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Supplementary Information

Device Parameter to Evaluate Exciton Energy Transfer in Organic Whispering-Gallery-Mode Microresonators and its Dependence on the Amplified Spontaneous Emission Threshold

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Figure S1. Dependence of photoluminescence spectra on the excitation intensity I_{ex} [(upper) $I_{ex} = 8.0 \ \mu J \ mm^{-2}$, (middle) $I_{ex} = 1.6 \ \mu J \ mm^{-2}$, (lower) $I_{ex} = 0.1 \ \mu J \ mm^{-2}$].

The dependence of simulated electric fields on dt



Figure S2. Simulated spectra of the electric fields horizontal to the substrates for (a) $d_t = 124.5$ nm, (b) $d_t = 70$ nm, and (c) $d_t = 35$ nm.



Figure S3. Dependence of the photoluminescence spectrum on the excitation intensity (I_{ex}) for (a) $d_{C545T} = 6 \text{ nm} [(\text{top}) I_{ex} = 10 \,\mu\text{J} \text{ mm}^{-2}, (\text{middle}) I_{ex} = 4.1 \,\mu\text{J} \text{ mm}^{-2}, (\text{bottom}) I_{ex} = 0.8 \,\mu\text{J} \text{ mm}^{-2}]$ and (b) $d_{C545T} = 2 \text{ nm} [(\text{top}) I_{ex} = 24 \,\mu\text{J} \text{ mm}^{-2}, (\text{middle}) I_{ex} = 7.6 \,\mu\text{J} \text{ mm}^{-2}, (\text{top}) I_{ex} = 0.8 \,\mu\text{J} \text{ mm}^{-2}].$

Photoluminescence intensity versus excitation intensity characteristics



Figure S4. Photoluminescence intensity versus excitation intensity characteristics for (a) $d_{BSB-Cz} = 2$ nm ($\lambda \sim 480$ nm), (b) $d_{C545T} = 2$ nm ($\lambda \sim 510$ nm), (c) $d_{BSB-Cz} = 6$ nm ($\lambda \sim 480$ nm), and (d) $d_{C545T} = 6$ nm ($\lambda \sim 510$ nm).

Calculation of the rate constant of the Förster energy transfer. The rate constant of the Förster energy transfer or fluorescent resonance energy transfer (k_{FRET}) is given by $k_{FRET} = \frac{9000c^4 ln10}{128\pi^5 n^4 N_A \tau r^6} \int f \varepsilon \frac{dv}{v^4}$, where *c* is the velocity of light in vacuum, *n* is the refractive index, N_A is Avogadro's number, τ is the radiation lifetime of BSB-Cz, k^2 is the orientation factor (2/3), *r* is the distance between the C545T ground-state and BSB-Cz excited-state molecules, *f* is the shape function of the PL spectrum for BSB-Cz, ε is the molar extinction coefficient of C545T, and *v* is the frequency of light. Calculation of k_{FRET} in the layer-stacked structures is complex because the light absorption intensity depends on the position in the BSB-Cz layers (by extinction of the excitation light intensity in the medium). Thus, we defined the intensity of the Förster energy transfer I_{FRET} by S-3

 $I_{FRET}(t) = \sum I_T(d) \cdot R \exp(-k_{FRET}(d) \cdot t)$, where t is time, d is the distance between the surface of the BSB-Cz top layer and the arbitrary position inside the BSB-Cz top and bottom layers, I_T is the transmitted intensity of the excitation light, which was obtained by considering the extinction coefficient of the BSB-Cz thin film, and R is the probability that BSB-Cz absorbs the excitation light at the arbitrary position. In the actual calculation, we used the simplified equation $I_{FRET}^{'}(t) = \frac{I_{FRET}(t)}{I_0 \cdot R} = \sum \frac{I_T(d)}{I_0} \exp(-k_{FRET}(d) \cdot t)$ to obtain the dimensionless value $I_{FRET}^{'}(t)$, where I_0 is the excitation intensity (the value was arbitrarily defined). The step of d for the calculation was set to 1 nm. In the calculation of $I_{FRET}^{'}(t)$, r is considered to be the distance between the arbitrary position and the nearest BSB-Cz/C545T interface. The thicknesses of the C545T layers are ignored because they are sufficiently thin with respect to the total thickness. The $I_{FRET}^{'}(t) - t$ characteristics showed multiexponential decay. We consider that the lifetime of the Förster energy transfer is the time that the $I_{FRET}^{'}(t)$ value becomes 1/e of the initial value $[I_{FRET}^{'}(0)]$, and that k_{FRET} is the inverse of the lifetime.