Supporting Information

Effect of Rare Earth (RE³⁺) Ionic Radii on Transparent Lanthanide Tellurite Glass-Ceramics: Correlation between 'Hole-Formalism' and Crystallization

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Supplementary Information (SI):



1. X-Ray diffraction of RE doped (Ce to Dy) glasses:

Fig. S1 X-ray diffraction of all the RE (Ce, Pr, Nd, Sm, Eu, Tb, Dy) doped glasses.

2. RMC simulation procedure:

For the RMC starting model a random atomic configuration was built up with a simulation box containing 10 000 atoms with density data 0.0636 atomsÅ⁻³ and half-box values r_{max} =26.98 Å for TTLG glass. In the RMC simulation procedure constraints have been used for the minimum interatomic distances between atom pairs (cut-off distances) to avoid unreasonable atom contacts. During the RMC simulations were used coordination constraints for Te, La and Gd surroundings. The starting cut-off distances have been take from previous studies.^{37,38,39,40,41} Several RMC runs have been performed by slightly modifying the cut-off distances in the way, that the results of each run have been carefully checked to obtain reliable data for each $g_{ij}(r)$ and coordination number distributions. For all the samples about 30-35 RMC configurations were obtained with more than 1 400 000 accepted moves of atoms.



Fig. S2 Co-ordination numbers (CN) for (a) Te-O, (b) Ti-O, (c) O-O and (d) La-O of LGTT-Eu2 and LGTT-Tb2 glass.

3. Heat capacity measurement:



Fig. S3 The method to identify and calculate T_g , $T_{g,offset}$, ΔT_g and ΔC_p values from Cp curve.



Fig. S4 DSC thermograms for all the RE doped glasses with four non-isothermal heating rate (β) of 10, 20, 30 and 40 K/min.

4. Thermal properties of different RE doped (Ce to Dy) glasses:

All the thermal characteristic temperatures like glass transition temperature (T_g), crystallization onset temperature (T_{x1}), first crystallization peak temperature (T_{P1}), melting point (T_m) have been tabulated in Table S1: glass thermal stability ($\Delta T=T_{x1}-T_g$) is calculated using respective T_g , T_{x1} , T_{P1} , T_m values, given in Table S1. For crystallization kinetics study non-isothermal DSC thermograms were recorded at different heating rates (β) of 10, 20, 30 and 40 K/min for all glasses in bulk form under N₂ atmosphere.

Table S1: Glass-transition (Tg, °C), first onset crystallization (Tx1, °C), first crystallization peak (Tp1, °C), melting (Tm, °C), glass thermal stability (ΔT , °C) of LGTT-Ce2, LGTT-Pr2, LGTT-Nd2, LGTT-Sm2, LGTT-Eu2, LGTT-Tb2 and LGTT-Dy2 glasses.

Glass Name	T_g	T_{xl}	T_{p1}	T_m	ΔT
LGTT-Ce2	417	457	482	759	40
LGTT-Pr2	436	476	495	766	40
LGTT-Nd2	433	482	510	768	49
LGTT-Sm2	434	474	494	771	40
LGTT-Eu2	432	475	500	772	43
LGTT-Tb2	435	480	495	771	45
LGTT-Dy2	431	472	492	770	41

Table S2: Result of the Rietveld refinements of different RE doped LGTT GCs.

Sample	$(\text{La/Ce Gd})_2\text{Te}_6\text{O}_{15}$		$(\text{La/Pr Gd})_2\text{Te}_6\text{O}_{15}$		
Chemical	$(La/Ce)_2Te_6O_{15}$	Gd ₂ Te ₆ O ₁₅	$(La/Pr)_2Te_6O_{15}$	Gd ₂ Te ₆ O ₁₅	
formula					
Temperature	298 K	298 K	298 K	298 K	
Wavelength	1.5458 Å	1.5458 Å	1.5458 Å	1.5458 Å	
Crystal system	Cubic	Cubic	Cubic	Cubic	
Space group	$Fm^{3}m$	Fm3m	Fm ³ m	Fm3m	
GOF	1.47		1.52		
wR	13.97%		15.12%		
$\mathbf{R}\mathbf{f}^2$	15.32%	16.36%	13.7%	11.54%	
RF	7.63%	8.56%	12.4%	11.12%	
$R = \Sigma F_o - F_c / \Sigma F_o , wR = (\Sigma [w(F_o ^2 - F_c ^2)^2] / \Sigma [w(F_o ^4)])^{1/2} \text{ and } w = 1/(\sigma^2 (I) + 0.0004I^2)$					

Sample	(La/Nd Gd) ₂ Te ₆ O ₁₅		$(\text{La Gd/Sm})_2\text{Te}_6\text{O}_{15}$		
Chemical	$(La/Nd)_2Te_6O_{15}$	$Gd_2Te_6O_{15}$	$La_2Te_6O_{15}$	$(Gd/Tb)_2Te_6O_{15}$	
formula					
Temperature	298 K	298 K	298 K	298 K	
Wavelength	1.5458 Å	1.5458 Å	1.5458 Å	1.5458 Å	
Crystal system	Cubic	Cubic	Cubic	Cubic	
Space group	Fm3m	Fm3m	Fm3m	Fm3m	
GOF	1.38		1.62		
wR	10.07%		11.56%		
$\mathbf{R}\mathbf{f}^2$	10.52%	11.54%	9.89%	10.25%	
RF	13.02%	11.12%	10.58%	10.49%	
$R = \Sigma F_o - F_c / \Sigma F_o , \ wR = (\Sigma [w(F_o ^2 - F_c ^2)^2 \] / \Sigma [w(F_o ^4)])^{1/2} \ \text{and} \ w = 1 / (\sigma^2 \ (I) + 0.0004 I^2)$					

Sample	(La Gd/	$(\text{La Gd/Tb})_2\text{Te}_6\text{O}_{15}$		(La Gd/Dy) ₂ Te ₆ O ₁₅	
Chemical	$La_2Te_6O_{15}$	$(Gd/Tb)_2Te_6O_{15}$	$La_2Te_6O_{15}$	$(Gd/Dy)_2Te_6O_{15}$	
formula					
Temperature	298 K	298 K	298 K	298 K	
Wavelength	1.5458 Å	1.5458 Å	1.5458 Å	1.5458 Å	
Crystal system	Cubic	Cubic	Cubic	Cubic	
Space group	Fm ³ m	Fm ³ m	Fm3m	Fm ³ m	
GOF	1.77		1.77		
wR	14.19%		14.19%		
$\mathbf{R}\mathbf{f}^2$	11.41%	10.25%	13.89%	13.39%	
RF	9.18%	10.49%	12.05%	11.25%	
$R = \Sigma F_0 - F_c / \Sigma F_0 $, $wR = (\Sigma [w(F_0 ^2 - F_c ^2)^2] / \Sigma [w(F_0 ^4)])^{1/2}$ and $w = 1/(\sigma^2 (I) + 0.0004I^2)$					



Fig. S5 Representative crystal structure of $La_2Te_6O_{15}$, and $(Gd/RE)_2Te_6O_{15}$ phases.



Fig. S6 FE-SEM images of the 3h heat-treated glass-ceramics (a) *LGTT-Ce2(GC-3h), (b) LGTT-Pr2(GC-3h), (c) LGTT-Nd2(GC-3h), (d) LGTT-Sm2(GC-3h), (e) LGTT-Tb2(GC-3h), (f) LGTT-Dy2(GC-3h).*



*Fig. S*7 *FE-SEM* images of the 24h heat-treated glass-ceramics (a) LGTT-Ce2(GC-24h), (b) LGTT-Pr2(GC-24h), (c) LGTT-Nd2(GC-24h), (d) LGTT-Sm2(GC-24h), (e) LGTT-Tb2(GC-24h), (f) LFTT-Dy2(GC-24h).



Fig. S8 FE-SEM images of the 36h heat-treated glass-ceramics after grinding the top surface ~0.5 mm: (a) *LGTT-Ce2(GC-36)*, (b) *LGTT-Pr2(GC-36)*, (c) *LGTT-Nd2(GC-36)*, (d) *LGTT-Sm2(GC-36)*, (e) *LGTT-Tb2(GC-36)*, (f) *LFTT-Dy2(GC-36)*.



Fig. S9 (a) *HR-TEM* image of *LGTT-glass* (b) *BF-TEM* image of *LGTT-Pr2(GC-36h)* (c) *FE-SEM* image of the nucleated *LGTT-glass* (at 400 °C).



Fig. 10 SAED-pattern of (a) LGTT-glass, (b) LGTT-Ce2(GC-36h), (c) LGTT-Pr2(GC-36h), (d) LGTT-Nd2(GC-36h), (e) LGTT-Sm2(GC-36h), (f) LGTT-Eu2(GC-36h) (g) LGTT-Tb2(GC-36h) (h) LGTT-Dy2(GC-36h).