

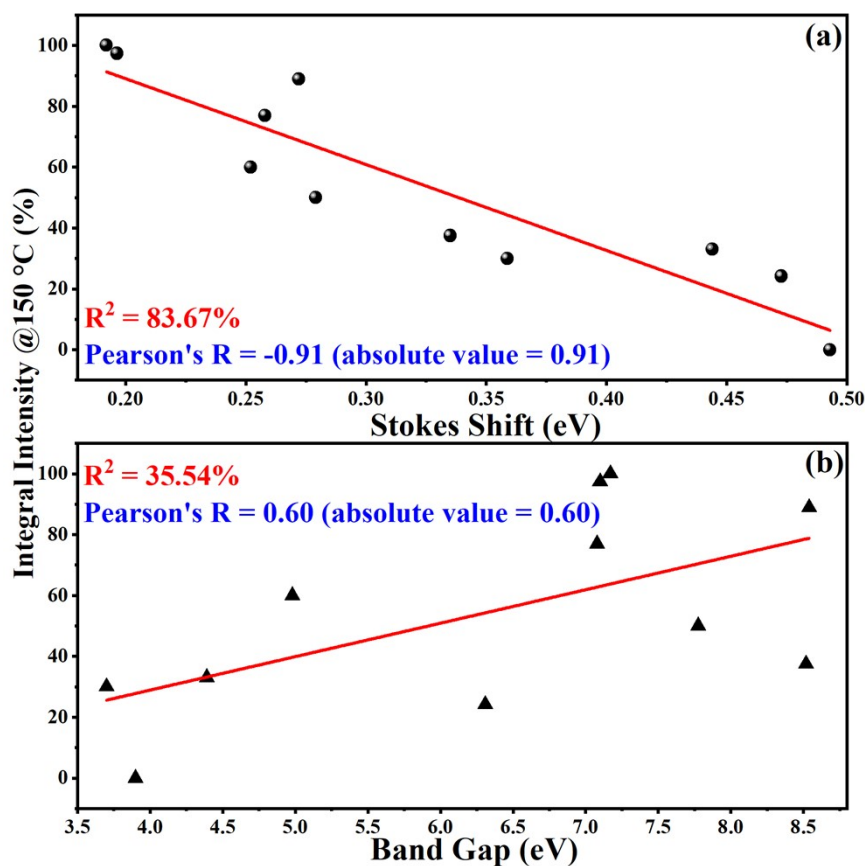
## Quantifying rigidity for thermally stable Cr<sup>3+</sup> phosphors

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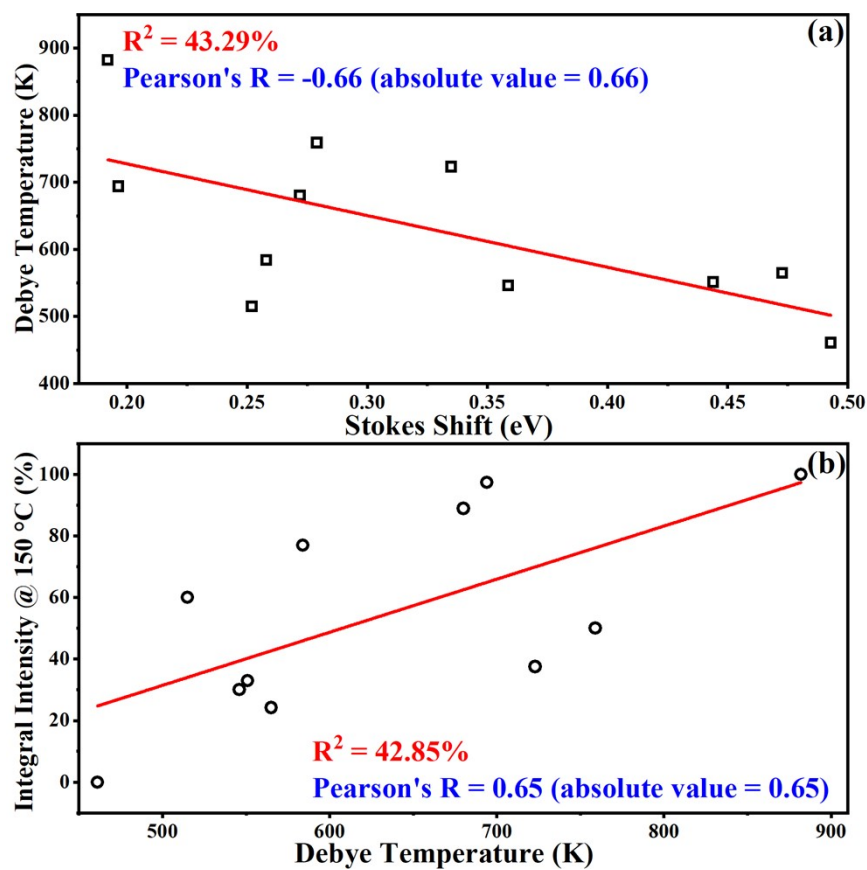
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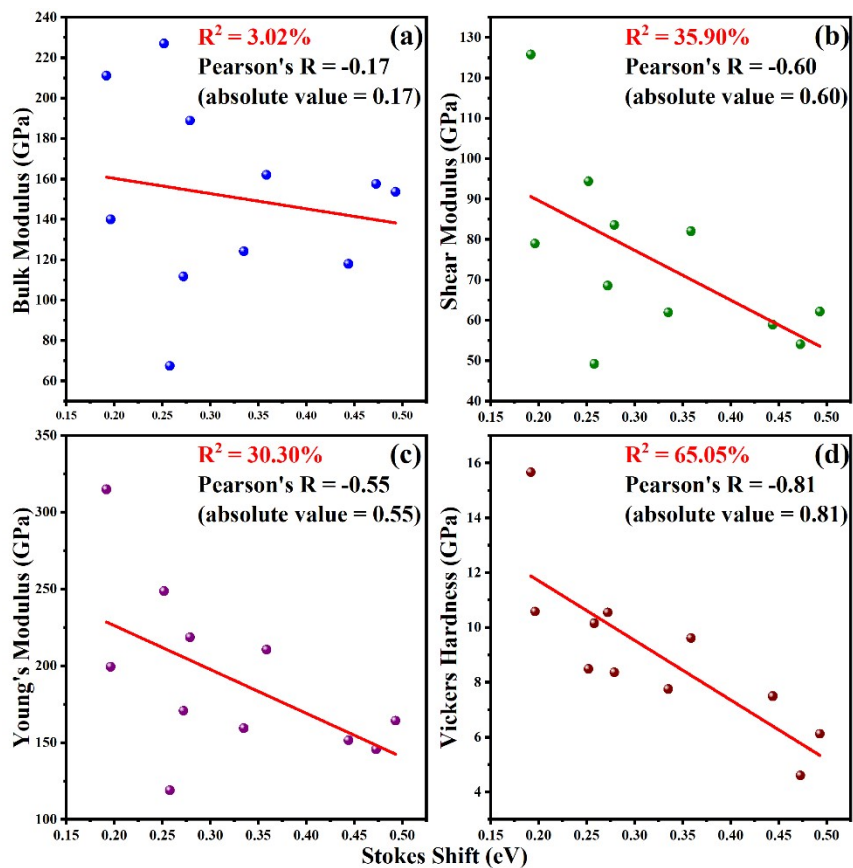
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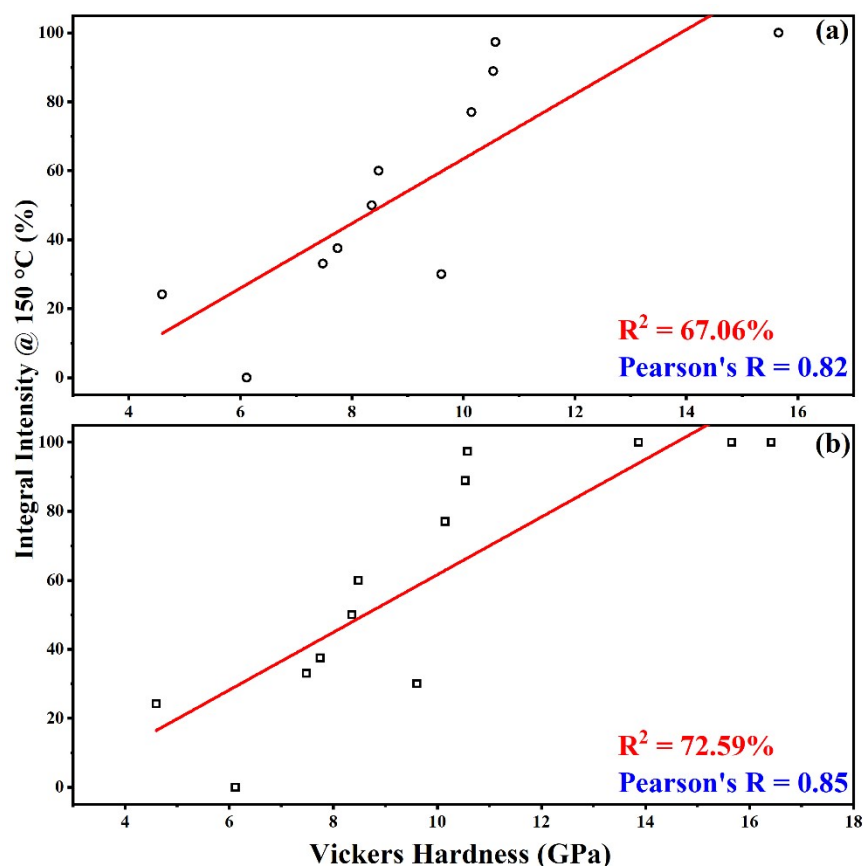
**Figure S1.** Correlation analysis of (a) Stokes shift vs thermal stability and (b) band gap vs thermal stability for Cr<sup>3+</sup>-doped phosphors (SrAl<sub>12</sub>O<sub>19</sub>, Ca<sub>3</sub>Sc<sub>2</sub>Si<sub>3</sub>O<sub>12</sub>, CaMgSi<sub>2</sub>O<sub>6</sub>, KAlP<sub>2</sub>O<sub>7</sub>, GaTaO<sub>4</sub>, ScBO<sub>3</sub>, Mg<sub>2</sub>B<sub>2</sub>O<sub>5</sub>, Mg<sub>2</sub>Ge<sub>2</sub>O<sub>6</sub>, Mg<sub>4</sub>Ta<sub>2</sub>O<sub>9</sub>, LaSc<sub>3</sub>(BO<sub>3</sub>)<sub>4</sub> and LiIn<sub>2</sub>SbO<sub>6</sub>). Pearson's R, also known as Pearson correlation coefficient, is a measure of linear correlation between two sets of data. Pearson's R ranged from -1 to 1, representing the negative to a positive correlation. The high absolute Pearson's R-value (close to -1 or 1) implies a strong correlation between the two sets of data while the low absolute Pearson's R-value (close to 0) implies a weak correlation.



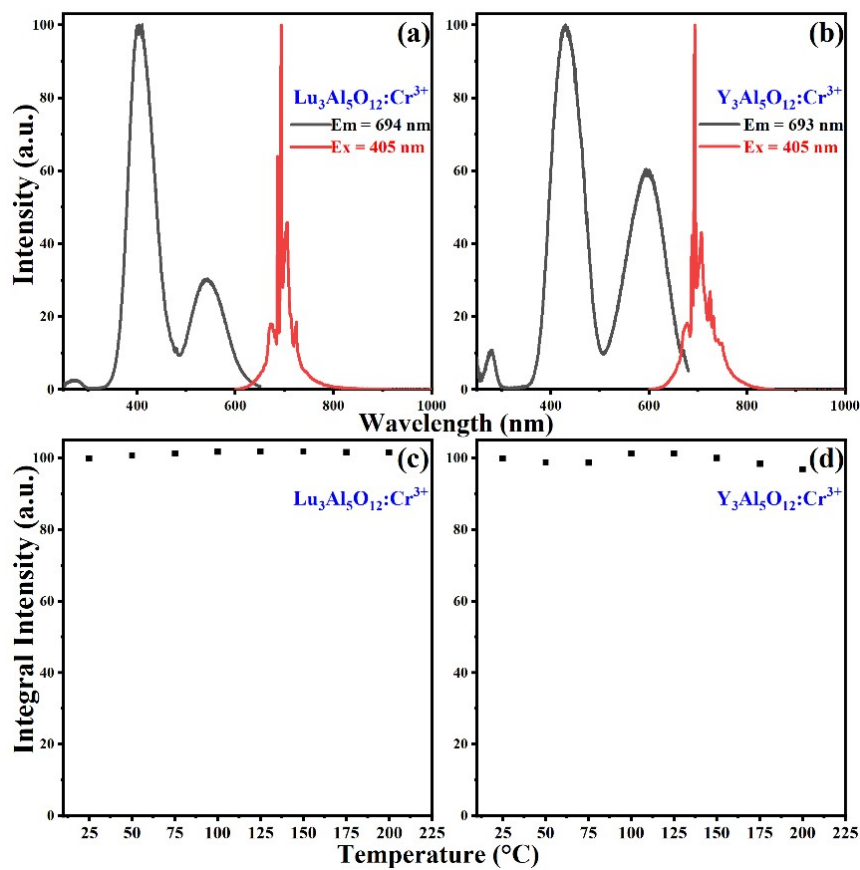
**Figure S2.** Correlation analysis of (a) Stokes shift vs Debye temperature and (b) Debye temperature and thermal stability for Cr<sup>3+</sup>-doped phosphors (SrAl<sub>12</sub>O<sub>19</sub>, Ca<sub>3</sub>Sc<sub>2</sub>Si<sub>3</sub>O<sub>12</sub>, CaMgSi<sub>2</sub>O<sub>6</sub>, KAlP<sub>2</sub>O<sub>7</sub>, GaTaO<sub>4</sub>, ScBO<sub>3</sub>, Mg<sub>2</sub>B<sub>2</sub>O<sub>5</sub>, Mg<sub>2</sub>Ge<sub>2</sub>O<sub>6</sub>, Mg<sub>4</sub>Ta<sub>2</sub>O<sub>9</sub>, LaSc<sub>3</sub>(BO<sub>3</sub>)<sub>4</sub> and LiIn<sub>2</sub>SbO<sub>6</sub>).



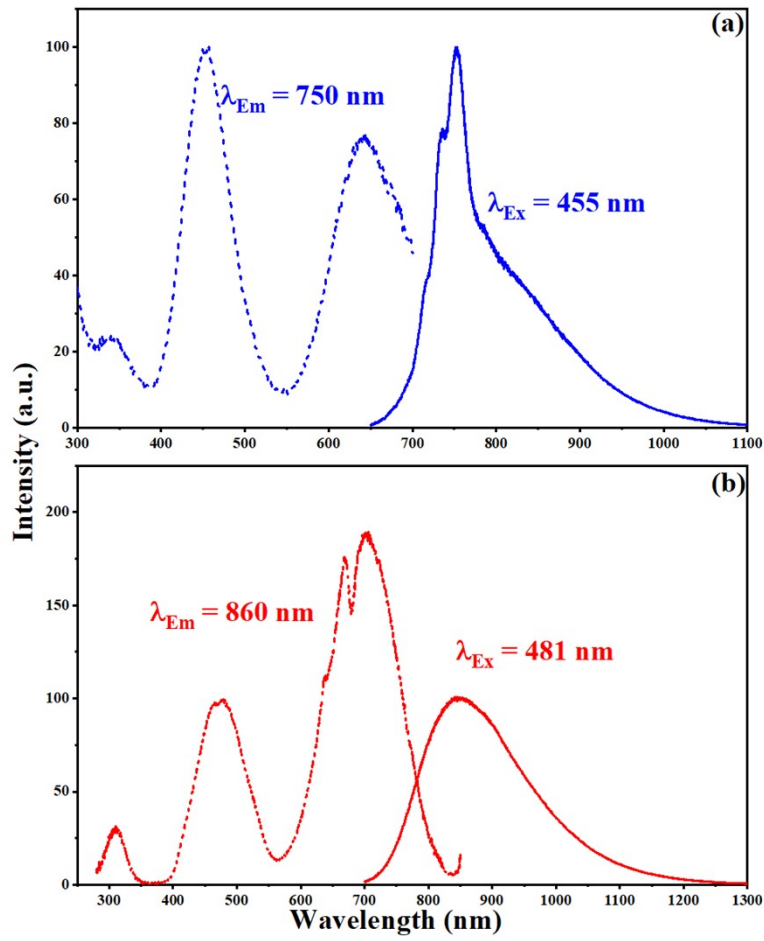
**Figure S3.** Correlation analysis of (a) Stokes vs Bulk modulus, (b) Stokes vs shear modulus, (c) Stokes vs Young's modulus and (d) Stokes vs Vickers hardness for Cr<sup>3+</sup>-doped phosphors (SrAl<sub>12</sub>O<sub>19</sub>, Ca<sub>3</sub>Sc<sub>2</sub>Si<sub>3</sub>O<sub>12</sub>, CaMgSi<sub>2</sub>O<sub>6</sub>, KAlP<sub>2</sub>O<sub>7</sub>, GaTaO<sub>4</sub>, ScBO<sub>3</sub>, Mg<sub>2</sub>B<sub>2</sub>O<sub>5</sub>, Mg<sub>2</sub>Ge<sub>2</sub>O<sub>6</sub>, Mg<sub>4</sub>Ta<sub>2</sub>O<sub>9</sub>, LaSc<sub>3</sub>(BO<sub>3</sub>)<sub>4</sub> and LiIn<sub>2</sub>SbO<sub>6</sub>).



**Figure S4.** Correlation analysis of Vickers hardness vs thermal stabilities of for  $\text{Cr}^{3+}$ -doped phosphors (a)  $\text{SrAl}_{12}\text{O}_{19}$ ,  $\text{Ca}_3\text{Sc}_2\text{Si}_3\text{O}_{12}$ ,  $\text{CaMgSi}_2\text{O}_6$ ,  $\text{KAlP}_2\text{O}_7$ ,  $\text{GaTaO}_4$ ,  $\text{ScBO}_3$ ,  $\text{Mg}_2\text{B}_2\text{O}_5$ ,  $\text{Mg}_2\text{Ge}_2\text{O}_6$ ,  $\text{Mg}_4\text{Ta}_2\text{O}_9$ ,  $\text{LaSc}_3(\text{BO}_3)_4$  and  $\text{LiIn}_2\text{SbO}_6$ , (b)  $\text{Lu}_3\text{Al}_5\text{O}_{12}$ ,  $\text{Y}_3\text{Al}_5\text{O}_{12}$ ,  $\text{SrAl}_{12}\text{O}_{19}$ ,  $\text{Ca}_3\text{Sc}_2\text{Si}_3\text{O}_{12}$ ,  $\text{CaMgSi}_2\text{O}_6$ ,  $\text{KAlP}_2\text{O}_7$ ,  $\text{GaTaO}_4$ ,  $\text{ScBO}_3$ ,  $\text{Mg}_2\text{B}_2\text{O}_5$ ,  $\text{Mg}_2\text{Ge}_2\text{O}_6$ ,  $\text{Mg}_4\text{Ta}_2\text{O}_9$ ,  $\text{LaSc}_3(\text{BO}_3)_4$  and  $\text{LiIn}_2\text{SbO}_6$ .



**Figure S5.** (a) PL and PLE spectra of  $\text{Lu}_3\text{Al}_5\text{O}_{12}:\text{Cr}^{3+}$ , (b) PL and PLE spectra of  $\text{Y}_3\text{Al}_5\text{O}_{12}:\text{Cr}^{3+}$ , (c) integral emission intensity of  $\text{Lu}_3\text{Al}_5\text{O}_{12}:\text{Cr}^{3+}$  dependent on temperature, (d) integral emission intensity of  $\text{Y}_3\text{Al}_5\text{O}_{12}:\text{Cr}^{3+}$  dependent on temperature.



**Figure S6.** PL and PLE spectra of (a) La<sub>2</sub>MgSnO<sub>6</sub>:Cr<sup>3+</sup> and (b) KMg(PO<sub>3</sub>)<sub>3</sub>:Cr<sup>3+</sup>.

**Table S1.** K-points setting of the systems.

System	K-point mesh (for PBEsol)	K-point mesh (for HSE06)
Lu <sub>3</sub> Al <sub>5</sub> O <sub>12</sub>	2×2×2	-
Y <sub>3</sub> Al <sub>5</sub> O <sub>12</sub>	2×2×2	-
SrAl <sub>12</sub> O <sub>19</sub>	5×5×1	-
Ca <sub>3</sub> Sc <sub>2</sub> Si <sub>3</sub> O <sub>12</sub>	2×2×2	-
CaMgSi <sub>2</sub> O <sub>6</sub>	3×3×5	-
KAlP <sub>2</sub> O <sub>7</sub>	4×3×3	1×1×1
GaTaO <sub>4</sub>	5×4×5	-
ScBO <sub>3</sub>	9×9×2	-
Mg <sub>2</sub> B <sub>2</sub> O <sub>5</sub>	4×3×8	2×2×2
Mg <sub>2</sub> Ge <sub>2</sub> O <sub>6</sub>	1×3×5	1×3×5
Mg <sub>4</sub> Ta <sub>2</sub> O <sub>9</sub>	9×9×2	-
LaSc <sub>3</sub> (BO <sub>3</sub> ) <sub>4</sub>	3×3×2	1×1×1
LiIn <sub>2</sub> SbO <sub>6</sub>	5×5×3	-
KMg(PO <sub>3</sub> ) <sub>3</sub>	4×4×3	2×2×1
La <sub>2</sub> MgSnO <sub>6</sub>	6×6×4	3×3×2



**Table S2.** Electron configurations for atoms in the calculations.

Atom	Configuration
Li	$2s^1$
B	$2s^2 2p^1$
O	$2s^2 2p^4$
Mg	$3s^2$
Al	$3s^2 3p^1$
Si	$3s^2 3p^2$
P	$3s^2 3p^3$
K	$3p^6 4s^1$
Ca	$3p^6 4s^2$
Sc	$3d^2 4s^1$
Ga	$4s^2 4p^1$
Ge	$4s^2 4p^2$
Sr	$4s^2 4p^6 5s^2$
Y	$4s^2 4p^6 4d^2 5s^1$
In	$5s^2 5p^1$
Sn	$5s^2 5p^2$
Sb	$5s^2 5p^3$
La	$5p^6 5d^1 6s^2$
Lu	$4f^{14} 5s^2 5p^6 5d^1 6s^2$
Ta	$5d^4 6s^1$

**Table S3.** Cell parameters of  $Y_3Al_5O_{12}$ ,  $Ca_3Sc_2Si_3O_{12}$ ,  $CaMgSi_2O_6$ ,  $GaTaO_4$ ,  $ScBO_3$  and  $LaSc_3(BO_3)_4$  from experimental data (Exp) and calculations by PBE and PBEsol functionals.

		a (Å)	b (Å)	c (Å)	V (Å <sup>3</sup> )	
$Y_3Al_5O_{12}$	Exp <sup>1</sup>	11.9900	11.9900	11.9900	1723.6835	
	PBE	12.1075	12.1075	12.1075	1774.8581	
	PBEsol	11.9958	11.9958	11.9958	1726.1871	
	PBE-Error	+0.98%	+0.98%	+0.98%	+2.97%	
	PBEsol-Error	+0.05%	+0.05%	+0.05%	+0.14%	
		a (Å)	b (Å)	c (Å)	V (Å <sup>3</sup> )	
$Ca_3Sc_2Si_3O_{12}$	Exp <sup>2</sup>	12.2500	12.2500	12.2500	1838.2656	
	PBE	12.3281	12.3281	12.3281	1873.6430	
	PBEsol	12.2008	12.2008	12.2008	1816.1975	
	PBE-Error	+0.64%	+0.64%	+0.64%	+1.92%	
	PBEsol-Error	-0.40%	-0.40%	-0.40%	-1.20%	
		a (Å)	b (Å)	c (Å)	$\beta$ (°)	V (Å <sup>3</sup> )
$CaMgSi_2O_6$	Exp <sup>3</sup>	9.7500	8.9260	5.2510	105.90	439.5029
	PBE	9.8588	9.0017	5.3080	106.06	452.6815
	PBEsol	9.7658	8.8985	5.2624	105.99	439.6119
	PBE-Error	+1.12%	+0.85%	+1.08%	+0.15%	+3.00%
	PBEsol-Error	+0.16%	-0.31%	+0.22%	+0.08%	+0.02%
		a (Å)	b (Å)	c (Å)	$\beta$ (°)	V (Å <sup>3</sup> )
$GaTaO_4$	Exp <sup>4</sup>	4.5879	5.5673	4.9589	90.20	126.6606
	PBE	4.6490	5.6495	5.0324	90.33	132.1715
	PBEsol	4.6093	5.5882	4.9863	90.51	128.4324
	PBE-Error	+1.33%	+1.48%	+1.48%	+0.15%	+4.35%
	PBEsol-Error	+0.47%	+0.38%	+0.55%	+0.35%	+1.40%
		a (Å)	b (Å)	c (Å)	V (Å <sup>3</sup> )	
$ScBO_3$	Exp <sup>5</sup>	4.7480	4.7480	15.2620	297.9638	
	PBE	4.7816	4.7816	15.3386	303.7162	
	PBEsol	4.7425	4.7425	15.1669	295.4189	
	PBE-Error	+0.71%	+0.71%	+0.50%	+1.93%	
	PBEsol-Error	-0.12%	-0.12%	-0.62%	-0.85%	

**Table S4.** Vickers hardness and Debye temperature data of the materials.

Material	Vickers Hardness (Gpa)	Debye Temperature (K)
$\text{Lu}_3\text{Al}_5\text{O}_{12}$	16.42	675
$\text{Y}_3\text{Al}_5\text{O}_{12}$	13.87	728
$\text{SrAl}_{12}\text{O}_{19}$	15.66	882
$\text{Ca}_3\text{Sc}_2\text{Si}_3\text{O}_{12}$	10.58	694
$\text{CaMgSi}_2\text{O}_6$	10.54	680
$\text{KAlP}_2\text{O}_7$	10.15	584
$\text{GaTaO}_4$	8.49	515
$\text{ScBO}_3$	8.36	759
$\text{Mg}_2\text{B}_2\text{O}_5$	7.75	723
$\text{Mg}_2\text{Ge}_2\text{O}_6$	7.49	551
$\text{Mg}_4\text{Ta}_2\text{O}_9$	9.61	546
$\text{LaSc}_3(\text{BO}_3)_4$	4.60	565
$\text{LiIn}_2\text{SbO}_6$	6.11	461

**Table S5.** Elastic parameters and band gap values of  $\text{La}_2\text{MgSnO}_6$  and  $\text{KMg}(\text{PO}_3)_3$ .

Material	Bulk modulus (GPa)	Shear modulus (GPa)	Young modulus (GPa)	Poisson ratio	Vickers hardness (Gpa)	Debye Temp (K)	Band Gap (eV)
$\text{La}_2\text{MgSnO}_6$	149.996	77.332	197.973	0.28	9.410	480.83	5.77
$\text{KMg}(\text{PO}_3)_3$	59.494	38.574	95.157	0.23	7.463	529.58	6.62

## References:

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