## Study of the Nernst effect in 2D materials using first-principles calculations

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## I. DENSITY FUNCTIONAL THEORY DETAILS

First- principles density functional theory (DFT) calculations were done based on plane wave self-consistent field (PWscf) and ultrasoft pseudopotential [1] method as treated in the generalized gradient approximation [2] and implemented in Quantum Espresso package (version 7.1) [3]. Brillouin zone was sampled using Monkhorst–Pack scheme. The cutoff energy for the plane-wave-basis set  $(E_{cut})$  and k-mesh were chosen with a convergence threshold for self-consistency of 10−<sup>8</sup> Ry. DFT input parameters of this article are summarized in Table I. The electron dispersion for each material was graphed along high symmetry k-points, and the conduction bands were shifted to match the experimental band gap. The DFT calculation parameters are provided in Table.I. The experimental lattice constant of 2.464 Å for carbon family,  $a = 3.31 \text{ Å}$ , and  $b = 4.37 \text{ Å}$  for phosphorene [4] were taken from literature. A vacuum layer of 15  $\AA$  along c-crystal axis was applied to eliminate the interactions between the 2D layer and its periodic images. The force on atoms along the c-axis was negligible which indicates a vacuum layer of  $15 \text{ Å}$  is sufficient. To have localized orbitals, maximally localized Wannier functions were used which represent a successful reproduction of band structures. The Engel–Vosko exchange functional [5] which was employed for band structure calculations includes an improvement factor  $(F^{ev93})$  with a Padé form that is multiplied by LDA-like part of the functional.

$$
F^{ev93} = \frac{1 + \alpha_1 g^2 + \alpha_2 g^4 + \alpha_2 g^6}{1 + \beta_1 g^2 + \beta_2 g^4 + \beta_2 g^6}
$$
\n<sup>(1)</sup>

Where  $g = |\nabla n|/2nk_F$  and  $k_F = \sqrt[3]{(3n\pi^2)}$  are the reduced gradient and the Fermi momentum.

	Material Cutoff energy (Ry)	k-mesh	Wan-mesh $E_q^{wan}$ (eV) $E_q^{Exp}$ (eV)			
MLG	60	$19 \times 19 \times 1$	200	0.277	0.00	
$AA-BLG$	70	$19 \times 19 \times 1$	300	0.155	0.00	
$AB-BLG$	60	$19 \times 19 \times 1$	260	0.151	0.00	
Graphite	60	$19 \times 19 \times 1$	225	0.103	0.00	
ABA-TLG	65	$19 \times 19 \times 1$	210	0.015	0.00	
ABC-BLG	65	$35 \times 35 \times 1$	180	0.018	0.00	
<b>MLP</b>	70	$15 \times 11 \times 1$	320	0.514	1.75	
<b>BLP</b>	70	$15 \times 11 \times 1$	290	0.397	1.40	
TLP	70	$30 \times 22 \times 1$	180	0.251	1.02	

TABLE I. DFT and Wannierization parameters for monolayer graphene (MLG), bilayer graphene (BLG), trilayer graphene (TLG), monolayer phosphorene (MLP), bilayer phosphorene (BLP), and trilayer phosphorene (TLP).

## II. FULL BAND STRUCTURES

The full band structures of carbon-family materials and trilayer phosphorene are shown in Figs. 1 and 2, respectively. The effect of van der Waals correction on the band structure of monolayer phosphorene is shown in Fig. 3. This demonstrates that the band structures with and without van der Waals correction are virtually indistinguishable and therefore the van der Waals correction is not expected to affect the calculated Nernst coefficients.



FIG. 1. DFT (orange solid lines) and wannierized (blue dashed lines) structure of graphite (a), monolayer (b), AB stacked bilayer (c), AA stacked bilayer (d), ABA stacked trilayer (e), and ABC stacked trilayer graphene (f). In each case zero is the intrinsic Fermi level.



FIG. 2. Wannierized band structure (blue dashed lines) of trilayer phosphorene along with DFT bands (orange solid lines).



FIG. 3. The band structure of monolayer phosphorene calculated with and without van der Waals correction (blue dashed and orange solid lines, respectively).

## III. SCATTERING RATES

Electron-phonon and ionized impurity scattering rates were computed using ElecTra package which requires Fermi surface (carried out by Quantum Espresso) and physical properties of each material. ElecTra code takes various scattering mechanisms into account, namely acoustic phonon deformation potential, polar optical phonons and ionized impurity scattering. The scattering rates' input parameters were adopted from experiments when available; otherwise, we computed them. Table II provides an overview of the input parameters for the materials investigated in this study.

$\epsilon$ z $\omega_{ph}$ (cm <sup>-1</sup> ) $\mathbf{G}$ (Pa) $\mathcal{D}_e^a$ (eV) $\mathcal{D}_h^a$ (eV) $\mathcal{D}_e^o$ (eV/A) $\mathcal{D}_h^o$ (eV/A) $\mathbf{E}$ (Pa) Material $1 \times 10^{12}$ [8] $2.8 \times 10^{11}$ [8] $9.30$ [9] 1 70 [6] 100 [7] 51[6] 100 [7] MLG $2\times10^{12}$ [12] $2.205\times10^{11}$ [12] $3.5$ [13] 1 $2.83$ [11] 7.25 $AA-BLG$ $0.93$ [11] 6.96 2.78 [14] $2.5 \times 10^{12}$ [15] $1.64 \times 10^{11}$ [16] $8 \begin{bmatrix} 17 \\ 1 \end{bmatrix}$ $AB-BLG$ $1.01$ [14] 7.5 5.8 1.49 $3.25 \times 10^{12}$ [18] $4.7 \times 10^{11}$ [18] ABA-TLG $6.2$ [19] 1 4.78 5.01 $0.56\,$ $1.47 \; 3.31 \times 10^{12} \; [20]$ $1.3 \times 10^{11}$ [20] $5.4$ [19] 1 ABC-TLG 0.55 4.15 4.90 0.253 [22] $3.8 \times 10^{10}$ [23] $4.2 \times 10^{9}$ [23] 17.1508 [9] 1 $0.249$ [22] $0.45$ [21] $0.50$ [21] Graphite $4.1 \times 10^{10}$ [26] 2.2 [25] $1.66 \times 10^{11}$ [26] $2.6$ [27] 1 $6.2$ [25] <b>MLP</b> $1.33$ [24] $1.11$ [24] $3.8 \times 10^{10}$ [26] $2.9$ [29] 1 2.28 [25] $1.62 \times 10^{11}$ [26] 1.40 [24] 1.65 [24] $1.7 \; [25]$ <b>BLP</b> $3.7 \times 10^{10}$ [26] 0.42 [30] $1.59 \times 10^{11}$ [26] TLP 1.51 [24] $1.62$ [24] $3.5$ [29] 1 439 [28] $0.50$ [30]					
					1586 [10] 1587 [10] 1588 [10] 1586 [10] 1586 [10] 1582 [10] 438 [28] 441 [28]

TABLE II. Acoustic  $(\mathcal{D}^a)$  and optical  $(\mathcal{D}^o)$  deformation potentials for electrons (e) and holes (h), bulk modulus (E), shear modulus (G), dielectric constant ( $\epsilon$ ), ionized impurity charge (z), and phonon frequency ( $\omega_{ph}$ ) used in this work.

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