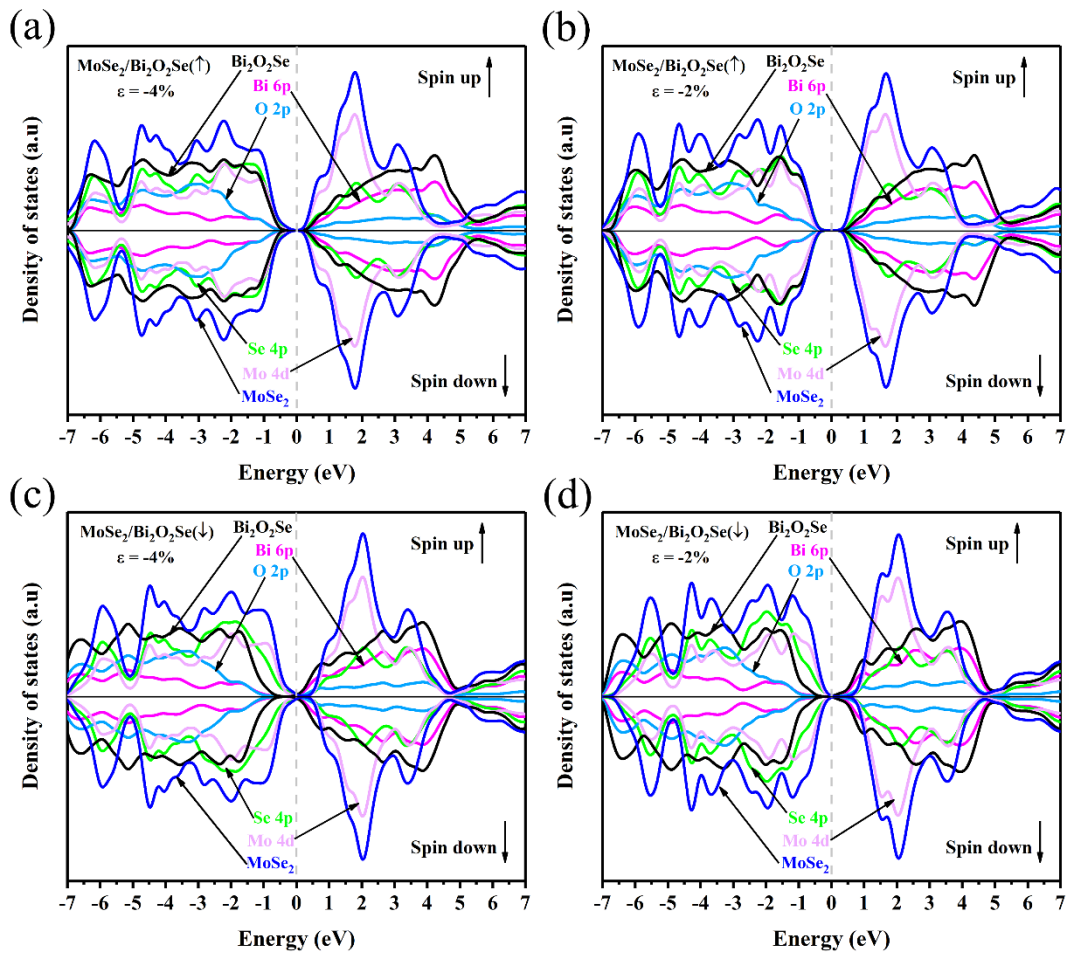


Fig. S15. Spin density of states of MoSe₂/Bi₂O₂Se (↑) under the in-plane strain of (a) $\varepsilon = -4\%$ and (b) $\varepsilon = -2\%$, and of MoSe₂/Bi₂O₂Se (↓) under the in-plane strain of (c) $\varepsilon = -4\%$ and (d) $\varepsilon = -2\%$.

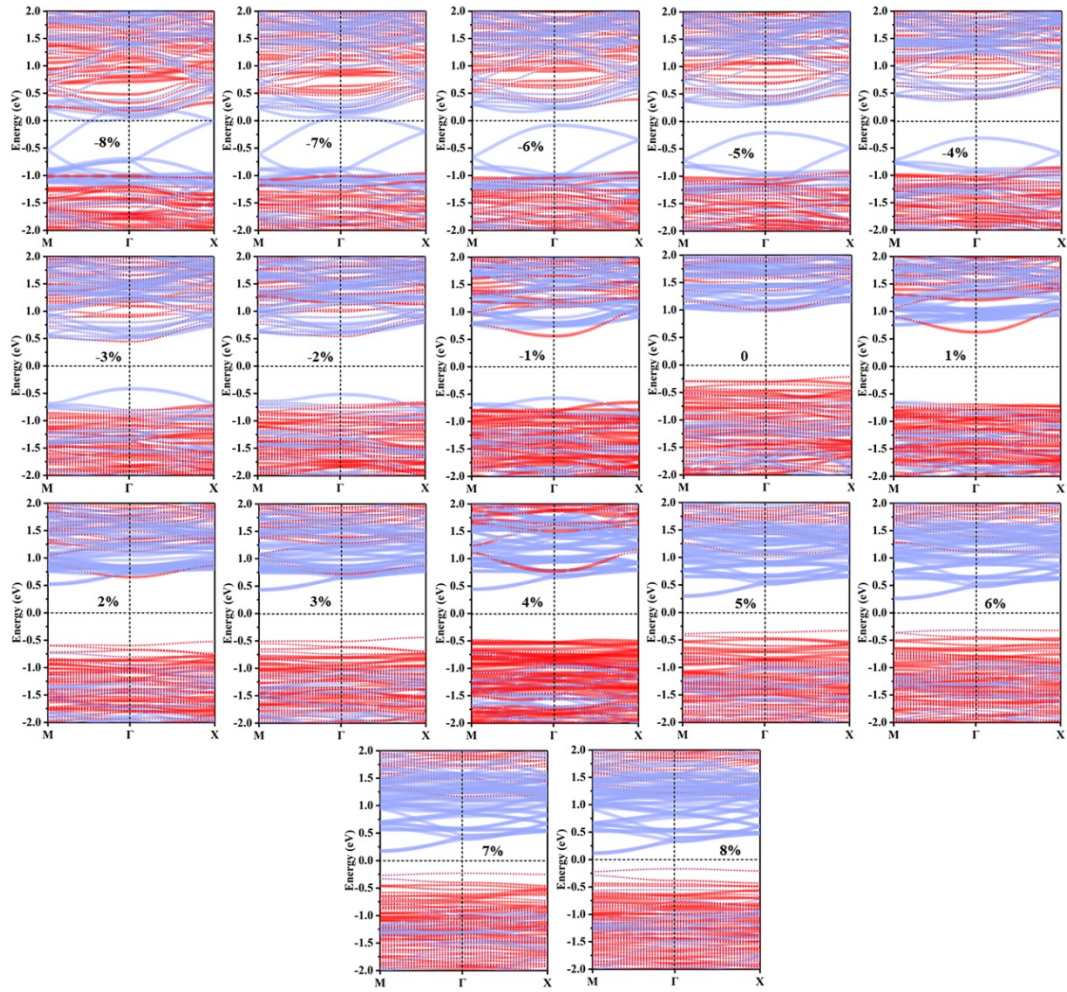


Fig. S16. Projected band structures of $\text{MoSe}_2/\text{Bi}_2\text{O}_2\text{Se}(\uparrow)$ under different in-plane strain. The Fermi level set to be zero. Red and blue dots represent the contributions of $\text{Bi}_2\text{O}_2\text{Se}$ and MoSe_2 layers, respectively.

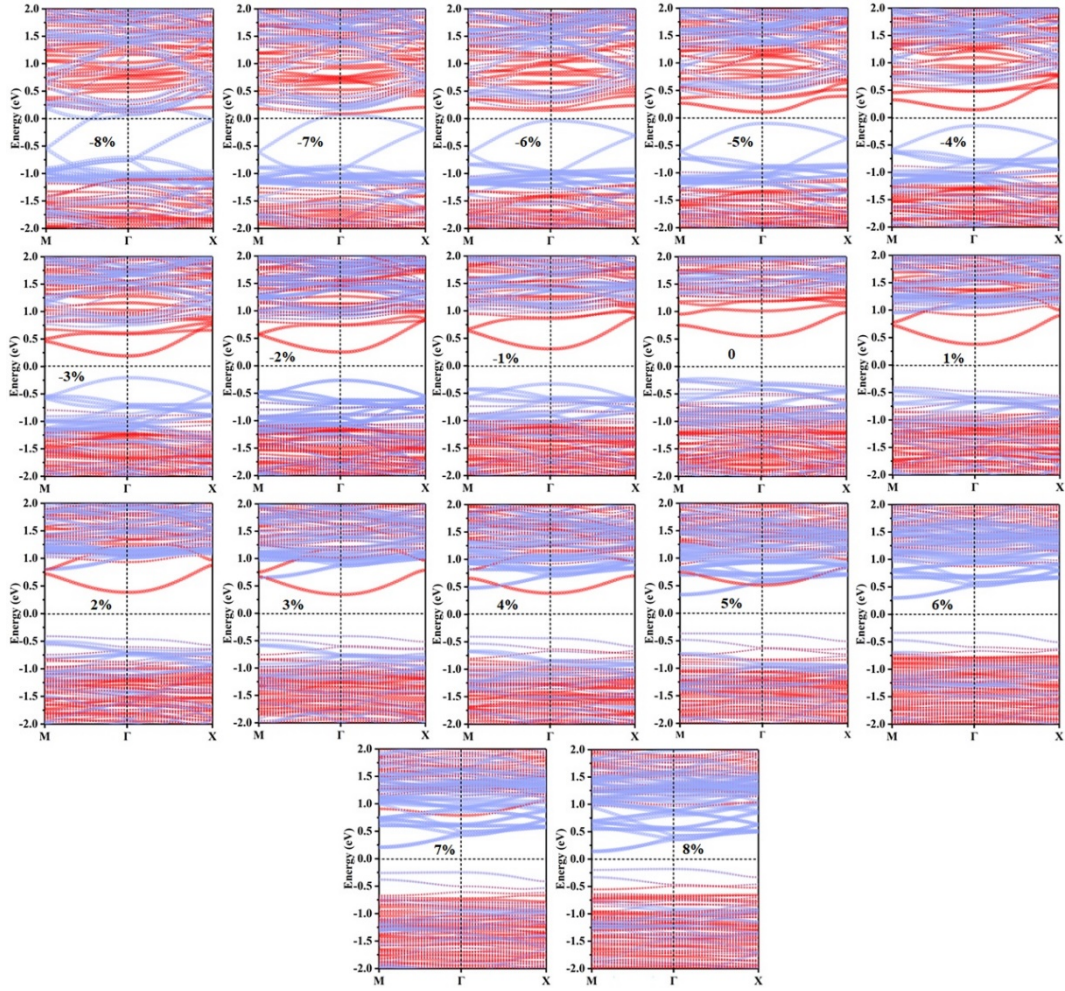


Fig. S17. Projected band structures of $\text{MoSe}_2/\text{Bi}_2\text{O}_2\text{Se}(\downarrow)$ under different in-plane strain. The Fermi level set to be zero. Red and blue dots represent the contributions of $\text{Bi}_2\text{O}_2\text{Se}$ and MoSe_2 layers, respectively.

Table S1. Formation energies (eV/atom) of 6 different Bi₂O₂Se monolayer models

Formation energy (eV/atom)	
Model 1	-0.912
Model 2	-0.891
Model 3	-0.882
Model 4	-0.897
Model 5	-0.901
Model 6	-0.895

Table S2. Binding energies E_b of the considered Bi₂O₂Se monolayer models in Fig. S7.

E_b (emV/Å ²)	
Model 1	157.43
Model 2	164.33
Model 3	167.40
Model 4	162.77
Model 5	160.95
Model 6	163.07

Table S3. Bond lengths (Å) of Bi-Se in Bi₂O₂Se and Mo-Se in MoSe₂ as a function of biaxial strain for MoSe₂/Bi₂O₂Se(↑) and MoSe₂/Bi₂O₂Se(↓)

	MoSe ₂ /Bi ₂ O ₂ Se(↑)		MoSe ₂ /Bi ₂ O ₂ Se(↓)	
	d_{Bi-Se}	d_{Mo-Se}	d_{Bi-Se}	d_{Mo-Se}
-8%	2.748	2.475	2.697	2.485
-6%	2.758	2.473	2.826	2.514
-4%	2.863	2.493	2.735	2.496
-2%	2.990	2.496	2.808	2.512
0%	3.019	2.518	2.883	2.529
2%	3.012	2.574	2.905	2.527
4%	3.173	2.600	2.975	2.540
6%	3.128	2.630	3.001	2.551
8%	3.335	2.657	3.178	2.572

