

## Systematic rare earth doping to adopt R32 huntite structure in $\text{NdSc}_3(\text{BO}_3)_4$ crystal.

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### Abstract

Huntite borates with R32 crystal structure have great potential in photonics applications as nonlinear and self-doubling media. This study is focused on determining the type and quantity of impurities responsible for converting the structure of  $\text{NdSc}_3(\text{BO}_3)_4$  to R32 polymorph. According to the single crystal X-ray diffraction of  $\text{R}_x\text{Nd}_y\text{Sc}_z(\text{BO}_3)_4$  ( $\text{R} = \text{Sm-Lu}$ ,  $x+y+z=4$ ), the obtained compounds crystallize in the space group R32 ( $\text{R} = \text{Eu, Er, Tm, Yb}$ ) and P3<sub>2</sub>21 ( $\text{R} = \text{Sm, Gd, Tb, Dy, Ho}$ ). Potential limitations to the future use of the crystals were identified, including compositional zoning and the possible presence of other polymorphic forms.

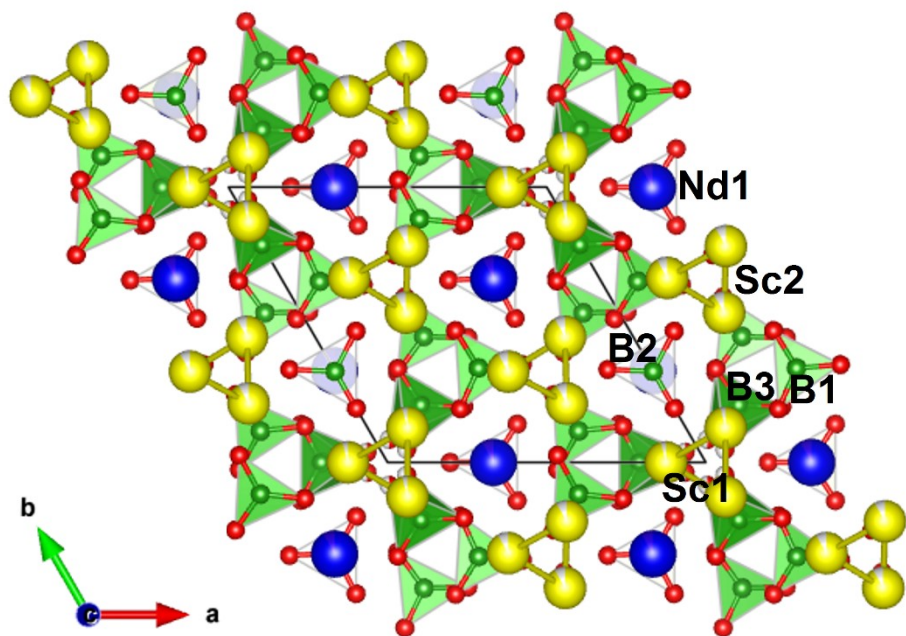


Figure S1. Crystal structure of NdSc<sub>3</sub>(BO<sub>3</sub>)<sub>4</sub>:R (R = Sm, Gd, Tb, Dy, Ho, Lu) (sp. gr. *P3<sub>2</sub>21*) compound projected down the *c* axis. Nd and Sc cations are blue and yellow spheres, BO<sub>3</sub> groups are shown as green triangles (B – green spheres, O – red spheres).

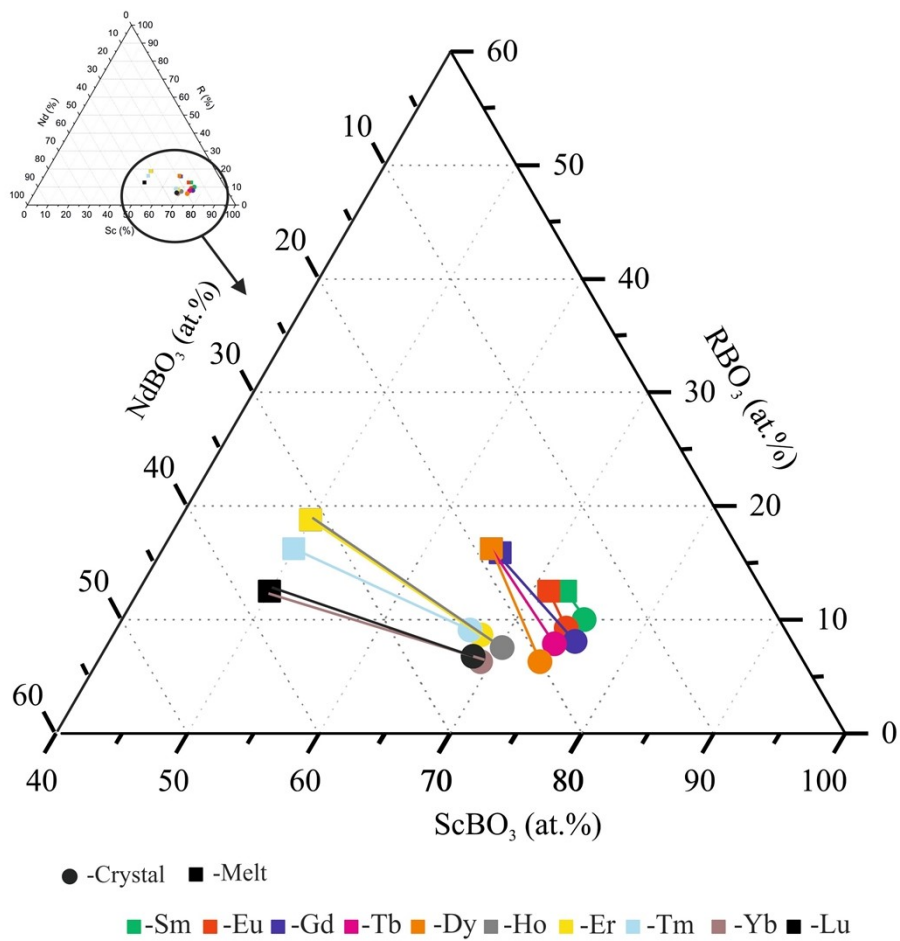


Figure S2. Relationship between the compositions in the melted batch and the compositions of the grown crystals.

**Table S1.** Selected bond distances (Å) for the coordination polyhedral of the studied NdSc<sub>3</sub>(BO<sub>3</sub>)<sub>4</sub>:R (R = Eu, Er, Tm, Yb) samples (sp. gr. R32).

	<b>R=Eu</b>	<b>R=Er</b>	<b>R=Tm</b>	<b>R=Yb</b>
Nd-O1 <sup>(×6)</sup>	2.43(2)	2.437(5)	2.440(2)	2.441(4)
<i>m.a.n. (e)</i>	64.491	64.640	62.859	65.870
Sc2-O1 <sup>(×2)</sup>	2.110(2)	2.1243(6)	2.1271(4)	2.1192(6)
Sc2-O2 <sup>(×2)</sup>	2.13(2)	2.142(6)	2.149(3)	2.142(5)
Sc2-O3 <sup>(×2)</sup>	2.06(1)	2.069(4)	2.070(3)	2.065(4)
<Sc2-O>	2.10	2.112	2.115	2.109
<i>m.a.n. (e)</i>	23.772	25.106	26.979	24.269
B1-O1 <sup>(×3)</sup>	1.374(7)	1.376(5)	1.378(3)	1.383(5)
B2-O2	1.36(3)	1.38(1)	1.366(6)	1.365(9)
B2-O3 <sup>(×2)</sup>	1.36(1)	1.365(6)	1.368(3)	1.372(4)
<B2-O >	1.36	1.37	1.367	1.370
O1-B1-O1	120.0	120.0	120	120
O2-B2-O3	117.9(6)	117.9(3)	118.1(2)	118.1(2)
O2-B2-O3'	117.9(6)	117.9(3)	118.1(2)	118.1(2)
O3-B2-O3'	124.2(7)	124.3(6)	123.8(3)	123.9(3)

**Table S2.** Valence balance calculation for studied sample NdSc<sub>3</sub>(BO<sub>3</sub>)<sub>4</sub>:R (R = Eu)

	<b>Nd1</b>	<b>Sc2</b>	<b>B1</b>	<b>B2</b>	<b>Σ</b>
O1	0.416 <sup>(×6)</sup>	0.482 <sup>(×2)</sup>	0.994 <sup>(×3)</sup>	-	<b>1.892</b>
O2		0.457 <sup>(×2)[×2]</sup>	-	1.049	<b>1.963</b>
O3		0.542 <sup>(×2)[×2]</sup>		1.023 <sup>(×2)</sup>	<b>2.107</b>
<b>Σ</b>	<b>2.496</b>	<b>2.962</b>	<b>2.982</b>	<b>3.095</b>	

<sup>(×2)</sup> – valence strengths doubled in the calculation of valence balance at the cations

[×2] – valence strengths doubled in the calculation of valence balance at the anions

**Table S3.** Valence balance calculation for studied sample NdSc<sub>3</sub>(BO<sub>3</sub>)<sub>4</sub>:R (R = Er)

	<b>Nd1</b>	<b>Sc2</b>	<b>B1</b>	<b>B2</b>	<b>Σ</b>
O1	0.406 <sup>(×6)</sup>	0.467 <sup>(×2)</sup>	0.989 <sup>(×3)</sup>	-	<b>1.862</b>
O2		0.449 <sup>(×2)</sup> [ <sup>×2</sup> ]	-	0.978	<b>1.876</b>
O3		0.528 <sup>(×2)</sup> [ <sup>×2</sup> ]		1.020 <sup>(×2)</sup>	<b>2.076</b>
<b>Σ</b>	<b>2.436</b>	<b>2.888</b>	<b>2.967</b>	<b>3.018</b>	

<sup>(×2)</sup> – valence strengths doubled in the calculation of valence balance at the cations

[<sup>×2</sup>] – valence strengths doubled in the calculation of valence balance at the anions

**Table S4.** Valence balance calculation for studied sample NdSc<sub>3</sub>(BO<sub>3</sub>)<sub>4</sub>:R (R = Tm)

	<b>Nd1</b>	<b>Sc2</b>	<b>B1</b>	<b>B2</b>	<b>Σ</b>
O1	0.403 <sup>(×6)</sup>	0.464 <sup>(×2)</sup>	0.983 <sup>(×3)</sup>	-	<b>1.850</b>
O2		0.442 <sup>(×2)</sup> [ <sup>×2</sup> ]	-	1.017	<b>1.901</b>
O3		0.526 <sup>(×2)</sup> [ <sup>×2</sup> ]		1.011 <sup>(×2)</sup>	<b>2.063</b>
<b>Σ</b>	<b>2.418</b>	<b>2.864</b>	<b>2.949</b>	<b>3.039</b>	

<sup>(×2)</sup> – valence strengths doubled in the calculation of valence balance at the cations

[<sup>×2</sup>] – valence strengths doubled in the calculation of valence balance at the anions

**Table S5.** Valence balance calculation for studied sample NdSc<sub>3</sub>(BO<sub>3</sub>)<sub>4</sub>:R (R = Yb)

	<b>Nd1</b>	<b>Sc2</b>	<b>B1</b>	<b>B2</b>	<b>Σ</b>
O1	0.402 <sup>(×6)</sup>	0.472 <sup>(×2)</sup>	0.970 <sup>(×3)</sup>	-	<b>1.844</b>
O2		0.449 <sup>(×2)</sup> [ <sup>×2</sup> ]	-	1.020	<b>1.918</b>
O3		0.532 <sup>(×2)</sup> [ <sup>×2</sup> ]		1.000 <sup>(×2)</sup>	<b>2.064</b>
<b>Σ</b>	<b>2.412</b>	<b>2.906</b>	<b>2.910</b>	<b>3.020</b>	

<sup>(×2)</sup> – valence strengths doubled in the calculation of valence balance at the cations

[<sup>×2</sup>] – valence strengths doubled in the calculation of valence balance at the anions

**Table S6.** Selected data on single crystals, data collection and structure refinement parameters of the studied NdSc<sub>3</sub>(BO<sub>3</sub>)<sub>4</sub>:R (R = Sm-Lu) samples.

	R=Sm	R=Eu	R=Gd	R=Tb	R=Dy	R=Ho	R=Er	R=Tm	R=Yb	R=Lu
<b>Crystal data</b>										
<i>a</i> (Å)	9.7768(3)	9.7610(3)	9.781(1)	9.7594(6)	9.7577(3)	9.7655(3)	9.7999(4)	9.8072(3)	9.804(1)	9.8013(4)
<i>c</i> (Å)	7.9305(3)	7.9185(2)	7.9407(8)	7.9234(5)	7.9240(3)	7.9374(2)	7.9735(3)	7.9928(3)	7.969(1)	7.9747(3)
<i>V</i> (Å <sup>3</sup> )	656.48(2)	653.38(2)	657.87(7)	653.56(4)	653.39(2)	655.54(2)	663.08(2)	665.76(2)	663.26(8)	663.46(2)
<i>Z</i>	3	3	3	3	3	3	3	3	3	3
Crystal dimensions (mm)	0.26×0.24× ×0.15	0.31×0.30× ×0.10	0.22×0.19× ×0.09	0.24×0.22× ×0.09	0.30×0.19× ×0.11	0.25×0.22× ×0.10	0.19×0.18× ×0.16	0.18×0.17× ×0.04	0.19×0.12× ×0.05	0.22×0.10× ×0.07
Crystal density	3.794	4.181	3.972	3.865	4.023	4.064	4.231	4.264	4.208	4.049
<b>Data collection</b>										
Reflections measured	30027	5566	29162	31713	19846	88792	8635	9737	12042	19026
Independent reflections	2121	710	2128	2110	2111	2932	728	733	575	1697
R <sub>merging</sub> [R <sub>(int)</sub> ] (%)	6.2	4.8	4.9	4.5	5.7	6.1	4.2	4.6	3.6	4.4
<i>h</i> <sub>min</sub> , <i>h</i> <sub>max</sub>	-16, 16	-16, 16	-16, 16	-16, 16	-16, 16	-18, 17	-16, 16	-16, 16	-15, 15	-15, 15
<i>k</i> <sub>min</sub> , <i>k</i> <sub>max</sub>	-16, 16	-16, 15	-16, 16	-16, 16	-16, 16	-18, 18	-16, 16	-16, 16	-15, 15	-15, 15
<i>l</i> <sub>min</sub> , <i>l</i> <sub>max</sub>	-13, 13	-11, 13	-13, 13	-13, 13	-13, 13	-14, 14	-13, 13	-13, 13	-12, 12	-12, 12
<b>Refinement</b>										
Space group	<i>P</i> <sub>3</sub> <sub>2</sub> <sub>1</sub>	<i>R</i> <sub>3</sub> <sub>2</sub>	<i>P</i> <sub>3</sub> <sub>2</sub> <sub>1</sub>	<i>P</i> <sub>3</sub> <sub>2</sub> <sub>1</sub>	<i>P</i> <sub>3</sub> <sub>2</sub> <sub>1</sub>	<i>P</i> <sub>3</sub> <sub>2</sub> <sub>1</sub>	<i>R</i> <sub>3</sub> <sub>2</sub>	<i>R</i> <sub>3</sub> <sub>2</sub>	<i>R</i> <sub>3</sub> <sub>2</sub>	<i>P</i> <sub>3</sub> <sub>2</sub> <sub>1</sub>
Reflections used in the refinement ( <i>I</i> > 3σ <sub>(<i>I</i>)</sub> )	1963	701	1929	1995	1899	2582	724	731	573	1563
N. of refined parameters	102	44	107	106	107	107	44	44	44	107
<i>R</i> <sup>a</sup> [on <i>F</i> ] (%)	7.95	5.24	2.12	6.59	6.79	6.64	3.10	1.73	2.81	6.70
<i>R</i> <sub>w</sub> <sup>b</sup> [on <i>F</i> ] (%)	8.52	5.83	2.92	8.13	8.54	7.35	3.44	1.83	3.46	9.48
Goof <sup>c</sup>	1.0269	1.0704	1.0560	1.0097	1.0248	1.1529	1.0808	1.0836	1.0240	0.9692
Δρ <sub>min</sub> /Δρ <sub>max</sub> (e <sup>-</sup> /Å <sup>3</sup> )	-6.95/2.92	-5.60/2.50	-4.70/2.66	-4.53/2.64	-7.37/2.59	-3.89/2.44	-3.52/1.40	-1.90/0.90	-3.26/1.04	-4.92/2.36

$$^a R = \frac{\sum[|F_o| - |F_c|]}{\sum|F_o|}$$

$$^b R_w = \frac{[\sum[w(F_o^2 - F_c^2)^2]/\sum[w(F_o^2)^2]]^{1/2}}{w} ; w = \text{Chebyshev optimized weights.}$$

$$^c \text{Goodness-of-fit} = [\sum[w(F_o^2 - F_c^2)^2]/(N-p)]^{1/2}, \text{ where } N \text{ and } p \text{ are the number of reflections and parameters, respectively.}$$

**Table S7.** Selected bond distances (Å) for the coordination polyhedra of the studied NdSc<sub>3</sub>(BO<sub>3</sub>)<sub>4</sub>:R (R = Sm, Gd, Tb, Dy, Ho, Lu) samples (sp. gr. P3<sub>2</sub>21).

	<b>R=Sm</b>	<b>R=Gd</b>	<b>R=Tb</b>	<b>R=Dy</b>	<b>R=Ho</b>	<b>R=Lu</b>
Nd1-O1 <sup>(×2)</sup>	2.422(6)	2.419(6)	2.415(6)	2.421(6)	2.424(6)	2.455(6)
Nd1-O2	2.802(5)	2.803(5)	2.791(4)	2.798(5)	2.820(5)	2.805(6)
Nd1-O3 <sup>(×2)</sup>	2.448(4)	2.447(3)	2.437(3)	2.441(3)	2.445(3)	2.453(4)
Nd1-O4 <sup>(×2)</sup>	3.009(5)	3.011(4)	2.999(4)	3.007(4)	3.002(4)	3.052(6)
Nd1-O5 <sup>(×2)</sup>	2.401(6)	2.401(6)	2.381(5)	2.401(6)	2.401(5)	2.438(7)
<Nd1-O>	2.596	2.595	2.584	2.593	2.596	2.622
<i>m.a.n. (e)</i>	<i>54.600</i>	<i>61.132</i>	<i>58.240</i>	<i>61.938</i>	<i>62.257</i>	<i>58.878</i>
Sc1-O2	2.026(8)	2.019(8)	2.023(7)	2.001(8)	2.005(8)	2.007(9)
Sc1-O2'	2.026(7)	2.019(7)	2.023(6)	2.002(7)	2.005(7)	2.007(8)
Sc1-O2''	2.363(7)	2.365(7)	2.340(6)	2.366(7)	2.345(7)	2.432(8)
Sc1-O2'''	2.363(6)	2.365(6)	2.340(6)	2.366(6)	2.346(6)	2.432(7)
Sc1-O5	2.121(5)	2.119(5)	2.130(4)	2.112(5)	2.103(4)	2.083(6)
Sc1-O5	2.122(7)	2.119(6)	2.131(5)	2.113(6)	2.103(6)	2.083(7)
Sc1-O6	2.148(4)	2.146(4)	2.136(4)	2.140(4)	2.148(4)	2.178(4)
Sc1-O6	2.148(4)	2.147(4)	2.136(4)	2.141(4)	2.148(4)	2.179(4)
<Sc1-O>	2.165	2.162	2.157	2.155	2.150	2.175
<i>m.a.n. (e)</i>	<i>19.194</i>	<i>20.013</i>	<i>18.837</i>	<i>20.286</i>	<i>21.126</i>	<i>20.916</i>
Sc2-O1	2.087(7)	2.093(7)	2.087(6)	2.094(7)	2.079(6)	2.097(7)
Sc2-O3	2.034(4)	2.031(3)	2.035(3)	2.033(3)	2.033(3)	2.038(4)
Sc2-O4	2.146(4)	2.154(4)	2.148(5)	2.149(4)	2.152(4)	2.157(5)
Sc2-O4'	2.161(6)	2.162(5)	2.148(4)	2.156(5)	2.159(5)	2.181(7)
Sc2-O7	2.105(4)	2.104(4)	2.096(3)	2.098(4)	2.096(3)	2.112(5)
Sc2-O7'	2.114(4)	2.119(4)	2.118(3)	2.118(4)	2.121(3)	2.126(4)
<Sc2-O>	2.108	2.111	2.105	2.108	2.107	2.119
<i>m.a.n. (e)</i>	<i>21.253</i>	<i>22.541</i>	<i>21.315</i>	<i>22.602</i>	<i>23.502</i>	<i>26.274</i>
B1-O3	1.363(8)	1.373(7)	1.362(7)	1.359(7)	1.347(7)	1.373(9)
B1-O4	1.362(5)	1.358(5)	1.362(5)	1.350(5)	1.359(5)	1.362(6)
B1-O5	1.362(9)	1.367(9)	1.369(8)	1.369(9)	1.397(8)	1.36(1)
<B1-O >	1.362	1.366	1.364	1.359	1.368	1.365

B2-O6	1.294(6)	1.318(5)	1.314(5)	1.304(5)	1.272(5)	1.307(6)
B2-O7 (*2)	1.401(8)	1.391(8)	1.392(7)	1.391(8)	1.410(7)	1.378(9)
<B2-O >	1.365	1.367	1.366	1.362	1.364	1.354
B3-O1 (*2)	1.339(6)	1.339(6)	1.337(5)	1.325(5)	1.351(5)	1.310(6)
B3-O2	1.533(9)	1.54(1)	1.532(9)	1.54(1)	1.514(9)	1.56(1)
B3-O2'	1.53(1)	1.54(1)	1.532(9)	1.54(1)	1.51(1)	1.56(1)
<B3-O >	1.404	1.406	1.402	1.468	1.458	1.393
O3-B1-O4	117.7(5)	116.9(4)	116.9(4)	117.3(4)	117.8(4)	115.7(5)
O3-B1-O5	125.2(5)	124.8(4)	125.5(4)	124.5(4)	124.7(4)	124.6(5)
O4-B1-O5	117.1(5)	118.3(4)	117.6(4)	118.1(4)	117.4(4)	119.8(5)
O6-B2-O7	123.1(4)	122.0(4)	122.4(5)	122.5(5)	123.4(5)	120.8(5)
O6-B2-O7'	123.1(5)	122.0(5)	122.4(5)	122.5(5)	123.4(5)	120.8(5)
O7-B2-O7'	113.8(5)	115.9(4)	115.3(4)	115.1(5)	113.1(4)	118.3(5)
O1-B3-O1'	124.9(8)	125.4(7)	124.5(7)	124.9(7)	122.7(7)	128.2(9)
O1-B3-O2	106.0(4)	105.8(4)	105.7(3)	106.2(4)	107.4(3)	105.8(4)
O1'-B3-O2	124.8(5)	124.5(4)	125.6(4)	124.3(4)	125.5(4)	121.1(5)

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**Table S8.** Valence balance calculation for studied sample NdSc<sub>3</sub>(BO<sub>3</sub>)<sub>4</sub>:R (R = Sm)

	<b>Nd1</b>	<b>Sc1</b>	<b>Sc2</b>	<b>B1</b>	<b>B2</b>	<b>B3</b>	<b>Σ</b>
O1	0.423 <sup>(×2)</sup>	-	0.507	-	-	1.097 <sup>(×2)</sup>	<b>2.027</b>
O2	0.152	0.580 <sup>(×2)</sup> 0.275 <sup>(×2)</sup>	-	-	-	0.637/0.642	<b>1.644/1.649</b>
O3	0.395 <sup>(×2)</sup>	-	0.776	1.026	-	-	<b>2.179</b>
O4	0.087 <sup>(×2)</sup>	-	0.445 0.430	1.028	-	-	<b>1.990</b>
O5	0.448 <sup>(×2)</sup>	0.470/0.469	-	1.028	-	-	<b>1.945/1.946</b>
O6	-	0.443 <sup>(×2)</sup> [×2]	-	-	1.244	-	<b>2.130</b>
O7	-	-	0.487 0.478	-	0.922 <sup>(×2)</sup>	-	<b>1.887</b>
<b>Σ</b>	<b>2.858</b>	<b>2.375/2.985</b>	<b>3.132</b>	<b>3.082</b>	<b>3.088</b>	<b>2.831/2.836</b>	

<sup>(×2)</sup> – valence strengths doubled in the calculation of valence balance at the cations

[×2] – valence strengths doubled in the calculation of valence balance at the anions

**Table S9.** Valence balance calculation for studied sample NdSc<sub>3</sub>(BO<sub>3</sub>)<sub>4</sub>:R (R = Gd)

	<b>Nd1</b>	<b>Sc1</b>	<b>Sc2</b>	<b>B1</b>	<b>B2</b>	<b>B3</b>	<b>Σ</b>
O1	0.427 <sup>(×2)</sup>	-	0.500	-	-	1.097 <sup>(×2)</sup>	<b>2.024</b>
O2	0.152	0.589 <sup>(×2)</sup> 0.274 <sup>(×2)</sup>	-	-	-	0.625	<b>1.640</b>
O3	0.396 <sup>(×2)</sup>	-	0.574	0.997	-	-	<b>1.967</b>
O4	0.087 <sup>(×2)</sup>	-	0.437 0.430	1.040	-	-	<b>1.994</b>
O5	0.448 <sup>(×2)</sup>	0.472 <sup>(×2)</sup>	-	1.014	-	-	<b>1.934</b>
O6	-	0.445 <sup>(×2)</sup> [×2]	-	-	1.163	-	<b>2.053</b>
O7	-	-	0.488 0.472	-	0.948 <sup>(×2)</sup>	-	<b>1.908</b>
<b>Σ</b>	<b>2.868</b>	<b>2.382/3.012</b>	<b>2.901</b>	<b>3.051</b>	<b>3.059</b>	<b>2.819</b>	

<sup>(×2)</sup> – valence strengths doubled in the calculation of valence balance at the cations

[×2] – valence strengths doubled in the calculation of valence balance at the anions

**Table S10.** Valence balance calculation for studied sample NdSc<sub>3</sub>(BO<sub>3</sub>)<sub>4</sub>:R (R = Tb)

	<b>Nd1</b>	<b>Sc1</b>	<b>Sc2</b>	<b>B1</b>	<b>B2</b>	<b>B3</b>	<b>Σ</b>
O1	0.431 <sup>(×2)</sup>	-	0.507	-	-	1.103 <sup>(×2)</sup>	<b>2.041</b>
O2	0.157	0.584 <sup>(×2)</sup> 0.290 <sup>(×2)</sup>	-	-	-	0.639	<b>1.670</b>
O3	0.406 <sup>(×2)</sup>	-	0.569	1.028	-	-	<b>2.003</b>
O4	0.089 <sup>(×2)</sup>	-	0.443 <sup>(×2)</sup> [ ×2]	1.028	-	-	<b>2.003</b>
O5	0.473 <sup>(×2)</sup>	0.460/0.461	-	1.008	-	-	<b>1.941/1.942</b>
O6	-	0.455 <sup>(×2)</sup> [ ×2]	-	-	1.176	-	<b>2.086</b>
O7	-	-	0.497 0.473	-	0.946 <sup>(×2)</sup>	-	<b>1.916</b>
<b>Σ</b>	<b>2.955</b>	<b>2.411/2.999</b>	<b>2.932</b>	<b>3.064</b>	<b>3.068</b>	<b>2.845</b>	

<sup>(×2)</sup> – valence strengths doubled in the calculation of valence balance at the cations

[×2] – valence strengths doubled in the calculation of valence balance at the anions

**Table S11.** Valence balance calculation for studied sample NdSc<sub>3</sub>(BO<sub>3</sub>)<sub>4</sub>:R (R = Dy)

	<b>Nd1</b>	<b>Sc1</b>	<b>Sc2</b>	<b>B1</b>	<b>B2</b>	<b>B3</b>	<b>Σ</b>
O1	0.424 <sup>(×2)</sup>	-	0.499	-	-	1.141 <sup>(×2)</sup>	<b>2.064</b>
O2	0.154	0.613/0.612 0.273 <sup>(×2)</sup>	-	-	-	0.625	<b>1.664/1.665</b>
O3	0.402 <sup>(×2)</sup>	-	0.571	1.037	-	-	<b>2.010</b>
O4	0.087 <sup>(×2)</sup>	-	0.442 0.435	1.064	-	-	<b>2.028</b>
O5	0.448 <sup>(×2)</sup>	0.480/0.479	-	1.008	-	-	<b>1.935/1.936</b>
O6	-	0.451 0.450	-	-	1.210	-	<b>2.111</b>
O7	-	-	0.495 0.473	-	0.948 <sup>(×2)</sup>	-	<b>1.916</b>
<b>Σ</b>	<b>2.876</b>	<b>2.406/3.085</b>	<b>2.915</b>	<b>3.109</b>	<b>3.106</b>	<b>2.391</b>	

<sup>(×2)</sup> – valence strengths doubled in the calculation of valence balance at the cations

[×2] – valence strengths doubled in the calculation of valence balance at the anions

**Table S12.** Valence balance calculation for studied sample NdSc<sub>3</sub>(BO<sub>3</sub>)<sub>4</sub>:R (R = Ho)

	<b>Nd1</b>	<b>Sc1</b>	<b>Sc2</b>	<b>B1</b>	<b>B2</b>	<b>B3</b>	<b>Σ</b>
O1	0.421 <sup>(×2)</sup>	-	0.516	-	-	1.061 <sup>(×2)</sup>	<b>2.064</b>
O2	0.145	0.608 <sup>(×2)</sup> 0.287/0.286	-	-	-	0.672/0.679	<b>1.71/1.72</b>
O3	0.398 <sup>(×2)</sup>	-	0.571	1.073	-	-	<b>2.042</b>
O4	0.089 <sup>(×2)</sup>	-	0.439 0.432	1.037	-	-	<b>1.997</b>
O5	0.448 <sup>(×2)</sup>	0.489 <sup>(×2)</sup>	-	0.932	-	-	<b>1.869</b>
O6	-	0.443 <sup>(×2)</sup> [ <sup>×2</sup> ]	-	-	1.323	-	<b>2.209</b>
O7	-	-	0.497 0.470	-	0.899 <sup>(×2)</sup>	-	<b>1.866</b>
<b>Σ</b>	<b>2.857</b>	<b>2.438/3.080</b>	<b>2.925</b>	<b>3.042</b>	<b>3.121</b>	<b>2.794/2.801</b>	

<sup>(×2)</sup> – valence strengths doubled in the calculation of valence balance at the cations

[<sup>×2</sup>] – valence strengths doubled in the calculation of valence balance at the anions

**Table S13.** Valence balance calculation for studied sample NdSc<sub>3</sub>(BO<sub>3</sub>)<sub>4</sub>:R (R = Lu)

	<b>Nd1</b>	<b>Sc1</b>	<b>Sc2</b>	<b>B1</b>	<b>B2</b>	<b>B3</b>	<b>Σ</b>
O1	0.387 <sup>(×2)</sup>	-	0.496	-	-	1.190 <sup>(×2)</sup>	<b>2.073</b>
O2	0.151 <sup>(×2)</sup>	0.605 <sup>(×2)</sup> 0.236 <sup>(×2)</sup>	-	-	-	0.591	<b>1.583</b>
O3	0.389 <sup>(×2)</sup>	-	0.565	0.997	-	-	<b>1.951</b>
O4	0.077 <sup>(×2)</sup>	-	0.434 0.412	1.028	-	-	<b>1.951</b>
O5	0.405 <sup>(×2)</sup>	0.512 <sup>(×2)</sup>	-	1.034	-	-	<b>1.951</b>
O6	-	0.415 0.414	-	-	1.200	-	<b>2.029</b>
O7	-	-	0.480 0.465	-	0.983 <sup>(×2)</sup>	-	<b>1.928</b>
<b>Σ</b>	<b>2.818</b>	<b>2.325/3.063</b>	<b>2.852</b>	<b>3.059</b>	<b>3.166</b>	<b>2.971</b>	

<sup>(×2)</sup> – valence strengths doubled in the calculation of valence balance at the cations

[<sup>×2</sup>] – valence strengths doubled in the calculation of valence balance at the anions

**Table S14.** Crystallographic coordinates, occupancies and equivalent/isotropic atomic displacement parameters ( $\text{\AA}^2$ ) of  $\text{NdSc}_3(\text{BO}_3)_4\text{:R}$  (R = Sm).

Site	x/a	y/b	z/c	Occ.	Ueq	U11	U22	U33	U23	U13	U12
Nd1	0.66725(5)	0.66725(5)	0.5	0.910(1)	0.0001	0.0002(2)	0.0002(2)	-0.0005(2)	-0.00020(6)	0.00020(6)	-0.0002(1)
Sc1	0	0.8744(3)	5/6	0.914(1)	0.0406	0.0019(6)	0.0010(5)	0.1190(9)	0.0022(4)	0.0044(7)	0.0010(3)
Sc2	0.2150(2)	0.6708(1)	0.4973(1)	0.891(1)	0.0007	0.0040(4)	0.001(4)	-0.0040(3)	-0.0006(3)	-0.0016(3)	0.0011(3)
Sm2	0.2150(2)	0.6708(1)	0.4973(1)	0.0410(9)	0.0007	0.0040(4)	0.001(4)	-0.0040(3)	-0.0006(3)	-0.0016(3)	0.0011(3)
O1	0.6576(6)	0.8606(6)	0.6829(7)	1	0.0179	0.0082(9)	0.0092(9)	0.0352(9)	0.0029(9)	0.0158(9)	0.0036(8)
O2	0.9628(7)	0.9155(7)	0.4005(8)	0.5	0.0046	0.0036(9)	-0.0001(9)	0.0093(9)	-0.0003(9)	0.0001(9)	0.0002(9)
O3	0.4506(5)	0.4785(5)	0.3212(5)	1	0.0008	0.0017(8)	0.0003(8)	0.0008(8)	0.0000(7)	-0.0011(7)	0.0009(7)
O4	0.3555(5)	0.6008(5)	0.6451(5)	1	0.0035	0.0078(8)	-0.0003(8)	0.0016(8)	-0.0003(8)	-0.0001(8)	0.0008(7)
O5	0.6721(6)	0.8668(6)	0.3195(6)	1	0.0154	0.0135(9)	0.0247(9)	0.0133(9)	-0.0144(8)	-0.0128(8)	0.0135(8)
O6	0.8025(6)	0.8025(6)	0	1	0.0360	0.0058(6)	0.058(6)	0.010(1)	0.0034(7)	-0.0034(7)	0.0055(8)
O7	0.6612(5)	0.5226(5)	0.0008(5)	1	0.0013	0.0055(8)	-0.0007(8)	-0.0010(8)	0.0009(7)	-0.0013(8)	0.0012(7)
B1	0.8866(6)	0.5439(6)	0.6731(6)	1	0.0009	0.0003(8)	0.0000(8)	0.0004(9)	0.0002(8)	-0.0002(8)	0.0015(8)
B2	0.6701(6)	0.6701(6)	0	1	0.0038	0.0023(6)	0.0023(6)	0.0049(9)	-0.0020(6)	0.0020(6)	0.0004(8)
B3	0.7906(8)	0	2/3	1	0.0393	0.0039(9)	0.0125(9)	0.104(1)	0.0006(9)	0.0003(4)	0.0062(4)

**Table S15.** Crystallographic coordinates, occupancies and equivalent/isotropic atomic displacement parameters ( $\text{\AA}^2$ ) of  $\text{NdSc}_3(\text{BO}_3)_4\text{:R}$  (R = Eu).

Site	x/a	y/b	z/c	Occ.	Ueq	U11	U22	U33	U23	U13	U12
Nd1	0	0	0	0.952(2)	0.0012	0.0012(4)	0.0012(4)	0.0013(5)	0.0000(1)	0.0000(1)	0.0006(2)
Eu1	0	0	0	0.117(2)	0.0012	0.0012(4)	0.0012(4)	0.0013(5)	0.0000(1)	0.0000(1)	0.0006(2)
Sc2	0.5449(5)	0	0	0.808(3)	0.0080	0.0051(9)	0.005(1)	0.014(1)	0.0024(9)	0.0012(4)	0.0023(5)
Eu2	0.5449(5)	0	0	0.108(2)	0.0080	0.0051(9)	0.005(1)	0.014(1)	0.0024(9)	0.0012(4)	0.0023(5)
O1	0.8592(14)	0	0.5	1	0.0041	0.001(2)	0.004(2)	0.008(2)	0.0000(1)	0.0000(1)	0.001(1)
O2	0.592(2)	0	0.5	1	0.0496	0.022(2)	0.066(2)	0.075(2)	-0.061(2)	-0.031(1)	0.033(1)
O3	0.4587(15)	0.1419(13)	0.5152(15)	1	0.0081	0.012(2)	0.003(2)	0.007(2)	0.000(2)	0.003(2)	0.002(2)
B1	0	0	0.5	1	0.0018	0.0000(1)	0.0000(1)	0.005(2)	0	0	0.0000(1)
B2	0.4532(18)	0	0.5	1	0.0070	0.001(2)	0.005(2)	0.016(2)	-0.002(2)	-0.001(1)	0.003(1)

**Table S16.** Crystallographic coordinates, occupancies and equivalent/isotropic atomic displacement parameters ( $\text{\AA}^2$ ) of  $\text{NdSc}_3(\text{BO}_3)_4\text{:R}$  (R = Gd).

Site	x/a	y/b	z/c	Occ.	Ueq	U11	U22	U33	U23	U13	U12
Nd1	0.66727(4)	0.66727(4)	0.5	0.909(1)	0.0045	0.0042(1)	0.0042(1)	0.0046(2)	-0.00012(5)	0.00012(5)	0.0017(1)
Gd1	0.66727(4)	0.66727(4)	0.5	0.103(1)	0.0045	0.0042(1)	0.0042(1)	0.0046(2)	-0.00012(5)	0.00012(5)	0.0017(1)
Sc1	0	0.8747(2)	5/6	0.953(1)	0.0321	0.0009(5)	-0.0002(4)	0.0957(9)	0.0008(3)	0.0017(6)	0.0003(3)
Sc2	0.2139(1)	0.6701(1)	0.49740(7)	0.871(1)	0.0011	0.0037(3)	0.0019(3)	-0.0026(3)	-0.0006(2)	-0.0015(2)	0.0012(2)
Gd2	0.2139(1)	0.6701(1)	0.49740(7)	0.0664(9)	0.0011	0.0037(3)	0.0019(3)	-0.0026(3)	-0.0006(2)	-0.0015(2)	0.0012(2)
O1	0.6586(6)	0.8604(6)	0.6831(7)	1	0.0212	0.0068(8)	0.0094(9)	0.0461(9)	-0.018(9)	0.0072(9)	0.0031(8)
O2	0.9627(7)	0.9161(7)	0.4013(7)	0.5	0.0078	0.0034(9)	0.0001(9)	0.0192(9)	-0.0005(9)	0.0000(9)	0.0004(8)
O3	0.4527(4)	0.4791(4)	0.3194(4)	1	0.0026	0.0034(8)	0.0000(8)	0.0047(8)	0.0002(7)	-0.0017(7)	0.0011(7)
O4	0.3555(5)	0.6013(4)	0.6447(5)	1	0.0066	0.0101(8)	0.0020(7)	0.0084(8)	-0.0034(7)	-0.0035(8)	0.0035(7)
O5	0.6734(5)	0.8676(6)	0.3202(6)	1	0.0131	0.0112(8)	0.0193(9)	0.0137(8)	-0.0081(8)	-0.0077(8)	0.0112(7)
O6	0.8029(6)	0.8029(6)	0	1	0.0411	0.0089(6)	0.0089(6)	0.1088(10)	0.0048(7)	-0.0048(7)	0.0068(8)
O7	0.6624(4)	0.5232(5)	0.0001(4)	1	0.0015	0.0053(8)	-0.0005(8)	-0.0001(8)	-0.0002(6)	-0.0010(7)	0.0013(6)
B1	0.8850(5)	0.5433(5)	0.6722(5)	1	0.0005	0.0001(8)	0.0012(8)	-0.0003(8)	0.0004(7)	0.0006(8)	0.0019(7)
B2	0.6682(5)	0.6682(5)	0	1	0.0023	0.0020(6)	0.0020(6)	0.0011(9)	-0.0007(5)	0.0007(5)	-0.0003(8)
B3	0.7913(8)	0	2/3	1	0.0349	0.0082(9)	0.0295(9)	0.0743(10)	0.0212(9)	0.0106(4)	0.0148(4)

**Table S17.** Crystallographic coordinates, occupancies and equivalent/isotropic atomic displacement parameters ( $\text{\AA}^2$ ) of  $\text{NdSc}_3(\text{BO}_3)_4\text{:R}$  (R = Tb).

Site	x/a	y/b	z/c	Occ.	Ueq	U11	U22	U33	U23	U13	U12
Nd1	0.66735(4)	0.66735(4)	0.5	0.884(1)	0.0043	0.0041(1)	0.0041(1)	0.0041(2)	-0.00012(5)	0.00012(5)	0.0016(1)
Tb1	0.66735(4)	0.66735(4)	0.5	0.080(1)	0.0043	0.0041(1)	0.0041(1)	0.0041(2)	-0.00012(5)	0.00012(5)	0.0016(1)
Sc1	0	0.8752(2)	5/6	0.897(1)	0.0341	0.0018(5)	0.0002(4)	0.1003(9)	0.0008(3)	0.0015(6)	0.0005(3)
Sc2	0.2145(2)	0.67030(9)	0.49728(7)	1.015(1)	0.0008	0.0031(3)	0.0017(3)	-0.0031(3)	-0.0004(2)	-0.0015(2)	0.0008(2)
O1	0.6578(5)	0.8607(6)	0.6824(7)	1	0.0265	0.0122(8)	0.0126(9)	0.0546(9)	0.0030(9)	0.0207(8)	0.0060(7)
O2	0.9614(6)	0.9156(6)	0.3993(7)	0.5	0.0091	0.0031(9)	0.0032(9)	0.0226(9)	-0.0011(9)	-0.0002(9)	0.0029(8)
O3	0.4533(4)	0.4793(4)	0.3197(4)	1	0.0051	0.0079(8)	0.0032(8)	0.0052(8)	-0.0002(7)	-0.0036(7)	0.0035(7)
O4	0.3559(4)	0.6019(4)	0.6434(4)	1	0.0062	0.0086(8)	0.0040(7)	0.0071(8)	-0.0036(7)	-0.0009(7)	0.0039(7)
O5	0.6727(5)	0.8663(5)	0.3217(5)	1	0.0168	0.0154(8)	0.0246(9)	0.0177(8)	-0.0177(8)	-0.0162(8)	0.0155(7)
O6	0.8038(6)	0.8038(6)	0	1	0.0522	0.0078(6)	0.0078(6)	0.1430(10)	0.0037(7)	-0.0037(7)	0.0054(8)
O7	0.6624(4)	0.5233(4)	-0.0008(3)	1	0.0030	0.0096(8)	-0.0002(7)	0.0002(8)	0.0003(6)	-0.0009(7)	0.0027(6)
B1	0.8856(5)	0.5432(5)	0.6723(5)	1	0.0007	0.0002(8)	0.0035(8)	0.0011(8)	0.0004(7)	0.0000(8)	0.0030(7)
B2	0.6692(5)	0.6692(5)	0	1	0.0040	0.0021(6)	0.0021(6)	0.0053(9)	-0.0014(5)	0.0014(5)	-0.0009(8)
B3	0.7912(7)	0	2/3	1	0.0401	0.0010(9)	0.0045(8)	0.1159(10)	0.0007(9)	0.0003(4)	0.0023(4)

**Table S18.** Crystallographic coordinates, occupancies and equivalent/isotropic atomic displacement parameters ( $\text{\AA}^2$ ) of  $\text{NdSc}_3(\text{BO}_3)_4\text{:R}$  (R = Dy).

Site	x/a	y/b	z/c	Occ.	Ueq	U11	U22	U33	U23	U13	U12
Nd1	0.66732(4)	0.66732(4)	0.5	0.919(1)	0.0039	0.0039(2)	0.0039(2)	0.0031(2)	-0.00014(5)	0.00014(5)	0.0014(1)
Dy1	0.66732(4)	0.66732(4)	0.5	0.103(1)	0.0039	0.0039(2)	0.0039(2)	0.0031(2)	-0.00014(5)	0.00014(5)	0.0014(1)
Sc1	0	0.8751(3)	5/6	0.966(1)	0.0330	0.0012(6)	-0.0004(4)	0.0984(9)	0.0008(3)	0.0016(7)	0.0004(3)
Sc2	0.2142(2)	0.6703(1)	0.49734(7)	0.850(1)	0.0009	0.0035(3)	0.0020(3)	-0.0031(3)	-0.0005(2)	-0.0015(2)	0.0012(2)
Dy2	0.2142(2)	0.6703(1)	0.49734(7)	0.072(1)	0.0009	0.0035(3)	0.0020(3)	-0.0031(3)	-0.0005(2)	-0.0015(2)	0.0012(2)
O1	0.6595(5)	0.8618(6)	0.6833(7)	1	0.0207	0.0068(8)	0.0115(9)	0.0419(9)	-0.0025(9)	0.0153(8)	0.0033(8)
O2	0.9632(7)	0.9167(7)	0.4027(8)	0.5	0.0093	0.0041(9)	-0.0003(9)	0.0242(9)	-0.0004(9)	0.0001(9)	0.0010(8)
O3	0.4530(4)	0.4787(4)	0.3194(4)	1	0.0016	0.0031(8)	0.0000(8)	0.0018(8)	0.0001(7)	-0.0012(7)	0.0008(7)
O4	0.3551(5)	0.6008(4)	0.6448(5)	1	0.0045	0.0076(8)	0.0001(7)	0.0045(8)	-0.0005(7)	-0.0003(8)	0.0009(7)
O5	0.6738(5)	0.8685(6)	0.3201(6)	1	0.0121	0.0092(8)	0.0205(9)	0.0110(9)	-0.0096(8)	-0.0092(8)	0.0108(7)
O6	0.8030(6)	0.8030(6)	0	1	0.0463	0.0050(6)	0.0050(6)	0.1299(10)	0.0074(7)	-0.0074(7)	0.0033(8)
O7	0.6623(4)	0.5234(5)	-0.0004(4)	1	0.0011	0.0059(8)	-0.0010(8)	-0.0008(8)	0.0004(6)	0.0012(7)	0.0018(7)
B1	0.8853(5)	0.5428(5)	0.6723(5)	1	0.0013	0.0005(8)	0.0006(8)	-0.0004(8)	0.0006(7)	0.0001(8)	0.0028(7)
B2	0.6694(5)	0.6694(5)	0	1	0.0016	0.0006(6)	0.0006(6)	0.0026(9)	-0.0012(6)	0.0012(6)	-0.0005(8)
B3	0.7914(8)	0	2/3	1	0.0353	0.0016(9)	0.0058(8)	0.0999(10)	0.0006(9)	0.0003(4)	0.0029(4)

**Table S19.** Crystallographic coordinates, occupancies and equivalent/isotropic atomic displacement parameters ( $\text{\AA}^2$ ) of  $\text{NdSc}_3(\text{BO}_3)_4\text{:R}$  (R = Ho).

Site	x/a	y/b	z/c	Occ.	Ueq	U11	U22	U33	U23	U13	U12
Nd1	0.66722(4)	0.66722(4)	0.5	0.936(1)	0.0113	0.0122(1)	0.0122(1)	0.0087(1)	-0.00026(4)	0.00026(4)	0.0055(1)
Ho1	0.66722(4)	0.66722(4)	0.5	0.091(1)	0.0113	0.0122(1)	0.0122(1)	0.0087(1)	-0.00026(4)	0.00026(4)	0.0055(1)
Sc1	0	0.8754(2)	5/6	1.006(1)	0.0353	0.0070(5)	0.0065(4)	0.0926(9)	0.0006(3)	0.0012(6)	0.0035(2)
Sc2	0.2137(1)	0.67005(9)	0.49742(5)	0.832(1)	0.0068	0.0107(3)	0.0092(2)	0.0002(2)	-0.0008(2)	-0.0016(1)	0.0046(2)
Ho2	0.2137(1)	0.67005(9)	0.49742(5)	0.090(1)	0.0068	0.0107(3)	0.0092(2)	0.0002(2)	-0.0008(2)	-0.0016(1)	0.0046(2)
O1	0.6569(5)	0.8607(5)	0.6827(7)	1	0.0280	0.0192(8)	0.0171(8)	0.0459(9)	0.0068(8)	0.0223(8)	0.0078(8)
O2	0.9645(7)	0.9175(7)	0.3987(7)	0.5	0.0164	0.0086(9)	0.0070(9)	0.0315(9)	-0.0035(9)	0.0020(9)	0.0024(8)
O3	0.4528(4)	0.4784(4)	0.3195(4)	1	0.0102	0.0151(8)	0.0113(8)	0.0065(7)	-0.0008(6)	-0.0027(6)	0.0083(6)
O4	0.3560(5)	0.6017(4)	0.6443(4)	1	0.0130	0.0194(8)	0.0118(7)	0.0099(7)	-0.0042(7)	-0.0035(7)	0.0093(7)
O5	0.6752(5)	0.8679(5)	0.3188(5)	1	0.0224	0.0294(8)	0.0343(9)	0.0154(8)	-0.0131(8)	-0.0139(7)	0.0248(7)
O6	0.8021(6)	0.8021(6)	0	1	0.0495	0.0137(6)	0.0137(6)	0.1218(10)	0.0057(7)	-0.0057(7)	0.0072(8)
O7	0.6618(4)	0.5227(4)	-0.0003(3)	1	0.0081	0.0145(8)	0.0073(8)	0.0045(7)	0.0003(6)	-0.0035(6)	0.0070(6)
B1	0.8862(5)	0.5424(5)	0.6718(4)	1	0.0059	0.0088(8)	0.0105(8)	0.0040(7)	0.0010(7)	0.0020(7)	0.0089(7)
B2	0.6718(5)	0.6718(5)	0	1	0.0083	0.0062(6)	0.0062(6)	0.0087(9)	-0.0049(5)	0.0049(5)	0.0001(8)
B3	0.7929(7)	0	2/3	1	0.0473	0.0090(9)	0.0288(9)	0.1107(10)	0.0076(9)	0.0038(4)	0.0144(4)

**Table S20.** Crystallographic coordinates, occupancies and equivalent/isotropic atomic displacement parameters ( $\text{\AA}^2$ ) of  $\text{NdSc}_3(\text{BO}_3)_4\text{:R}$  (R = Er).

Site	x/a	y/b	z/c	Occ.	Ueq	U11	U22	U33	U23	U13	U12
Nd1	0	0	0	0.964(1)	0.0046	0.0046(1)	0.0046(1)	0.0045(2)	0.0000(1)	0.0000(1)	0.0023(7)
Er1	0	0	0	0.100(1)	0.0046	0.0046(1)	0.0046(1)	0.0045(2)	0.0000(1)	0.0000(1)	0.0023(7)
Sc2	0.5440(1)	0	0	0.658(1)	0.0062	0.0037(3)	0.0035(3)	0.0111(4)	0.0017(2)	0.0009(1)	0.0017(2)
Er2	0.5440(1)	0	0	0.166(1)	0.0062	0.0037(3)	0.0035(3)	0.0111(4)	0.0017(2)	0.0009(1)	0.0017(2)
O1	0.8596(5)	0	0.5	1	0.0064	0.0024(9)	0.0072(10)	0.0113(11)	-0.0009(9)	-0.0004(5)	0.0036(5)
O2	0.5935(8)	0	0.5	1	0.0690	0.024(1)	0.088(1)	0.116(1)	-0.094(1)	-0.0471(5)	0.0443(6)
O3	0.4588(5)	0.1415(5)	0.5144(5)	1	0.0102	0.0156(10)	0.0042(9)	0.0088(10)	0.0001(8)	0.0033(9)	0.0035(8)
B1	0	0	0.5	1	0.0027	0.0025(8)	0.0025(8)	0.0030(12)	0	0	0.0013(4)
B2	0.4531(7)	0	0.5	1	0.0101	0.0056(10)	0.009(1)	0.017(1)	-0.009(1)	-0.0046(5)	0.0048(5)

**Table S21.** Crystallographic coordinates, occupancies and equivalent/isotropic atomic displacement parameters ( $\text{\AA}^2$ ) of  $\text{NdSc}_3(\text{BO}_3)_4\text{:R}$  (R = Tm).

Site	x/a	y/b	z/c	Occ.	Ueq	U11	U22	U33	U23	U13	U12
Nd1	0	0	0	0.897(1)	0.0077	0.00746(8)	0.00746(8)	0.0082(1)	0.0000(1)	0.0000(1)	0.00373(4)
Tm1	0	0	0	0.131(1)	0.0077	0.00746(8)	0.00746(8)	0.0082(1)	0.0000(1)	0.0000(1)	0.00373(4)
Sc2	0.54377(6)	0	0	0.782(1)	0.0081	0.0056(1)	0.0052(2)	0.0133(2)	0.0016(1)	0.00081(5)	0.00251(8)
Tm2	0.54377(6)	0	0	0.153(1)	0.0081	0.0056(1)	0.0052(2)	0.0133(2)	0.0016(1)	0.00081(5)	0.00251(8)
O1	0.8595(3)	0	0.5	1	0.0087	0.0045(5)	0.0084(7)	0.0145(8)	-0.0010(6)	-0.0005(3)	0.0042(3)
O2	0.5930(4)	0	0.5	1	0.0697	0.0223(7)	0.0834(10)	0.124(1)	-0.0916(9)	-0.0458(5)	0.0417(5)
O3	0.4588(3)	0.1415(2)	0.5144(3)	1	0.0127	0.0175(7)	0.0068(6)	0.0121(6)	0.0004(5)	0.0033(6)	0.0048(5)
B1	0	0	0.5	1	0.0060	0.0053(6)	0.0053(6)	0.0074(10)	0	0	0.0026(3)
B2	0.4537(4)	0	0.5	1	0.0136	0.0077(7)	0.0145(9)	0.0208(9)	-0.0102(9)	-0.0051(4)	0.0072(5)

**Table S22.** Crystallographic coordinates, occupancies and equivalent/isotropic atomic displacement parameters ( $\text{\AA}^2$ ) of  $\text{NdSc}_3(\text{BO}_3)_4\text{:R}$  (R = Yb).

Site	x/a	y/b	z/c	Occ.	Ueq	U11	U22	U33	U23	U13	U12
Nd1	0	0	0	0.966(1)	0.0050	0.0051(2)	0.0051(2)	0.0048(2)	0.0000(1)	0.0000(1)	0.00253(8)
Yb1	0	0	0	0.113(1)	0.0050	0.0051(2)	0.0051(2)	0.0048(2)	0.0000(1)	0.0000(1)	0.00253(8)
Sc2	0.5449(1)	0	0	0.659(1)	0.0051	0.0027(3)	0.0023(3)	0.0103(5)	0.0017(2)	0.0008(1)	0.0012(2)
Yb2	0.5449(1)	0	0	0.149(1)	0.0051	0.0027(3)	0.0023(3)	0.0103(5)	0.0017(2)	0.0008(1)	0.0012(2)
O1	0.8589(5)	0	0.5	1	0.0061	0.0027(9)	0.0043(9)	0.0118(10)	-0.0004(9)	-0.0002(4)	0.0021(4)
O2	0.5925(7)	0	0.5	1	0.0602	0.0190(10)	0.0723(10)	0.107(1)	-0.0776(10)	-0.0388(5)	0.0362(5)
O3	0.4584(5)	0.1419(5)	0.5152(5)	1	0.0096	0.0127(9)	0.0048(9)	0.0085(9)	0.0001(8)	0.0044(9)	0.0023(8)
B1	0	0	0.5	1	0.0037	0.0032(7)	0.0032(7)	0.0047(11)	0	0	0.0016(4)
B2	0.4533(6)	0	0.5	1	0.0099	0.0033(9)	0.0109(10)	0.0180(10)	-0.0102(10)	-0.0051(5)	0.0054(5)

**Table S23.** Crystallographic coordinates, occupancies and equivalent/isotropic atomic displacement parameters ( $\text{\AA}^2$ ) of  $\text{NdSc}_3(\text{BO}_3)_4\text{:R}$  (R = Lu).

Site	x/a	y/b	z/c	Occ.	Ueq	U11	U22	U33	U23	U13	U12
Nd1	0.66687(5)	0.66687(5)	0.5	0.889(1)	0.0059	0.0059(2)	0.0059(2)	0.0054(3)	-0.00024(7)	0.00024(7)	0.0026(2)
Lu1	0.66687(5)	0.66687(5)	0.5	0.078(1)	0.0059	0.0059(2)	0.0059(2)	0.0054(3)	-0.00024(7)	0.00024(7)	0.0026(2)
Sc1	0	0.8745(3)	5/6	0.996(1)	0.0280	-0.0001(6)	-0.0024(5)	0.0871(9)	0.0004(3)	0.0008(7)	-0.0001(3)
Sc2	0.2130(2)	0.6698(1)	0.49795(7)	0.886(1)	0.0008	0.0034(3)	0.0015(3)	-0.0030(3)	-0.0002(3)	-0.0021(2)	0.0008(2)
Lu2	0.2130(2)	0.6698(1)	0.49795(7)	0.108(1)	0.0008	0.0034(3)	0.0015(3)	-0.0030(3)	-0.0002(3)	-0.0021(2)	0.0008(2)
O1	0.6616(6)	0.8626(6)	0.6879(7)	1	0.0230	0.0076(9)	0.0068(9)	0.0478(9)	-0.0027(9)	0.0164(9)	-0.0016(8)
O2	0.9645(8)	0.9150(8)	0.4081(8)	0.5	0.0176	0.0104(9)	-0.0007(9)	0.0424(9)	0.0001(9)	-0.0004(9)	0.0018(9)
O3	0.4540(5)	0.4781(5)	0.3182(5)	1	0.0048	0.0052(8)	0.0057(8)	0.0040(8)	-0.0003(8)	0.0018(8)	0.0032(7)
O4	0.3525(6)	0.5992(6)	0.6495(5)	1	0.0134	0.0245(9)	0.0067(9)	0.0054(8)	0.0018(8)	-0.0025(9)	0.0052(8)
O5	0.6775(6)	0.8720(7)	0.3182(6)	1	0.0201	0.0200(9)	0.0367(9)	0.0171(9)	-0.0193(9)	-0.0151(8)	0.0243(8)
O6	0.7987(6)	0.7987(6)	0	1	0.0408	0.0045(6)	0.0045(6)	0.1167(10)	0.0005(7)	-0.0005(7)	0.0048(9)
O7	0.6630(5)	0.5236(6)	-0.0004(4)	1	0.0026	0.0074(9)	-0.0006(8)	-0.0018(9)	0.0009(7)	-0.0005(8)	0.0023(7)
B1	0.8848(6)	0.5456(6)	0.6717(6)	1	0.0021	0.0017(9)	0.0038(9)	0.0006(9)	0.0010(8)	0.0004(9)	0.0013(8)
B2	0.6654(6)	0.6654(6)	0	1	0.0047	0.0039(6)	0.0039(6)	0.0038(9)	-0.0013(6)	0.0013(6)	-0.0001(9)
B3	0.7887(9)	0	2/3	1	0.0374	0.0178(9)	0.0297(8)	0.0688(10)	0.0281(8)	0.0140(4)	0.0149(4)



