External Electric field Driven Electronic Structures: Tunable Nonlinear Optical Properties in Helical Bilayer Nanographenes

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Figure S1. Evolutions of the non-covalent interaction (NCI) and reduced density gradient (RDG) maps of the [9]HBNG under the vertical F_z ($F_z = 1 \times 10^{-4}$, au).



Figure S2. Evolutions of dipole moment (μ) of ground state under the vertical F_z ($F_z = 1 \times 10^{-4}$, au).



Figure S3. Evolutions of the first hyperpolarizabilities (β_{tot}) of [9]HBNG under the vertical F_z ($F_z = 1 \times 10^4$, au) at the M06-2X/6-31G**, CAM-B3LYP/6-31G** and BHandHLYP/6-31G** levels.



Figure S4. Evolutions of the electron density difference maps (EDDM) of the [9]HBNG under the vertical F_z ($F_z = 1 \times 10^{-4}$, au).



Figure S5. Evolutions of the 2D second-order NLO spectra the [9]HBNG ((a) $F_z = 0$ au, (b) $F_z = 100 \times 10^{-4}$ au).



Figure S6. Evolutions of the electron circular dichroism (ECD) spectrum of the [9]HBNG under the F_z ($F_z = 1 \times 10^{-4}$, au).

$F_z = 1 \times 10^{-4} (au)$	βx	β _y	βz	$\beta_{\rm tot}$
0	653	0	0	653
20	654	143	538	859
40	670	337	1121	1349
60	689	584	2028	2219
80	707	1011	4369	4540
100	1023	1603	12434	12579

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