# **Supporting Information**

# Effect of Rare Earth (RE<sup>3+</sup>) Ionic Radii on Transparent Lanthanide Tellurite Glass-Ceramics: Correlation between 'Hole-Formalism' and Crystallization

Pritha Patra,<sup>1,2</sup> K. Jayanthi,<sup>3</sup> Margit Fabian,<sup>4</sup> Shweta R. Keshri,<sup>5</sup> Sandip Bysakh,<sup>6</sup> Kaushik Biswas,<sup>1,2</sup> Nitya Nand Gosvami,<sup>5</sup> N. M. Anoop Krishnan,<sup>7</sup> Amarnath R. Allu,<sup>2,8</sup> Kalyandurg Annapurna<sup>1,2,\*</sup>

<sup>1</sup> Specialty Glass Division, CSIR-Central Glass and Ceramic Research Institute, 196, Raja S. C. Mullick Road, Kolkata 700 032, India.

<sup>2</sup>Academy of Scientific and Innovative Research (AcSIR), CSIR- Human Resource Development

Centre, (CSIR-HRDC) Campus, Postal Staff College Area, Sector 19, Kamla Nehru Nagar, Ghaziabad, Uttar Pradesh- 201 002, India.

<sup>3</sup>ORNL, USA

<sup>4</sup>Centre for Energy Research, 1121, Budapest, Konkoly-Thege st. 29-33, Hungary.

<sup>5</sup>Department of Materials Science and Engineering, Indian Institute of Technology Delhi, Hauz Khas, New Delhi 10016, India

<sup>6</sup>Advanced Material Characterization unit, Material Characterization and Instrumentation Division, CSIR-Central Glass and Ceramic Research Institute,196 Raja S C Mullick Road, 700032, Kolkata, India.

<sup>7</sup>Department of Civil Engineering, Indian Institute of Technology Delhi, Hauz Khas, New Delhi 10016, India

<sup>8</sup>Energy Materials and Devices Division, CSIR-Central Glass and Ceramic Research Institute,196 Raja S C Mullick Road, 700032, Kolkata, India.

E-mail address: <u>annapurnak@cgcri.res.in</u>(K. Annapurna)

<sup>\*</sup>Corresponding authors:

telephone: +91-33-24733496

Fax: +91-33-24730957

### **Supplementary Information (SI):**



#### 1. X-Ray diffraction of RE doped (Ce to Dy) glasses:

Fig. S1 X-ray diffraction of all the RE (Ce, Pr, Nd, Sm, Eu, Tb, Dy) doped glasses.

### 2. RMC simulation procedure:

For the RMC starting model a random atomic configuration was built up with a simulation box containing 10 000 atoms with density data 0.0636 atomsÅ<sup>-3</sup> and half-box values  $r_{max}$ =26.98 Å for TTLG glass. In the RMC simulation procedure constraints have been used for the minimum interatomic distances between atom pairs (cut-off distances) to avoid unreasonable atom contacts. During the RMC simulations were used coordination constraints for Te, La and Gd surroundings. The starting cut-off distances have been take from previous studies.<sup>37,38,39,40,41</sup> Several RMC runs have been performed by slightly modifying the cut-off distances in the way, that the results of each run have been carefully checked to obtain reliable data for each  $g_{ij}(r)$  and coordination number distributions. For all the samples about 30-35 RMC configurations were obtained with more than 1 400 000 accepted moves of atoms.



*Fig. S2 Co-ordination numbers (CN) for (a) Te-O, (b) Ti-O, (c) O-O and (d) La-O of LGTT-Eu2 and LGTT-Tb2 glass.* 

# 3. Heat capacity measurement:



**Fig. S3** The method to identify and calculate  $T_g$ ,  $T_{g,offseb}$ ,  $\Delta T_g$  and  $\Delta C_p$  values from Cp curve.



Fig. S4 DSC thermograms for all the RE doped glasses with four non-isothermal heating rate ( $\beta$ ) of 10, 20, 30 and 40 K/min.

## 4. Thermal properties of different RE doped (Ce to Dy) glasses:

All the thermal characteristic temperatures like glass transition temperature ( $T_g$ ), crystallization onset temperature ( $T_{x1}$ ), first crystallization peak temperature ( $T_{P1}$ ), melting point ( $T_m$ ) have been tabulated in Table S1: glass thermal stability ( $\Delta T=T_{x1}-T_g$ ) is calculated using respective  $T_g$ ,  $T_{x1}$ ,  $T_{P1}$ ,  $T_m$  values, given in Table S1. For crystallization kinetics study non-isothermal DSC thermograms were recorded at different heating rates ( $\beta$ ) of 10, 20, 30 and 40 K/min for all glasses in bulk form under N<sub>2</sub> atmosphere.

Table S1: Glass-transition (Tg, °C), first onset crystallization (Tx1, °C), first crystallization peak (Tp1, °C), melting (Tm, °C), glass thermal stability ( $\Delta T$ , °C) of LGTT-Ce2, LGTT-Pr2, LGTT-Nd2, LGTT-Sm2, LGTT-Eu2, LGTT-Tb2 and LGTT-Dy2 glasses.

| Glass Name | $T_g$ | $T_{xl}$ | $T_{p1}$ | $T_m$ | ΔT |
|------------|-------|----------|----------|-------|----|
| LGTT-Ce2   | 417   | 457      | 482      | 759   | 40 |
| LGTT-Pr2   | 436   | 476      | 495      | 766   | 40 |
| LGTT-Nd2   | 433   | 482      | 510      | 768   | 49 |
| LGTT-Sm2   | 434   | 474      | 494      | 771   | 40 |
| LGTT-Eu2   | 432   | 475      | 500      | 772   | 43 |
| LGTT-Tb2   | 435   | 480      | 495      | 771   | 45 |
| LGTT-Dy2   | 431   | 472      | 492      | 770   | 41 |

Table S2: Result of the Rietveld refinements of different RE doped LGTT GCs.

| Sample  | $(\text{La/Ce Gd})_2\text{Te}_6\text{O}_{15}$ |   | $(\text{La/Pr Gd})_2\text{Te}_6\text{O}_{15}$ |   |  |
|---|---|---|---|---|--|
| Chemical  | $(La/Ce)_2Te_6O_{15}$                         | Gd <sub>2</sub> Te <sub>6</sub> O <sub>15</sub> | $(La/Pr)_2Te_6O_{15}$                         | Gd <sub>2</sub> Te <sub>6</sub> O <sub>15</sub> |  |
| formula   |   |   |   |   |  |
| Temperature   | 298 K   | 298 K   | 298 K   | 298 K   |  |
| Wavelength  | 1.5458 Å                                      | 1.5458 Å  | 1.5458 Å                                      | 1.5458 Å  |  |
| Crystal system  | Cubic   | Cubic   | Cubic   | Cubic   |  |
| Space group   | $Fm^{3}m$                                     | Fm3m  | Fm <sup>3</sup> m                             | Fm3m  |  |
| GOF   | 1.47  |   | 1.52  |   |  |
| wR  | 13.97%  |   | 15.12%  |   |  |
| $\mathbf{R}\mathbf{f}^2$  | 15.32%  | 16.36%  | 13.7%   | 11.54%  |  |
| RF  | 7.63%   | 8.56%   | 12.4%   | 11.12%  |  |
| $R = \Sigma   F_o  -  F_c   / \Sigma  F_o , wR = (\Sigma [w( F_o ^2 -  F_c ^2)^2] / \Sigma [w( F_o ^4)])^{1/2} \text{ and } w = 1/(\sigma^2 (I) + 0.0004I^2)$ |   |   |   |   |  |

| Sample  | (La/Nd Gd) <sub>2</sub> Te <sub>6</sub> O <sub>15</sub> |                  | $(\text{La Gd/Sm})_2\text{Te}_6\text{O}_{15}$ |                       |  |
|---|---|------------------|---|-----------------------|--|
| Chemical  | $(La/Nd)_2Te_6O_{15}$                                   | $Gd_2Te_6O_{15}$ | $La_2Te_6O_{15}$                              | $(Gd/Tb)_2Te_6O_{15}$ |  |
| formula   |   |                  |   |                       |  |
| Temperature   | 298 K   | 298 K            | 298 K   | 298 K                 |  |
| Wavelength  | 1.5458 Å  | 1.5458 Å         | 1.5458 Å                                      | 1.5458 Å              |  |
| <b>Crystal system</b>   | Cubic   | Cubic            | Cubic   | Cubic                 |  |
| Space group   | Fm3m  | Fm3m             | Fm3m  | Fm3m                  |  |
| GOF   | 1.38  |                  | 1.62  |                       |  |
| wR  | 10.07%  |                  | 11.56%  |                       |  |
| $\mathbf{R}\mathbf{f}^2$  | 10.52%  | 11.54%           | 9.89%   | 10.25%                |  |
| RF  | 13.02%  | 11.12%           | 10.58%  | 10.49%                |  |
| $R = \Sigma   F_o  -  F_c   / \Sigma  F_o , \ wR = (\Sigma [w( F_o ^2 -  F_c ^2)^2 \ ] / \Sigma [w( F_o ^4)])^{1/2} \ \text{and} \ w = 1 / (\sigma^2 \ (I) + 0.0004 I^2)$ |   |                  |   |                       |  |

| Sample  | (La Gd/           | $(\text{La Gd/Tb})_2\text{Te}_6\text{O}_{15}$ |                  | (La Gd/Dy) <sub>2</sub> Te <sub>6</sub> O <sub>15</sub> |  |
|---|-------------------|---|------------------|---|--|
| Chemical  | $La_2Te_6O_{15}$  | $(Gd/Tb)_2Te_6O_{15}$                         | $La_2Te_6O_{15}$ | $(Gd/Dy)_2Te_6O_{15}$                                   |  |
| formula   |                   |   |                  |   |  |
| Temperature   | 298 K             | 298 K   | 298 K            | 298 K   |  |
| Wavelength  | 1.5458 Å          | 1.5458 Å                                      | 1.5458 Å         | 1.5458 Å  |  |
| Crystal system  | Cubic             | Cubic   | Cubic            | Cubic   |  |
| Space group   | Fm <sup>3</sup> m | Fm <sup>3</sup> m                             | Fm3m             | Fm <sup>3</sup> m                                       |  |
| GOF   | 1.77              |   | 1.77             |   |  |
| wR  | 14.19%            |   | 14.19%           |   |  |
| $\mathbf{R}\mathbf{f}^2$  | 11.41%            | 10.25%  | 13.89%           | 13.39%  |  |
| RF  | 9.18%             | 10.49%  | 12.05%           | 11.25%  |  |
| $R = \Sigma   F_0  -  F_c   / \Sigma  F_0 $ , $wR = (\Sigma [w( F_0 ^2 -  F_c ^2)^2] / \Sigma [w( F_0 ^4)])^{1/2}$ and $w = 1/(\sigma^2 (I) + 0.0004I^2)$ |                   |   |                  |   |  |



Fig. S5 Representative crystal structure of  $La_2Te_6O_{15}$ , and  $(Gd/RE)_2Te_6O_{15}$  phases.



*Fig. S6 FE-SEM* images of the 3h heat-treated glass-ceramics (a) *LGTT-Ce2(GC-3h), (b) LGTT-Pr2(GC-3h), (c) LGTT-Nd2(GC-3h), (d) LGTT-Sm2(GC-3h), (e) LGTT-Tb2(GC-3h), (f) LGTT-Dy2(GC-3h).* 



*Fig. S7 FE-SEM images of the 24h heat-treated glass-ceramics (a) LGTT-Ce2(GC-24h), (b) LGTT-Pr2(GC-24h), (c) LGTT-Nd2(GC-24h), (d) LGTT-Sm2(GC-24h), (e) LGTT-Tb2(GC-24h), (f) LFTT-Dy2(GC-24h).* 



*Fig. S8 FE-SEM* images of the 36h heat-treated glass-ceramics after grinding the top surface ~0.5 mm: (a) *LGTT-Ce2(GC-36)*, (b) *LGTT-Pr2(GC-36)*, (c) *LGTT-Nd2(GC-36)*, (d) *LGTT-Sm2(GC-36)*, (e) *LGTT-Tb2(GC-36)*, (f) *LFTT-Dy2(GC-36)*.



*Fig. S9* (a) *HR-TEM* image of *LGTT-glass* (b) *BF-TEM* image of *LGTT-Pr2(GC-36h)* (c) *FE-SEM* image of the nucleated *LGTT-glass* (at 400 °C).



*Fig. 10* SAED-pattern of (a) LGTT-glass, (b) LGTT-Ce2(GC-36h), (c) LGTT-Pr2(GC-36h), (d) LGTT-Nd2(GC-36h), (e) LGTT-Sm2(GC-36h), (f) LGTT-Eu2(GC-36h) (g) LGTT-Tb2(GC-36h) (h) LGTT-Dy2(GC-36h).