Supplementary Material:

Hard Carbon Microspheres with Bimodal Size Distribution and Hierarchical Porosity via Hydrothermal Carbonization of Trehalose

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Supplementary Figure 1: HIM images of (A) Tre-pMS before and (B) Tre-HCMS after pyrolysis. Scale bars are 10 µm.



Supplementary Figure 2: HIM images of (A) Glu-pMS before and (B) Glu-HCMS after pyrolysis. Scale bars are 2 µm.



Supplementary Figure 3: Unedited HIM images of (a) Tre-pMS before and (b) Tre-HCMS after pyrolysis.



Supplementary Figure 4: XPS core-level spectra of Glu-pMS and Glu-HCMS.



Supplementary Figure 5: Nitrogen adsorption isotherms of Tre-HCMS and Glu-HCMS.

Supplementary Information on SAXS Measurements:

The SAXS data (Figure 4in the paper) were deconvoluted according to the Debye-Bueche model [1,2]:

$$I(Q) = I_{porod} + I_{pores} \tag{1}$$

$$I_{porod} = \frac{A}{Q^p} \tag{2}$$

$$I_{pores} = \sum_{i=1}^{N} \frac{B_i}{(1+\xi_i^2 \cdot Q^2)^2}$$
(3)

 I_{porod} and I_{pores} are the signal contributions of the macroscopic sphere surfaces and the pores within the spheres, respectively. Here, the sum over *N* pore sizes is taken to account for a multimodal pore size distribution. *A* and *B_i* are constants related to the total surface area and the scattering length density contrast of the sample. *p* is the Porod exponent, which is related to the smoothness of the sphere surface. ξ_i is the characteristic length over which electron density variations occur, related to the radius of gyration of the scattering object, i.e. the pores [3].

The scattering vector *q* is defined by

$$q = \frac{4\pi}{\lambda} \sin\left[\frac{\theta}{2}\right]$$
(4)

where λ is the wavelength and θ is the scattering angle.

The average pore diameter *d* is given by

$$d = 2 \cdot \xi_i \cdot \sqrt{10}.$$

The fit parameters and the resulting correlation lengths are listed in Supplementary Table 1. Three different pore sizes were found for Tre-HCMS, resulting in two additional parameters B_2 and B_3 .

Supplementary Table 1: Fit parameters for the data shown in Figure 4.

sample	Α	p	B_1	ξ_1	d_1	<i>B</i> ₂	ξ_2	d_2	<i>B</i> ₃	ξ_3	d_3
	(Å⁻¤)			(Å)	(nm)		(Å)	(nm)		(Å)	(nm)
Tre-HCMS	2.3e-06	4	0.70	2.3	1.45	26.54	24	15.18	25629	225	142.30
Glu-HCMS	3.5e-06	4	0.21	2.3	1.45	-	-		-	-	

Supplementary References

- [1] Debye, P., Anderson Jr, H. R., & Brumberger, H. (**1957**). Scattering by an inhomogeneous solid. II. The correlation function and its application. Journal of applied Physics, 28(6), 679-683. DOI: 10.1063/1.1722830
- [2] Debye, P., & Bueche, A. M. (**1949**). Scattering by an inhomogeneous solid. Journal of Applied Physics, 20(6), 518-525. DOI: 10.1063/1.1698419
- [3] Stevens, D. A., & Dahn, J. R. (**2000**). An in situ small-angle X-ray scattering study of sodium insertion into a nanoporous carbon anode material within an operating electrochemical cell. Journal of The Electrochemical Society, 147(12), 4428. DOI: 10.1149/1.1394081