

# Supplemental Information of “Electronic band structure change with structural transition of buckled $\text{Au}_2\text{X}$ monolayers induced by strain”

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## S1. SUPPLEMENTAL INFORMATION

In Sec. S1 A, figures and tables about  $\text{Au}_2\text{S}$  are shown. We show the convergence of energy and lattice length for the number of k-mesh and energy cutoff in Table S1 and S2. The Table S3 shows the function types for CB2, CB1, VB1 and VB2. The electronic band structures and DOSs of  $\text{Au}_2\text{S}$  and their decomposed results are shown in Fig. S1 - S3. The Figs. S4 and S5 show molecular orbitals of VB2, VB1, CB1, and CB2 at the  $\Gamma$  point.

In Sec. S1 B, figures and tables about  $\text{Au}_2\text{X}$  ( $\text{X}=\text{S}, \text{Se}, \text{Te}, \text{Si}, \text{Ge}$ ) and  $\text{Au}_4\text{SSe}$  are shown. The phonon bands are shown in Figs. S6 and S7. The energy curves, electronic band structures, and optical conductivities are shown in Figs. S8 - S11.

### A. $\text{Au}_2\text{S}$ monolayers

TABLE S1: Convergence of energy for the number of k-mesh and energy cutoff  $E_{\text{cut}}$ .

k-mesh	$E_{\text{cut}}$ [Ry]	Energy [a.u.]		
		$\eta\text{-Au}_2\text{S}$	$\theta\text{-Au}_2\text{S}$	$E_\theta - E_\eta$
$5 \times 5 \times 1$	240	-443.3502	-443.3477	0.0026
$7 \times 7 \times 1$	240	-443.3505	-443.3484	0.0021
$5 \times 5 \times 1$	320	-443.3511	-443.3483	0.0028
$7 \times 7 \times 1$	320	-443.3514	-443.3491	0.0023
$9 \times 9 \times 1$	600	-443.3534	-443.3516	0.0018

TABLE S2: Convergence of lattice length for the number of k-mesh and energy cutoff  $E_{\text{cut}}$ .

k-mesh	$E_{\text{cut}}$ [Ry]	Lattice length [ $\text{\AA}$ ]	
		$\eta\text{-Au}_2\text{S}$	$\theta\text{-Au}_2\text{S}$
$5 \times 5 \times 1$	240	5.805	5.610
$9 \times 9 \times 1$	600	5.803	5.605

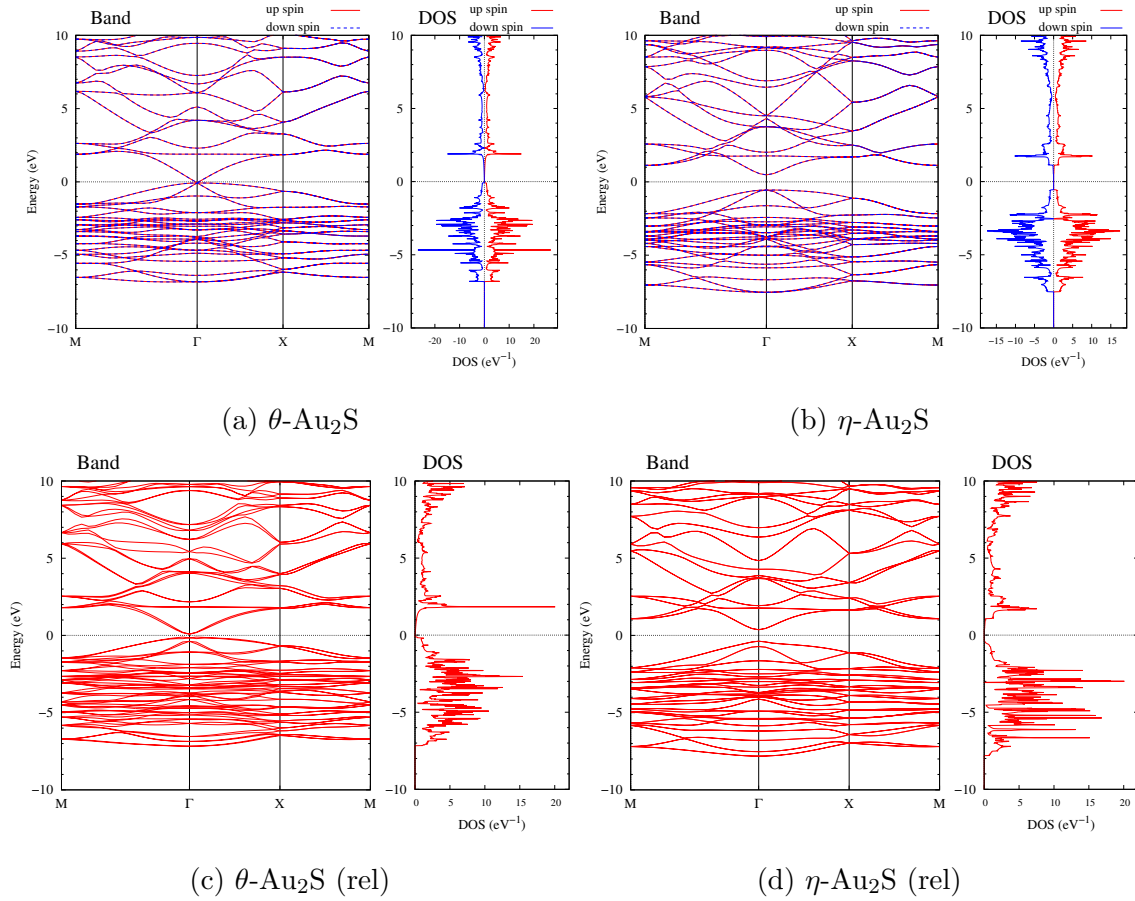


FIG. S1: Electronic band structures and DOSs of  $\text{Au}_2\text{S}$  monolayers based on non-relativistic DFT (a,b) and that with spin-orbit coupling term (c,d). Non-relativistic DFT calculations also include relativistic effect in the pseudopotentials. The  $y$  axis is taken so that the Fermi energy is zero.

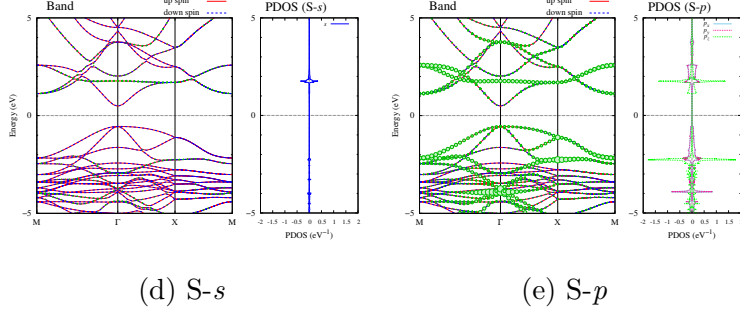
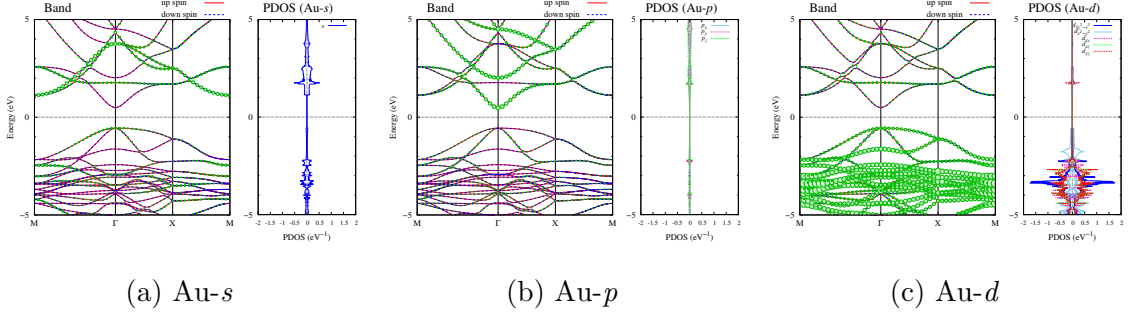


FIG. S2: Weight of the electronic band and partial DOS of Au and S atoms of *buckled- $\eta$ -Au<sub>2</sub>S* monolayers. The weight is projected on *s*, *p* and *d* type functions.

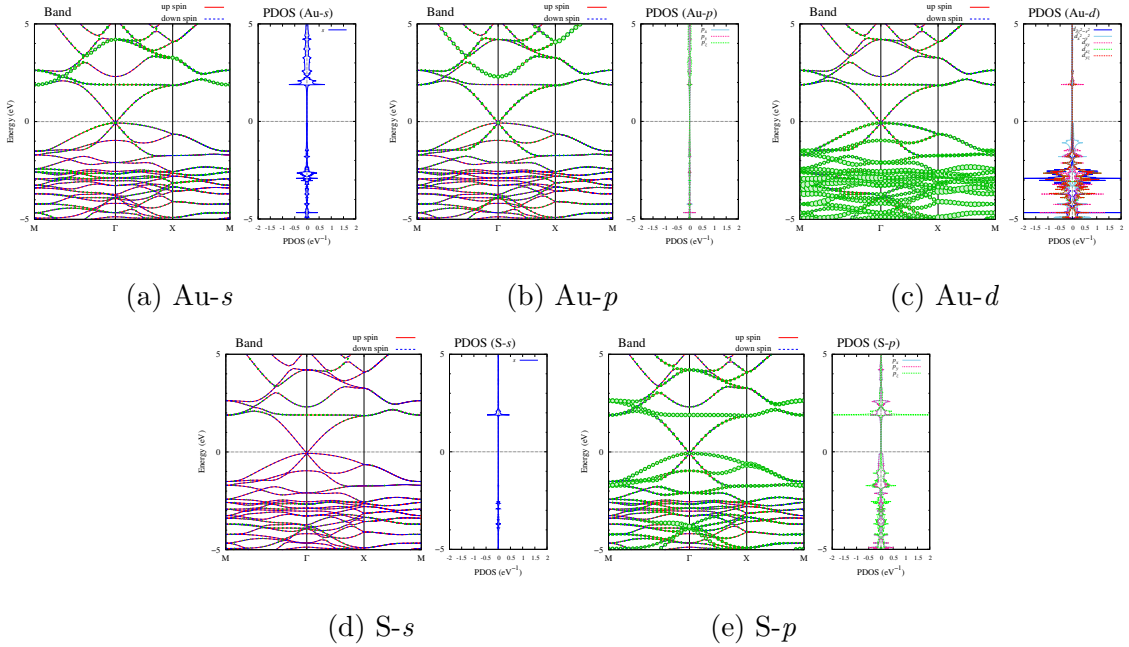


FIG. S3: Weight of the electronic band and partial DOS of Au and S atoms of *buckled- $\theta$ -Au<sub>2</sub>S* monolayers. The weight is projected on *s*, *p* and *d* type functions.

TABLE S3: Function types for each band.

Band Function Types	
CB2	Au- $s,d$ , S- $p_z$
CB1	Au- $p_x,p_y$
VB1	Au- $d$ , S- $p_x,p_y$
VB2	Au- $d$ , S- $p_x,p_y$

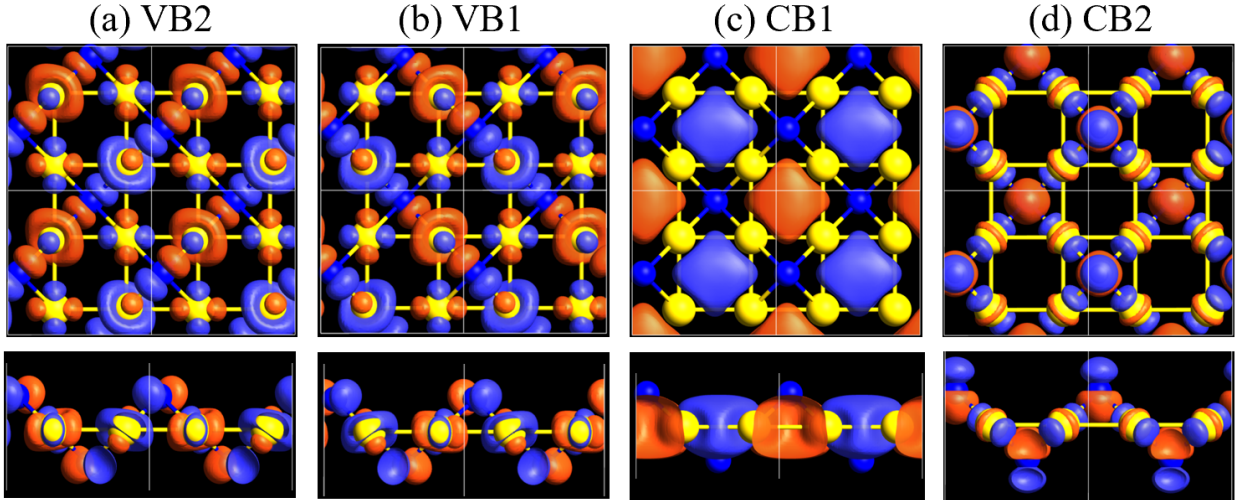


FIG. S4: Molecular orbitals (MO) of VB2, VB1, CV1, and CV2 of *buckled- $\eta$ -Au<sub>2</sub>S* monolayers at  $\Gamma$  point. The threshold value of isosurfaces of the MOs is taken as 0.04 a.u. .

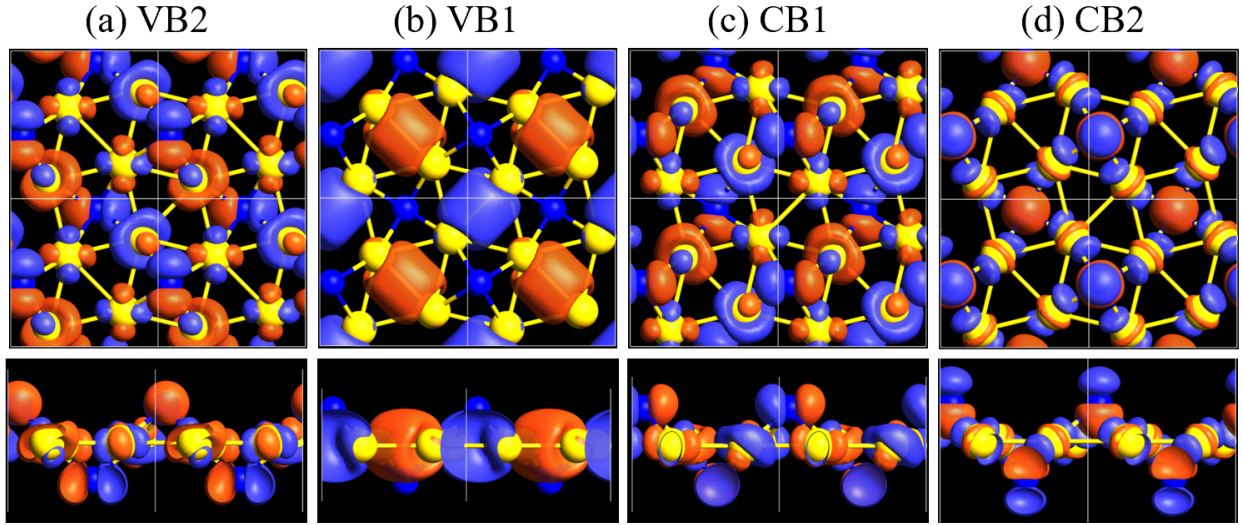


FIG. S5: Molecular orbitals (MO) of VB2, VB1, CV1, and CV2 of *buckled- $\theta$ -Au<sub>2</sub>S* monolayers at  $\Gamma$  point. The threshold value of isosurfaces of the MOs is taken as 0.04 a.u. . The CB1, VB1 and VB2 are almost degenerate at  $\Gamma$  point.

## B. $\text{Au}_2\text{X}$ monolayers

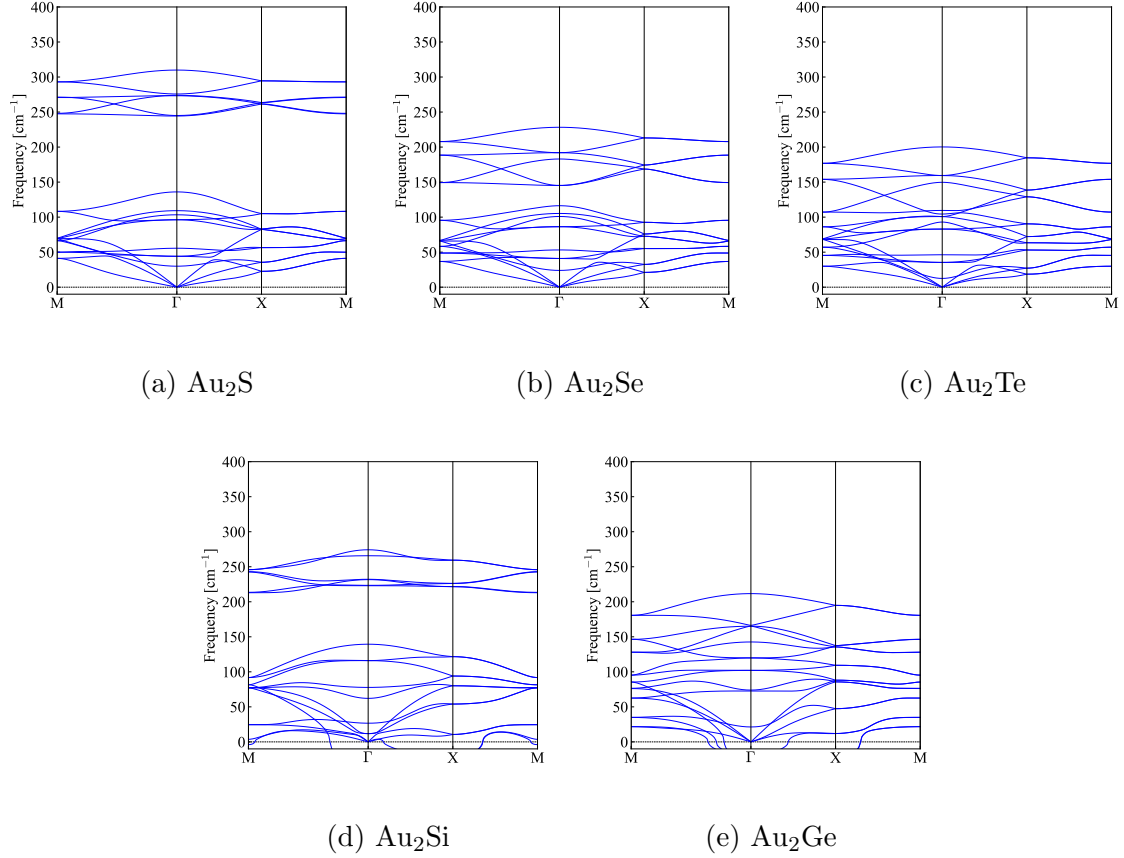


FIG. S6: Phonon band of *buckled- $\eta$ - $\text{Au}_2\text{X}$*  ( $\text{X}=\text{S}, \text{Se}, \text{Te}, \text{Si}, \text{Ge}$ ). The phonon band is calculated based on the partition method. We applied the  $r^{-4}$  weight for atoms in the region  $0.4r_{\text{inner}} < r < r_{\text{outer}}$  to obtain proper results.

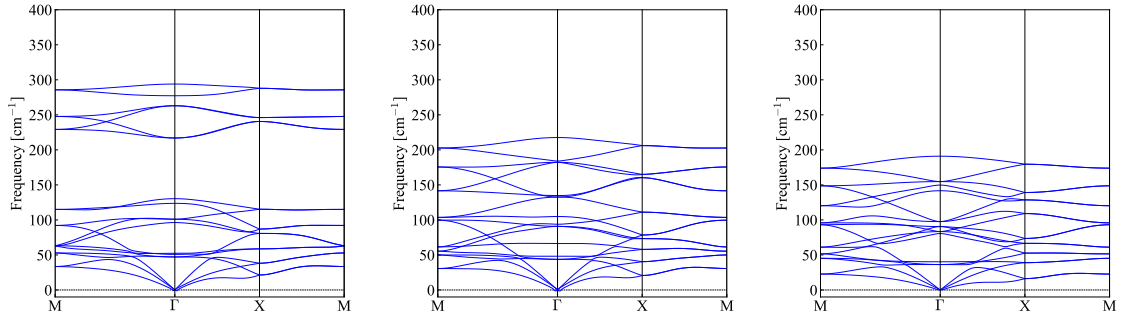
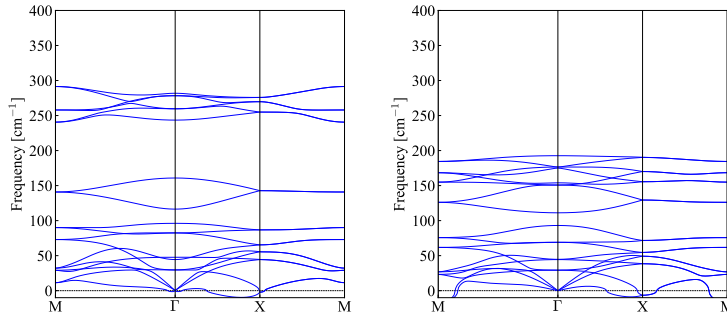
(a) Au<sub>2</sub>S(b) Au<sub>2</sub>Se(c) Au<sub>2</sub>Te(d) Au<sub>2</sub>Si(e) Au<sub>2</sub>Ge

FIG. S7: Phonon band of *buckled- $\theta$ -Au<sub>2</sub>X* (X=S, Se, Te, Si, Ge). The phonon band is calculated based on the partition method. We applied the  $r^{-4}$  weight for atoms in the region  $0.4r_{\text{inner}} < r < r_{\text{outer}}$  to obtain proper results. For Au<sub>2</sub>S and Au<sub>2</sub>Se, we applied the  $r^{-3}$  weight to obtain proper results.



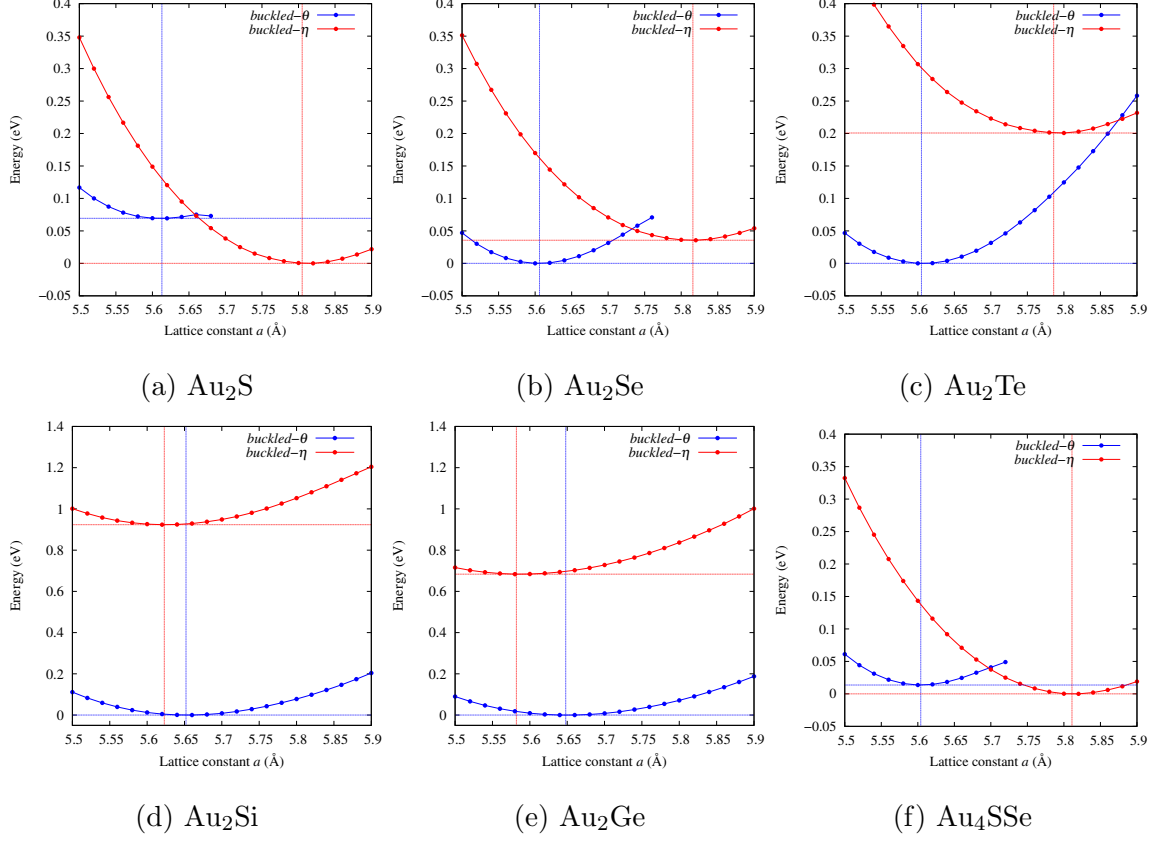
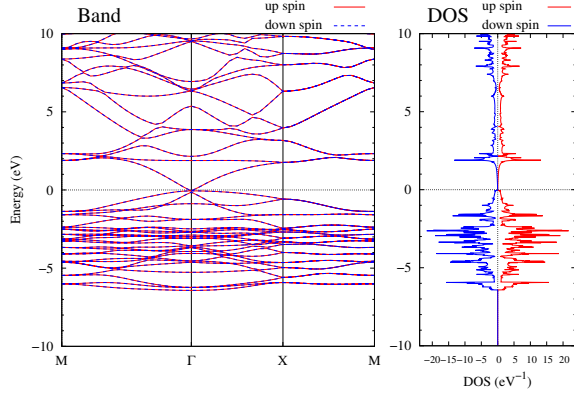
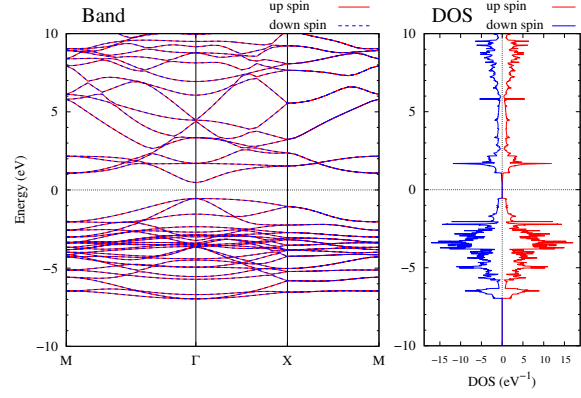


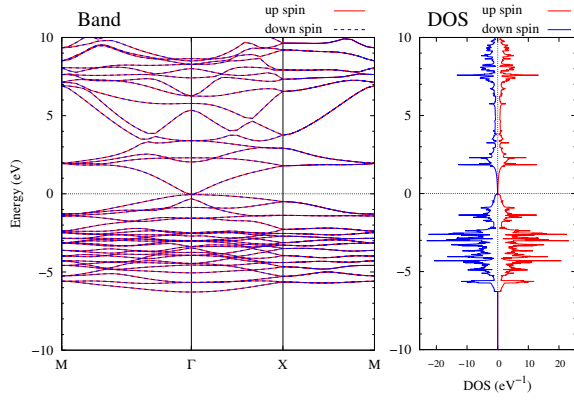
FIG. S8: Energy curve of *buckled- $\eta$* - and *buckled- $\theta$* -  $\text{Au}_2\text{X}$  ( $\text{X}=\text{S}, \text{Se}, \text{Te}, \text{Si}, \text{Ge}$ ) and  $\text{Au}_4\text{SSe}$  monolayers. The red (blue) line represents the energy curve of  $\eta$ -phase ( $\theta$ -phase).



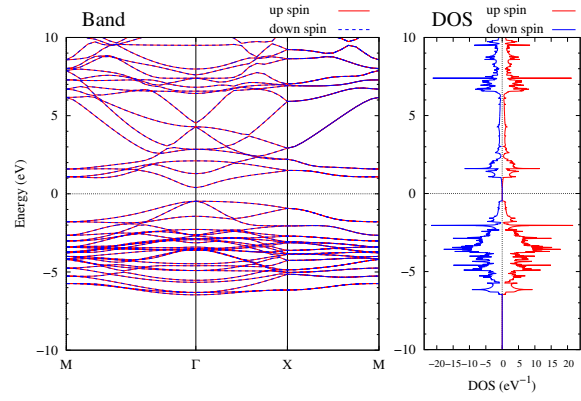
(a) *buckled- $\theta$ -Au<sub>2</sub>Se*



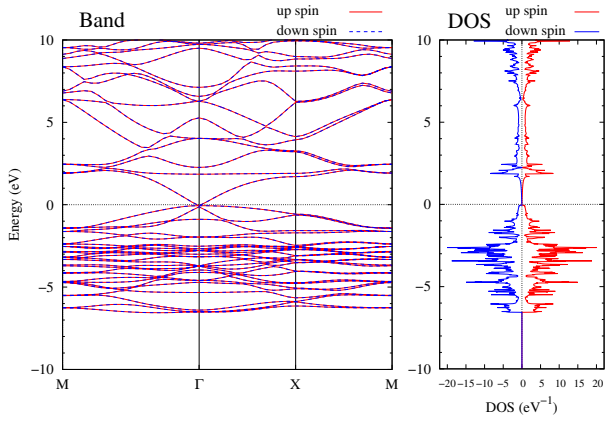
(b) *buckled- $\eta$ -Au<sub>2</sub>Se*



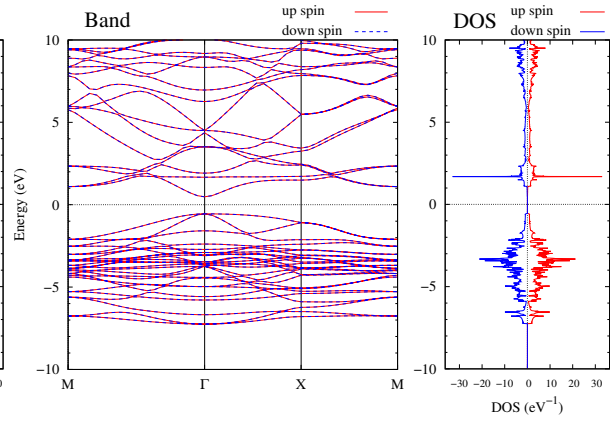
(c) *buckled- $\theta$ -Au<sub>2</sub>Te*



(d) *buckled- $\eta$ -Au<sub>2</sub>Te*

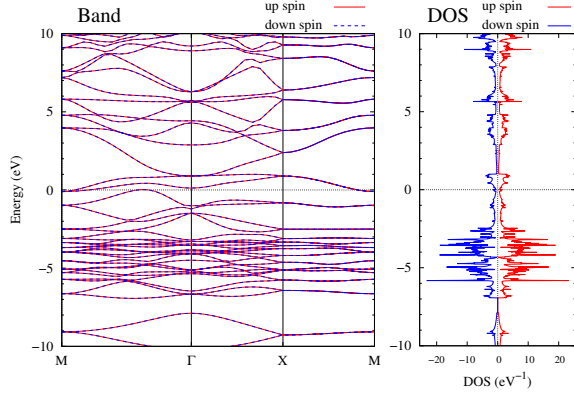


(e) *buckled- $\theta$ -Au<sub>4</sub>SSe*

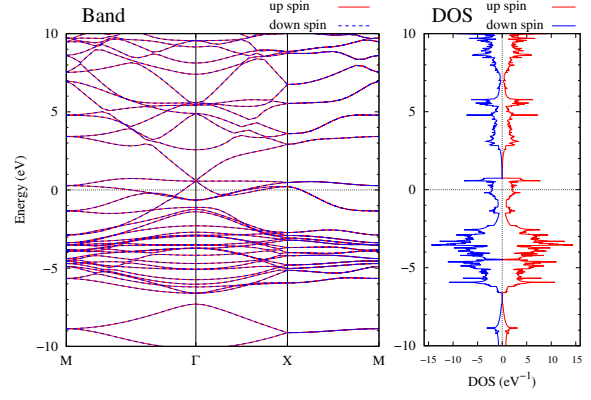


(f) *buckled- $\eta$ -Au<sub>4</sub>SSe*

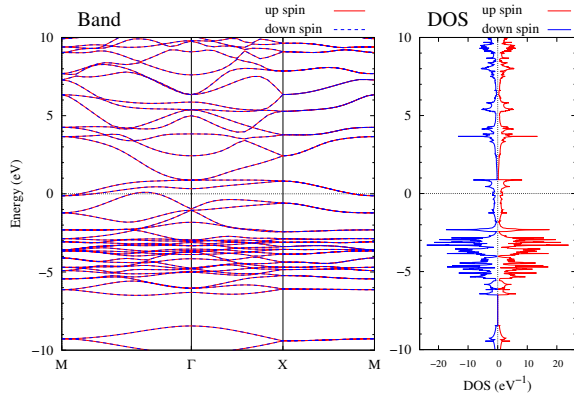
FIG. S9: Electronic band and DOS of Au<sub>2</sub>X (X=Se, Te) and Au<sub>4</sub>SSe monolayers.



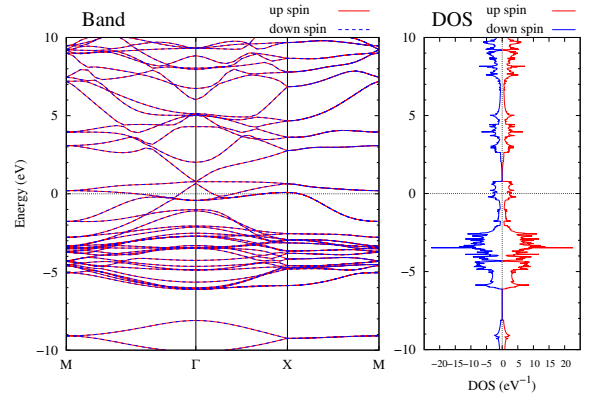
(a) *buckled- $\theta$ -Au<sub>2</sub>Si*



(b) *buckled- $\eta$ -Au<sub>2</sub>Si*



(c) *buckled- $\theta$ -Au<sub>2</sub>Ge*



(d) *buckled- $\eta$ -Au<sub>2</sub>Ge*

FIG. S10: Electronic band and DOS of Au<sub>2</sub>X (X=Si, Ge) monolayers.

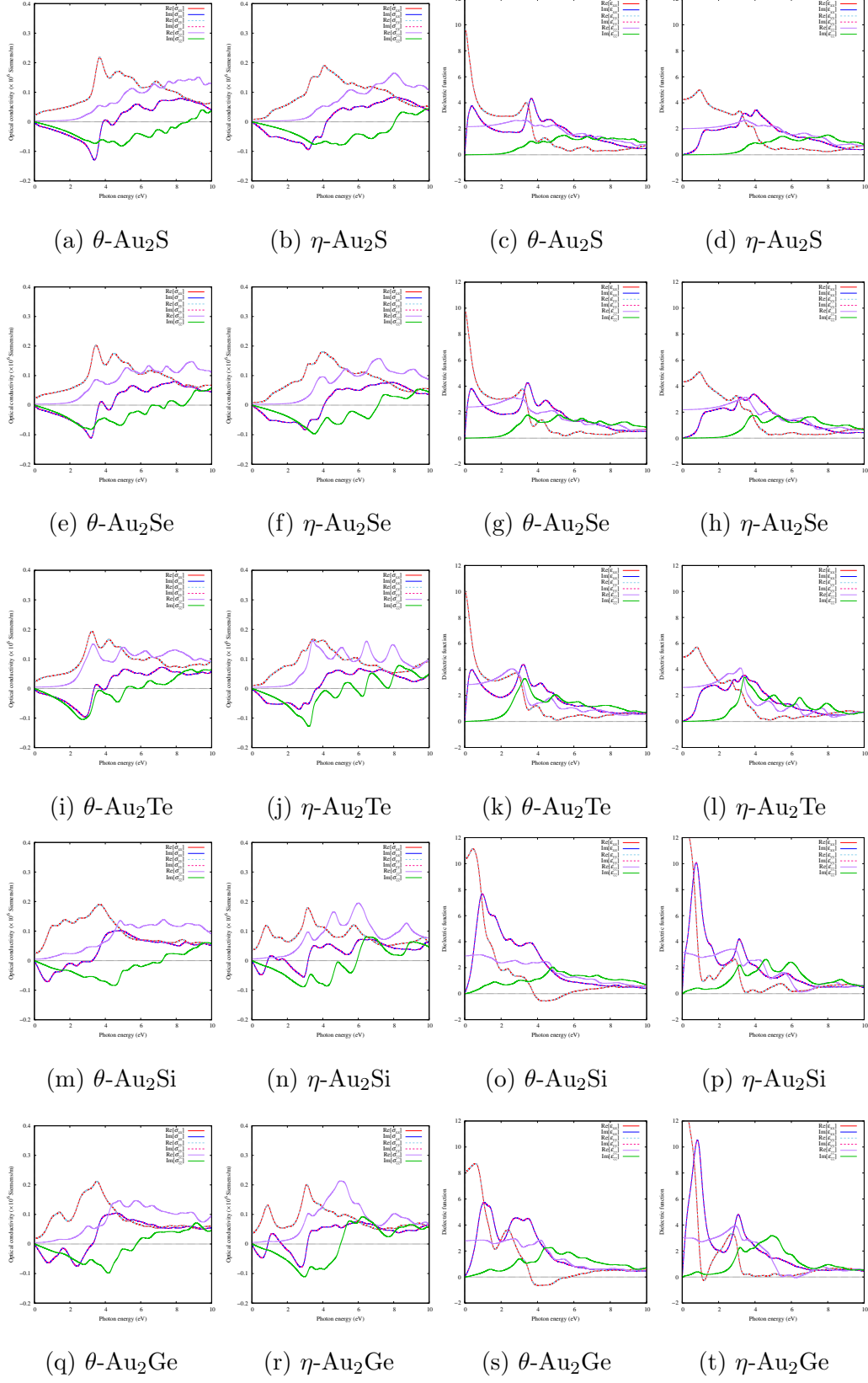


FIG. S11: Optical conductivities (left two columns) and dielectric functions (right two columns) of Au<sub>2</sub>X (X=S, Se, Te, Si, Ge) monolayers.