## Supporting Information for

## Charge and Spin Thermoelectric Transport in Benzene-Based Molecular Nano-Junctions: A Quantum Many-Body Study

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Figure S 1. Sketch of the energetics for the  $6 \rightarrow 7$  transition in benzene (positive bias regime). The bold line represents the appropriate possible transitions for which current flow occurs, while the dotted line (only for ortho and meta-connections) represents the forbidden transitions that result in a current blocking situation yielding NDC at specific bias ranges. There is no current-blocking state in the para connection of benzene.



Figure S 2. The charge density distribution of 6-electron ground state  $(\phi_6^{gs})$ , spin down and spin up of 7-electron ground state  $(\phi_{7\downarrow}^{gs})$  and first excited state  $(\phi_{7\uparrow}^{1es})$  over the sites of benzene at (a) B = 2T,(b) B = 5T and (c) B = 10T respectively.

Table S I. 6e-gs and 7e-gs energy level splitting in benzene molecule weakly coupled to normal electrode at different magnetic field (B). Note: in NE,  $\phi_{7\uparrow}^{1es}$  will be  $\phi_{7\uparrow}^{gs}$ .

Electrode	$\phi_6^{gs}$	$\phi^{gs}_{7\downarrow}$	$\phi_{7\uparrow}^{1es}$
NE	-30.73	-25.68	-25.68
NE $(B=2T)$	-30.73	-25.91	-25.45
NE $(B=5T)$	-30.73	-26.25	-25.10
NE $(B=10T)$	-30.73	-26.83	-24.53

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Figure S 3. (a) The electrical conductance, (b) Seebeck coefficient, and (c) the probabilities of occupying  $4e^-$ ,  $5e^-$ ,  $6e^-$ ,  $7e^-$  and  $8e^-$  states as a function of chemical potential ( $\mu$ ) at  $k_BT = 0.1eV$ .



Figure S 4. The 2D plot of charge Seebeck coefficient as a function of different chemical potentials with varying five different temperatures showing saw-tooth pattern.



Figure S 5. (a) Represents the 2D plot of electrical conductance (b) derivative of Fermi-Dirac distribution  $(f'(\delta \varepsilon))$ , where  $\varepsilon$  is transition energy) as a function of  $\mu$  at  $T = 0.005k_BT$  (only taking the 6 $\rightarrow$ 7 transition). The inset of the figure provides a magnified view of a specific region.



Figure S 6. The maximum value of  $Z_s T$  as a function of different polarization (p).



Figure S 7. The maximum value of  $Z_s T$  as a function of different magnetic field (B).