

Pressure-induced novel semiconductor materials with high dielectric constant in ZrN_4 : a first-principles study

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Table S1 The lattice parameters and Wyckoff positions of the eight novel phases(Å).

Phase	Lattice parameters (Å, degree)	Wyckoff positions						
		atom	site	x	y	z		
α - $P1$	$a = 6.433, b = 3.586, c = 8.961$ $\alpha = 88.9^\circ, \beta = 103.7^\circ, \gamma = 90.6^\circ$	Zr1	1a	0.211	0.601	0.608		
		Zr2	1a	0.815	0.098	0.511		
		N1	1a	0.052	0.142	0.085		
		N2	1a	0.643	0.682	0.009		
		N3	1a	0.506	0.484	-0.003		
		N4	1a	0.195	0.989	0.151		
		N5	1a	0.934	0.618	0.442		
		N6	1a	0.469	0.242	0.520		
P_4/mmm	$a = 3.711, b = 3.676, c = 4.020$ $\alpha = 90.0^\circ, \beta = 90.0^\circ, \gamma = 90.0^\circ$	Zr1	1b	1.000	1.000	0.500		
		N1	4i	1.000	0.500	0.152		
		α - $P\bar{1}$	$a = 3.998, b = 4.909, c = 5.161$ $\alpha = 76.2^\circ, \beta = 90.1^\circ, \gamma = 97.8^\circ$	Zr1	2i	-0.733	1.166	-1.282
				N1	2i	-0.297	0.602	-1.249
				N2	2i	-0.239	1.107	-1.414
				N3	2i	0.040	1.531	-1.885
		α - $P2_1/m$	$a = 4.381, b = 4.930, c = 4.017$ $\alpha = 90.0^\circ, \beta = 91.8^\circ, \gamma = 90.0^\circ$	N4	2i	-0.304	0.877	-1.175
				Zr1	2e	0.780	0.250	1.417
N1	2e			0.699	0.750	0.988		
N2	2e			0.317	0.250	1.658		
β - $P\bar{1}$	$a = 4.976, b = 4.459, c = 4.797$ $\alpha = 77.8^\circ, \beta = 100.8^\circ, \gamma = 111.4^\circ$	N3	4f	0.858	0.511	1.892		
		Zr1	2i	0.279	0.713	0.783		
		N1	2i	-0.032	-0.058	0.879		
		N2	2i	-0.237	0.032	0.687		
γ - $P\bar{1}$	$a = 4.111, b = 4.962, c = 4.443$ $\alpha = 78.6^\circ, \beta = 97.0^\circ, \gamma = 87.9^\circ$	N3	2i	-0.244	0.345	0.720		
		N4	2i	0.524	0.715	1.193		
		Zr1	2i	0.291	0.833	0.788		
		N1	2i	0.241	0.375	0.401		
β - $P2_1/m$	$a = 4.730, b = 4.898, c = 4.118$ $\alpha = 90.0^\circ, \beta = 109.2^\circ, \gamma = 90.0^\circ$	N2	2i	0.757	0.635	0.267		
		N3	2i	0.902	0.359	0.777		
		N4	2i	0.205	0.905	0.281		
		Zr1	2e	1.218	0.250	1.505		
β - $P1$	$a = 4.970, b = 4.462, c = 7.041$ $\alpha = 83.6^\circ, \beta = 74.5^\circ, \gamma = 107.4^\circ$	N1	2e	1.288	0.750	1.119		
		N2	2e	1.696	0.250	1.529		
		N3	4f	0.858	0.490	0.046		
		Zr1	1a	0.728	0.933	0.315		
		Zr2	1a	0.082	0.347	0.708		
		Zr3	1a	0.446	0.869	0.960		
		N1	1a	0.436	0.355	0.067		
		N2	1a	0.718	0.308	0.044		

N3	1a	0.261	0.920	0.322
N4	1a	0.111	0.813	0.540
N5	1a	0.651	0.361	0.439
N6	1a	0.594	0.345	0.663
N7	1a	0.404	0.435	0.399
N8	1a	0.578	0.651	0.691
N9	1a	0.268	0.248	0.274
N10	1a	0.863	0.915	0.586
N11	1a	0.972	0.601	0.965
N12	1a	0.892	0.875	0.983

Table S2 Variation of lattice constants normalized with respect to their respective ground state values (i.e. $\Delta a=(a_{150}-a_0)/a_0\times 100\%$, $\Delta b=(b_{150}-b_0)/b_0\times 100\%$, $\Delta c=(c_{150}-c_0)/c_0\times 100\%$) for ZrN_4 semiconductor phases at 150 GPa.

Phase	Δa	Δb	Δc
$\alpha\text{-}P\bar{1}$	-22.23	-15.28	-2.92
$\beta\text{-}P\bar{1}$	-20.85	-18.25	5.93
$\gamma\text{-}P\bar{1}$	-10.72	-11.2	-8.08
$\beta\text{-}P1$	-14.79	-6.21	-15.81

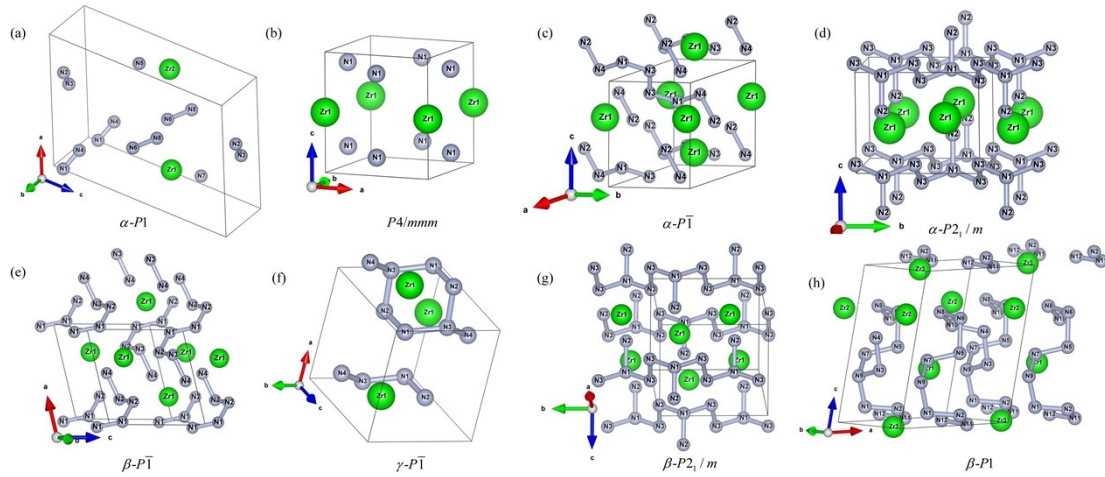


Fig. S1 Configurations of the nitrogen chains in (a) $\alpha\text{-}P1$, (b) $P4/mmm$, (c) $\alpha\text{-}P\bar{1}$, (d) $\alpha\text{-}P2_1/m$, (e) $\beta\text{-}P\bar{1}$, (f) $\gamma\text{-}P\bar{1}$, (g) $\beta\text{-}P2_1/m$, and (h) $\beta\text{-}P1$ phase for ZrN_4 at 0 GPa. The green and gray balls denote the Zr and N atoms, respectively.

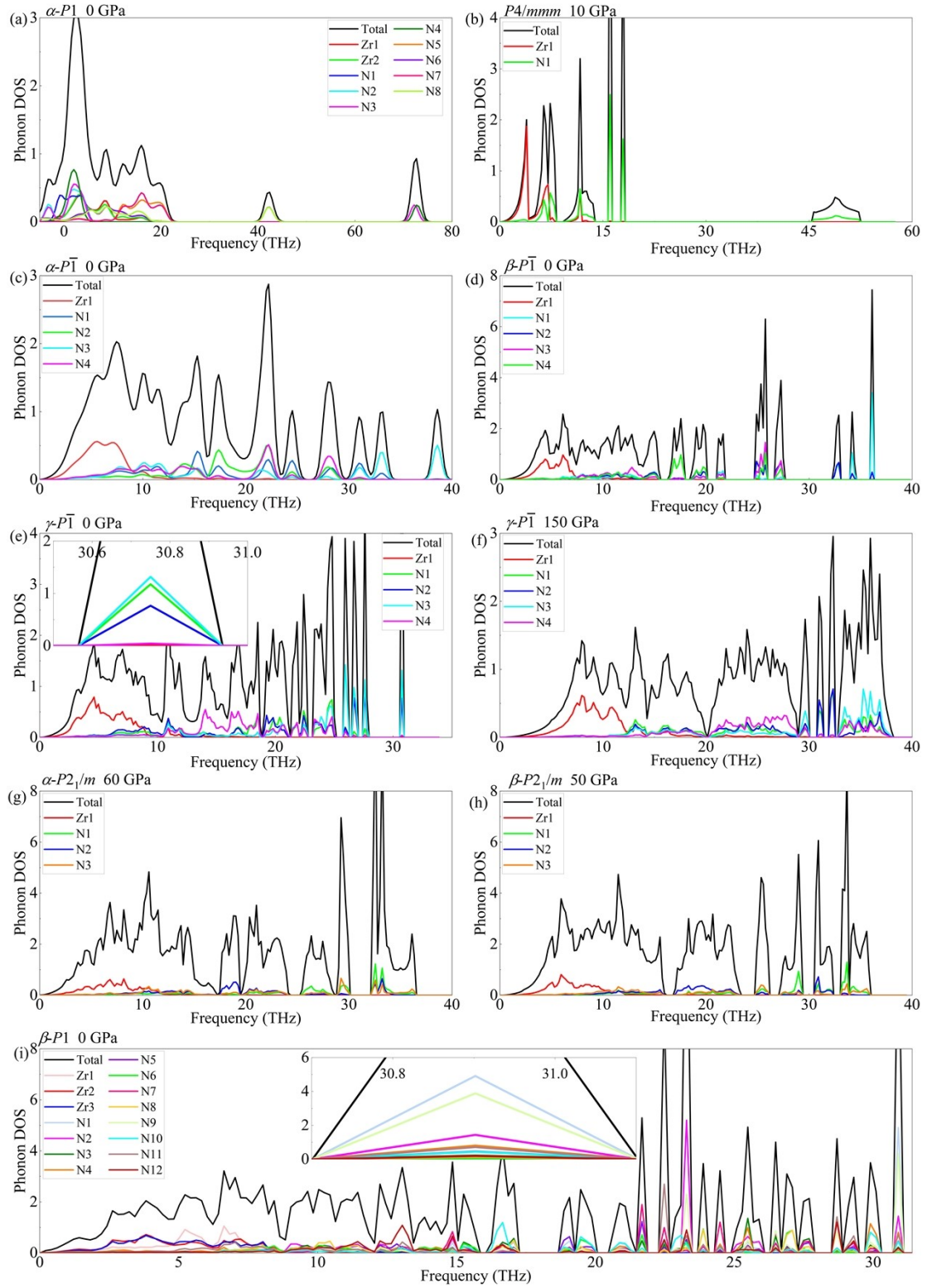


Fig. S2 Total phonon DOS and Partial phonon DOS for Zr and N atoms in ZrN₄. The inset in (e) and (i) shows the phonon DOS in the frequency range of 30.5–31 GPa and 30.7–31.1 GPa, respectively.

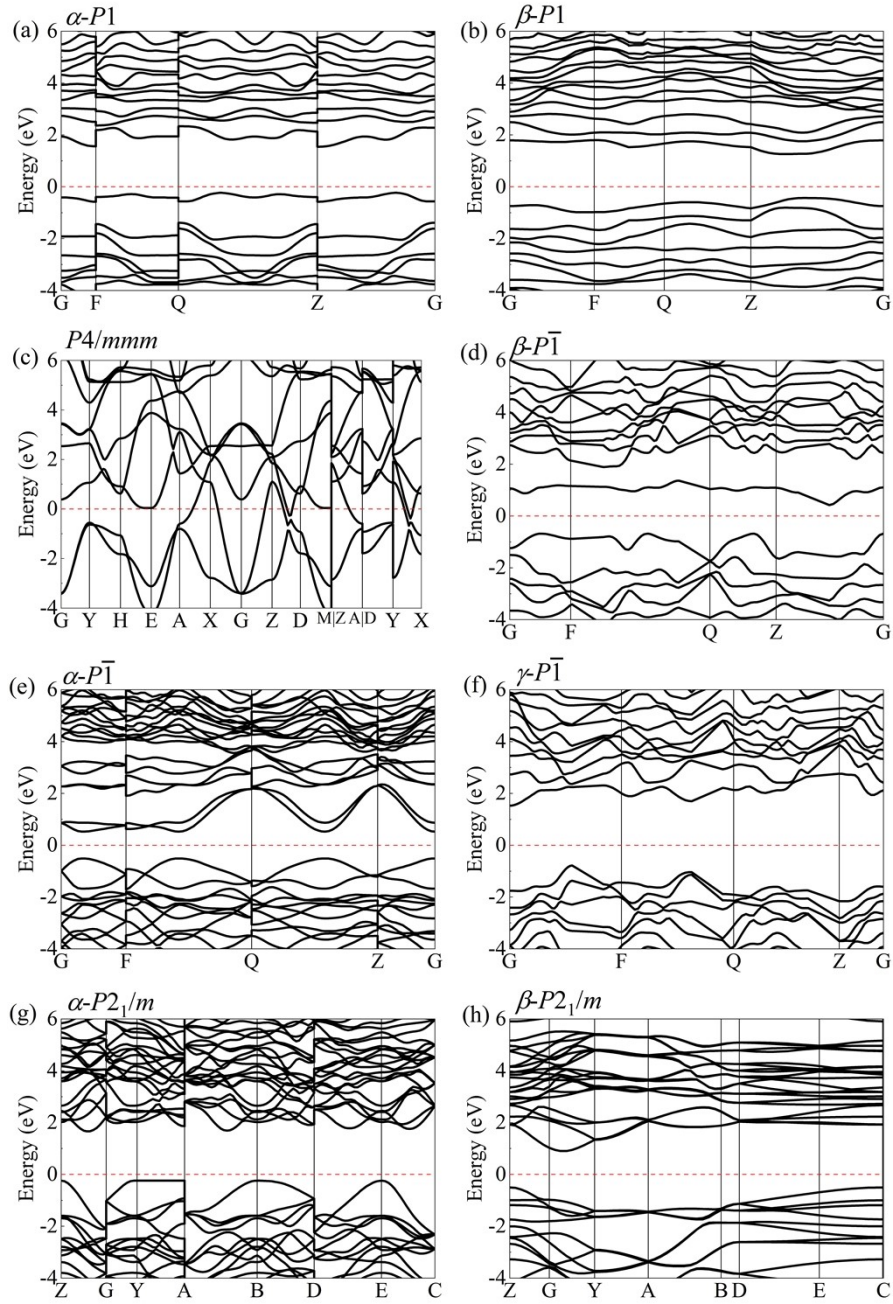


Fig. S3 The band of (a) α -P1, (b) β -P1, (c) $P4/mmm$, (d) β - $P\bar{1}$, (e) α - $P\bar{1}$, (f) γ - $P\bar{1}$, (g) α - $P2_1/m$, and (h) β - $P2_1/m$ under HSE06 functional.