

Oxynitride $K_2Ba_{6.72}Si_{16}O_{40-1.5y}N_y:0.28\text{ Eu}^{2+}$ phosphor with high thermal stability realized by crystal field engineering

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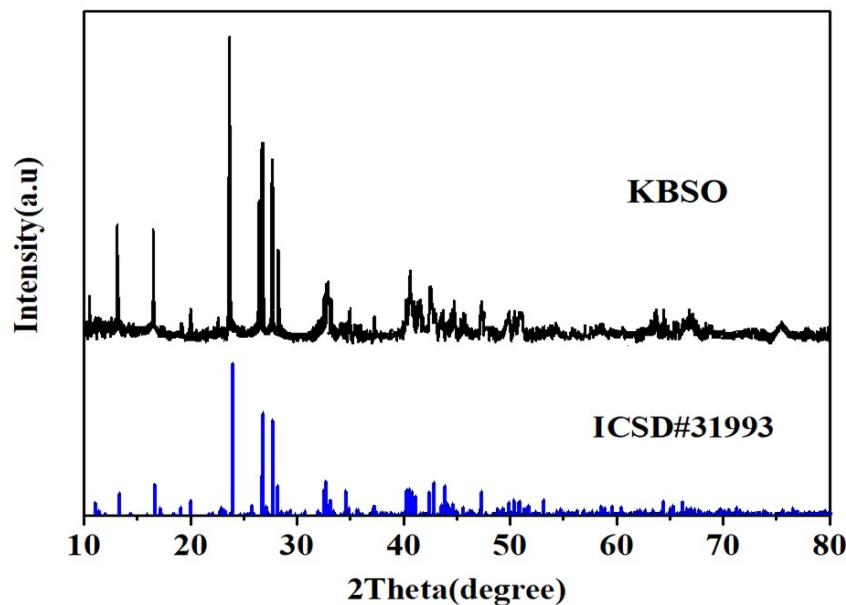


Fig.S1. XRD pattern of $K_2Ba_7Si_{16}O_{40}$ (KBSO), together with the reference model $K_2Ba_7Si_{16}O_{40}$ (ICSD#31993)

| Phase data | | | | | | |
|-------------------|---|------|--------|------------|------------|-------------|
| Space-group | C 1 2/m 1 (12) - monoclinic | | | | | |
| Cell | a=31.991(9) Å b=7.704(2) Å c=8.255(2) Å β=100.60 (2)° V=1999.8(9) Å ³ Z=2 | | | | | |
| Atomic parameters | | | | | | |
| Atom | Wyck. | Site | S.O.F. | x/a | y/b | z/c |
| Ba1 | 4i | m | | 0.1491(1) | 0 | 0.0582(2) |
| Ba2 | 4i | m | | 0.2699(1) | 0 | 0.8960(3) |
| Ba3 | 4i | m | | 0.3864(1) | 0 | 0.6887(3) |
| Ba4 | 4i | m | 0.333 | 0.0384(2) | 0 | 0.2764(7) |
| Ba5 | 2d | 2/m | 0.333 | 1/2 | 0 | 1/2 |
| K1 | 4i | m | 0.666 | 0.0384(4) | 0 | 0.2764(13) |
| K2 | 2d | 2/m | 0.666 | 1/2 | 0 | 1/2 |
| Si1 | 8j | 1 | | 0.0739(2) | 0.2007(8) | 0.6545(7) |
| Si2 | 8j | 1 | | 0.2007(2) | 0.2070(8) | 0.4348(7) |
| Si3 | 8j | 1 | | 0.1674(2) | 0.2977(8) | 0.7531(7) |
| Si4 | 8j | 1 | | 0.0460(2) | 0.2971(8) | 0.9755(7) |
| O1 | 8j | 1 | | 0.2033(6) | 0.2187(21) | 0.8876(18) |
| O2 | 8j | 1 | | 0.1842(6) | 0.2761(23) | 0.2602(19) |
| O3 | 4i | m | | 0.0572(8) | 0 | 0.6370(27) |
| O4 | 4i | m | | 0.1938(10) | 0 | 0.4415(36) |
| O5 | 4i | m | | 0.3391(8) | 0 | 0.1988(27) |
| O6 | 4i | m | | 0.4544(8) | 0 | -0.0369(26) |
| O7 | 8j | 1 | | 0.0839(6) | 0.2057(21) | 0.0865(19) |
| O8 | 8j | 1 | | 0.0674(5) | 0.2892(21) | 0.4823(19) |
| O9 | 4g | 2 | | 0 | 0.2095(27) | 0 |
| O10 | 8j | 1 | | 0.0453(5) | 0.2887(21) | 0.7796(18) |
| O11 | 8j | 1 | | 0.1227(5) | 0.1979(19) | 0.7592(17) |
| O12 | 8j | 1 | | 0.1741(5) | 0.296(2) | 0.5628(17) |
| O13 | 4f | -1 | | 1/4 | 1/4 | 1/2 |

Table S1. The refined phase data and atomic parameters of K₂Ba₇Si₁₆O₄₀

| Phase data | | | | | | | | |
|-------------------|-------|---|----------|---------|---------|---------|---------------------|--|
| Space-group | | C 1 2/m 1 (12) - monoclinic | | | | | | |
| Cell | | a=31.72(9) Å b=7.607(23) Å c=8.333(26) Å β=101.59(6)° V=1969.71(1700) Å ³ Z=2 | | | | | | |
| Atomic parameters | | | | | | | | |
| Atom | Wyck. | Site | S.O.F. | x/a | y/b | z/c | U [Å ²] | |
| Ba1 | 4i | m | 0.72(14) | 0.1491 | 0 | 0.0582 | 0.0250 | |
| Ba2 | 4i | m | 1.02(11) | 0.2699 | 0 | 0.896 | 0.0250 | |
| Ba3 | 4i | m | | 0.3864 | 0 | 0.6887 | 0.0250 | |
| Ba4 | 4i | m | | 0.0384 | 0 | 0.2764 | 0.0250 | |
| Ba5 | 2d | 2/m | | 1/2 | 0 | 1/2 | 0.0250 | |
| K1 | 4i | m | 0.666 | 0.0384 | 0 | 0.2764 | 0.0250 | |
| K2 | 2d | 2/m | 0.666 | 1/2 | 0 | 1/2 | 0.0250 | |
| Si1 | 8j | 1 | | 0.07390 | 0.20070 | 0.65450 | 0.0250 | |
| Si2 | 8j | 1 | | 0.20070 | 0.20700 | 0.43480 | 0.0250 | |
| Si3 | 8j | 1 | | 0.16740 | 0.29770 | 0.75310 | 0.0250 | |
| Si4 | 8j | 1 | | 0.04600 | 0.29710 | 0.97550 | 0.0250 | |
| O1 | 8j | 1 | | 0.20330 | 0.21870 | 0.88760 | 0.0250 | |
| O2 | 8j | 1 | | 0.18420 | 0.27610 | 0.26020 | 0.0250 | |
| O3 | 4i | m | | 0.0572 | 0 | 0.637 | 0.0250 | |
| O4 | 4i | m | | 0.1938 | 0 | 0.4415 | 0.0250 | |
| O5 | 4i | m | | 0.3391 | 0 | 0.1988 | 0.0250 | |
| O6 | 4i | m | | 0.4544 | 0 | -0.0369 | 0.0250 | |
| O7 | 8j | 1 | | 0.08390 | 0.20570 | 0.08650 | 0.0250 | |
| O8 | 8j | 1 | | 0.06740 | 0.28920 | 0.48230 | 0.0250 | |
| O9 | 4g | 2 | | 0 | 0.2095 | 0 | 0.0250 | |
| O10 | 8j | 1 | | 0.04530 | 0.28870 | 0.77960 | 0.0250 | |
| O11 | 8j | 1 | | 0.12270 | 0.19790 | 0.75920 | 0.0250 | |
| O12 | 8j | 1 | | 0.17410 | 0.29600 | 0.56280 | 0.0250 | |
| O13 | 4f | -1 | | 1/4 | 1/4 | 1/2 | 0.0250 | |
| Eu1 | 4i | m | | 0.1491 | 0 | 0.0582 | 0.0250 | |
| Eu2 | 4i | m | | 0.2699 | 0 | 0.896 | 0.0250 | |
| Eu3 | 4i | m | | 0.3864 | 0 | 0.6887 | 0.0250 | |
| Eu4 | 4i | m | | 0.0384 | 0 | 0.2764 | 0.0250 | |
| Eu5 | 2d | 2/m | | 1/2 | 0 | 1/2 | 0.0250 | |

Table S2. The refined phase data and atomic parameters of 0.28Eu

| Phase data | | | | | | | | |
|-------------------|-------|--|--------|---------|---------|---------|---------------------|--|
| Space-group | | C 1 2/m 1 (12) - monoclinic | | | | | | |
| Cell | | a=32.187(7) Å b=7.6752(18) Å c=8.2463(23) Å β=100.809(22)° V=2001.04(50) Å ³ | | | | | | |
| Atomic parameters | | | | | | | | |
| Atom | Wyck. | Site | S.O.F. | x/a | y/b | z/c | U [Å ²] | |
| Ba1 | 4i | m | 0.96 | 0.1491 | 0 | 0.0582 | 0.0250 | |
| Ba2 | 4i | m | 0.96 | 0.2699 | 0 | 0.896 | 0.0250 | |
| Ba3 | 4i | m | 0.96 | 0.3864 | 0 | 0.6887 | 0.0250 | |
| Ba4 | 4i | m | 0.313 | 0.0384 | 0 | 0.2764 | 0.0250 | |
| Ba5 | 2d | 2/m | 0.313 | 1/2 | 0 | 1/2 | 0.0250 | |
| K1 | 4i | m | 0.666 | 0.0384 | 0 | 0.2764 | 0.0250 | |
| K2 | 2d | 2/m | 0.666 | 1/2 | 0 | 1/2 | 0.0250 | |
| Si1 | 8j | 1 | 0.85 | 0.07390 | 0.20070 | 0.65450 | 0.0250 | |
| Si2 | 8j | 1 | 0.85 | 0.20070 | 0.20700 | 0.43480 | 0.0250 | |
| Si3 | 8j | 1 | 0.85 | 0.16740 | 0.29770 | 0.75310 | 0.0250 | |
| Si4 | 8j | 1 | 0.85 | 0.04600 | 0.29710 | 0.97550 | 0.0250 | |
| O1 | 8j | 1 | 0.85 | 0.20330 | 0.21870 | 0.88760 | 0.0250 | |
| O2 | 8j | 1 | 0.85 | 0.18420 | 0.27610 | 0.26020 | 0.0250 | |
| O3 | 4i | m | 0.85 | 0.0572 | 0 | 0.637 | 0.0250 | |
| O4 | 4i | m | 0.85 | 0.1938 | 0 | 0.4415 | 0.0250 | |
| O5 | 4i | m | 0.85 | 0.3391 | 0 | 0.1988 | 0.0250 | |
| O6 | 4i | m | 0.85 | 0.4544 | 0 | -0.0369 | 0.0250 | |
| O7 | 8j | 1 | 0.85 | 0.08390 | 0.20570 | 0.08650 | 0.0250 | |
| O8 | 8j | 1 | 0.85 | 0.06740 | 0.28920 | 0.48230 | 0.0250 | |
| O9 | 4g | 2 | 0.85 | 0 | 0.2095 | 0 | 0.0250 | |
| O10 | 8j | 1 | 0.85 | 0.04530 | 0.28870 | 0.77960 | 0.0250 | |
| O11 | 8j | 1 | 0.85 | 0.12270 | 0.19790 | 0.75920 | 0.0250 | |
| O12 | 8j | 1 | 0.85 | 0.17410 | 0.29600 | 0.56280 | 0.0250 | |
| O13 | 4f | -1 | 0.85 | 1/4 | 1/4 | 1/2 | 0.0250 | |
| Eu1 | 4i | m | 0.04 | 0.1491 | 0 | 0.0582 | 0.0250 | |
| Eu2 | 4i | m | 0.04 | 0.2699 | 0 | 0.896 | 0.0250 | |
| Eu3 | 4i | m | 0.04 | 0.3864 | 0 | 0.6887 | 0.0250 | |
| Eu4 | 4i | m | 0.02 | 0.0384 | 0 | 0.2764 | 0.0250 | |
| Eu5 | 2d | 2/m | 0.02 | 1/2 | 0 | 1/2 | 0.0250 | |
| N1 | 8j | 1 | 0.15 | 0.20330 | 0.21870 | 0.88760 | 0.0250 | |
| N2 | 8j | 1 | 0.15 | 0.18420 | 0.27610 | 0.26020 | 0.0250 | |
| N3 | 4i | m | 0.15 | 0.0572 | 0 | 0.637 | 0.0250 | |
| N4 | 4i | m | 0.15 | 0.1938 | 0 | 0.4415 | 0.0250 | |
| N5 | 4i | m | 0.15 | 0.3391 | 0 | 0.1988 | 0.0250 | |
| N6 | 4i | m | 0.15 | 0.4544 | 0 | -0.0369 | 0.0250 | |
| N7 | 8j | 1 | 0.15 | 0.08390 | 0.20570 | 0.08650 | 0.0250 | |
| N8 | 8j | 1 | 0.15 | 0.06740 | 0.28920 | 0.48230 | 0.0250 | |
| N9 | 4g | 2 | 0.15 | 0 | 0.2095 | 0 | 0.0250 | |
| N10 | 8j | 1 | 0.15 | 0.04530 | 0.28870 | 0.77960 | 0.0250 | |
| N11 | 8j | 1 | 0.15 | 0.12270 | 0.19790 | 0.75920 | 0.0250 | |
| N12 | 8j | 1 | 0.15 | 0.17410 | 0.29600 | 0.56280 | 0.0250 | |
| N13 | 4f | -1 | 0.15 | 1/4 | 1/4 | 1/2 | 0.0250 | |

Table S3. The refined phase data and atomic parameters of N6

| Phase data | | | | | | | |
|-------------------|--|------|--------|---------|---------|---------|---------------------|
| Space-group | C 1 2/m 1 (12) - monoclinic | | | | | | |
| Cell | a=31.00(7) Å b=7.562(19) Å c=7.971(16) Å β=100.72(9)° V=1835.97(1100) Å ³ Z=32 | | | | | | |
| Atomic parameters | | | | | | | |
| Atom | Wyck. | Site | S.O.F. | x/a | y/b | z/c | U [Å ²] |
| Ba1 | 4i | m | 0.96 | 0.1491 | 0 | 0.0582 | 0.0250 |
| Ba2 | 4i | m | 0.96 | 0.2699 | 0 | 0.896 | 0.0250 |
| Ba3 | 4i | m | 0.96 | 0.3864 | 0 | 0.6887 | 0.0250 |
| Ba4 | 4i | m | 0.313 | 0.0384 | 0 | 0.2764 | 0.0250 |
| Ba5 | 2d | 2/m | 0.313 | 1/2 | 0 | 1/2 | 0.0250 |
| K1 | 4i | m | 0.666 | 0.0384 | 0 | 0.2764 | 0.0250 |
| K2 | 2d | 2/m | 0.666 | 1/2 | 0 | 1/2 | 0.0250 |
| Si1 | 8j | 1 | | 0.07390 | 0.20070 | 0.65450 | 0.0250 |
| Si2 | 8j | 1 | | 0.20070 | 0.20700 | 0.43480 | 0.0250 |
| Si3 | 8j | 1 | | 0.16740 | 0.29770 | 0.75310 | 0.0250 |
| Si4 | 8j | 1 | | 0.04600 | 0.29710 | 0.97550 | 0.0250 |
| O1 | 8j | 1 | 0.8 | 0.20330 | 0.21870 | 0.88760 | 0.0250 |
| O2 | 8j | 1 | 0.8 | 0.18420 | 0.27610 | 0.26020 | 0.0250 |
| O3 | 4i | m | 0.8 | 0.0572 | 0 | 0.637 | 0.0250 |
| O4 | 4i | m | 0.8 | 0.1938 | 0 | 0.4415 | 0.0250 |
| O5 | 4i | m | 0.8 | 0.3391 | 0 | 0.1988 | 0.0250 |
| O6 | 4i | m | 0.8 | 0.4544 | 0 | -0.0369 | 0.0250 |
| O7 | 8j | 1 | 0.8 | 0.08390 | 0.20570 | 0.08650 | 0.0250 |
| O8 | 8j | 1 | 0.8 | 0.06740 | 0.28920 | 0.48230 | 0.0250 |
| O9 | 4g | 2 | 0.8 | 0 | 0.2095 | 0 | 0.0250 |
| O10 | 8j | 1 | 0.8 | 0.04530 | 0.28870 | 0.77960 | 0.0250 |
| O11 | 8j | 1 | 0.8 | 0.12270 | 0.19790 | 0.75920 | 0.0250 |
| O12 | 8j | 1 | 0.8 | 0.17410 | 0.29600 | 0.56280 | 0.0250 |
| O13 | 4f | -1 | 0.8 | 1/4 | 1/4 | 1/2 | 0.0250 |
| Eu1 | 4i | m | 0.04 | 0.1491 | 0 | 0.0582 | 0.0250 |
| Eu2 | 4i | m | 0.04 | 0.2699 | 0 | 0.896 | 0.0250 |
| Eu3 | 4i | m | 0.04 | 0.3864 | 0 | 0.6887 | 0.0250 |
| Eu4 | 4i | m | 0.02 | 0.0384 | 0 | 0.2764 | 0.0250 |
| Eu5 | 2d | 2/m | 0.02 | 1/2 | 0 | 1/2 | 0.0250 |
| N1 | 8j | 1 | 0.2 | 0.20330 | 0.21870 | 0.88760 | 0.0250 |
| N2 | 8j | 1 | 0.2 | 0.18420 | 0.27610 | 0.26020 | 0.0250 |
| N3 | 4i | m | 0.2 | 0.0572 | 0 | 0.637 | 0.0250 |
| N4 | 4i | m | 0.2 | 0.1938 | 0 | 0.4415 | 0.0250 |
| N5 | 4i | m | 0.2 | 0.3391 | 0 | 0.1988 | 0.0250 |
| N6 | 4i | m | 0.2 | 0.4544 | 0 | -0.0369 | 0.0250 |
| N7 | 8j | 1 | 0.2 | 0.08390 | 0.20570 | 0.08650 | 0.0250 |
| N8 | 8j | 1 | 0.2 | 0.06740 | 0.28920 | 0.48230 | 0.0250 |
| N9 | 4g | 2 | 0.2 | 0 | 0.2095 | 0 | 0.0250 |
| N10 | 8j | 1 | 0.2 | 0.04530 | 0.28870 | 0.77960 | 0.0250 |
| N11 | 8j | 1 | 0.2 | 0.12270 | 0.19790 | 0.75920 | 0.0250 |
| N12 | 8j | 1 | 0.2 | 0.17410 | 0.29600 | 0.56280 | 0.0250 |
| N13 | 4f | -1 | 0.2 | 1/4 | 1/4 | 1/2 | 0.0250 |

Table S4. The refined phase data and atomic parameters of N8

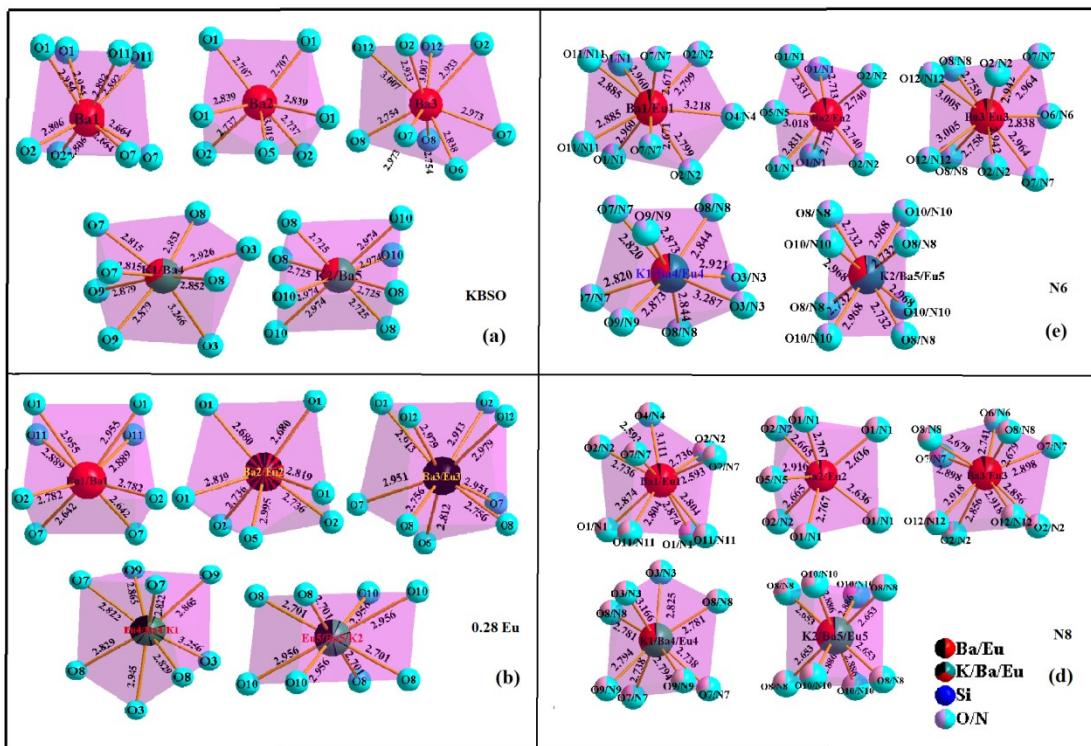


Fig.S2. the corresponding coordination environments of K^+ / Ba^{2+} / Eu^{2+} in (a)

$\text{K}_2\text{Ba}_7\text{Si}_{16}\text{O}_{40}$, (b) 0.28Eu, (c) N6, (d) N8

Distance of Ba/Eu-O in compound lattices

| (a) Distance of Ba1/Ba2/Ba3/Ba4/Ba5-O in $K_2Ba_7Si_{16}O_{40}$ | | | | | | | | | |
|---|------------|--------|------------|---------|------------|-----------|------------|------------|------------|
| Bond | Length (Å) | Bond | Length (Å) | Bond | Length (Å) | Bond | Length (Å) | Bond | Length (Å) |
| Ba1-O1 | 2.954 | Ba2-O1 | 2.707 | Ba3-O2 | 2.933 | Ba4/K1-O3 | 2.926 | Ba5/K2-O8 | 2.725 |
| Ba1-O1 | 2.954 | Ba2-O1 | 2.707 | Ba3-O2 | 2.933 | Ba4/K1-O3 | 2.926 | Ba5/K2-O8 | 2.725 |
| Ba1-O2 | 2.806 | Ba2-O1 | 2.839 | Ba3-O6 | 2.838 | Ba4/K1-O7 | 2.815 | Ba5/K2-O8 | 2.725 |
| Ba1-O2 | 2.806 | Ba2-O1 | 2.839 | Ba3-O7 | 2.973 | Ba4/K1-O7 | 2.815 | Ba5/K2-O8 | 2.725 |
| Ba1-O7 | 2.664 | Ba2-O5 | 3.019 | Ba3-O7 | 2.973 | Ba4/K1-O8 | 2.852 | Ba5/K2-O10 | 2.974 |
| Ba1-O7 | 2.664 | Ba2-O2 | 2.737 | Ba3-O8 | 2.754 | Ba4/K1-O8 | 2.852 | Ba5/K2-O10 | 2.974 |
| Ba1-O11 | 2.892 | Ba2-O2 | 2.737 | Ba3-O8 | 2.754 | Ba4/K1-O9 | 2.879 | Ba5/K2-O10 | 2.974 |
| Ba1-O11 | 2.892 | | | Ba3-O12 | 3.007 | Ba4/K1-O9 | 2.879 | Ba5/K2-O10 | 2.974 |
| | | | | Ba3-O12 | 3.007 | | | | |
| Average | 2.829 | | 2.798 | | 2.908 | | 2.868 | | 2.850 |

| (b) Distance of M1/M2/M3/M4/M5(M:Ba/Eu)-O in 0.28Eu | | | | | | | | | |
|---|------------|-------|------------|--------|------------|----------|------------|-----------|------------|
| Bond | Length (Å) | Bond | Length (Å) | Bond | Length (Å) | Bond | Length (Å) | Bond | Length (Å) |
| M1-O1 | 2.955 | M2-O1 | 2.680 | M3-O2 | 2.913 | M4/K1-O3 | 2.945 | M5/K2-O8 | 2.701 |
| M1-O1 | 2.955 | M2-O1 | 2.680 | M3-O2 | 2.913 | M4/K1-O3 | 2.945 | M5/K2-O8 | 2.701 |
| M1-O2 | 2.782 | M2-O1 | 2.819 | M3-O6 | 2.812 | M4/K1-O7 | 2.822 | M5/K2-O8 | 2.701 |
| M1-O2 | 2.782 | M2-O1 | 2.819 | M3-O7 | 2.951 | M4/K1-O7 | 2.822 | M5/K2-O8 | 2.701 |
| M1-O7 | 2.642 | M2-O5 | 2.995 | M3-O7 | 2.951 | M4/K1-O8 | 2.829 | M5/K2-O10 | 2.956 |
| M1-O7 | 2.642 | M2-O2 | 2.736 | M3-O8 | 2.756 | M4/K1-O8 | 2.829 | M5/K2-O10 | 2.956 |
| M1-O11 | 2.889 | M2-O2 | 2.736 | M3-O8 | 2.756 | M4/K1-O9 | 2.865 | M5/K2-O10 | 2.956 |
| M1-O11 | 2.889 | | | M3-O12 | 2.979 | M4/K1-O9 | 2.865 | M5/K2-O10 | 2.956 |
| | | | | M3-O12 | 2.979 | | | | |
| Average | 2.817 | | 2.780 | | 2.890 | | 2.865 | | 2.840 |

| (c) Distance of M1/M2/M3/M4/M5(M:Ba/Eu)-O/N in N6 | | | | | | | | | |
|---|------------|---------|------------|----------|------------|------------|------------|-------------|------------|
| Bond | Length (Å) | Bond | Length (Å) | Bond | Length (Å) | Bond | Length (Å) | Bond | Length (Å) |
| M1-O/N1 | 2.885 | M2-O/N1 | 2.831 | M3-O/N2 | 2.942 | M4/K1-O/N3 | 2.921 | M5/K2-O/N8 | 2.732 |
| M1-O/N1 | 2.885 | M2-O/N1 | 2.831 | M3-O/N2 | 2.942 | M4/K1-O/N3 | 2.921 | M5/K2-O/N8 | 2.732 |
| M1-O/N2 | 2.799 | M2-O/N1 | 2.713 | M3-O/N6 | 2.836 | M4/K1-O/N7 | 2.820 | M5/K2-O/N8 | 2.732 |
| M1-O/N2 | 2.799 | M2-O/N1 | 2.713 | M3-O/N7 | 2.964 | M4/K1-O/N7 | 2.820 | M5/K2-O/N8 | 2.732 |
| M1-O/N7 | 2.671 | M2-O/N5 | 3.018 | M3-O/N7 | 2.964 | M4/K1-O/N8 | 2.844 | M5/K2-O/N10 | 2.964 |
| M1-O/N7 | 2.671 | M2-O/N2 | 2.740 | M3-O/N8 | 2.758 | M4/K1-O/N8 | 2.844 | M5/K2-O/N10 | 2.963 |
| M1-O/N11 | 2.960 | M2-O/N2 | 2.740 | M3-O/N8 | 2.758 | M4/K1-O/N9 | 2.873 | M5/K2-O/N10 | 2.964 |
| M1-O/N11 | 2.960 | | | M3-O/N12 | 3.005 | M4/K1-O/N9 | 2.873 | M5/K2-O/N10 | 2.964 |
| | | | | M3-O/N12 | 3.005 | | | | |
| Average | 2.828 | | 2.798 | | 2.907 | | 2.864 | | 2.848 |

| (d) Distance of M1/M2/M3/M4/M5(M:Ba/Eu)-O/N in N8 | | | | | | | | | |
|---|------------|---------|------------|----------|------------|------------|------------|-------------|------------|
| Bond | Length (Å) | Bond | Length (Å) | Bond | Length (Å) | Bond | Length (Å) | Bond | Length (Å) |
| M1-O/N1 | 2.874 | M2-O/N1 | 2.767 | M3-O/N2 | 2.856 | M4/K1-O/N3 | 2.794 | M5/K2-O/N8 | 2.653 |
| M1-O/N1 | 2.874 | M2-O/N1 | 2.767 | M3-O/N2 | 2.856 | M4/K1-O/N3 | 2.794 | M5/K2-O/N8 | 2.653 |
| M1-O/N2 | 2.736 | M2-O/N1 | 2.338 | M3-O/N6 | 2.741 | M4/K1-O/N7 | 2.738 | M5/K2-O/N8 | 2.653 |
| M1-O/N2 | 2.736 | M2-O/N1 | 2.338 | M3-O/N7 | 2.898 | M4/K1-O/N7 | 2.738 | M5/K2-O/N8 | 2.653 |
| M1-O/N7 | 2.593 | M2-O/N5 | 2.916 | M3-O/N7 | 2.898 | M4/K1-O/N8 | 2.825 | M5/K2-O/N10 | 2.886 |
| M1-O/N7 | 2.593 | M2-O/N2 | 2.665 | M3-O/N8 | 2.679 | M4/K1-O/N8 | 2.825 | M5/K2-O/N10 | 2.886 |
| M1-O/N11 | 2.804 | M2-O/N2 | 2.665 | M3-O/N8 | 2.679 | M4/K1-O/N9 | 2.781 | M5/K2-O/N10 | 2.886 |
| M1-O/N11 | 2.804 | | | M3-O/N12 | 2.918 | M4/K1-O/N9 | 2.781 | M5/K2-O/N10 | 2.886 |
| | | | | M3-O/N12 | 2.918 | | | | |
| Average | 2.752 | | 2.637 | | 2.827 | | 2.784 | | 2.770 |

Table. S5 The distance of M(Ba/Eu/K)-O/N in compound (a) K₂Ba₇Si₁₆O₄₀, (b) 0.28Eu, (c) N6, (d) N8 lattice.