

Supporting Information

d- and p-block Single-atom Catalysts Supported by BN Nanocages toward electrochemical Reactions of N₂ and O₂

Chenhui Wang[‡], Fan Huang[‡], Haikuan Liang, Wei Nong[†], Fei Tian*, Yan Li* and Chengxin Wang

State Key Laboratory of Optoelectronic Materials and Technologies, School of Materials Science and Engineering, Sun Yat-Sen (Zhongshan) University, Guangzhou 510275, People's Republic of China

* Corresponding Authors.

E-mail: tianf9@mail.sysu.edu.cn; liyan266@mail.sysu.edu.cn

‡ These authors contributed equally to this work.

†Wei Nong's present address: School of Materials Science and Engineering, Nanyang Technological University, 50 Nanyang Avenue, Singapore 639798, Singapore

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Note1. Supplementary computational details

The adsorption energy (E_{ads}) of the molecule (N₂, O₂ and H₂O) and atom (H, N, O and metals) on the substrate is calculated by

$$E_{ads} = E_{total} - E_{sub} - E_{adsorbate} \quad \text{Eq. 1}$$

where E_{total} is the total energy of the substrate with absorbed molecule or atom, E_{sub} is the total energy of the substrate, and $E_{adsorbate}$ is the energy of adsorbate. In particular, the free energy of the O₂ gas molecule is determined by the equation¹:

$$G_{O_2(g)} = 4.92 - 2 \times G_{H_2O(l)} - G_{H_2(g)} \quad \text{Eq. 2}$$

in which $G(H_2O(l))$ can be calculated by carrying out calculation of $G(H_2O(g))$ at a pressure of 0.035 bar.

The cohesive energies are obtained from experimental data².

The Gibbs free energy (G) was obtained using the computational hydrogen electrode (CHE) model³. At the standard hydrogen electrode (SHE), the chemical potential of H⁺/e⁻ pair in aqueous solution is equal to half that of hydrogen gas. According to the CHE model, the free energy change of reaction (ΔG) for each elementary step of NRR is expressed as

$$\Delta G = \Delta E - T\Delta S + \Delta ZPE - \Delta G_U + \Delta G_{pH} \quad \text{Eq. 3}$$

where ΔE is the change in total energies of the species involved in each step, ΔS and ΔZPE are the change in entropy and zero-point energies, respectively. Note that the entropies of gas molecules (N₂, H₂ and NH₃) are obtained from the NIST database⁴, while those of the absorbed intermediates were set to zero. The zero-point energies of both gas molecules and intermediates were calculated using VASP and could be determined as $ZPE = \frac{1}{2}\sum_i h\nu_i$, here h and ν_i are Planck constant and vibrational frequencies, respectively. T is the temperature and was set as 298.15 K here. $\Delta G_U = n e U$ is the free energy contributed by electrode potential, here n and U are the number of electrons transferred and the applied electrode potential, respectively. $\Delta G_{pH} = k_B T \times \ln 10 \times pH$ is the correction of pH, here k_B is the Boltzmann constant, and pH = 0 was considered in this work.

The d band center, ε_d , was calculated as:

$$\varepsilon_d = \int_{-\infty}^{+\infty} \rho \varepsilon d\varepsilon / \int_{-\infty}^{+\infty} \rho d\varepsilon \quad \text{Eq. 4}$$

where ρ and ε refer to the projected density of states (PDOS) of d orbital and energy level, respectively.

The limiting potential (LP) of the whole process is used to estimate the performance of NRR catalysts, which is determined by the potential determining step (PDS) that has the maximum ΔG values (ΔG_{PDS}) and by $\Delta G(\text{*H})$ for NRR and HER, respectively, and can be calculated by

$$\text{LP} = -\frac{\Delta G}{e} \quad \text{Eq. 5}$$

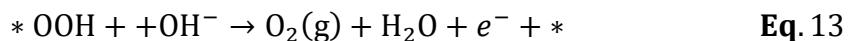
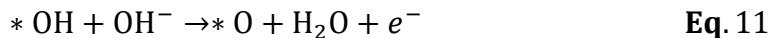
All the potential values are referenced to SHE.

We explored the 4e pathway of ORR and OER in an alkaline solution whose reactions are denoted as follows, in which * refers to the adsorption site.

The process of ORR:



and the process of OER:



where * indicates the active center of the catalyst, (g) refers to the gas phase.

The adsorption free energy of intermediates during ORR/OER ($*\text{O}_i\text{H}_j$, i.e. $*\text{OOH}$, $*\text{O}$, $*\text{OH}$) are calculated by the following equation:

$$\Delta G_{*\text{O}_i\text{H}_j} = G_{*\text{O}_i\text{H}_j} - G_* - i \times G_0 - j/2 \times G_{*\text{H}_2} \quad \text{Eq. 14}$$

where G_0 was calculated according to the difference of $G(\text{H}_2\text{O})$ and $G(\text{H}_2)$.

The Gibbs free energy change during ORR and OER can be obtained by the follows:

For ORR (Eq. 6-9):

$$\Delta G_1 = \Delta G_{*OOH} - 4.92 \quad \text{Eq. 15}$$

$$\Delta G_2 = \Delta G_{*O} - \Delta G_{*OOH} \quad \text{Eq. 16}$$

$$\Delta G_3 = \Delta G_{*OH} - \Delta G_{*O} \quad \text{Eq. 17}$$

$$\Delta G_4 = -\Delta G_{*OH} \quad \text{Eq. 18}$$

For OER (Eq. 10-13):

$$\Delta G_5 = \Delta G_{*OH} \quad \text{Eq. 19}$$

$$\Delta G_6 = \Delta G_{*O} - \Delta G_{*OH} \quad \text{Eq. 20}$$

$$\Delta G_7 = \Delta G_{*OOH} - \Delta G_{*O} \quad \text{Eq. 21}$$

$$\Delta G_8 = 4.92 - \Delta G_{*OOH} \quad \text{Eq. 22}$$

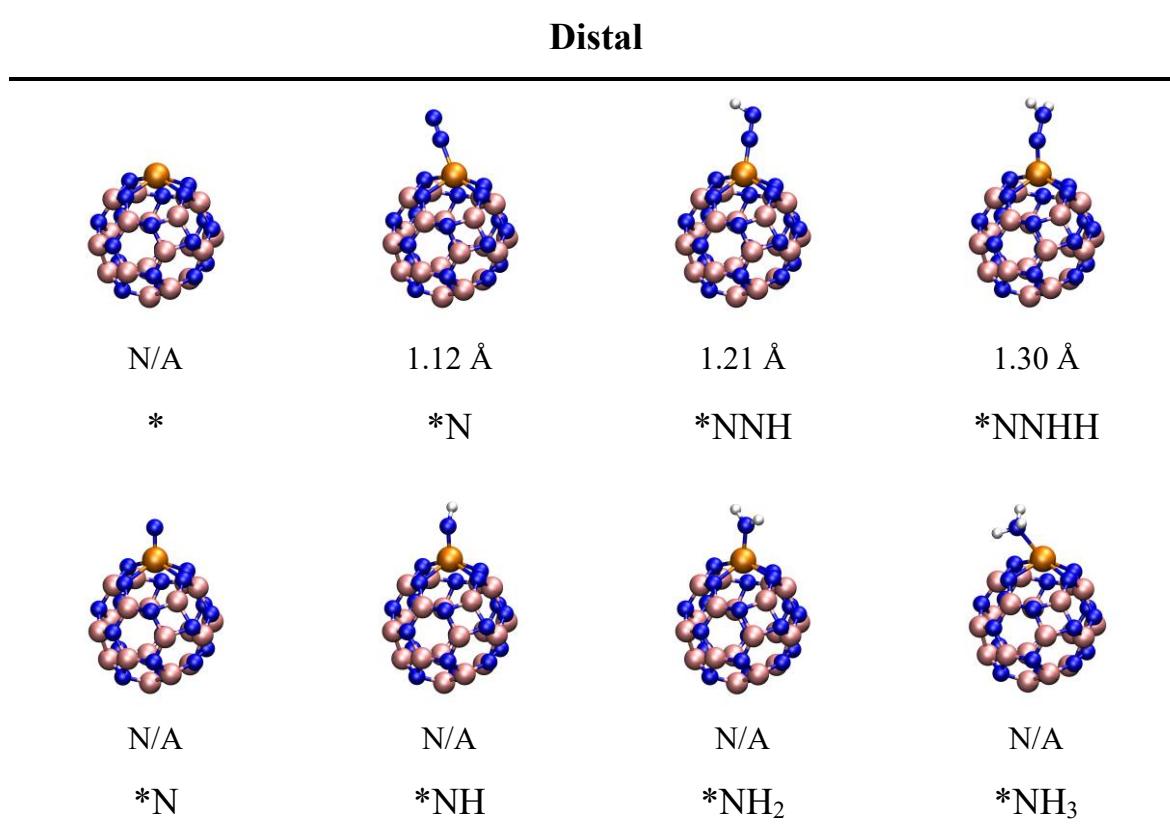
The overpotential η_{ORR} and η_{OER} are obtained by the following equations:

$$\eta_{ORR} = 1.23 + \max(\Delta G_1, \Delta G_2, \Delta G_3, \Delta G_4) \quad \text{Eq. 23}$$

$$\eta_{OER} = \max(\Delta G_5, \Delta G_6, \Delta G_7, \Delta G_8) - 1.23 \quad \text{Eq. 24}$$

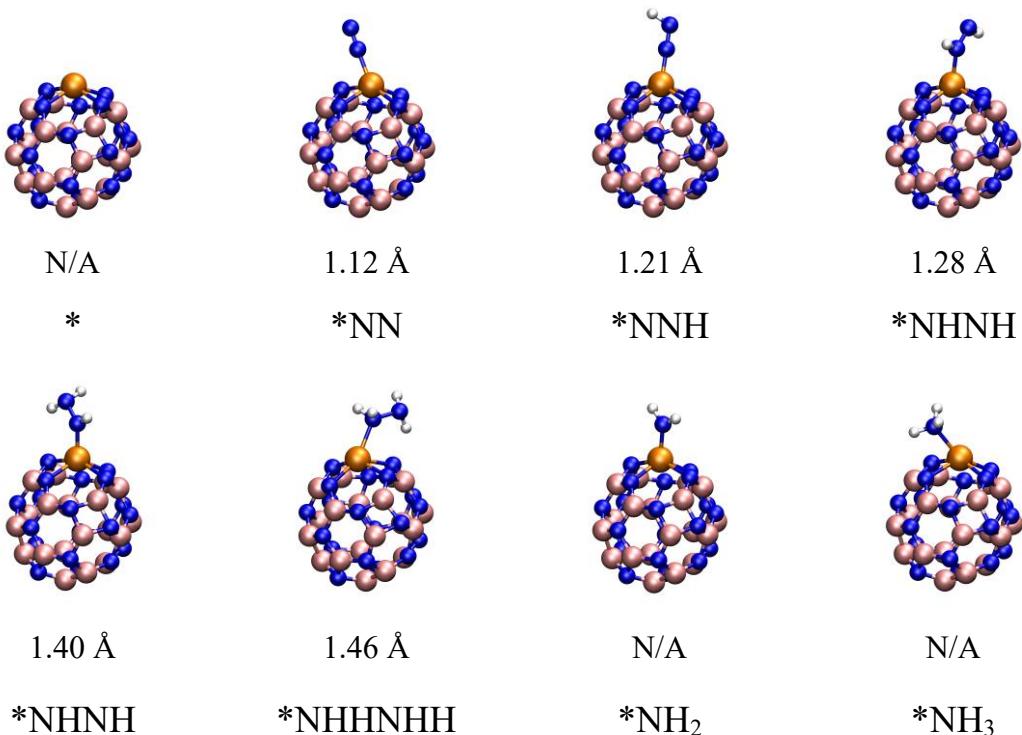
Note2 Structure and features of TM@BNNC

Note2.1. Optimized configuration of the intermediates of the NRR distal pathway catalyzed by Os@BNNC and the N-N bond length of adsorbates.



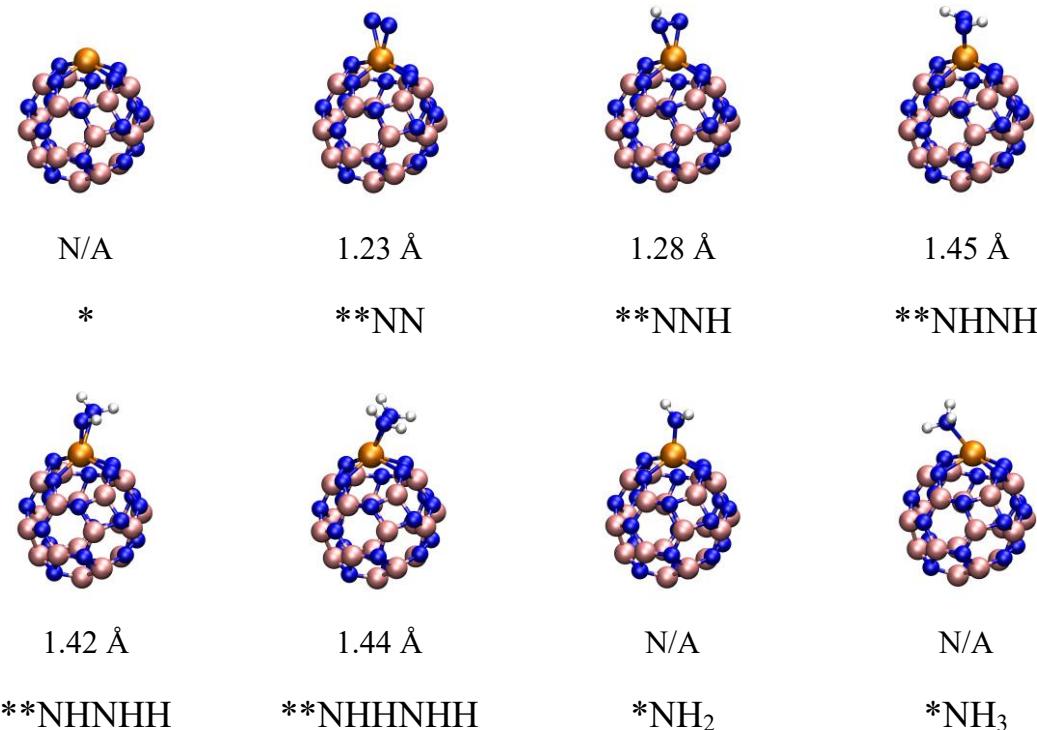
Note2.2. Optimized configuration of the intermediates of the NRR alternating pathway catalyzed by Os@BNNC and the N-N bond length of adsorbates.

Alternating



Note2.3. Optimized configuration of the intermediates of the NRR enzymatic pathway catalyzed by Os@BNNC and the N-N bond length of adsorbates.

Enzymatic



Data1. For Section 3.1

Table S1. Adsorption energies (E_{ads}) of TM on BN nanocage, cohesive energies (E_{coh}) of the corresponding metal atom and the difference between them ($E_{\text{ads}} - E_{\text{coh}}$). The bold data refer to unstable TM@BNNCs. The unit is eV.

TM	E_{ads}	E_{coh}	$E_{\text{ads}} - E_{\text{coh}}$
Al	-7.34	-3.39	-3.95
Sc	-9.45	-3.90	-5.55
Ti	-10.71	-4.85	-5.86
V	-9.10	-5.31	-3.79
Cr	-6.85	-4.10	-2.75
Mn	-6.50	-2.92	-3.58
Fe	-7.02	-4.28	-2.74
Co	-6.30	-4.39	-1.91
Ni	-5.96	-4.44	-1.52
Cu	-3.90	-3.49	-0.41
Zn	-1.84	-1.35	-0.49
Y	-9.68	-4.37	-5.31
Zr	-12.35	-6.25	-6.10
Nb	-10.86	-7.57	-3.29
Mo	-8.56	-6.82	-1.74
Tc	-8.33	-6.85	-1.48
Ru	-7.87	-6.74	-1.13
Rh	-6.62	-5.75	-0.87
Pd	-3.94	-3.89	-0.05
Ag	-2.06	-2.95	0.89
Cd	-0.82	-1.16	0.34
Lu	-9.57	-4.43	-5.14
Hf	-12.45	-6.44	-6.01
Ta	-12.47	-8.10	-4.37
W	-12.17	-8.90	-3.27
Re	-10.53	-6.03	-4.50
Os	-8.50	-8.17	-0.33
Ir	-8.04	-6.94	-1.10
Pt	-6.08	-5.64	-0.44
Au	-3.09	-3.81	0.72
Hg	0.22	-0.67	0.89

Data2. For Section 3.2

Table S2. Adsorption energies (E_{ads}), ZPE and adsorption free energies (ΔG) during N_2 adsorption on TM@BNNCs. The unit is eV.

TM	E_{ads}	ZPE	ΔG	E_{ads}	ZPE	ΔG
Initial configuration	End-on(*NN)			Side-on(**NN)		
Sc	-0.41	0.17	0.20	-0.41	0.17	0.20
Ti	-0.65	0.19	-0.02	-0.64	0.19	-0.02
V	-0.60	0.19	0.03	-0.05	0.17	0.56
Cr	-0.36	0.19	0.27	0.31	0.18	0.92
Mn	-0.18	0.15	0.41	-0.22	0.18	0.39
Fe	-0.29	0.15	0.30	1.20	0.18	1.81
Co	0.00	0.23	0.67	-0.16	0.16	0.45
Ni	0.03	0.17	0.64	-0.07	0.16	0.53
Cu	-0.08	0.17	0.53	-0.06	0.17	0.54
Zn	-0.17	0.17	0.44	-0.17	0.16	0.44
Y	-0.33	0.18	0.29	-0.33	0.18	0.29
Zr	-0.56	0.18	0.06	-0.56	0.18	0.06
Nb	-0.68	0.19	-0.05	-0.48	0.19	0.15
Mo	-0.48	0.18	0.14	-0.26	0.20	0.38
Tc	-0.47	0.20	0.17	-0.21	0.20	0.42
Ru	-0.40	0.21	0.25	-0.12	0.20	0.52
Rh	-0.34	0.21	0.31	-0.05	0.16	0.54
Pd	-0.05	0.16	0.54	-0.07	0.16	0.53
Lu	-0.38	0.18	0.23	-0.38	0.17	0.23
Hf	-0.64	0.18	-0.02	-0.64	0.18	-0.02
Ta	-0.72	0.18	-0.10	-0.56	0.18	0.06
W	-0.77	0.18	-0.15	-0.75	0.20	-0.11
Re	-0.78	0.20	-0.14	-0.72	0.19	-0.10
Os	-0.55	0.21	0.10	-0.43	0.21	0.22
Ir	-0.48	0.22	0.18	-0.06	0.16	0.54
Pt	-0.14	0.21	0.51	-0.06	0.16	0.54

Table S3. Values of ΔG_{1-6} (eV) for NRR on TM@BNNCs (TM = Sc, Ti, V, Zr, Nb, Mo, Tc, Hf, Ta, W, Re, Os and Ir).

Element	ΔG_1	ΔG_1	ΔG_2	ΔG_2	ΔG_2	ΔG_6
Adsorption configuration	*NNH	**NNH	*NNHH	*NHNH	**NHNH	*NH ₃
Sc	1.92	2.09	-0.21	-0.47	-0.49	-1.84
Ti	1.74	1.88	-0.17	-0.53	-0.43	-1.31
V	0.99		-0.26	-0.22		0.01
Zr	1.68		-0.10	-0.40		-1.12
Nb	0.63	0.34	-0.40	-0.10	-0.41	1.12
Mo	0.58		-0.66	-0.08		0.82
Tc	0.46		-0.75	0.24		0.56
Hf	1.59	1.68	-0.16	-0.42	-0.52	-1.03
Ta	0.42	0.08	-0.46	-0.10	-0.36	1.79
W	0.19	-0.10	-0.81	0.26	-0.52	1.25
Re	0.06	-0.25	-0.80	0.53	0.18	0.73
Os	0.27	0.73	-0.69	0.39	-0.18	0.29
Ir	0.61		-0.01	0.29		-0.37

Table S4. Gibbs free energy changes (eV) during the distal mechanism of NRR on TM@BNNCs (TM = Tc, Re, Os and Ir).

Step	Absorbate	TM = Tc	TM = Re	TM = Os	TM = Ir
0	*N ₂	0.17	-0.14	0.10	0.18
1	*NNH	0.46	0.06	0.27	0.61
2	*NNH ₂	-0.75	-0.80	-0.69	-0.01
3	*N	-0.16	-0.12	-0.63	-1.31
4	*NH	-0.72	-0.91	-0.33	0.85
5	*NH ₂	-0.73	-0.30	-0.32	-1.22
6	*NH ₃	0.56	0.73	0.29	-0.37
LP	/	-0.56	-0.73	-0.29	-0.85

Table S5. Gibbs free energy changes (eV) during the alternating mechanism of NRR on TM@BNNCs (TM = Tc, Re, Os and Ir).

Step	Absorbate	TM = Tc	TM = Re	TM = Os	TM = Ir
0	*N ₂	0.17	-0.14	0.10	0.18
1	*NNH	0.46	0.06	0.27	0.61
2	*NHNH	0.24	0.53	0.39	0.29
3	*NHNHH	-0.84	-0.79	-0.69	-0.71
4	*NHHNHH	0.81	0.85	0.61	0.27
5	*NH ₂	-2.57	-2.72	-2.27	-1.54
6	*NH ₃	0.56	0.73	0.29	-0.37
LP	/	-0.81	-0.85	-0.61	-0.61

Table S6. Gibbs free energy changes (eV) during the enzymatic mechanism of NRR on TM@BNNCs (TM = Re and Os).

Step	Absorbate	TM = Re	TM = Os
0	**N ₂	-0.10	0.22
1	**NNH	-0.25	0.73
2	**NHNH	0.18	-0.18
3	**NHNHH	-0.21	-0.40
4	**NHHNHH	0.81	0.36
5	*NH ₂	-2.66	-2.33
6	*NH ₃	0.73	0.29
LP	/	-0.81	-0.73

Table S7. Summary of SACs for NRR and their supports, single atom (SA), coordination and limiting potential (LP).

Supports	SA	Coordination	LP(V)	Reference
C ₃ N	Sc	MC ₂ N	-0.66	Refs. ⁵
	Ti	MC ₂ N	-0.67	
	V	MC ₂ N	-0.63	
	Cr	MC ₂ N	-0.80	
	Mn	MC ₂ N	-0.75	
	Fe	MC ₂ N	-0.78	
	Co	MC ₂ N	-0.83	
	Ni	MC ₂ N	-0.75	
	Cu	MC ₂ N	-1.77	
	Zn	MC ₂ N	-1.40	
	Y	MC ₂ N	-0.73	
	Zr	MC ₂ N	-0.67	
	Nb	MC ₂ N	-0.97	
	Tc	MC ₂ N	-0.82	
	Ru	MC ₂ N	-0.94	
	Rh	MC ₂ N	-0.85	
	Pd	MC ₂ N	-0.66	
	Lu	MC ₂ N	-0.51	
	Hf	MC ₂ N	-0.84	
	Ta	MC ₂ N	-1.27	
	Re	MC ₂ N	-1.16	
	Ir	MC ₂ N	-0.74	
	Pt	MC ₂ N	-0.74	
Sc	Sc	MC ₃	-0.84	
	Ti	MC ₃	-0.93	
	V	MC ₃	-0.59	
	Cr	MC ₃	-0.80	
	Mn	MC ₃	-0.65	
	Fe	MC ₃	-0.89	
	Co	MC ₃	-1.19	
	Ni	MC ₃	-0.98	
	Zn	MC ₃	-1.32	
	Y	MC ₃	-1.00	
	Zr	MC ₃	-1.03	
	Nb	MC ₃	-0.78	

	Tc	MC ₃	-0.60	Refs. ⁵
	Ru	MC ₃	-1.39	
	Rh	MC ₃	-1.46	
	Pd	MC ₃	-0.95	
	Lu	MC ₃	-0.94	
	Hf	MC ₃	-1.17	
	Ta	MC ₃	-0.70	
	Re	MC ₃	-0.86	
	Ir	MC ₃	-1.16	
	Pt	MC ₃	-0.74	
	Sc	MC ₄	-1.13	
	Ti	MC ₄	-0.66	
	V	MC ₄	-0.73	
	Cr	MC ₄	-0.45	
	Mn	MC ₄	-0.47	
	Fe	MC ₄	-0.75	
	Co	MC ₄	-1.17	
	Ni	MC ₄	-2.01	
	Cu	MC ₄	-2.30	
	Zn	MC ₄	-1.21	
	Y	MC ₄	-1.20	
	Zr	MC ₄	-0.68	
	Nb	MC ₄	-0.89	
	Mo	MC ₄	-0.92	
	Tc	MC ₄	-0.67	
	Ru	MC ₄	-0.83	
	Rh	MC ₄	-1.17	
	Pd	MC ₄	-2.07	
	Ag	MC ₄	-2.24	
	Lu	MC ₄	-1.07	
	Hf	MC ₄	-0.75	
	Ta	MC ₄	-1.28	
	W	MC ₄	-1.27	
	Re	MC ₄	-3.07	
	Os	MC ₄	-0.54	
	Ir	MC ₄	-0.96	
	Pt	MC ₄	-1.98	
	Au	MC ₄	-2.21	

Hg	MC_4	-2.17	Refs. ⁵
Sc	MC_2N_2	-0.77	
Ti	MC_2N_2	-0.84	
V	MC_2N_2	-0.62	
Cr	MC_2N_2	-0.40	
Mn	MC_2N_2	-0.79	
Fe	MC_2N_2	-0.62	
Co	MC_2N_2	-1.04	
Ni	MC_2N_2	-2.30	
Cu	MC_2N_2	-2.31	
Zn	MC_2N_2	-1.85	
Y	MC_2N_2	-0.88	
Zr	MC_2N_2	-0.95	
Nb	MC_2N_2	-0.81	
Mo	MC_2N_2	-0.80	
Tc	MC_2N_2	-0.65	
Ru	MC_2N_2	-1.01	
Rh	MC_2N_2	-0.87	
Pd	MC_2N_2	-2.48	
Ag	MC_2N_2	-2.25	
Cd	MC_2N_2	-1.63	
Lu	MC_2N_2	-0.76	
Hf	MC_2N_2	-1.14	
Ta	MC_2N_2	-1.14	
W	MC_2N_2	-1.05	
Re	MC_2N_2	-1.01	
Os	MC_2N_2	-0.55	
Ir	MC_2N_2	-0.79	
Pt	MC_2N_2	-2.43	
Au	MC_2N_2	-2.18	
Hg	MC_2N_2	-1.32	
Graphene			
	Mo	MC_3	-0.89
	Nb	MC_3	-0.83
	V	MC_3	-0.99
	W	MC_3	-0.75
	Ir	MC_4	-0.66
	Co	MC_4	-1.00
	Ir	MC_4	-0.79

	Mo	MC ₄	-0.69	Refs. ⁶
	Nb	MC ₄	-0.61	
	Os	MC ₄	-0.69	
	V	MC ₄	-0.70	
	Ta	MC ₄	-0.92	
	Re	MC ₄	-0.60	
	La	MN ₃	-0.70	
	Mn	MN ₃	-1.00	
	Sc	MN ₃	-0.89	
	Ti	MN ₃	-0.77	
	Y	MN ₃	-0.97	
	V	MN ₄	-0.87	
	Cr	MN ₄	-0.98	
	Sc	MN ₄	-0.81	
	Y	MN ₄	-0.97	
	Ti	MN ₄	-0.69	
Graphene oxide	Pt	cluster	-0.68	Refs. ⁷
	Cu	cluster	-1.52	
	Co	cluster	-1.24	
	Ni	cluster	-1.52	
Graphene	Fe	MN ₃	-0.66	Refs. ⁸
	Fe	MC ₃	-1.37	
	Fe	MC ₂ N	-1.16	
	Fe	MCN ₂	-0.80	
	Fe	MP ₃	-0.92	
C ₂ N	Ru	MN ₂	-0.96	Refs. ⁹
γ-graphyne	Ru	MC ₆	-0.98	
t-C ₃ N ₄	Ru	MN ₃	-0.94	
g-C ₃ N ₄ (corrugated+ N)	V	MC ₂ N ₃	-0.53	Refs. ¹⁰
	Ti	MCN ₂	-0.51	
Graphene	Mo	MC ₂ N	-0.40	Refs. ¹¹
C ₂ N	Mo	MN ₂	-0.17	Refs. ¹²
	Ti	MN ₂	-0.45	
	V	MN ₂	-0.55	
	Ni	MN ₂	-0.79	
Graphene	Nb	MC ₃	-0.45	Refs. ¹³
	Re	MC ₃	-0.43	

	V	MC ₂ N	-0.52	Refs. ¹³
	Nb	MC ₂ N	-0.41	
	Mo	MC ₂ N	-0.40	
	V	MN ₄	-0.41	
	Ru	MC ₂ N	-0.60	
	V	MCN ₃	-0.35	
	W	MC ₃	-0.25	
	Zr	MC ₂ N	-0.55	
<i>g-C₃N₄</i>	Fe	MN ₄	-1.38	Refs. ¹⁴
	Co	MN ₄	-1.09	
	Ru	MN ₄	-1.27	
	Rh	MN ₄	-1.23	
	Mo	MN ₄	-0.67	
	W	MN ₄	-1.08	
<i>g-C₃N₄</i>	Pt	MN ₄	-0.24	Refs. ¹⁵
	W	MN ₂	-0.35	Refs. ¹⁶
	V	MN ₆	-0.52	Refs. ¹⁷
	Cr	MN ₆	-1.23	
	Mn	MN ₆	-1.23	
	Fe	MN ₆	-0.81	
	Ag	MN ₆	-2.20	
	Au	MN ₆	-0.94	
	Ru	MN ₆	-0.33	
	Rh	MN ₆	-0.45	
	Co	MN ₆	-0.61	
	Ni	MN ₆	-1.15	
	Cu	MN ₆	-1.79	
	Pd	MN ₆	-1.13	
	Nb	MN ₆	-0.53	
	Mo	MN ₆	-0.62	
	Tc	MN ₆	-0.43	
	Ta	MN ₆	-1.00	
	W	MN ₆	-0.65	
<i>α</i> -Boron sheet	Re	MN ₆	-0.83	
	Ir	MN ₆	-0.98	
	Pt	MN ₆	-0.98	
	Ru	MB ₆	-0.42	Refs. ¹⁸
	Ru	MB ₆	-0.44	

C ₂ N	Cr	MN ₂	-1.69	Refs. ¹⁹
	Mn	MN ₂	-0.69	
	Fe	MN ₂	-1.06	
	Co	MN ₂	-1.02	
	Ni	MN ₂	-1.22	
	Cr	M ₂ N ₄	-0.34	
	Co	M ₂ N ₄	-0.54	
	Ni	M ₂ N ₄	-0.42	
	Mn	M ₂ N ₄	-0.23	
	Fe	M ₂ N ₄	-0.24	
	Mo	M ₂ N ₆	-0.41	Refs. ²⁰
	Fe	M ₂ N ₆	-1.23	
MoS ₂	Fe	M	-1.02	Refs. ²¹
	AuCu	MO _x	-1.82	Refs. ²²
Black phosphorus	B	MP ₃	-0.58	Refs. ²³
	B	M ₂ P ₆	-0.19	
MoS ₂	Mo	MoS ₃	-0.44	Refs. ²⁴
C ₂ N	B	BN ₂	-0.25	Refs. ²⁵
Graphene	Ru	MN ₃	-0.73	Refs. ²⁶
LiFeO ₂ (111)	Fe	M	-0.63	Refs. ²⁷
BO-MnO ₂ (VO)	Mn	M	-0.83	Refs. ²⁸
BS-VS ₂ (VS)	V	M	-0.77	Refs. ²⁹
Fe-CeO ₂ (VO)	Ce	M	-0.81	Refs. ³⁰
MoSn-SnS ₂ (VS)	MoSn	M	-0.73	Refs. ³¹
GDY(graphdiyne)	B	/	-0.77	Refs. ³²
GDY	BN	/	-0.48	
CN	Fe2	/	-0.47	Refs. ³³
	Co	/	-0.87	
h-BN	Mo	MN ₃	-0.35	Refs. ³⁴
ZIF-8 precursor	Ni	/	-0.79	Refs. ³⁵
graphene	FeMo	/	-1.79	
GY(graphyne)	Mn	/	-0.36	Refs. ³⁶
MnO ₂	none	/	-1.59	Refs. ²⁸
	B	/	-0.83	
Re ₂ MnS ₆	Ultrathin nanosheets		-0.51	Refs. ³⁷

Data3. For Section 3.4

Table S8. *d*-band centers (ε_d) of TM@BNNCs. The unit is eV.

TM	d-total	dxy	dyz	dx ²	dxz	dz ²
Sc	2.94	0.46	2.87	3.59	3.08	3.34
Ti	0.62	0.69	0.35	0.87	0.50	0.66
V	0.09	0.02	0.07	0.05	0.09	0.25
Cr	-0.01	0.21	-0.28	0.13	-0.07	-0.07
Mn	-0.41	-0.26	-0.48	-0.44	-0.48	-0.42
Fe	-1.78	-1.72	-1.88	-1.87	-1.75	-1.67
Co	-1.38	-1.25	-1.28	-1.52	-1.43	-1.43
Ni	-1.67	-1.66	-1.65	-1.97	-1.51	-1.58
Cu	-2.45	-2.54	-2.36	-2.85	-2.33	-2.17
Zn	-6.11	-5.89	-6.23	-6.22	-6.19	-6.04
Y	2.99	-1.34	2.40	4.16	3.01	3.91
Zr	0.49	-2.66	0.28	1.41	0.59	1.21
Nb	-0.44	-2.66	-0.37	-0.01	-0.19	0.19
Mo	-0.81	-1.62	-1.06	-0.35	-0.73	-0.47
Tc	-1.39	-1.39	-1.65	-1.29	-1.40	-1.23
Ru	-1.25	-0.91	-1.58	-1.23	-1.30	-1.22
Rh	-1.75	-1.50	-1.91	-1.86	-1.78	-1.69
Pd	-2.26	-2.21	-2.25	-2.54	-2.25	-2.06
Lu	2.79	-2.32	2.24	4.48	3.01	3.66
Hf	0.67	-3.86	0.39	1.96	0.81	1.61
Ta	-0.68	-4.54	-0.61	0.07	-0.24	0.20
W	-0.90	-3.41	-0.91	-0.17	-0.63	-0.35
Re	-1.73	-3.60	-1.74	-1.22	-1.40	-1.21
Os	-1.96	-2.80	-2.11	-1.41	-1.96	-1.70
Ir	-2.12	-2.35	-2.20	-2.15	-1.93	-1.94
Pt	-2.49	-2.54	-2.54	-2.77	-2.36	-2.24

Table S9. Global magnetic moment of TM@BNNCs with the local magnetic moment of TM. The unit is $\mu_B/\text{\AA}^3$.

Element	TM@BNNC	TM	Element	TM@BNNC	TM
Sc	0.81	0.01	Ru	0.26	0.05
Ti	0.00	0.00	Rh	1.00	0.59
V	1.00	0.94	Pd	0.02	0.02
Cr	2.00	2.20	Lu	0.78	0.03
Mn	3.08	3.20	Hf	0.00	0.00
Fe	3.92	3.06	Ta	1.00	0.54
Co	2.90	1.82	W	1.99	1.53
Ni	1.93	0.81	Re	3.00	2.30
Cu	0.89	0.06	Os	2.09	1.44
Zn	0.67	0.03	Ir	1.00	0.63
Y	0.81	0.01	Pt	0.00	0.00
Zr	0.00	0.00			
Nb	1.00	0.59			
Mo	2.00	1.65			
Tc	3.00	2.34			

Table S10. Adsorption energies (eV) of O₂ and H₂O on TM@BNNCs.

TM	<i>E</i> _{ads} (*O ₂)	<i>E</i> _{ads} (*H ₂ O)	TM	<i>E</i> _{ads} (*O ₂)	<i>E</i> _{ads} (*H ₂ O)
Sc	-0.61	-1.08	Ru	-1.63	-0.66
Ti	-1.37	-1.40	Rh	-0.81	-0.68
V	-2.41	-1.15	Pd	-0.28	-0.40
Cr	-2.02	-1.88	Lu	-0.74	-1.05
Mn	-0.90	-1.34	Hf	-1.62	-1.43
Fe	-0.60	-0.76	Ta	-3.33	-0.83
Co	-0.61	-0.70	W	-4.59	-0.87
Ni	-0.23	-0.41	Re	-3.68	-0.82
Cu	-0.06	-0.31	Os	-2.27	-0.60
Zn	-0.11	-0.64	Ir	-0.81	-0.63
Y	-0.65	-0.93	Pt	-0.29	-0.48
Zr	-1.37	-1.28			
Nb	-3.08	-0.79			
Mo	-3.62	-0.88			
Tc	-2.87	-0.62			

Table S11. Adsorption Gibbs free energies (eV) of reaction intermediates of OOH, O and OH and overpotentials for ORR/OER on TM@BNNCs. The bold data refer to TM@BNNCs with competitive catalytic performance for ORR/OER.

ORR-OER					
TM	$\Delta G^*\text{OOH}$	$\Delta G^*\text{O}$	$\Delta G^*\text{OH}$	η_{ORR}	η_{OER}
Sc	3.99	3.51	0.64	0.75	1.64
Ti	3.05	1.85	-0.41	1.64	1.03
V	2.20	-0.20	-1.31	2.54	1.49
Cr	2.72	-0.05	-0.76	1.99	1.54
Mn	3.53	0.58	0.16	1.07	1.72
Fe	3.81	1.24	0.77	0.76	1.34
Co	3.67	2.07	0.91	0.32	0.37
Ni	4.63	3.33	1.55	0.94	0.55
Cu	5.20	1.81	2.53	1.95	2.16
Zn	4.88	0.96	1.68	1.95	2.69
Y	3.99	3.58	0.65	0.82	1.70
Zr	2.96	2.09	-0.51	1.74	1.37
Nb	1.36	-0.71	-2.14	3.37	2.33
Mo	0.16	-1.48	-1.71	2.94	3.53
Tc	0.49	-1.48	-1.19	2.42	3.20
Ru	2.08	-0.86	-0.44	1.67	1.71
Rh	3.54	1.25	0.35	0.88	1.06
Pd	4.49	3.24	1.50	0.80	0.51
Lu	3.89	3.50	0.52	0.84	1.75
Hf	2.72	1.94	-0.80	2.03	1.51
Ta	1.09	-0.82	-2.48	3.71	2.60
W	-0.83	-2.41	-2.21	3.44	4.52
Re	-0.86	-2.30	-1.62	2.85	4.55
Os	0.91	-1.57	-0.70	2.10	2.78
Ir	3.10	0.61	0.04	1.19	1.26
Pt	4.29	2.82	1.20	0.60	0.39

Table S12. Summary of Bifunctional catalysts, their supports and overpotentials (V).

CATALYSTS	Supports or Comments	η_{ORR}	η_{OER}	Refs.
Au	C ₂ N	0.38	0.79	Refs. ³⁸
Pd		0.40	0.71	
Cu		0.51	0.71	
Rh		0.67	0.37	
Ni		0.71	0.55	
Cd		0.81	1.54	
Ag		1.08	1.12	
Pt		1.14	0.40	
Ir		1.14	0.60	
Co		1.17	0.71	
Ru		1.24	0.92	
Fe		1.41	0.83	
Cr		1.45	1.85	
Os		1.46	1.09	
Zn		1.71	1.53	
Mn		1.81	1.56	
Mo		1.92	4.56	
V		2.09	3.61	
La		2.39	1.58	
Ta		2.62	5.99	
Nb		2.76	5.55	
Ti		2.84	4.52	
Y		2.85	2.02	
Sc		2.94	1.92	
Zr		3.13	4.86	
Hf		3.41	5.05	
W		3.47	6.01	
IrN ₄	G	0.26	0.30	Refs. ³⁹
Ir	pyrrolic-N ₄ -G	0.34	0.32	Refs. ⁴⁰
Co-Ag	MN ₄ -O-MN ₄	0.35	0.33	Refs. ⁴¹
Co-Cu		0.35	0.38	
Fe-Cu		0.36	0.41	
Co-Ni		0.43	0.42	
A-1	N-doped graphene nanoribbon	0.45	0.91	Refs. ⁴²
A-3		0.55	0.50	
Ad-1		1.09	1.72	
A-2		0.63	0.74	
Zd-2		0.63	1.21	
At-3		1.34	2.00	
Z-1		0.67	1.24	

Ad-2	N-doped graphene nanoribbon	0.77	1.07	Refs. ⁴²
Ad-3		0.77	1.42	
Z-2		0.85	0.95	
At-1		0.87	1.48	
At-4		0.87	1.49	
Z-3		0.88	0.96	
Zd-1		1.30	2.02	
2gN-1	N-doped graphene nanosheet	0.60	1.02	
1gN-1		0.65	0.67	
PC		1.03	1.08	
1pdN-1		1.17	1.09	
1prN-2		1.30	0.95	
3gN-1		1.39	2.08	
CoN1	N-doped graphene	0.94	1.68	Refs. ⁴³
CoN ₂ -opp		1.10	1.81	
CoN ₂ -pen		0.98	1.69	
CoN ₂ -hex		0.61	1.36	
CoN ₃		0.63	1.36	
CoN ₄		0.47	0.69	
CoN ₁	N-doped graphene	1.08	0.90	Refs. ⁴⁴
CoN ₂		0.69	0.63	
CoN ₃		0.53	0.73	
CoN ₄		0.30	0.41	
Ni-Mo ₂ B ₂ O ₂	MXenes	0.23	0.54	Refs. ⁴⁵
(001)	V ₄ C ₃	0.89	1.56	Refs. ⁴⁶
(110)		3.98	6.51	
(111)		2.84	6.68	
(001)	VC	1.11	1.91	
(110)		2.72	5.16	
(111)		4.11	7.66	
(001)	V ₈ C ₇	0.91	1.55	
(110)		2.39	5.68	
(111)		2.17	2.55	
Pure	M-cementite	0.89	1.52	Refs. ⁴⁷
Co dope at Fe1		0.85	1.55	
Co dope at Fe2		0.85	1.46	
Co dope at Fe3		0.88	1.50	
Co dope at Fe4		0.87	1.50	
Co dope at Fe		0.68	1.12	
Mn dope at Fe1		1.09	1.93	
Ni dope at Fe1		0.64	0.78	
TiC ₂	MC ₂	0.66	0.95	Refs. ⁴⁸
VC ₂		0.78	0.68	

NbC ₂	MC ₂	0.66	0.93	Refs. ⁴⁸
TaC ₂		0.37	0.72	
MoC ₂		0.47	0.45	
Ni _{1.5} Co _{1.5} N	PF/Ni _{1.5} Co _{1.5} N	1.18	1.81	Refs. ⁴⁹
PF/Ni _{1.5} Co _{1.5} N		0.68	1.02	
Nb ₂ CO ₂	Nb ₂ CT ₂	1.04	0.94	Refs. ⁵⁰
Nb ₂ CF ₂		1.01	1.57	
Nb ₂ CO ₂ –Pd		0.90	0.56	
Nb ₂ CO ₂ –Pt		0.72	1.11	
Nb ₂ CF ₂ –Pd		0.78	0.45	
Nb ₂ CF ₂ –Pt		0.71	0.52	
Nb ₂ CO ₂ –VO–Pd		0.51	0.46	
Nb ₂ CO ₂ –VO–Pt		0.47	0.39	
Nb ₂ CF ₂ –VF–Pd		0.47	0.88	
Nb ₂ CF ₂ –VF–Pt		0.40	0.37	
Sc	pyridine-4N	3.52	2.50	Refs. ⁵¹
Ti		2.79	2.10	
V		2.38	1.64	
Cr		1.20	1.89	
Mn		1.08	1.49	
Fe		0.42	0.72	
Co		0.50	0.37	
Ni		0.60	0.33	
Cu		0.57	0.48	
Zn		1.33	0.84	
Y		3.30	2.46	
Zr		2.52	1.94	
Nb		2.09	2.16	
Mo		1.23	1.78	
Tc		0.97	1.49	
Ru		0.89	0.45	
Rh		0.77	0.36	
Pd		1.64	1.31	
Ag		0.75	0.55	
Cd		1.30	0.66	
Hf		2.73	2.05	
Ta		2.42	1.72	
W		1.75	2.36	
Re		1.50	2.25	
Os		0.68	1.16	
Ir		0.94	0.37	
Pt		1.41	1.21	
Au		2.13	1.99	
Sc	pyrrole-4N	3.36	2.44	

	pyrrole-4N			Refs. ⁵¹
Ti		2.72	1.80	
V		2.25	1.71	
Cr		0.80	1.22	
Mn		0.59	1.20	
Fe		0.45	0.86	
Co		0.60	0.32	
Ni		1.47	0.85	
Cu		2.01	1.49	
Zn		2.18	1.45	
Y		3.57	2.81	
Zr		2.76	2.01	
Nb		1.66	2.28	
Mo		0.65	0.96	
Tc		0.40	1.13	
Ru		0.91	0.41	
Rh		1.69	0.91	
Pd		2.52	1.89	
Ag		2.55	1.82	
Cd		2.43	1.77	
Hf		2.87	2.18	
Ta		2.39	1.57	
W		1.40	2.29	
Re		0.68	0.88	
Os		0.47	0.62	
Ir		0.60	0.29	
Pt		1.67	0.94	
Au		2.83	2.11	

Supplementary Figures

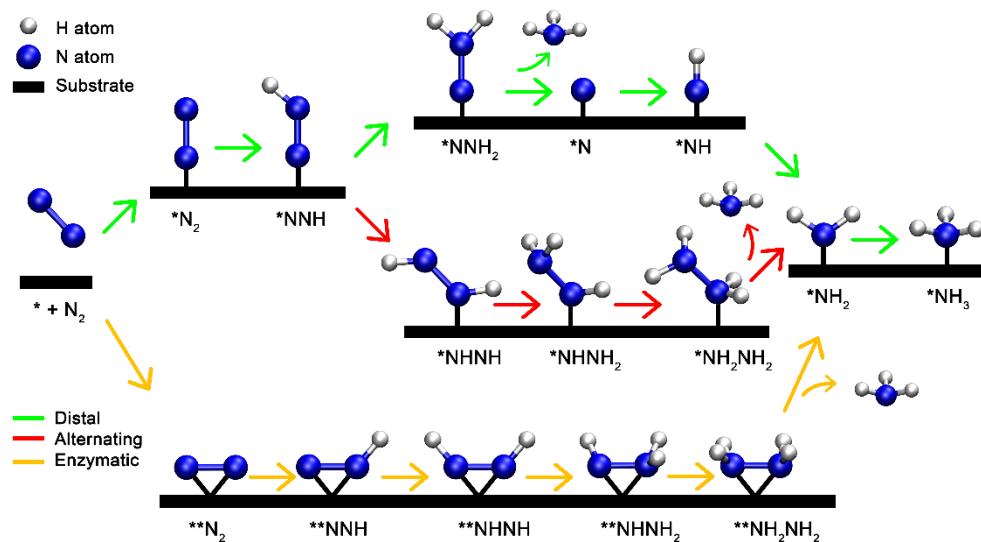


Fig. S1. Schematic depiction of possible reaction pathways of NRR. Imaginary atomic configurations of involved intermediates are illustrated. * means adsorption site. ** + intermediate (N_2 , NNH , NHNH , etc.) and * + intermediate are for side-on and end-on adsorption nitrogen fixed pathway respectively. Besides, the first N in $*\text{NN}$ means proximal nitrogen atom, and the second N means distal one.

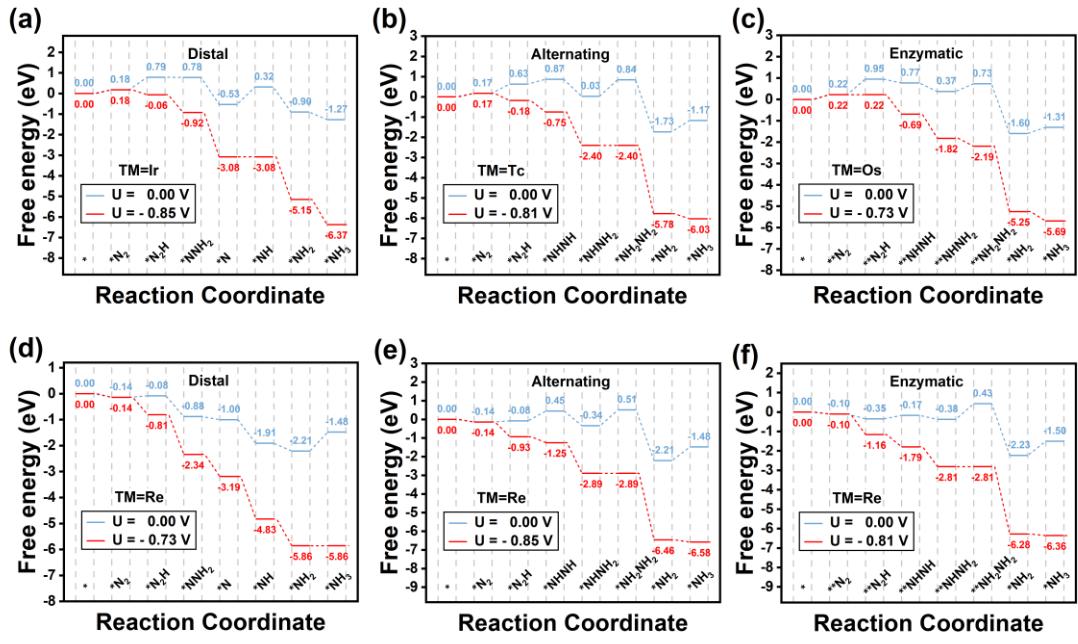


Fig. S2. Free-energy diagrams through various mechanisms for NRR on (a) Ir@BNNC, (b) Tc@BNNC, (c) Os@BNNC and (d-f) Re@BNNC at zero and applied potentials, respectively.

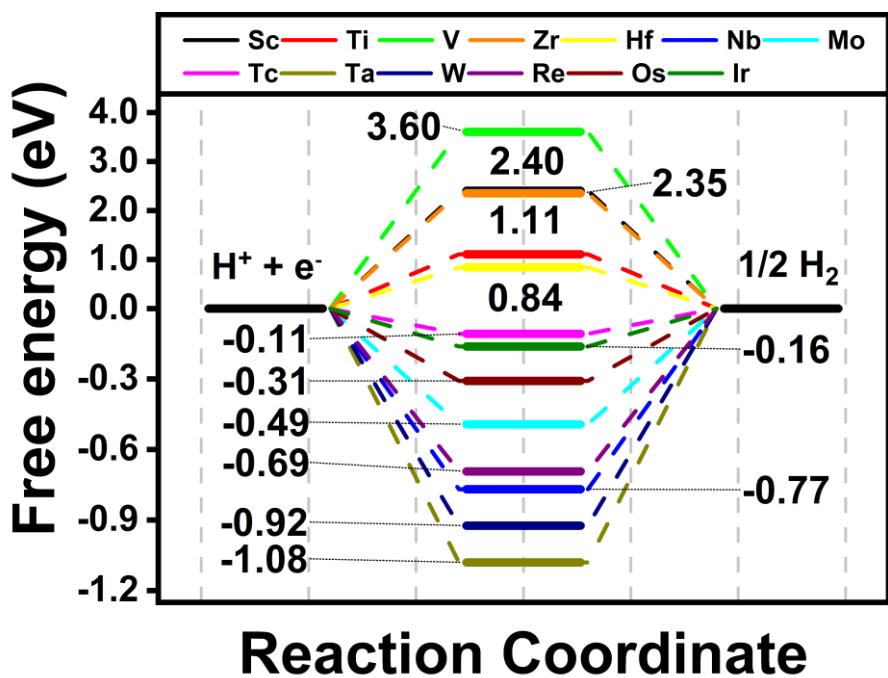


Fig. S3. The free energy changes of HER on TM@BNNCs that pass the screening.

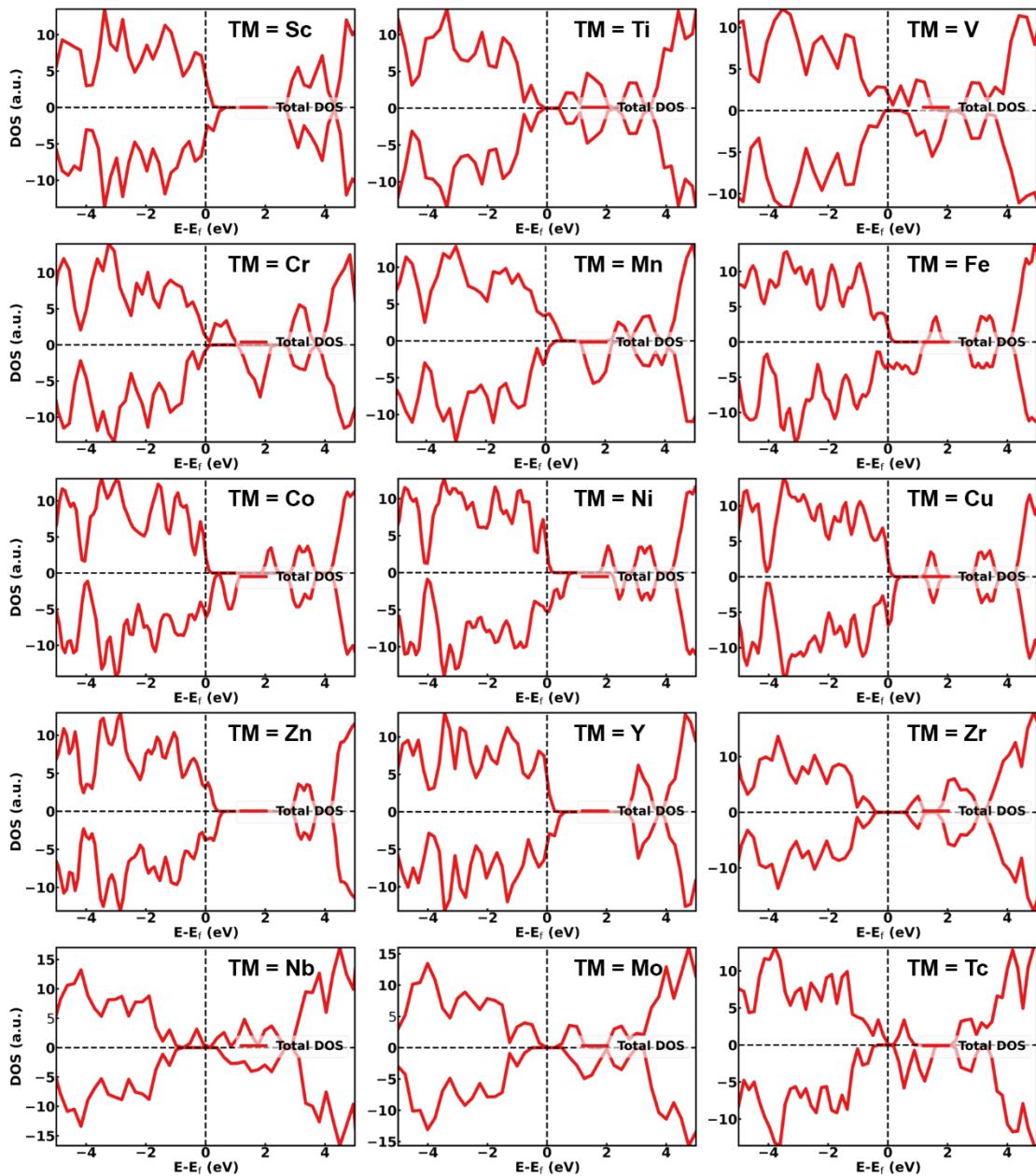


Fig. S4. Density of states (DOS) of TM@BNNCs (TM = Sc, Ti, V, Cr, Mn, Fe, Co, Ni, Cu, Zn, Y, Zr, Nb, Mo and Tc).

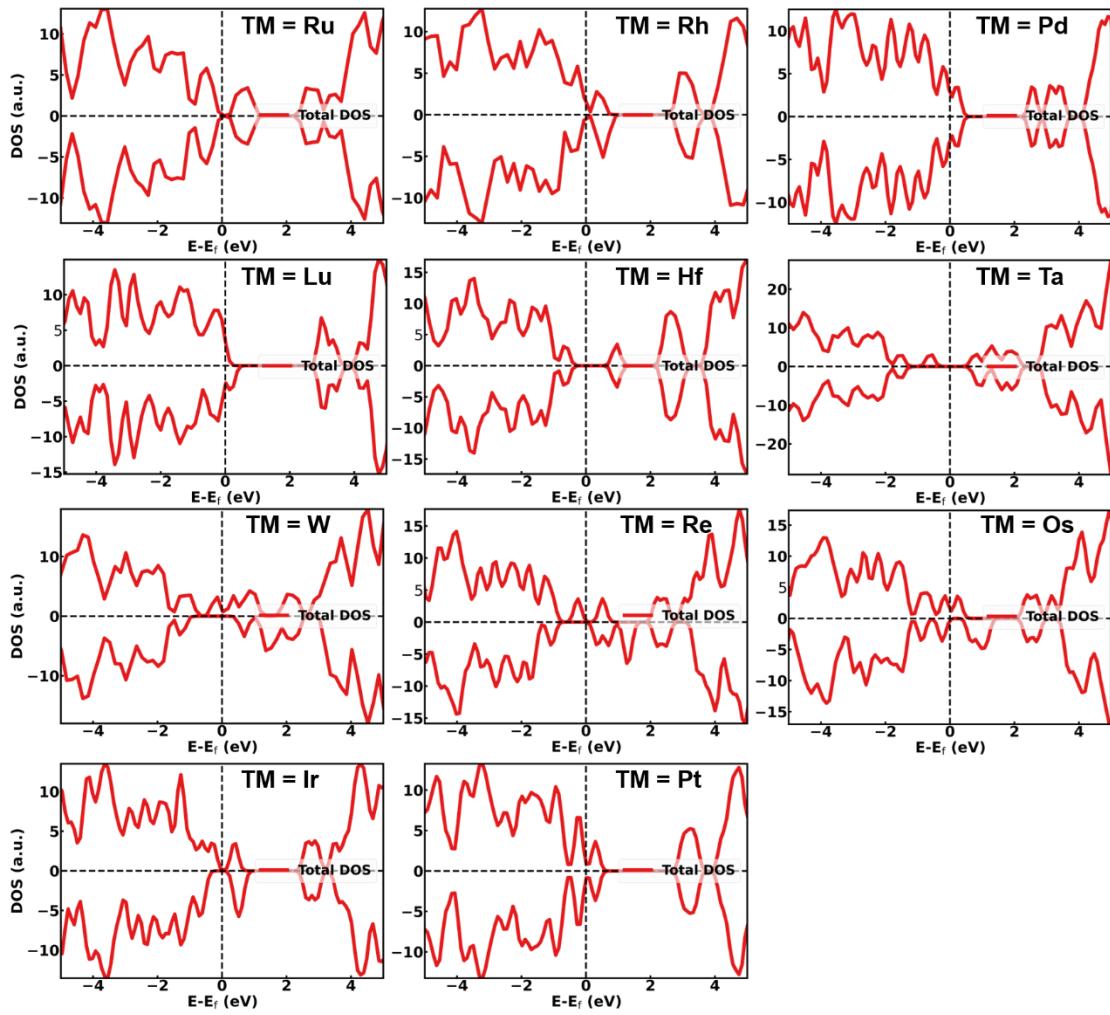


Fig. S5. Density of states (DOS) of TM@BNNCs (TM = Ru, Rh, Pd, Lu, Hf, Ta, W, Re, Os, Ir, and Pt).

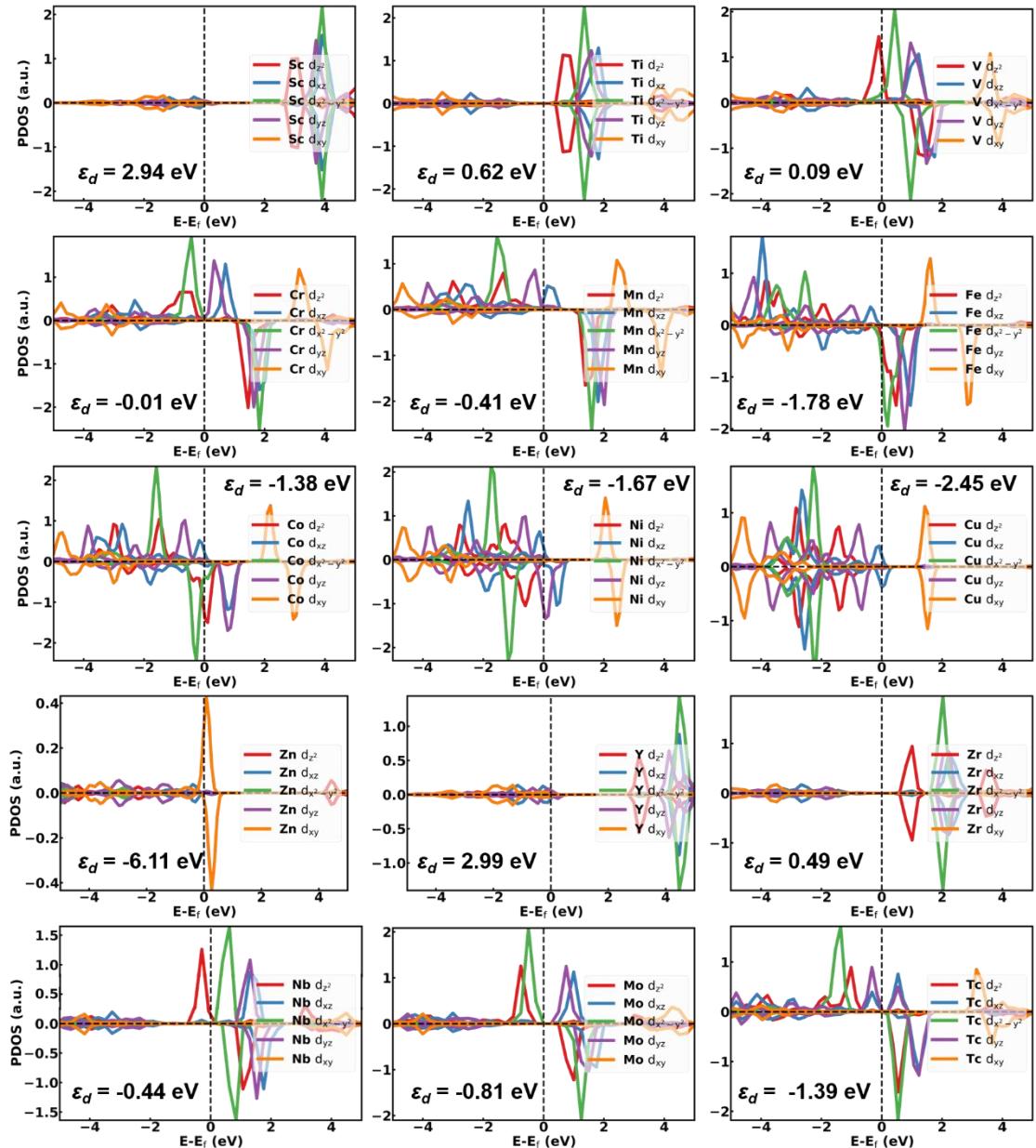


Fig. S6. Projected density of states (PDOS) of *d* orbitals and corresponding *d*-band centers for TM@BNNCs (TM = Sc, Ti, V, Cr, Mn, Fe, Co, Ni, Cu, Zn, Y, Zr, Nb, Mo and Tc).

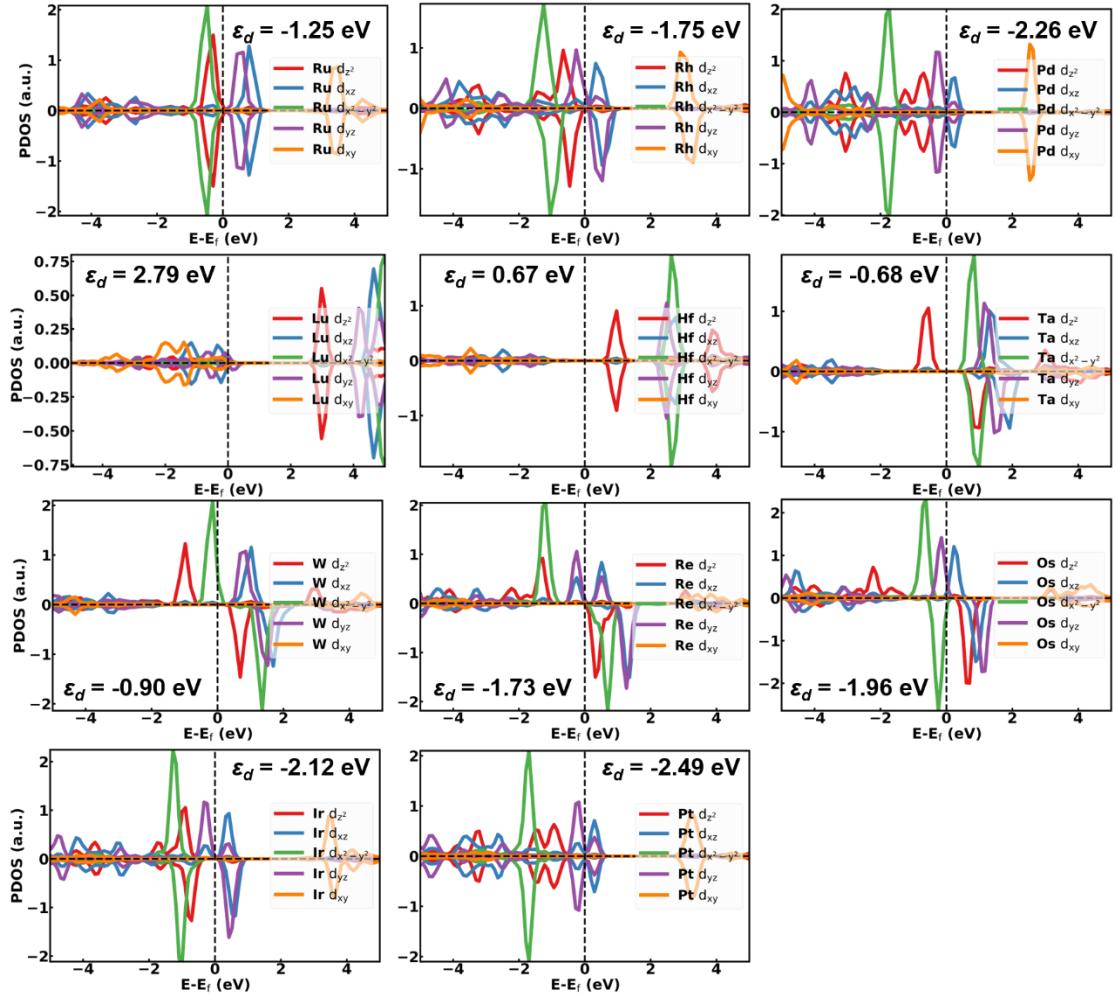


Fig. S7. Projected density of states (PDOS) of d orbitals and corresponding d -band centers for TM@BNNCs (TM = Ru, Rh, Pd, Lu, Hf, Ta, W, Re, Os, Ir, and Pt).

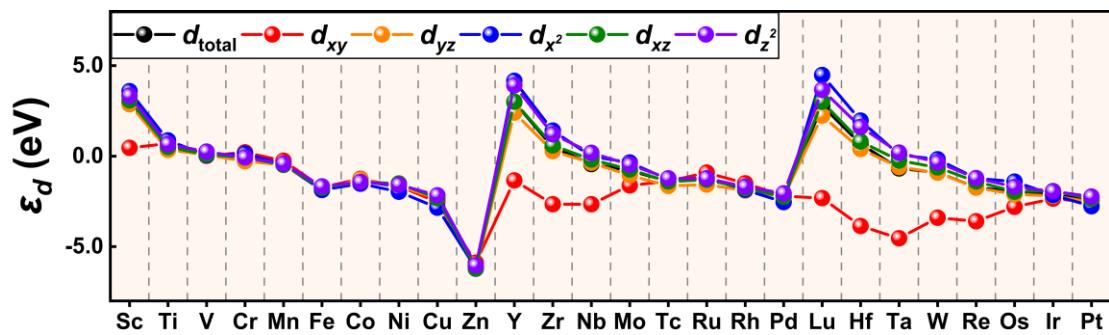


Fig. S8. d -band centers (ε_d) of d orbitals for TM@BNNCs (orbitals = d , d_{xy} , d_{yz} , d_x^2 , d_{xz} and d_z^2).

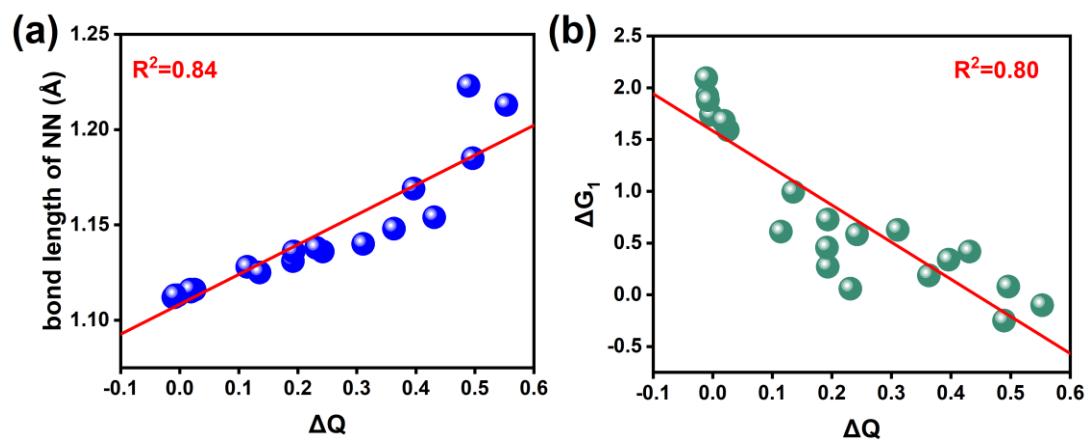


Fig. S9. The correlation of (a) ΔQ versus bond length of $*\text{N}_2$ and (b) ΔQ versus ΔG_1 on TM@BNNCs during various corresponding NRR pathways.

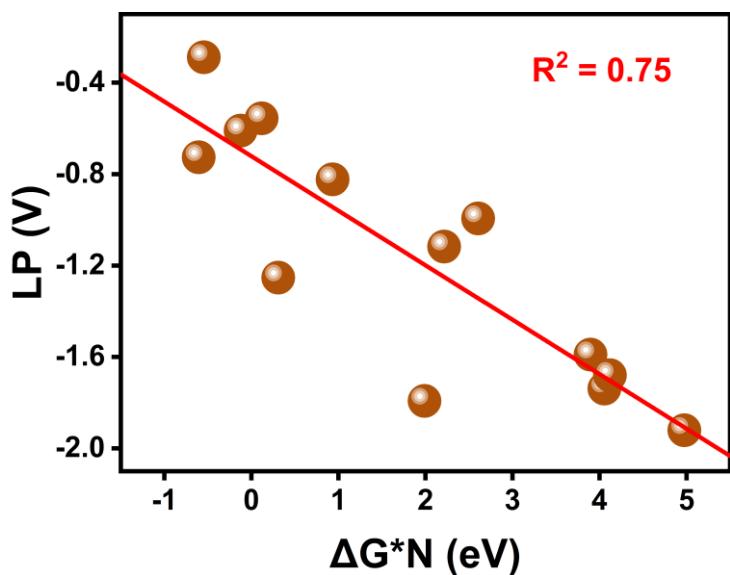


Fig. S10. The linear fit between LP and $\Delta G^*N = G^*N - G^*$. The catalysts are TM@BNNCs that pass the screening.

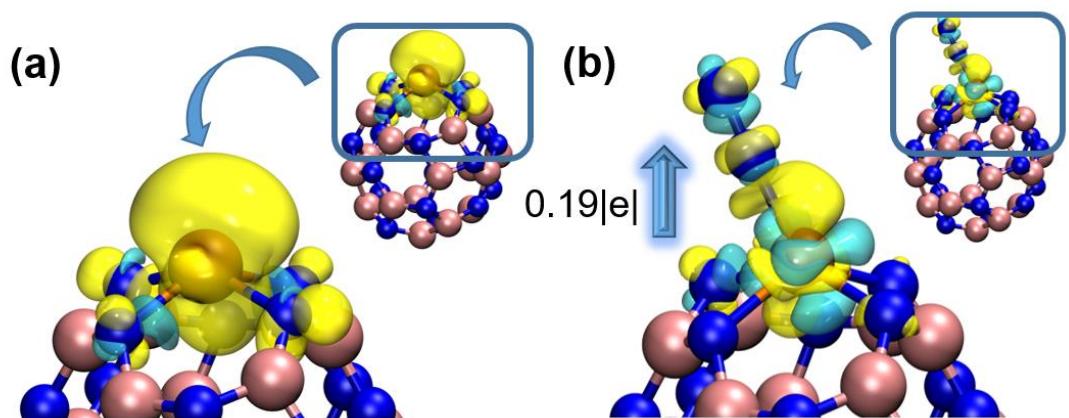


Fig. S11. (a) Magnetization distribution (spin density) and (b) charge difference (Charge density) with charge transfer from Os@BNNC to N₂ caused by adsorption of N₂.

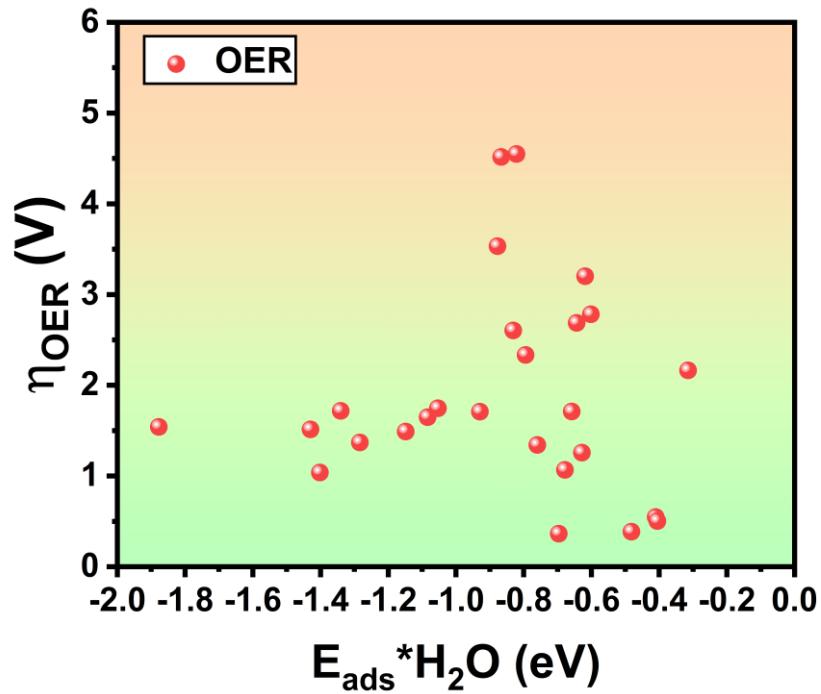


Fig. S12. The scatter plot of overpotential of OER with $E_{\text{ads}}(*\text{H}_2\text{O})$ for TM@BNNCs.

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