

Supporting Information

Modulating Optical Performance by Phase Transition in a Nonlinear Optical Material β -Li₂RbBi(PO₄)₂

Lei Wu,^a Ruixin Zhang,^b Qun Jing,^{*b} Hongyu Huang,^a Xianmeng He,^a Zhongchang Wang,^{*c} Zhaohui
Chen^{*a}

^a Key Laboratory of Oil & Gas Fine Chemicals, Ministry of Education and Xinjiang Uyghur Autonomous
Region, School of Chemical Engineering and Technology, Xinjiang University, Urumqi 830017, China

^b Xinjiang Key Laboratory of Solid State Physics and Devices, School of Physical Science and Technology,
Xinjiang University, Urumqi 830017, China

^c International Iberian Nanotechnology Laboratory (INL), Braga 4715-330, Portugal

*To whom correspondence should be addressed. E-mails: chenzhaohui@xju.edu.cn (Z.H.C.);
qunjing@xju.edu.cn (Q.J.); zhongchang.wang@inl.int (Z.C.W.)

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Table S1. Crystal data and structure refinements for the β -Li₂RbBi(PO₄)₂.

Empirical formula	Li ₂ RbBi(PO ₄) ₂
Formula weight	498.27
Temperature/K	273(2)
Wavelength/ Å	0.71073
Crystal system	Monoclinic
Space group	<i>P</i> 2 ₁
<i>a</i> /Å	8.1067(3)
<i>b</i> /Å	5.0152(2)
<i>c</i> /Å	18.6456(7)
α /°	90.00
β /°	91.0760(10)
γ /°	90.00
Volume/Å ³	757.94(5)
Z, Calculated density/ (g/cm ³)	4, 4.376
Absorption coefficient / (mm ⁻¹)	30.074
<i>F</i> (000)	880.0
Crystal size/mm ³	0.17 × 0.058 × 0.025
2 θ range for data collection/°	6.56 to 52
Index ranges	-9 ≤ <i>h</i> ≤ 9, -6 ≤ <i>k</i> ≤ 6, -22 ≤ <i>l</i> ≤ 22
Reflections collected / unique	10992 / 2961 [R(int) = 0.0376]
Completeness to theta = 26.00	99.6 %
Absorption correction	30.074
Refinement method	Full-matrix least-squares on <i>F</i> ²
Data/restraints/parameters	2961/73/272
Goodness-of-fit on <i>F</i> ²	1.061
Final <i>R</i> indexes [<i>I</i> ≥ 2 σ (<i>I</i>)]	<i>R</i> ₁ = 0.0353, <i>wR</i> ₂ = 0.0962
Final <i>R</i> indexes [all data]	<i>R</i> ₁ = 0.0374, <i>wR</i> ₂ = 0.0974
Extinction coefficient	0.00488(14)
Largest diff. peak/hole / e Å ⁻³	2.62/-3.04

$$^a R_1 = \sum ||F_o| - |F_c|| / \sum |F_o| \text{ and } wR_2 = [\sum w(F_o^2 - F_c^2)^2 / \sum wF_o^4]^{1/2} \text{ for } F_o^2 > 2\sigma(F_o^2)$$

Table S2. Atomic coordinates ($\times 10^4$) and equivalent isotropic displacement parameters ($\text{\AA}^2 \times 10^3$) for the β - $\text{Li}_2\text{RbBi}(\text{PO}_4)_2$.

Atom	x	y	z	U(eq)
Li(1)	4722(15)	8390(30)	5873(7)	7(1)
Li(2)	11585(16)	13380(30)	7820(7)	10(1)
Li(3)	14532(16)	13440(30)	6938(7)	9(1)
Li(4)	6660(20)	3220(40)	9668(9)	27(4)
Rb(1)	4867(1)	8216(2)	8565(1)	10(1)
Rb(2)	11823(1)	3480(2)	5646(1)	10(1)
Bi(1)	8156(1)	7678(1)	6806(1)	8(1)
Bi(2)	-17(1)	8073(1)	8930(1)	25(1)
P(1)	6876(2)	3346(4)	5680(1)	6(1)
P(2)	7747(3)	3418(4)	8056(1)	10(1)
P(3)	2625(3)	3240(5)	9516(1)	21(1)
P(4)	12206(2)	8415(4)	7078(1)	7(1)
O(1)	13128(8)	8701(13)	5115(3)	15(2)
O(2)	9259(8)	4796(14)	7696(4)	18(2)
O(3)	-2254(10)	4507(16)	8816(4)	30(1)
O(4)	2376(10)	10257(17)	9569(5)	32(2)
O(5)	2594(8)	5484(12)	7137(3)	12(2)
O(6)	7968(10)	461(15)	8062(5)	35(2)
O(7)	6208(9)	4227(16)	7640(4)	27(2)
O(8)	5445(8)	4757(13)	6038(3)	12(1)
O(9)	8521(8)	4628(13)	6000(4)	15(2)
O(10)	1861(11)	4370(17)	8832(5)	38(1)
O(11)	11802(8)	9567(13)	7819(3)	14(2)
O(12)	10655(8)	8823(14)	6587(3)	18(2)
O(13)	6919(7)	300(12)	5858(3)	10(1)
O(14)	13620(8)	9917(12)	6739(3)	11(1)
O(15A)	4120(20)	4550(40)	9816(10)	40(1)
O(15B)	4520(20)	3340(40)	9276(10)	48(1)
O(16A)	2190(20)	4600(30)	10187(9)	30(1)
O(16B)	1000(30)	4760(40)	9974(12)	55(1)

U_{eq} is defined as one-third of the trace of the orthogonalized U_{ij} tensor.

Table S3. Selected bond distances (Å) and angles (deg) for the β -Li₂RbBi(PO₄)₂.

Li(1)-O(1) ^{#1}	1.903(14)	P(1)-O(1) ^{#13}	1.492(6)
Li(1)-O(8)	1.938(15)	P(1)-O(8)	1.525(7)
Li(1)-O(14) ^{#1}	2.012(14)	P(1)-O(13)	1.564(6)
Li(1)-O(13) ^{#2}	2.023(14)	P(1)-O(9)	1.587(7)
Li(2)-O(5) ^{#5}	1.855(15)	P(2)-O(6)	1.494(8)
Li(2)-O(11)	1.920(15)	P(2)-O(7)	1.513(7)
Li(2)-O(10) ^{#5}	1.959(16)	P(2)-O(3) ^{#6}	1.518(8)
Li(2)-O(2) ^{#2}	2.024(15)	P(2)-O(2)	1.570(7)
Li(3)-O(7) ^{#5}	1.909(15)	P(3)-O(16A)	1.475(16)
Li(3)-O(5) ^{#5}	1.919(15)	P(3)-O(15A)	1.482(18)
Li(3)-O(14)	1.948(15)	P(3)-O(4) ^{#9}	1.513(9)
Li(3)-O(8) ^{#5}	1.961(15)	P(3)-O(10)	1.517(9)
Li(4)-O(15B)	1.86(2)	P(3)-O(15B)	1.612(18)
Li(4)-O(4) ^{#7}	1.907(19)	P(3)-O(16B)	1.76(2)
Li(4)-O(3) ^{#6}	1.943(19)	P(4)-O(5) ^{#6}	1.507(6)
Li(4)-O(16A) ^{#7}	2.06(2)	P(4)-O(14)	1.519(7)
Li(4)-O(15A)	2.18(3)	P(4)-O(11)	1.539(6)
Li(4)-O(15A) ^{#7}	2.18(3)	P(4)-O(12)	1.555(6)
Li(4)-O(16B) ^{#7}	2.65(3)	O(1) ^{#13} -P(1)-O(8)	113.1(4)
Rb(1)-O(15B)	2.80(2)	O(1) ^{#13} -P(1)-O(13)	109.1(4)
Rb(1)-O(7)	2.869(8)	O(8)-P(1)-O(13)	112.0(4)
Rb(1)-O(15B) ^{#2}	2.91(2)	O(1) ^{#13} -P(1)-O(9)	108.1(4)
Rb(1)-O(11) ^{#1}	2.905(7)	O(8)-P(1)-O(9)	106.7(4)
Rb(1)-O(6) ^{#2}	2.925(9)	O(13)-P(1)-O(9)	107.5(3)
Rb(1)-O(4)	2.962(8)	O(6)-P(2)-O(7)	111.6(5)
Rb(1)-O(3) ^{#6}	3.014(8)	O(6)-P(2)-O(3) ^{#6}	110.6(5)
Rb(1)-O(15A)	3.039(19)	O(7)-P(2)-O(3) ^{#6}	111.6(4)
Rb(1)-O(10)	3.155(9)	O(6)-P(2)-O(2)	110.2(4)
Rb(1)-O(15A) ^{#8}	3.184(18)	O(7)-P(2)-O(2)	107.8(4)
Rb(1)-O(16A) ^{#8}	3.373(16)	O(3) ^{#6} -P(2)-O(2)	104.8(4)
Rb(2)-O(1) ^{#9}	2.807(6)	O(16A)-P(3)-O(15A)	71.5(10)

Rb(2)-O(9)	2.828(6)	O(16A)-P(3)-O(4)#9	111.5(7)
Rb(2)-O(1)	2.999(6)	O(15A)-P(3)-O(4)#9	121.5(8)
Rb(2)-O(5)#6	3.012(6)	O(16A)-P(3)-O(10)	116.2(7)
Rb(2)-O(14)#9	3.060(6)	O(15A)-P(3)-O(10)	118.1(8)
Rb(2)-O(8)#6	3.080(6)	O(4)#9-P(3)-O(10)	111.8(5)
Rb(2)-O(12)#9	3.081(7)	O(16A)-P(3)-O(15B)	117.7(9)
Rb(2)-O(13)#10	3.137(6)	O(15A)-P(3)-O(15B)	46.3(10)
Rb(2)-O(12)	3.350(7)	O(4)#9-P(3)-O(15B)	100.3(8)
Bi(1)-O(12)	2.153(6)	O(10)-P(3)-O(15B)	97.6(7)
Bi(1)-O(9)	2.168(7)	O(16A)-P(3)-O(16B)	36.2(9)
Bi(1)-O(2)	2.364(7)	O(15A)-P(3)-O(16B)	103.9(10)
Bi(1)-O(13)#2	2.406(6)	O(4)#9-P(3)-O(16B)	107.2(8)
Bi(1)-O(6)#2	2.734(9)	O(10)-P(3)-O(16B)	87.0(8)
Bi(2)-O(16B)#12	2.36(2)	O(15B)-P(3)-O(16B)	148.1(11)
Bi(2)-O(10)	2.411(9)	O(5)#6-P(4)-O(14)	110.9(4)
Bi(2)-O(4)	2.509(8)	O(5)#6-P(4)-O(11)	110.4(4)
Bi(2)-O(3)	2.553(8)	O(14)-P(4)-O(11)	111.2(4)
Bi(2)-O(16A)#12	2.550(16)	O(5)#6-P(4)-O(12)	109.7(4)
Bi(2)-O(6)#4	2.573(9)	O(14)-P(4)-O(12)	107.3(4)
Bi(2)-O(11)#1	2.673(6)	O(11)-P(4)-O(12)	107.2(4)
Bi(2)-O(16B)	2.68(2)		

Symmetry transformations used to generate equivalent atoms:

#1	$x-1, y, z$	#2	$x, y+1, z$	#3	$x-1, y-1, z$
#4	$x-1, y+1, z$	#5	$x+1, y+1, z$	#6	$x+1, y, z$
#7	$-x+1, y-1/2, -z+2$	#8	$-x+1, y+1/2, -z+2$	#9	$x, y-1, z$
#10	$-x+2, y+1/2, -z+1$	#11	$x+1, y-1, z$	#12	$-x, y+1/2, -z+2$
#13	$-x+2, y-1/2, -z+1$	#14	$-x, y-1/2, -z+2$		

Table S4. Anisotropic displacement parameters ($\text{Å}^2 \times 10^3$) for the $\beta\text{-Li}_2\text{RbBi}(\text{PO}_4)_2$.

	U11	U22	U33	U23	U13	U12
Li(1)	7(2)	6(2)	7(2)	0(1)	0(1)	0(1)
Li(2)	10(2)	10(2)	10(2)	0(1)	0(1)	0(1)
Li(3)	9(2)	9(2)	9(2)	0(1)	0(1)	0(1)
Li(4)	34(8)	21(9)	24(8)	6(8)	-14(7)	-6(8)
Rb(1)	6(1)	12(1)	12(1)	-1(1)	3(1)	0(1)
Rb(2)	11(1)	10(1)	10(1)	0(1)	3(1)	2(1)
Bi(1)	9(1)	9(1)	6(1)	0(1)	-1(1)	1(1)
Bi(2)	25(1)	24(1)	26(1)	-3(1)	-4(1)	1(1)
P(1)	8(1)	5(1)	5(1)	1(1)	-1(1)	-2(1)
P(2)	10(1)	10(1)	11(1)	4(1)	-1(1)	0(1)
P(3)	25(1)	25(1)	12(1)	2(1)	-4(1)	-16(1)
P(4)	7(1)	5(1)	10(1)	-3(1)	2(1)	-2(1)
O(1)	18(3)	18(3)	9(3)	-8(2)	-5(2)	-3(3)
O(2)	17(3)	22(3)	14(3)	10(3)	-3(3)	-5(3)
O(3)	31(1)	30(1)	28(2)	2(1)	1(1)	1(1)
O(4)	27(4)	38(5)	32(4)	7(4)	-3(4)	-3(4)
O(5)	8(3)	9(3)	17(3)	2(3)	-4(3)	3(2)
O(6)	32(4)	19(4)	53(5)	14(4)	7(4)	2(3)
O(7)	16(3)	39(4)	27(4)	-10(3)	-8(3)	4(3)
O(8)	13(1)	12(1)	13(1)	1(1)	0(1)	2(1)
O(9)	13(1)	11(3)	19(3)	-4(3)	-7(3)	-7(3)
O(10)	40(1)	38(2)	37(2)	0(1)	-1(1)	1(1)
O(11)	21(3)	15(3)	7(3)	-4(2)	6(3)	4(3)
O(12)	13(3)	28(4)	14(3)	8(3)	-4(3)	-3(3)
O(13)	10(1)	10(1)	10(1)	1(1)	-1(1)	0(1)
O(14)	11(1)	10(1)	11(1)	0(1)	0(1)	-1(1)
O(15A)	40(2)	40(2)	40(2)	1(1)	0(1)	0(1)
O(15B)	48(2)	48(2)	49(2)	0(1)	1(1)	0(1)
O(16A)	30(2)	30(2)	29(2)	-1(1)	1(1)	0(1)
O(16B)	55(2)	55(2)	55(2)	0(1)	2(1)	0(1)

Table S5. Bond valence analysis of the β -Li₂RbBi(PO₄)₂.

β -Li ₂ RbBi(PO ₄) ₂								
Atom	Li(1)	Li(2)	Li(3)	Li(4)	Rb(1)	Rb(2)	Bi(1)	Bi(2)
Σ Cations	1.04	1.13	1.13	1.09	1.26	1.19	2.73	2.56
Atom	P(1)	P(2)	P(3)	P(4)	O(1)	O(2)	O(3)	O(4)
Σ Cations	4.76	4.99	4.77	4.90	2.02	1.80	1.95	2.05
Atom	O(5)	O(6)	O(7)	O(8)	O(9)	O(10)	O(11)	O(12)
Σ Cations	2.08	1.96	1.77	1.89	2.07	2.04	1.87	2.15
Atom	O(13)	O(14)	O(15)	O(16)				
Σ Cations	1.86	1.87	1.88	1.79				

Table S6. SHG response of all the Bi-based phosphates.

materials	Group	SHG(\times KDP)	ref
$\text{Li}_2\text{KBi}(\text{PO}_4)_2$	$P2_1$	5	1
$\beta\text{-Li}_2\text{RbBi}(\text{PO}_4)_2$	$P2_1$	5.2	this work
$\alpha\text{-Li}_2\text{RbBi}(\text{PO}_4)_2$	$C2$	3.1	1
$\text{Li}_2\text{CsBi}(\text{PO}_4)_2$	$C2$	2.5	1
$\text{CsBi}(\text{P}_4\text{O}_{12})$	$\bar{I}A_3d$	4.2	2
$\text{K}_3\text{SrBi}(\text{P}_2\text{O}_7)_2$	$P2_1$	4	3
$\text{Bi}_{32}\text{Cd}_3\text{P}_{10}\text{O}_{76}$	$C2$	4	4
$\text{Cd}_3\text{Bi}(\text{PO}_4)_3$	$\bar{I}A_3d$	3.8	5
$\text{Pb}_3\text{Bi}(\text{PO}_4)_3$	$\bar{I}A_3d$	3	5
$\text{Sr}_3\text{Bi}(\text{PO}_4)_3$	$\bar{I}A_3d$	2.85	5
$\text{Rb}_3\text{PbBi}(\text{P}_2\text{O}_7)_2$	$P2_1$	2.8	6
$\text{Rb}_3\text{BaBi}(\text{P}_2\text{O}_7)_2$	$P2_1$	2.5	7
$\text{Bi}_6\text{ZnO}_7(\text{PO}_4)_2$	$I2$	2.5	8
$\text{Rb}_3\text{SrBi}(\text{P}_2\text{O}_7)_2$	$P2_1$	2.1	3
$\text{Cs}_3\text{PbBi}(\text{P}_2\text{O}_7)_2$	$P2_12_12_1$	1.1	6
$\text{Cs}_3\text{BaBi}(\text{P}_2\text{O}_7)_2$	$P2_12_12_1$	0.8	7
$\text{RbPbBi}_2(\text{PO}_4)_3$	$P3_12_1$	0.7	9
$\text{Ca}_3\text{Bi}(\text{PO}_4)_3$	$\bar{I}A_3d$	0.64	5
$\text{Ba}_3\text{Bi}(\text{PO}_4)_3$	$\bar{I}A_3d$	0.5	10
$\text{K}_6\text{Bi}_{13}(\text{PO}_4)_{15}$	$C2$	weak	11

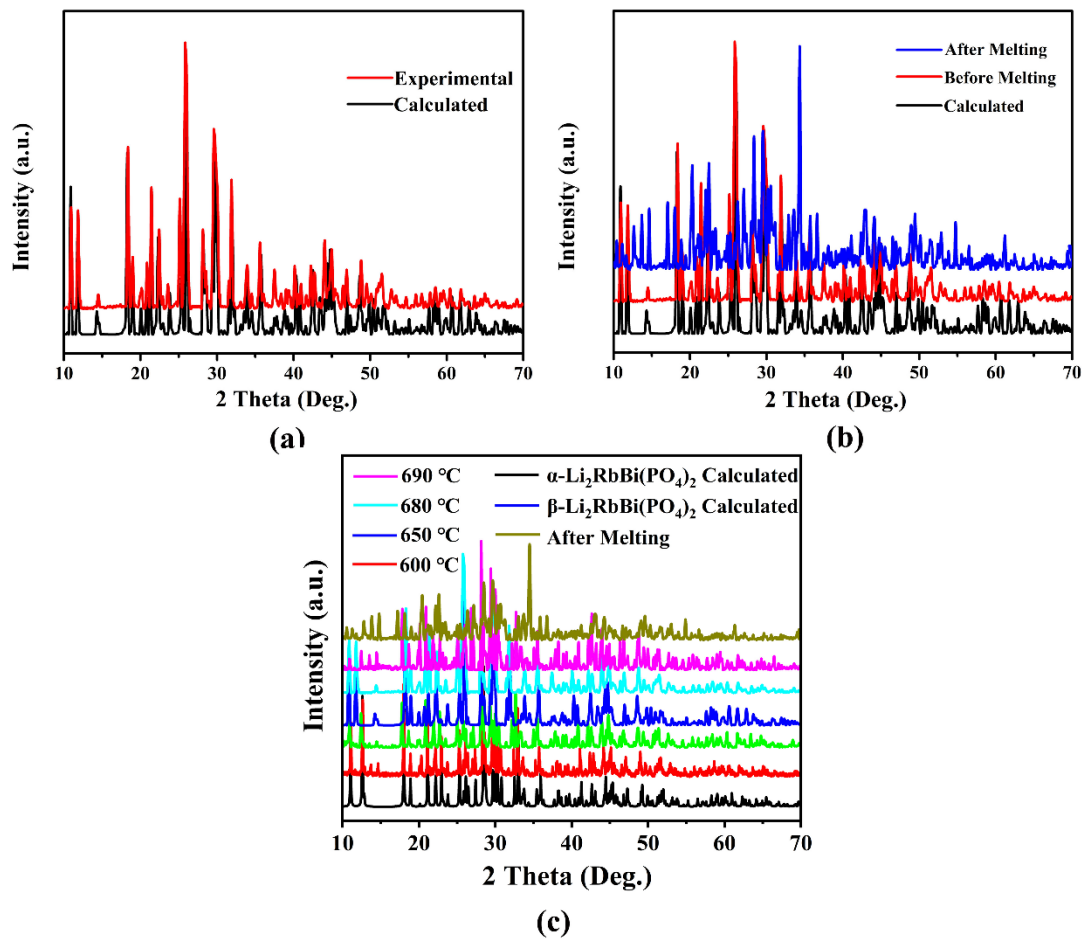


Figure S1. XRD patterns of β - $\text{Li}_2\text{RbBi}(\text{PO}_4)_2$. (a) Experimental and calculated XRD patterns of the β - $\text{Li}_2\text{RbBi}(\text{PO}_4)_2$. (b) XRD patterns of the β - $\text{Li}_2\text{RbBi}(\text{PO}_4)_2$ before and after melting. (c) XRD phase analysis of the sintered samples at different temperatures.

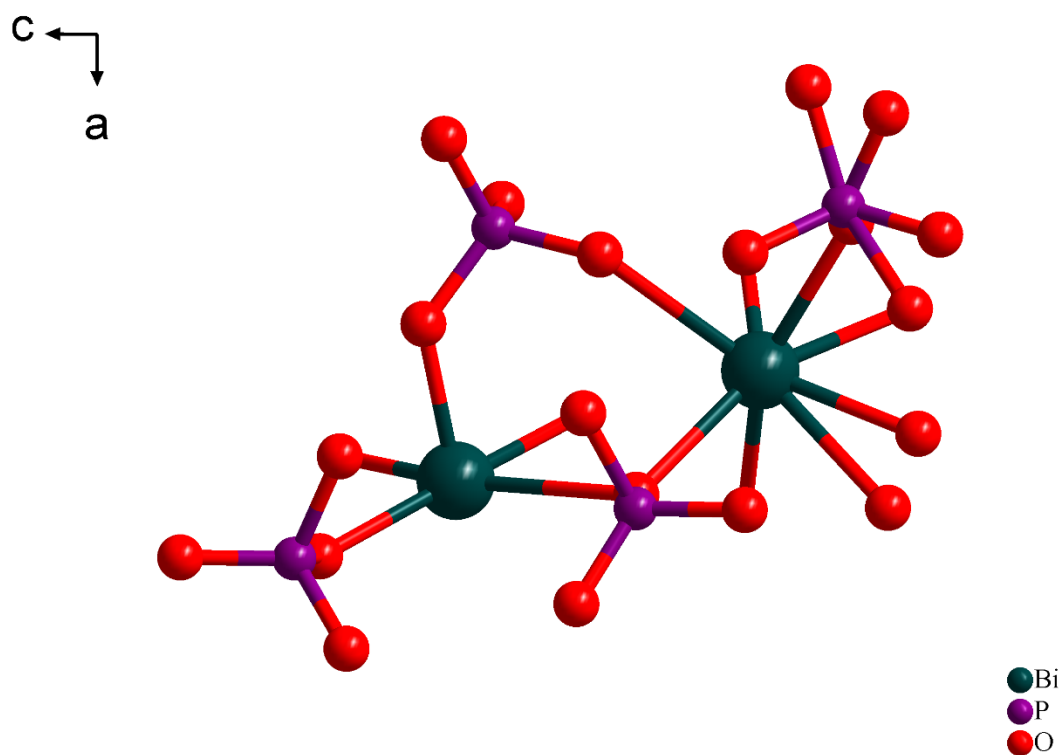


Figure S2. Coordinated environment of Bi atoms in the β - $\text{Li}_2\text{RbBi}(\text{PO}_4)_2$.

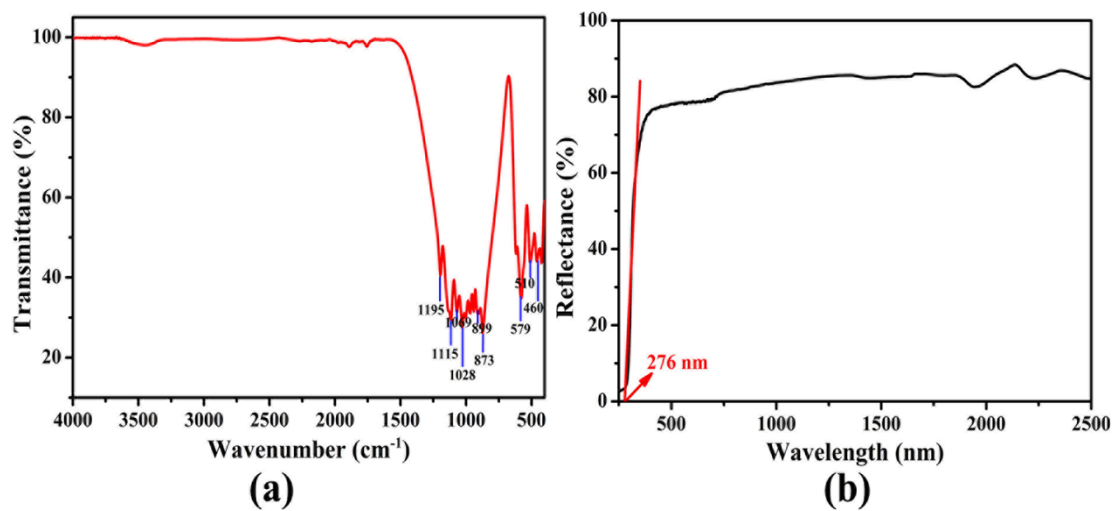


Figure S3. (a,b) IR (a) and UV-Vis-NIR (b) diffuse reflectance spectra of the β -Li₂RbBi(PO₄)₂.

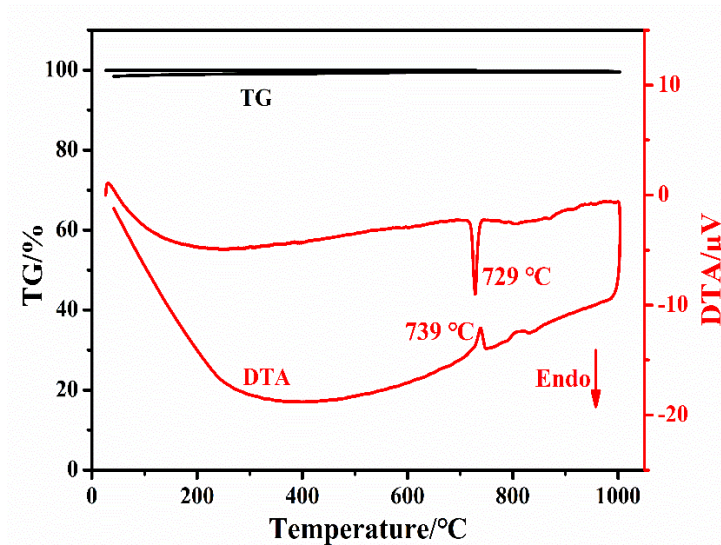


Figure S4. TG-DTA analysis of the $\beta\text{-Li}_2\text{RbBi}(\text{PO}_4)_2$.

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