## SUPPLEMENTARY INFORMATION

## Boron-Based Ternary MgTa<sub>2</sub>B<sub>6</sub> Cluster: A Turning Nanoclock with Dynamic Structural Fluxionality

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## Supplementary Information – Part I

- **Table S1**Cartesian coordinates for optimized global-minimum (GM) and transition-state<br/>(TS) structures of MgTa2B6 cluster at the PBE0-D3BJ/def2-TZVP level.
- **Table S2**Orbital composition analysis for occupied canonical molecular orbitals (CMOs)of GM (1,  $C_s$ ,  $^1A'$ ) MgTa<sub>2</sub>B<sub>6</sub> cluster. Main components are highlighted in bold.
- **Table S3**Orbital composition analysis for occupied CMOs of TS (1',  $C_s$ ,  $^1A'$ ) MgTa<sub>2</sub>B<sub>6</sub>cluster. Main components are highlighted in bold.
- **Table S4**Calculated NICS<br/><sub>zz</sub> and NICS (shown in *italics* in brackets) of GM (1,  $C_s$ ,  $^1A'$ )<br/>MgTa2B6 cluster at the PBE0/Ta/def2-TZVP/B,Mg/6-311+G(d) level. These<br/>values are calculated at the center of B6 ring or B4 trapezoid, as well as at 1 Å<br/>above the center.
- **Figure S1** Optimized geometric structures for the top 20 low-lying isomers of MgTa<sub>2</sub>B<sub>6</sub> cluster at the PBE0-D3BJ/def2-TZVP level along with their relative energies (in

*italics*), including corrections for the zero-point energies (ZPEs). Relative energies are also listed at the single-point CCSD(T)/def2-TZVP//PBE0-D3BJ/ def2-TZVP level with ZPE corrections, as well as at the single-point CCSD(T)/def2-TZVP//BP86-D3BJ/def2-TZVP level (in brackets) with ZPE corrections. All energies are shown in kcal mol<sup>-1</sup>.

- Figure S2 Calculated bond distances (in Å; black color) and Wiberg bond indices (WBIs; in blue color) for GM MgTa<sub>2</sub>B<sub>6</sub> cluster at the PBE0-D3BJ/def2-TZVP level. The WBI values are obtained from the natural bond orbital (NBO) analysis.
- **Figure S3** Calculated (a) bond distances (in Å; black color) and (b) WBIs (blue color) for TS MgTa<sub>2</sub>B<sub>6</sub> cluster. The WBIs are obtained from the NBO analysis.
- **Figure S4** Pictures of occupied CMOs of GM (1,  $C_s$ , <sup>1</sup>A') MgTa<sub>2</sub>B<sub>6</sub> cluster, sorted to five subsets. (a) Six CMOs for skeleton, localized B–B  $\sigma$  bonds along the peripheral B<sub>6</sub> ring. (b) Three delocalized  $\pi$  CMOs; that is, the  $\pi$  sextet. (c) Three delocalized  $\sigma$  CMOs. (d) Two Ta 5d-based CMOs that are approximately Ta–Ta nonbonding, with secondary d-p  $\sigma$  bonding. (e) One  $\sigma$  bond within the Ta8–Mg9 unit (see Fig. 1(a) for atom labels), as well as the lowest unoccupied molecular orbital (LUMO). Subsets (b) and (c) collectively render the MgTa<sub>2</sub>B<sub>6</sub> cluster  $6\pi/6\sigma$  double aromaticity.
- **Figure S5** Calculated natural atomic charges (in |e|) of a model  $D_{6h} CB_6^{2-}$  cluster from the NBO analysis at the PBE0-D3BJ/def2-TZVP level.
- **Figure S6** An alternative chemical bonding scheme for  $GM(1, C_s, {}^1A')MgTa_2B_6$  cluster on the basis of adaptive natural density partitioning (AdNDP) analysis. Occupation numbers (ONs) are indicated.
- Figure S7 Isosurfaces of electron localization functions (ELFs) for GM MgTa<sub>2</sub>B<sub>6</sub> cluster. (a) At the B<sub>6</sub> plane. (b) At the plane of B3–Ta8–B6–Ta7 rhombus.
- **Figure S8** Pictures of occupied CMOs of TS (1',  $C_s$ , <sup>1</sup>A') structure of MgTa<sub>2</sub>B<sub>6</sub> cluster. (a) Six CMOs for localized B–B  $\sigma$  bonds along the peripheral B<sub>6</sub> ring. (b) Three

delocalized  $\pi$  CMOs. (c) Three delocalized  $\sigma$  CMOs. (d) Two Ta 5d-based CMOs that are approximately Ta–Ta nonbonding. (e) One  $\sigma$  bond within the Ta8–Mg9 unit, as well as the LUMO.

Figure S9 AdNDP bonding scheme for the TS structure of MgTa<sub>2</sub>B<sub>6</sub> cluster. The ONs are shown. This bonding scheme is to be compared to that of GM MgTa<sub>2</sub>B<sub>6</sub> cluster as shown in Fig. 4.

## Supplementary Information – Part II

A short movie extracted from the Born-Oppenheimer molecular dynamics (BOMD) simulation for GM MgTa<sub>2</sub>B<sub>6</sub> cluster. The simulation was performed at near room temperature (300 K) for a time duration of 60 ps. The movie roughly covers a time span of 12 ps.

**Table S1**Cartesian coordinates for optimized global-minimum (GM) and transition-state<br/>(TS) structures of MgTa2B6 cluster at the PBE0-D3BJ/def2-TZVP level.

1 (GM,  $C_{\rm s}$ , <sup>1</sup>A')

| В  | 0.79142705  | 1.39983409  | 0.00265237  |
|----|-------------|-------------|-------------|
| В  | -0.82052483 | 1.38297912  | 0.00265237  |
| В  | -1.59640516 | -0.01904227 | 0.00592409  |
| В  | -0.78469099 | -1.39741379 | -0.00857646 |
| В  | 0.81373964  | -1.38070020 | -0.00857646 |
| В  | 1.59645430  | 0.01434306  | 0.00592409  |
| Ta | 0.00001937  | -0.00185289 | -1.47094945 |
| Ta | 0.00001937  | -0.00185289 | 1.51355369  |
| Mg | -0.02720039 | 2.60135261  | 2.67545797  |

**1'** (TS,  $C_{\rm s}$ , <sup>1</sup>A')

| В  | 0.01759854  | 1.61053394  | -0.00964987 |
|----|-------------|-------------|-------------|
| В  | -1.38027195 | 0.81283623  | 0.00512060  |
| В  | -1.39059116 | -0.78526101 | -0.01234223 |
| В  | -0.01753949 | -1.60512975 | 0.02409312  |
| В  | 1.37309985  | -0.81546027 | -0.01234223 |
| В  | 1.39770421  | 0.78248087  | 0.00512060  |
| Та | 0.00000293  | 0.00026830  | 1.47148794  |
| Та | 0.00000293  | 0.00026830  | -1.51217717 |
| Mg | 0.02827561  | 2.58764807  | -2.74741123 |

**Table S2**Orbital composition analysis for occupied canonical molecular orbitals (CMOs)of GM  $(1, C_s, {}^1A')$  MgTa<sub>2</sub>B<sub>6</sub> cluster. Main components are highlighted in bold.

| Subsystem        | СМО                          | B <sub>6</sub> (% | <b>b</b> ) | Ta <sub>2</sub> (%)  |       | Mg (%)           |       |
|------------------|------------------------------|-------------------|------------|----------------------|-------|------------------|-------|
|                  |                              | s/p               | total      | s/p/d                | total | s/p              | total |
| B–B              |                              | 0.2/ <b>96.7</b>  | 96.9       | 0.0/0.1/0.4          | 0.5   | 0.2/0.0          | 0.2   |
| 2c-2e σ          |                              |                   |            |                      |       |                  |       |
|                  | HOMO–7 (a')                  |                   |            |                      |       |                  |       |
|                  |                              | 23.4/54.9         | 78.3       | 0.0/0.0/19.8         | 19.8  | 0.0/0.0          | 0.0   |
|                  | HOMO-10 (a")<br>HOMO-11 (a') | 22.7/54.9         | 77.6       | 0.1/0.2/ <b>20.0</b> | 20.3  | 0.3/0.0          | 0.3   |
|                  | HOMO-12 (a")                 | 36.0/27.7         | 63.7       | 0.0/4.6/25.5         | 30.1  | 0.0/0.0          | 0.0   |
|                  | НОМО-13 (а')                 | 36.0/27.6         | 63.6       | 0.0/4.8/25.3         | 30.1  | 0.1/0.1          | 0.2   |
|                  | HOMO-14 (a')                 | <b>48.5</b> /18.6 | 67.1       | 7.3/5.6/4.1          | 17.0  | 0.2/0.1          | 0.3   |
| Mg–Ta<br>2c-2e σ | HOMO (a')                    | 2.0/ <b>22.2</b>  | 24.2       | 3.9/5.4/ <b>32.5</b> | 41.8  | <b>30.3</b> /1.9 | 32.2  |

| 6π          |                             | 0.1/ <b>60.7</b>  | 60.8 | 0.0/2.2/ <b>34.5</b> | 36.7  | 0.0/0.1  | 0.1  |
|-------------|-----------------------------|-------------------|------|----------------------|-------|----------|------|
| aromaticity |                             |                   |      |                      |       |          |      |
|             |                             |                   |      |                      |       |          |      |
|             |                             |                   |      |                      |       |          |      |
|             |                             | 1 7/59 1          | 60.8 | 0 3/3 8/27 0         | 31.1  | 5 3/0 1  | 54   |
|             |                             | 1.77071           | 00.0 | 0.5/5.0/2/00         | 0111  | 0.0/0.1  | 5.1  |
|             |                             |                   |      |                      |       |          |      |
|             | <b>•</b>                    |                   |      |                      |       |          |      |
|             | HOMO-6 (a')                 |                   |      |                      |       |          |      |
|             |                             | 0.6/ <b>67.5</b>  | 68.1 | 12.6/2.5/6.5         | 21.6  | 3.9/0.1  | 4.0  |
|             |                             |                   |      |                      |       |          |      |
|             |                             |                   |      |                      |       |          |      |
|             | HOMO-9 (a')                 |                   |      |                      |       |          |      |
| 6σ          |                             | 16.2/ <b>55.0</b> | 71.2 | 0.0/6.7/ <b>20.1</b> | 26.8  | 0.0/0.3  | 0.3  |
| aromaticity |                             |                   |      |                      |       |          |      |
|             |                             |                   |      |                      |       |          |      |
|             |                             |                   |      |                      |       |          |      |
|             | HOMO $-3$ (a <sup>*</sup> ) | 8 2/36 0          | 44.2 | 1 0/6 1/ <b>28 8</b> | 35.9  | 17.9/0.0 | 17.9 |
|             |                             | 0.2/30.0          | 77.2 | 1.0/0.1/20.0         | 55.7  | 17.9/0.0 | 17.7 |
|             |                             |                   |      |                      |       |          |      |
|             | HOMO-4 (a')                 |                   |      |                      |       |          |      |
|             |                             | 23.7/36.8         | 60.5 | 1.7/0.2/34.2         | 36.1  | 1.0/0.0  | 1.0  |
|             |                             | 2011/0010         | 0010 | 1.770.270.112        | 0.011 | 110/010  | 110  |
|             |                             |                   |      |                      |       |          |      |
|             |                             |                   |      |                      |       |          |      |
|             | HOMO-8 (a')                 |                   |      |                      |       |          |      |
| Ta d-based  |                             | 0.2/ <b>28.7</b>  | 28.9 | 0.0/0.1/70.2         | 70.3  | 0.0/0.2  | 0.2  |
| CMOS        |                             |                   |      |                      |       |          |      |
|             |                             |                   |      |                      |       |          |      |
|             | HOMO-1 (a")                 |                   |      |                      |       |          |      |
|             |                             | 5.7/35.3          | 41.0 | 1.2/2.5/ <b>45.3</b> | 49.0  | 8.3/0.4  | 8.7  |
|             |                             |                   |      |                      |       |          |      |
|             |                             |                   |      |                      |       |          |      |
|             | HOMO $_2$ (a')              |                   |      |                      |       |          |      |
|             | 1101110 2 (a)               |                   |      | 1                    |       | 1        |      |

| Subsystem | СМО          | B <sub>6</sub> (% | <b>)</b> | Ta <sub>2</sub> (%)  |       | Mg (%)           |       |
|-----------|--------------|-------------------|----------|----------------------|-------|------------------|-------|
|           |              | s/p               | total    | s/p/d                | total | s/p              | total |
| B–B       |              | 0.0/ <b>97.7</b>  | 97.7     | 0.0/0.0/0.1          | 0.1   | 0.0/0.0          | 0.0   |
| 2c-2e σ   |              |                   |          |                      |       |                  |       |
|           |              |                   |          |                      |       |                  |       |
|           | HOMO-7 (a")  |                   |          |                      |       |                  |       |
|           |              | 23.2/55.2         | 78.4     | 0.0/0.0/19.7         | 19.7  | 0.0/0.0          | 0.0   |
|           |              |                   |          |                      |       |                  |       |
|           | HOMO-10 (a") |                   |          |                      |       |                  |       |
|           |              | 23.2/54.4         | 77.6     | 0.1/0.1/20.2         | 20.4  | 0.2/0.0          | 0.2   |
|           |              |                   |          |                      |       |                  |       |
|           | HOMO-11 (a') |                   |          |                      |       |                  |       |
|           |              | 36.0/27.7         | 63.7     | 0.0/4.6/25.5         | 30.1  | 0.0/0.0          | 0.0   |
|           | -            |                   |          |                      |       |                  |       |
|           | HOMO-12 (a") |                   |          |                      |       |                  |       |
|           |              | 36.1/27.5         | 63.6     | 0.0/4.7/ <b>25.4</b> | 30.1  | 0.1/0.1          | 0.2   |
|           | <b>O</b>     |                   |          |                      |       |                  |       |
|           | HOMO-13 (a') |                   |          |                      |       |                  |       |
|           | 2            | <b>48.5</b> /18.6 | 67.1     | 7.3/5.6/4.1          | 17.0  | 0.2/0.1          | 0.3   |
|           | <b>(</b>     |                   |          |                      |       |                  |       |
|           |              |                   |          |                      |       |                  |       |
|           | HOMO-14 (a') |                   |          |                      |       |                  |       |
| Mg–Ta     |              | 2.0/23.1          | 25.1     | 3.5/5.0/ <b>35.3</b> | 43.8  | <b>27.8</b> /1.6 | 29.4  |
| 2c-2e σ   |              |                   |          |                      |       |                  |       |
|           | HOMO (a')    |                   |          |                      |       |                  |       |

**Table S3**Orbital composition analysis for occupied CMOs of TS (1',  $C_s$ ,  $^1A'$ ) MgTa<sub>2</sub>B<sub>6</sub>cluster. Main components are highlighted in bold.

| 6π<br>aromaticity             |             | 0.1/ <b>60.6</b>  | 60.7 | 0.0/2.1/ <b>34.6</b> | 36.7 | 0.0/0.1  | 0.1  |
|-------------------------------|-------------|-------------------|------|----------------------|------|----------|------|
|                               | <b></b>     |                   |      |                      |      |          |      |
|                               | HOMO-5 (a") |                   |      |                      |      |          |      |
|                               | <b>*</b>    | 2.2/ <b>57.5</b>  | 59.7 | 0.4/4.3/ <b>25.6</b> | 30.3 | 7.2/0.0  | 7.2  |
|                               | HOMO-6 (a') |                   |      |                      |      |          |      |
|                               | номо-9 (a') | 0.5/ <b>67.4</b>  | 67.9 | 12.7/2.6/6.3         | 21.6 | 4.0/0.1  | 4.1  |
| 6 <del>σ</del><br>aromaticity | HOMO-3 (a") | 16.1/ <b>55.1</b> | 71.2 | 0.0/6.7/ <b>20.2</b> | 26.9 | 0.0/0.3  | 0.3  |
|                               | номо-4 (a') | 7.3/ <b>35.3</b>  | 42.6 | 1.1/5.7/ <b>30.2</b> | 37.0 | 18.3/0.0 | 18.3 |
|                               | номо-8 (a') | 23.8/36.5         | 60.3 | 1.7/0.2/ <b>34.5</b> | 36.4 | 0.9/0.0  | 0.9  |
| Ta d-based<br>CMOs            | НОМО-1 (а") | 0.2/ <b>28.0</b>  | 28.2 | 0.0/0.1/ <b>71.0</b> | 71.1 | 0.0/0.2  | 0.2  |
|                               | НОМО-2 (а') | 6.3/ <b>36.7</b>  | 43.0 | 1.3/2.8/ <b>42.0</b> | 46.1 | 9.2/0.4  | 9.6  |

**Table S4**Calculated NICS<br/><sub>zz</sub> and NICS (shown in *italics* in brackets) of GM (1,  $C_s$ , <sup>1</sup>A')MgTa2B6 cluster at the PBE0/Ta/def2-TZVP/B,Mg/6-311+G(d) level. These<br/>values are calculated at the center of B6 ring or B4 trapezoid, as well as at 1 Å<br/>above the center.

| R (Å) | B <sub>6</sub> ring               | 6<br>6<br>1<br>2<br>3<br>3<br>B <sub>4</sub> trapezoid | 6<br>5<br>4<br>3<br>B <sub>4</sub> trapezoid | 6<br>6<br>1<br>2<br>3<br>B <sub>4</sub> trapezoid | 6<br>5<br>1<br>4<br>2<br>3<br>B <sub>4</sub> trapezoid |
|-------|-----------------------------------|--|--|---|--|
| 0.0   | -91.43<br>(- <i>100.03</i> )      | -77.20 (-54.11)  | -74.01 (-52.78)                              | -67.00 (-49.28)                                   | -64.77 (-46.68ª)                                       |
| 1.0   | -141.14<br>(+57.84 <sup>b</sup> ) | -59.94 (+5.11 <sup>b</sup> )                           | -52.62 (+7.73 <sup>b</sup> )                 | -39.08 (+10.35 <sup>b</sup> )                     | -36.18 (+9.51 <sup>b</sup> )                           |

<sup>a</sup> The dissected contributions from a subset of CMOs to the total NICS value can be evaluated using the NBO 6.0 package. As an example, we shall analyze a point located 0.5 Å below the center of B3B4B5B6 trapezoid. Here the total NICS value is highly negative (-39.62 ppm), to which the delocalized  $6\pi$  and  $6\sigma$  frameworks (Fig. S4(b) and S4(c)) contribute by 74.5% collectively. To be specific, the three delocalized  $\sigma$  CMOs have a contribution of -19.54 ppm, as compared to -10.03 ppm from three delocalized  $\pi$  CMOs. In other words, the delocalized  $\sigma$  and  $\pi$  CMOs account for 49.2% and 25.3% of the total NICS value, respectively. Note that these numbers are merely an example. This analysis further validates the concept of double  $\pi/\sigma$  aromaticity in the ternary cluster.

<sup>b</sup> These NICS(1) values are not a very reliable indicator of  $\pi$  aromaticity, due to the perturbation of a Ta atom in the vicinity. The Ta atom is 1.49 Å above/below the B<sub>6</sub> plane.

Figure S1 Optimized geometric structures for the top 20 low-lying isomers of MgTa<sub>2</sub>B<sub>6</sub> cluster at the PBE0-D3BJ/def2-TZVP level along with their relative energies (in italics), including corrections for the zero-point energies (ZPEs). Relative energies are also listed at the single-point CCSD(T)/def2-TZVP//PBE0-D3BJ/ def2-TZVP level with ZPE corrections, as well as at the single-point CCSD(T)/def2-TZVP//BP86-D3BJ/def2-TZVP level (in brackets) with ZPE corrections. All energies are shown in kcal mol<sup>-1</sup>.



**1**  $C_{\rm s}$  (<sup>1</sup>A') 0.00 (0.00) 0.00

6 C2v (3B2)

16.97

**11** C<sub>1</sub> (<sup>1</sup>A)

28.33 (28.58)

24.76

**16** C<sub>1</sub> (<sup>1</sup>A)

29.79 (30.58)

29.28



13.61 (13.66) 13.82



**7**  $C_{\rm s}$  (<sup>1</sup>A') 25.64 (26.50) 21.31 (21.35) 26.17



12 C<sub>1</sub> (<sup>1</sup>A) 28.38 (28.43) 25.38



**17** C<sub>1</sub> (<sup>3</sup>A) 30.79 (31.67) 16.03



3 C<sub>s</sub> (<sup>1</sup>A') 14.68 (15.02) 12.20



8 Cs (1A') 26.02 (26.24) 26.99



**13** C<sub>1</sub> (<sup>1</sup>A) 28.74 (29.05) 25.50



18 C<sub>s</sub> (<sup>1</sup>A') 31.05 (31.37) 29.07



4 C<sub>2v</sub> (<sup>1</sup>A<sub>1</sub>) 17.08 (17.44) 18.61



9 C1 (1A) 26.80 (27.03) 24.57



14 C<sub>1</sub> (<sup>1</sup>A) 29.30 (29.86) 26.74



**19** C<sub>1</sub> (<sup>1</sup>A) 32.26 (32.53) 27.17



5 C<sub>s</sub> (<sup>1</sup>A') 20.30 (20.50) 16.73



10 C<sub>s</sub> (<sup>3</sup>A') 27.97 (30.38) 18.08



**15** C<sub>1</sub> (<sup>1</sup>A) 29.48 (30.12) 22.43



20 C1 (1A) 32.41 (32.88) 28.24

Figure S2Calculated bond distances (in Å; black color) and Wiberg bond indices (WBIs; in<br/>blue color) for GM MgTa2B6 cluster at the PBE0-D3BJ/def2-TZVP level. The<br/>WBI values are obtained from the natural bond orbital (NBO) analysis.



Figure S3Calculated (a) bond distances (in Å; black color) and (b) WBIs (blue color) for TSMgTa2B6 cluster. The WBIs are obtained from the NBO analysis.



**Figure S4** Pictures of occupied CMOs of GM (1,  $C_s$ , <sup>1</sup>A') MgTa<sub>2</sub>B<sub>6</sub> cluster, sorted to five subsets. (a) Six CMOs for skeleton, localized B–B  $\sigma$  bonds along the peripheral B<sub>6</sub> ring. (b) Three delocalized  $\pi$  CMOs; that is, the  $\pi$  sextet. (c) Three delocalized  $\sigma$  CMOs. (d) Two Ta 5d-based CMOs that are approximately Ta–Ta nonbonding, with secondary d-p  $\sigma$  bonding. (e) One  $\sigma$  bond within the Ta8–Mg9 unit (see Fig. 1(a) for atom labels), as well as the lowest unoccupied molecular orbital (LUMO). Subsets (b) and (c) collectively render the MgTa<sub>2</sub>B<sub>6</sub> cluster  $6\pi/6\sigma$  double aromaticity.

 $\begin{array}{c} (a) \\ (b) \\ (b)$ 

**Figure S5** Calculated natural atomic charges (in |e|) of a model  $D_{6h} CB_6^{2-}$  cluster from the NBO analysis at the PBE0-D3BJ/def2-TZVP level.



Figure S6An alternative chemical bonding scheme for  $GM(1, C_s, {}^1A') MgTa_2B_6$  cluster on<br/>the basis of adaptive natural density partitioning (AdNDP) analysis. Occupation<br/>numbers (ONs) are indicated.



**Figure S7** Isosurfaces of electron localization functions (ELFs) for GM MgTa<sub>2</sub>B<sub>6</sub> cluster. (a) At the B<sub>6</sub> plane. (b) At the plane of B3–Ta8–B6–Ta7 rhombus.



Pictures of occupied CMOs of TS (1',  $C_s$ , <sup>1</sup>A') structure of MgTa<sub>2</sub>B<sub>6</sub> cluster. (a) Figure S8 Six CMOs for localized B–B  $\sigma$  bonds along the peripheral B<sub>6</sub> ring. (b) Three delocalized  $\pi$  CMOs. (c) Three delocalized  $\sigma$  CMOs. (d) Two Ta 5d-based CMOs that are approximately Ta–Ta nonbonding. (e) One  $\sigma$  bond within the Ta8–Mg9 unit, as well as the LUMO.



HOMO-14 (a')

HOMO-9 (a')

HOMO-8 (a')

HOMO-2 (a')

HOMO (a')

Figure S9 AdNDP bonding scheme for the TS structure of MgTa<sub>2</sub>B<sub>6</sub> cluster. The ONs are shown. This bonding scheme is to be compared to that of GM MgTa<sub>2</sub>B<sub>6</sub> cluster as shown in Fig. 4.

