Supporting Information

Morphological study of bicontinuous concentric lamellar silica synthesized at atmospheric pressure and its application as an internal micro-reflector in dye-sensitized solar cells

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Figure S1. FESEM images and particle-size distributions of *bcl* silica that were synthesized at different times: (a) 6 h, (b) 8 h, (c) 12 h, (d) 18 h, and (e) 72 h.



Figure S2. FESEM and binary images of *bcl* silica samples that were synthesized at different times: (a) 6 h, (b) 8 h, (c) 12 h, (d) 18 h, and (e) 72 h.



Figure S3. Kubelka-Munk model's light path. (a) The reflectance factor for a single sheet over a black background, R_0 and (b) the reflectance when the specimen is infinitely thick, R_{∞} .



Figure S4. Refractive index (*n*) as a function of wavelength for TiO₂ crystals (ordinary ray),¹ TiO₂ nanoparticles,² α -Quartz,^{3,4} and fused silica.^{5,6}



Figure S5. (a) The effective refractive index for *bcl* silica synthesized for different times compared with non-porous silica. (b) Comparison of the effective refractive indexes between the nano-spherical titania and *bcl* silica systems. The effective refractive index of nano-spherical titania film varied from the closed-packed system of hcp lattice with a filling factor of 0.74 (74% TiO₂) to a 3D random contact network of packed spheres with the threshold of 0.31 (31% TiO₂).^{7,8} The green dotted line shows the visible light range. The effective refractive indexes are calculated using Bruggeman effective medium approximation by mixing the refractive index of pure silica/SiO₂⁹ or titania/TiO₂ with the void in different volume fractions. The optical constants/refractive index of TiO₂ was obtained from the J.A. Woollam Co. materials database.



Figure S6. Microscope images of SiO₂ microbeads.

D	Gamma	Iterations	Simulation results	AL/Atotal (%)
5	5	10000		49.256
10	5	10000		49.654
15	5	10000		49.388
20	5	10000		49.654
25	5	10000		49.633

Table S1. The quantization results of the Cahn-Hilliard spinodal decomposition model (variation in D values)

D	Gamma	Iterations	Simulation results	AL/Atotal (%)
10	3	10000		49.170
10	6	10000		49.348
10	9	10000		50.251
10	12	10000		48.939
10	14	10000		49.591

Table S2. The quantization results of the Cahn-Hilliard spinodal decomposition model (variation in gamma values)

D	Gamma	Iterations	Simulation results	AL/Atotal (%)
10	3	10000		49.170
10	3	20000		49.594
10	3	30000		49.010
10	3	40000		49.832
10	3	50000		49.559
10	3	60000		49.331

Table S3. The quantization results of the Cahn-Hilliard spinodal decomposition model (variation in the number of iterations)

Synthesis	FESEM images before thresholding			Graph	<h></h>
time (n)	1	2	3		
6	倚			0.06 0.06 0.05 0.05 0.05 0.05 0.05 0.05	5.213
8	A.			0.03 0.02 0.04 0.04 0.05 0 0.05 0 0.05 000 0000000000	5.963
12				0.00 0.00	5.575
18	SRE	S.S.		6 00 6 0 6	6.486
72					6.440

Table S4. The average calculation of Shannon entropy of the FESEM image before thresholding

Additional References:

- 1 J. R. DeVore, Refractive indices of rutile and sphalerite, *Journal of the Optical Society of Amerika*, 1951, **41**, 416–419.
- 2 I. Bodurov, I. Vlaeva, A. Viraneva, T. Yovcheva and S. Sainov, Modified design of a laser refractometer, *Nanoscience & Nanotechnology*, 2016, **16**, 31–33.
- 3 T. Radhakrishnan, in *Proceedings of the Indian Academy of Sciences-Section A*, Springer India, 1947, vol. 25, p. 260.
- 4 T. Radhakrishnan, in *Proceedings of the Indian Academy of Sciences-section A*, Springer India, 1951, vol. 33, p. 22.
- 5 I. H. Malitson, Interspecimen comparison of the refractive index of fused silica, *Journal of the Optical Society of Amerika*, 1965, **55**, 1205–1209.
- 6 C. Z. Tan, Determination of refractive index of silica glass for infrared wavelengths by IR spectroscopy, *Journal of Non-Crystalline Solids*, 1998, **223**, 158–163.
- 7 M. J. Powell, Site percolation in randomly packed spheres, *Phys. Rev. B*, 1979, **20**, 4194–4198.

- 8 R. M. Ziff and S. Torquato, Percolation of disordered jammed sphere packings, *J. Phys. A: Math. Theor.*, 2017, **50**, 085001.
- 9 E. D. Palik, *Handbook of Optical Constants of Solids*, Academic Press, 1st edn., 1991, vol. 2.