

**Supplemental Material for “Non-volatile control of topological
phase transition in an asymmetric ferroelectric In₂Te₂S
monolayer”**

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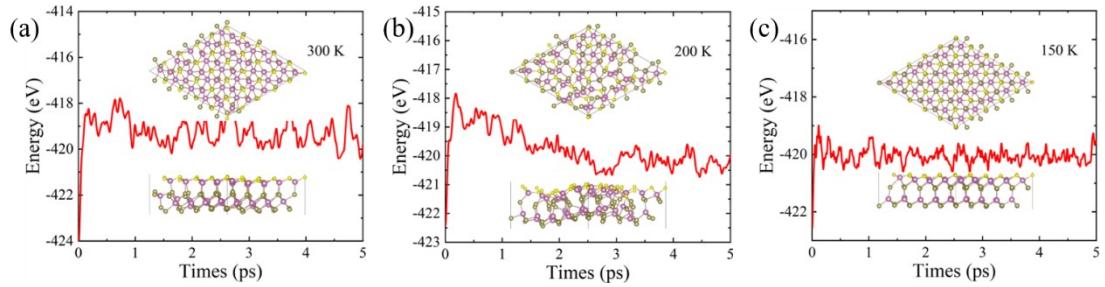


Fig. S1. (a) Snapshots of the atomic configuration at 5 ps and total energy fluctuations for (a) $\text{In}_2\text{Te}_2\text{S}$ monolayer under $P(\uparrow)$ state at 300 K (b) $\text{In}_2\text{Te}_2\text{S}$ monolayer under $P(\downarrow)$ state at 200 K, (c) $\text{In}_2\text{Te}_2\text{S}$ monolayer under $P(\downarrow)$ state at 150 K.

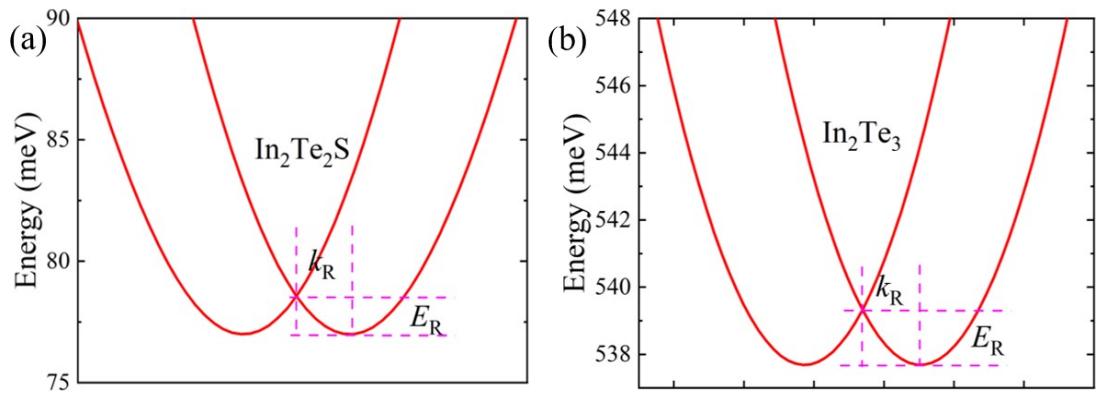


Fig. S2. The Rashba splitting for $\text{In}_2\text{Te}_2\text{S}$ and In_2Te_3 monolayers.

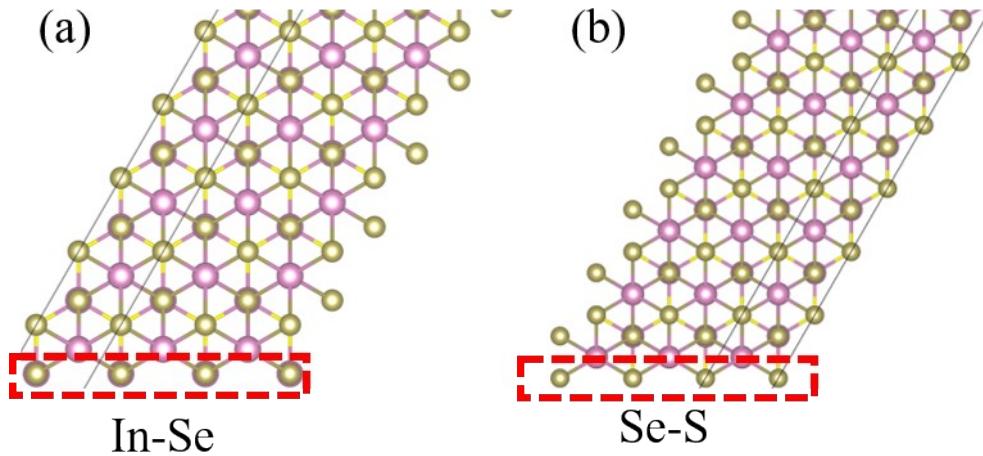


Fig. S3. The crystal structure of different terminal.

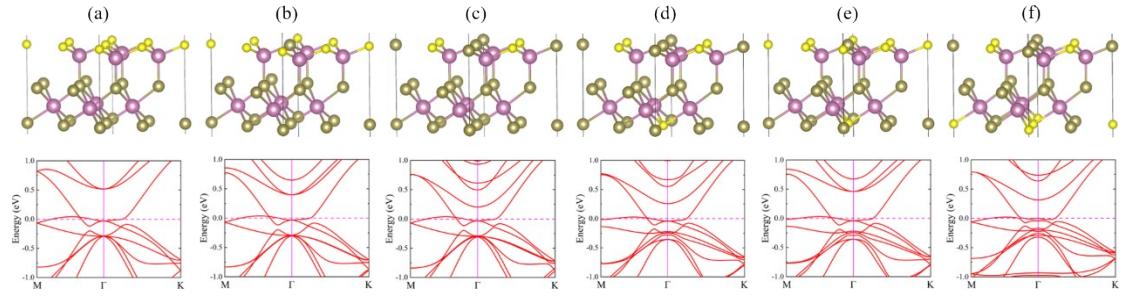


Fig. S4. The calculated band structures for the mixed structure.

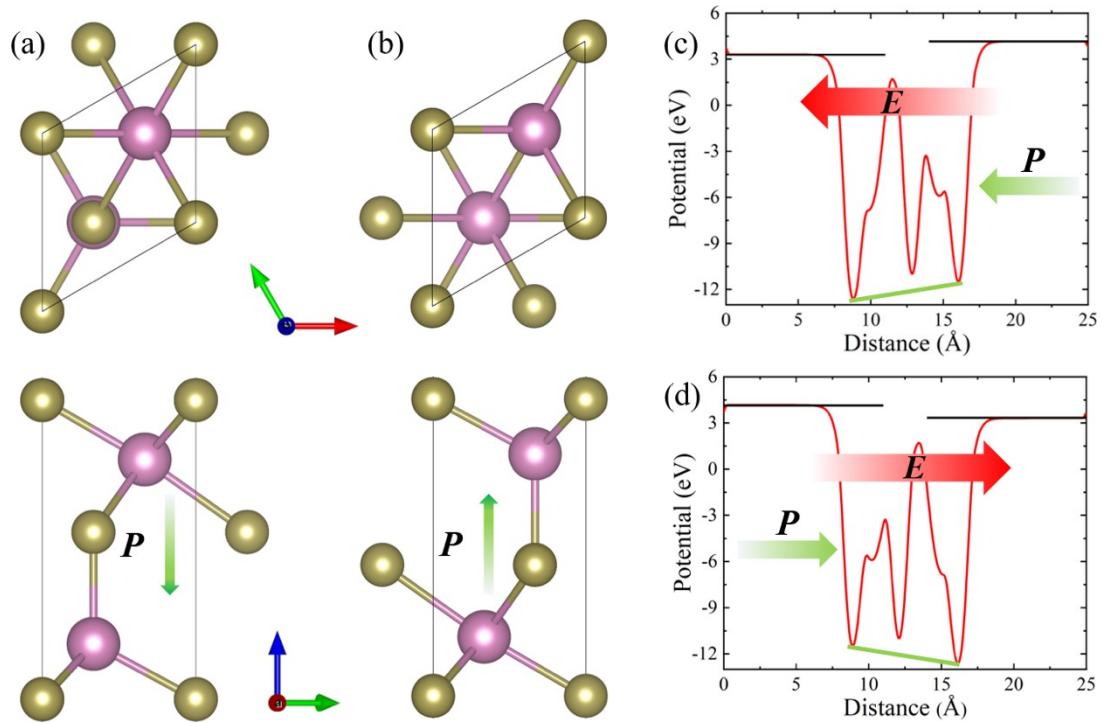


Fig. S5. Crystal structure of In_2Te_3 monolayer under $P\downarrow$ (a) and $P\uparrow$ (b). Plane-averaged potential of In_2Te_3 monolayer along its normal, z. (c) $P\downarrow$. (d) $P\uparrow$.

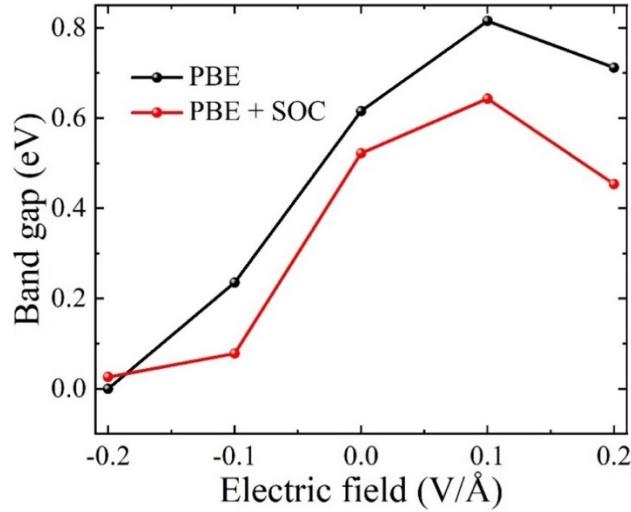


Fig. S6. The calculated band gap as a functional of external electric filed for In_2Te_3 monolayer.

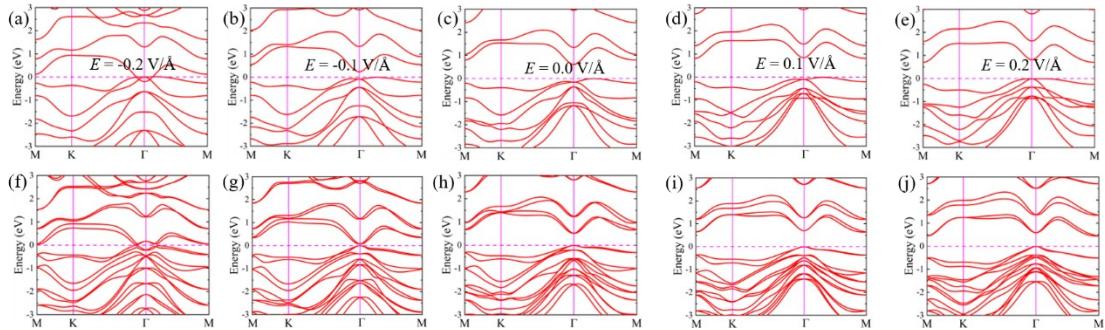


Fig. S7. The calculated band structure as a functional of external electric filed for In_2Te_3 monolayer.
(a)-(e) PBE method without SOC. (f)-(j) PBE method with SOC

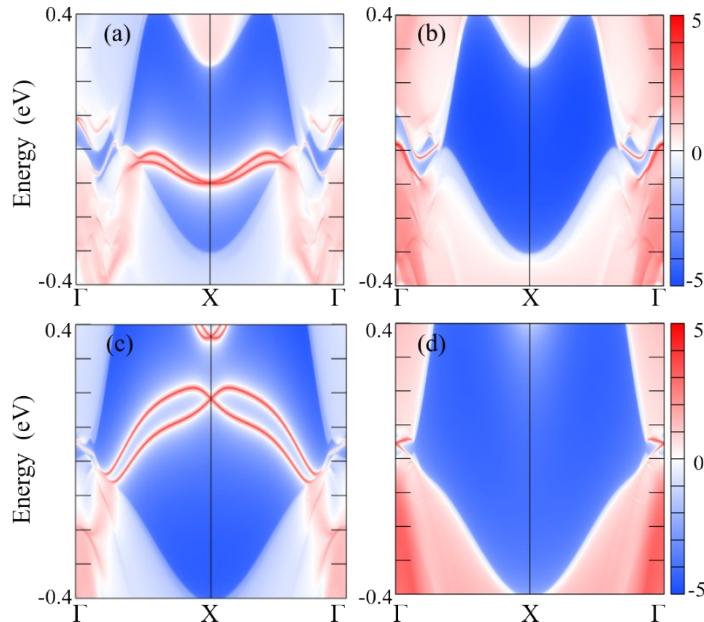


Fig. S8. Topological left (a) and right (b) edge states for $\text{In}_2\text{Te}_2\text{S}$ monolayer under $P\uparrow$ state at $E = -0.1 \text{ V}/\text{\AA}$. Topological left (c) and right (d) edge states for $\text{In}_2\text{Te}_2\text{S}$ monolayer under $P\uparrow$ state at $E = 0.1 \text{ V}/\text{\AA}$.

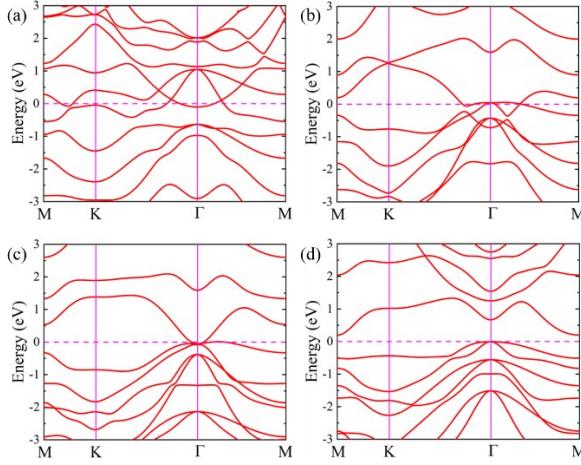


Fig. S9. Band structure of $\text{In}_2\text{Te}_2\text{S}$ monolayer under different electric field. (a) -0.5 V/ Å; (b) -0.1 V/ Å; (c) 0.1 V/ Å; (d) 0.5 V/ Å.

Table SI. The calculated lattice parameters for $\text{In}_2\text{Te}_2\text{S}$ and In_2Te_3 monolayers. The 1, 2, 3, 4, and 5 represent the S (Te), In, Te, In, and Te atoms.

	a (Å)	h (Å)	1-2	2-3	3-4	4-5
$\text{In}_2\text{Te}_2\text{S-up}$	4.227	7.187	2.682	3.068	2.750	2.847
$\text{In}_2\text{Te}_2\text{S-down}$	4.224	7.182	2.626	2.795	3.056	2.901
$\text{In}_2\text{Te}_3\text{-up}$	4.406	7.403	2.938	3.112	2.767	2.890
$\text{In}_2\text{Te}_3\text{-down}$	4.406	7.403	2.890	2.767	3.112	2.938

Table SII. The calculated charge for different atom with Bader method.

	Te	In	Te	In	S
$\text{In}_2\text{Te}_2\text{S-up}$	6.405	2.288	6.486	2.071	6.750
$\text{In}_2\text{Te}_2\text{S-down}$	6.443	2.371	6.477	2.000	6.707
$\text{In}_2\text{Te}_3\text{-up}$	6.413	2.368	6.480	2.284	6.453
$\text{In}_2\text{Te}_3\text{-down}$	6.453	2.284	6.480	2.368	6.413