

## Supporting Information

### Investigation of Sodium-ion Transport Mechanism and Elastic Properties of Double Anti-perovskite $\text{Na}_3\text{S}_{0.5}\text{O}_{0.5}\text{I}$

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**Table S1. Relative energies of different conformations of Na<sub>3</sub>S<sub>0.5</sub>O<sub>0.5</sub>I.**

Conformation	Relative energy (eV)
1	0.13
2	0.17
3	0.09
4	0.14
5	<b>0.00</b>

**Table S2.  $E_{defect}$  of different intrinsic defect configurations of Na<sub>3</sub>OI and****Na<sub>3</sub>S<sub>0.5</sub>O<sub>0.5</sub>I.**

Material	Defect	$E_{defect}$ (eV)		
		NN	2NN	3NN
Na <sub>3</sub> OI	NaI Schottky	<b>1.65</b>	1.70	1.81
	Na <sub>2</sub> O Schottky	1.81	<b>1.72</b>	3.58
	Na Frenkel	<b>2.56</b>	2.62	2.71
Na <sub>3</sub> S <sub>0.5</sub> O <sub>0.5</sub> I	NaI Schottky	<b>1.28</b>	1.29	1.40
	Na <sub>2</sub> O Schottky	<b>2.33</b>	2.42	4.44
	Na <sub>2</sub> S Schottky	<b>1.15</b>	1.16	to NN
	Na Frenkel	<b>1.63</b>	1.75	1.76

**Table S3.  $E_{solution}$  of different doping configurations of Na<sub>3</sub>OI and Na<sub>3</sub>S<sub>0.5</sub>O<sub>0.5</sub>I.**

Material	Defect	$E_{solution}$ (eV)				
		NN	2NN	3NN	4NN	5NN
Na <sub>3</sub> OI	$Mg_{Na}^{\bullet}$	-1.34	<b>-1.58</b>	-1.11	-1.04	-1.05
	$Ca_{Na}^{\bullet}$	<b>-0.46</b>	-0.43	-0.21	-0.15	-0.17
	$Sr_{Na}^{\bullet}$	<b>0.04</b>	0.26	0.34	0.41	0.37

	$Ba_{Na}^{\bullet}$	<b>0.72</b>	1.15	1.15	1.22	1.15
$Na_3S_{0.5}O_{0.5}I$	$Mg_{Na}^{\bullet}$	-0.98	<b>-1.17</b>	-0.68	-0.67	-0.67
	$Ca_{Na}^{\bullet}$	-0.37	<b>-0.45</b>	-0.06	-0.06	-0.06
	$Sr_{Na}^{\bullet}$	-0.05	<b>-0.08</b>	0.30	0.31	0.27
	$Ba_{Na}^{\bullet}$	<b>0.26</b>	0.43	0.88	0.89	0.81

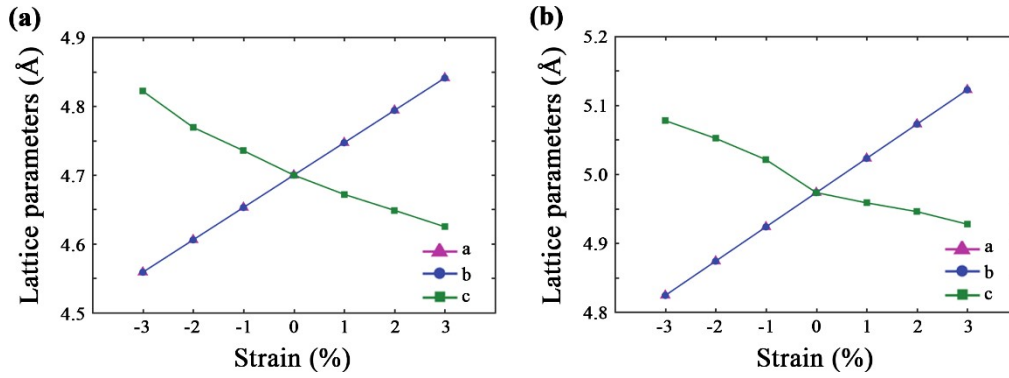
**Table S4.**  $E_b$  along different paths in the lowest energy doping configuration.

Material	Defect	$E_b$ (eV)				
		Path 1	Path 2	Path 3	Path 4	Path 5
$Na_3OI$	$Mg_{Na}^{\bullet}$	0.58	0.63			
	$Ca_{Na}^{\bullet}$	0.62	0.50	0.56	0.66	0.57
	$Sr_{Na}^{\bullet}$	0.67	0.63	0.55	0.68	0.59
	$Ba_{Na}^{\bullet}$	0.76	0.77	0.56	0.75	0.64
$Na_3S_{0.5}O_{0.5}I$	$Mg_{Na}^{\bullet}$	0.32	0.60			
	$Ca_{Na}^{\bullet}$	0.28	0.65			
	$Sr_{Na}^{\bullet}$	0.21	0.64			
	$Ba_{Na}^{\bullet}$	0.92	0.28	0.55	0.49	0.75

**Table S5. Ionic conductivities and activation energies of  $Na_3S_{0.5}O_{0.5}I$ ,  $Na_3OI$  and other  $Na^+$  conducting materials.**

Material	Ionic conductivity	activation energy	References
$Na_{10}GeP_2S_{12}$	$4.7 \times 10^{-3} \text{ S cm}^{-1}$	0.2	[58]

$\text{Na}_{3+x}\text{Si}_x\text{P}_{1-x}\text{S}_4$	$1.66 \times 10^{-3} \text{ S cm}^{-1}$	0.24	[59]
$\text{Na}_{3+x}\text{Ge}_x\text{P}_{1-x}\text{S}_4$	$5.4 \times 10^{-4} \text{ S cm}^{-1}$	0.28	[59]
$\text{Na}_{3+x}\text{Sn}_x\text{P}_{1-x}\text{S}_4$	$1.07 \times 10^{-2} \text{ S cm}^{-1}$	0.17	[59]
$\text{Na}_{3.1}\text{Zr}_{1.95}\text{Mg}_{0.05}\text{Si}_2\text{PO}_{12}$	$3.5 \times 10^{-3} \text{ S cm}^{-1}$	0.25	[60]
$\text{Na}_{11}\text{Sn}_2\text{PS}_{12}$	$1.4 \times 10^{-3} \text{ S cm}^{-1}$	0.25	[61]
$\text{Na}_{10}\text{SnP}_2\text{S}_{12}$	$4 \times 10^{-4} \text{ S cm}^{-1}$	0.356	[62]
$\text{Na}_3\text{S}_{0.5}\text{O}_{0.5}\text{I}$	$1.2 \times 10^{-3} \text{ S cm}^{-1}$	0.20	Our work
$\text{Na}_3\text{OI}$	$1.5 \times 10^{-6} \text{ S cm}^{-1}$	0.42	Our work



**Fig. S1. Structural parameters of (a) Na<sub>3</sub>OI and (b) Na<sub>3</sub>S<sub>0.5</sub>O<sub>0.5</sub>I under various biaxial strains in the a-b plane.**