

Supporting information for

**Predicted superconductivity in one-dimensional  $A_3Hf_2B_3$ -type electrides**

Yulong Chen, Teng Xie, Ziqiang Chen, Zhou Cui, Cuilian Wen\*, and Baisheng Sa\*

*Multiscale Computational Materials Facility & Materials Genome Institute, School of Materials  
Science and Engineering, Fuzhou University, Fuzhou 350108, P. R. China*

**Corresponding Authors:** \*clwen@fzu.edu.cn (C. Wen); \*bssa@fzu.edu.cn (B. Sa)

Table S1. The structure information and formation energies ( $E_f$ ) for  $\text{Ca}_3\text{Hf}_2\text{Ge}_3$ ,  $\text{Ca}_3\text{Hf}_2\text{Sn}_3$ , and  $\text{Sr}_3\text{Hf}_2\text{Pb}_3$

Compounds	Space group	Lattice parameters (Å)	$E_f$ (eV/atom)
$\text{Ca}_3\text{Hf}_2\text{Ge}_3$	$\bar{\text{P}63/mcm}$	$a = 8.426, c = 6.084$	-0.40
$\text{Ca}_3\text{Hf}_2\text{Sn}_3$	$\bar{\text{P}63/mcm}$	$a = 8.972, c = 6.187$	-0.32
$\text{Sr}_3\text{Hf}_2\text{Pb}_3$	$\bar{\text{P}63/mcm}$	$a = 9.454, c = 6.400$	-0.05

**Table S2.** The EPC parameter ( $\lambda$ ),  $\omega_{\log}$ ,  $T_c$  for  $\text{Ca}_3\text{Hf}_2\text{Ge}_3$ ,  $\text{Ca}_3\text{Hf}_2\text{Sn}_3$ , and  $\text{Sr}_3\text{Hf}_2\text{Pb}_3$

Compound	Pressure (GPa)	$\lambda$	$\omega_{\log}$ (K)	$T_c$ (K)
$\text{Ca}_3\text{Hf}_2\text{Ge}_3$	0	0.46	139.35	1.16
$\text{Ca}_3\text{Hf}_2\text{Ge}_3$	15	0.54	128.09	1.96
$\text{Ca}_3\text{Hf}_2\text{Sn}_3$	0	0.46	122.63	1.04
$\text{Ca}_3\text{Hf}_2\text{Sn}_3$	12	0.42	138.82	0.71
$\text{Sr}_3\text{Hf}_2\text{Pb}_3$	0	0.74	73.62	4.02
$\text{Sr}_3\text{Hf}_2\text{Pb}_3$	9.3	0.67	101.08	2.69

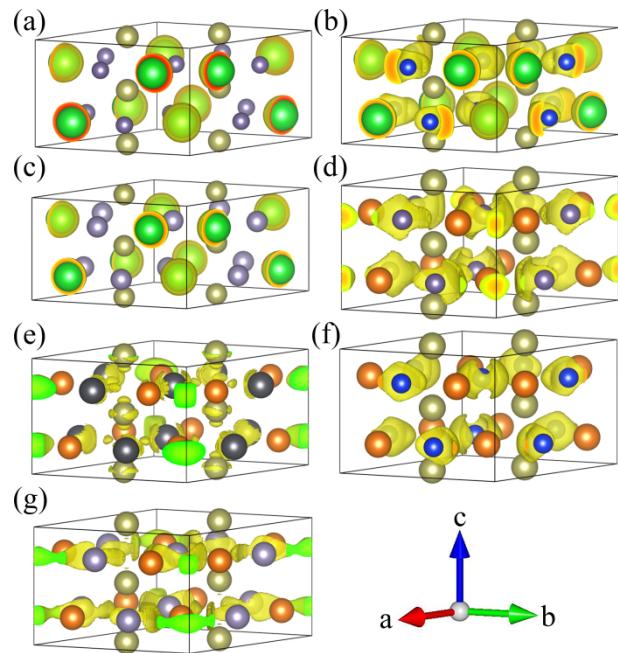


Figure S1. The ELF 3D plots with isosurface value of 0.75 for (a)  $\text{Ba}_3\text{Hf}_2\text{Ge}_3$ , (b)  $\text{Ba}_3\text{Hf}_2\text{Si}_3$ , (c)  $\text{Ba}_3\text{Hf}_2\text{Sn}_3$ , (d)  $\text{Mg}_3\text{Hf}_2\text{Ge}_3$ , (e)  $\text{Mg}_3\text{Hf}_2\text{Pb}_3$ , (f)  $\text{Mg}_3\text{Hf}_2\text{Si}_3$  and (g)  $\text{Mg}_3\text{Hf}_2\text{Sn}_3$ . The isosurfaces are plotted at values of 0.75 in (a, b, c, and f), and 0.55 in (d, e, and g), respectively.

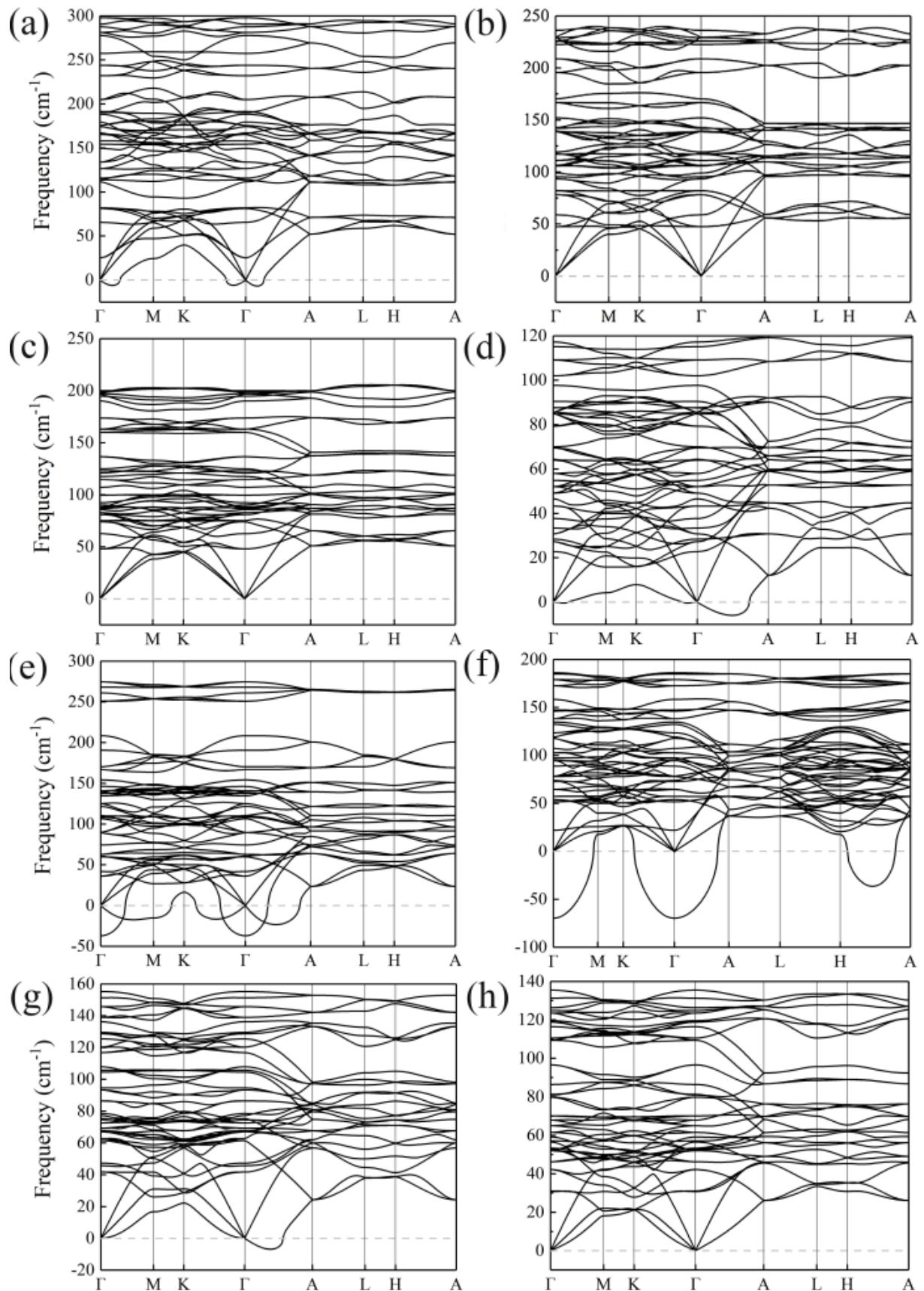
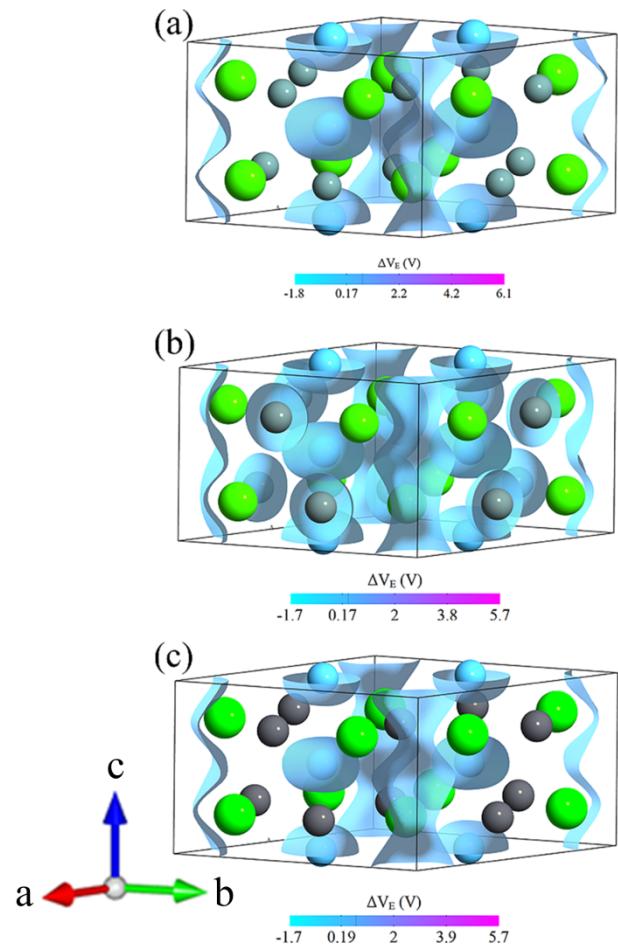


Figure S2. The phonon dispersion curves for (a)  $\text{Ca}_3\text{Hf}_2\text{Si}_3$ , (b)  $\text{Ca}_3\text{Hf}_2\text{Ge}_3$ , (c)  $\text{Ca}_3\text{Hf}_2\text{Sn}_3$ , (d)  $\text{Ba}_3\text{Hf}_2\text{Pb}_3$ , (e)  $\text{Sr}_3\text{Hf}_2\text{Si}_3$ , (f)  $\text{Sr}_3\text{Hf}_2\text{Ge}_3$ , (g)  $\text{Sr}_3\text{Hf}_2\text{Sn}_3$  and (h)  $\text{Sr}_3\text{Hf}_2\text{Pb}_3$ .



**Figure S3.** The electrostatic difference potential for (a)  $\text{Ca}_3\text{Hf}_2\text{Ge}_3$ , (b)  $\text{Ca}_3\text{Hf}_2\text{Sn}_3$ , and (c)  $\text{Sr}_3\text{Hf}_2\text{Pb}_3$  with an isosurface value of 0.77 V, 0.38 V, and 0.7 V, respectively.

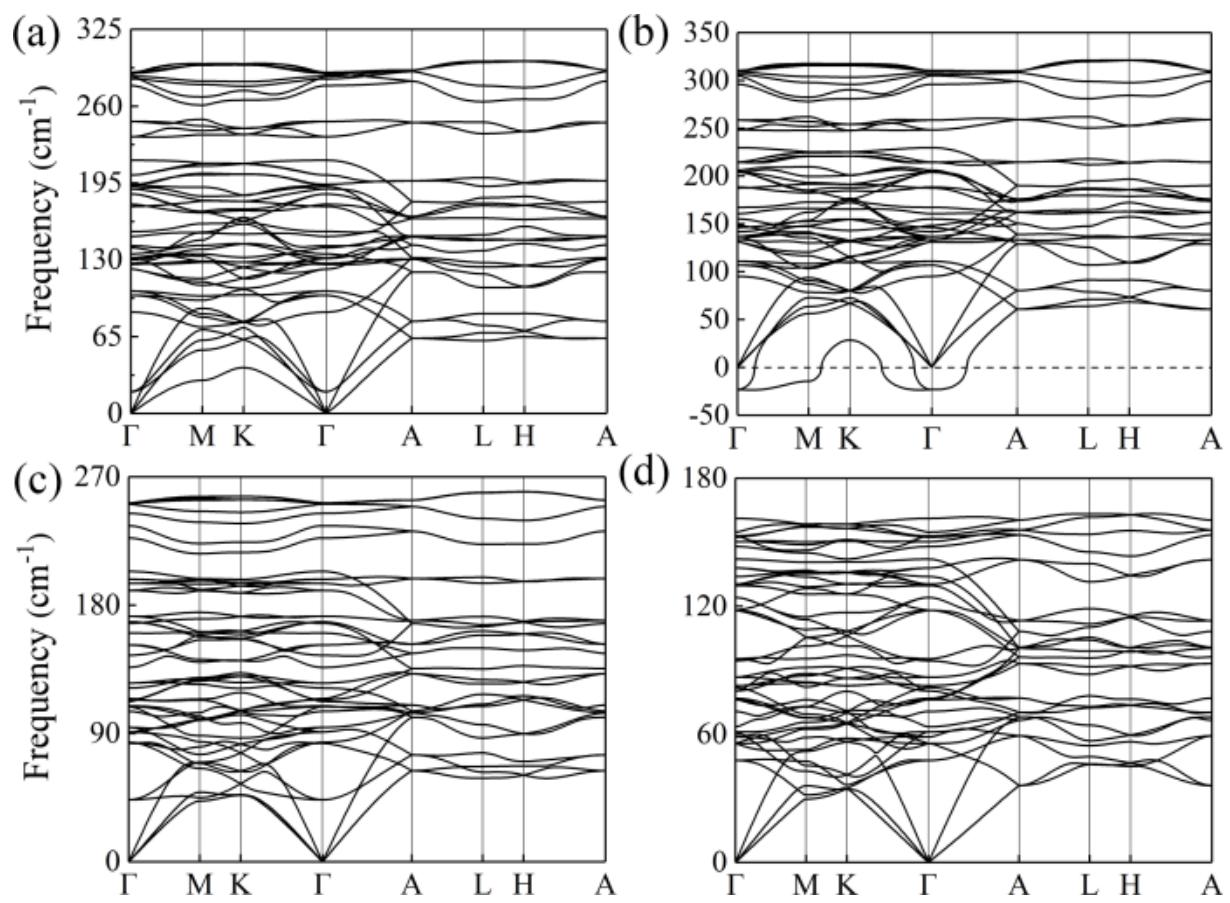


Figure S4. The phonon dispersion curves for  $\text{Ca}_3\text{Hf}_2\text{Ge}_3$  at (a) 15 GPa, (b) 20 GPa, (c)  $\text{Ca}_3\text{Hf}_2\text{Sn}_3$  at 12 GPa, and (d)  $\text{Sr}_3\text{Hf}_2\text{Pb}_3$  at 9.3 GPa.

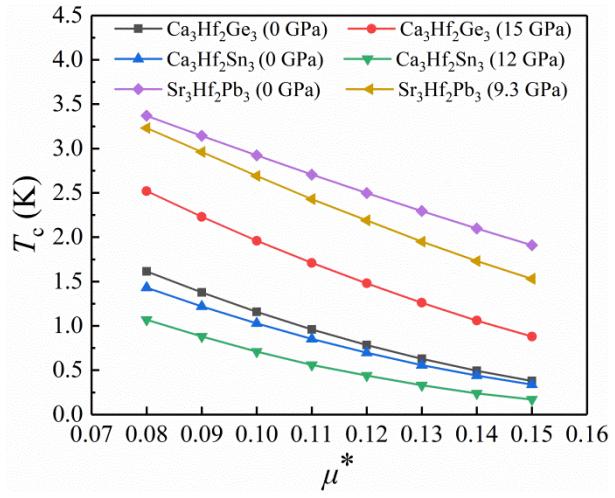


Figure S5. The variation of superconducting transition temperature  $T_c$  for  $\text{Ca}_3\text{Hf}_2\text{Ge}_3$ ,  $\text{Ca}_3\text{Hf}_2\text{Sn}_3$ ,  $\text{Sr}_3\text{Hf}_2\text{Pb}_3$  with the Coulomb pseudopotential coefficient under different pressures.