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Electronic Supplementary Information

Metal-carbon bonding in early lanthanide substituted cyclopentadienyl complexes probed by pulsed EPR spectroscopy

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1. Synthetic Procedures for 1-Ln

[La(Cp^t)₃] (1-La). THF (30 mL) was added to a pre-cooled (-78 °C) ampoule containing LaCl₃ (0.491 g, 2 mmol) and KCp^{tt} (1.298 g, 6 mmol). The reaction mixture was allowed to reflux for 16 hours. The solvent was removed *in vacuo* and toluene (30 mL) was added. The reaction mixture was allowed to reflux for 40 hours. The resultant pale yellow suspension was allowed to settle for 3 hours and filtered. The pale yellow solution was concentrated to 2 mL and stored at 8 °C to afford 1-La as colourless crystals (0.550 g, 41%). Anal calcd (%) for C₃₉H₆₃La: C, 69.81; H, 9.47. Found (%): C, 67.03; H, 9.50. ¹H NMR (C₆D₆, 400 MHz, 298 K): $\delta = 1.35$ (s, 54H, C(CH₃)₃), 6.21 (s, 3H, Cp-*H*), 6.28 (s, 6H, Cp-*H*) ppm. ¹³C{¹H} NMR (C₆D₆, 100 MHz, 298 K): $\delta = 32.77$ (C(CH₃)₃), 33.75 (*C*(CH₃)₃), 110.57 (*C*H-Cp ring), 110.69 (*C*H-Cp ring), 143.45 (*C*-Cp ring) ppm. FTIR (ATR, microcrystalline): $\tilde{v} = 2960$ (s), 2899 (w), 2862 (w), 1459 (m), 1388 (w), 1356 (m), 1252 (s), 1198 (w), 1163 (w), 1088 (br, s), 1018 (s), 927 (w), 803 (s), 736 (s), 660 (w), 605 (w) cm⁻¹.

[Ce(Cp^t)₃] (1-Ce). THF (30 mL) was added to a pre-cooled (-78 °C) ampoule containing CeCl₃ (0.493 g, 2 mmol) and KCp^{tt} (1.298 g, 6 mmol). The reaction mixture was allowed to reflux for 16 hours. The solvent was removed *in vacuo* and toluene (30 mL) was added. The dark green reaction mixture was allowed to reflux for 40 hours. The resultant suspension was allowed to settle for 3 hours and filtered. The dark purple solution was concentrated to 2 mL and stored at 8 °C to afford 1-Ce as blue crystals (0.721 g, 54%). Anal calcd (%) for C₃₉H₆₃Ce: C, 69.68; H, 9.45. Found (%): C, 67.49; H, 9.43. ¹H NMR (C₆D₆, 500 MHz, 298 K): $\delta = -5.01$ (s, 54H, C(CH₃)₃), 17.14 (s, 6H, Cp-*H*), 26.30 (s, 3H, Cp-*H*) ppm. The paramagnetism of 1-Ce precluded assignment of its ¹³C{¹H} NMR spectrum. FTIR (ATR, microcrystalline): $\tilde{v} = 2951$ (br, s), 2899 (w), 2863 (w), 1459 (s), 1388 (m), 1356 (s), 1298 (w), 1251 (s), 1198 (m), 1164 (s), 1051 (m), 1021 (m), 927 (s), 806 (s), 738 (s), 674 (s), 659 (s), 604 (w), 556 (br, w), 480 (w), 422 (m) cm⁻¹.

[Nd(Cp^{tt})₃] (1-Nd). THF (30 mL) was added to a pre-cooled (-78 °C) ampoule containing NdCl₃ (0.501 g, 2 mmol) and KCp^{tt} (1.298 g, 6 mmol). The light blue mixture was allowed to reflux for 16 hours. The solvent was removed in *vacuo* and toluene (30 mL) was added. The reaction mixture was allowed to reflux for 40 hours. The resultant suspension was allowed to settle for 3 hours and filtered. The green solution was concentrated to 2 mL and stored at 8 °C to give 1-Nd as green crystals (0.460 g, 34%). Anal calcd (%) for C₃₉H₆₃Nd: C, 69.26; H, 9.40. Found (%): C, 65.81; H, 9.30. ¹H NMR (C₆D₆, 400 MHz, 298 K): $\delta = -9.06$ (s, 54H, C(CH₃)₃), 12.68 (s, 6H, Cp-*H*), 34.47 (s, 3H, Cp-*H*). The paramagnetism of 1-Nd precluded assignment of its ¹³C{¹H} NMR spectrum. FTIR (ATR, microcrystalline): $\tilde{v} = 2950$ (s), 2899 (w), 2863 (w), 1459 (s), 1388 (w), 1356 (s), 1251 (s), 1164 (m), 1060 (br, w), 1021 (w), 927 (s), 806 (s), 737 (s), 659 (s), 605 (w), 423 (w) cm⁻¹.

[Sm(Cp^{tt})₃] (1-Sm). THF (30 mL) was added to a pre-cooled (-78 °C) ampoule containing SmCl₃ (0.513 g, 2 mmol) and KCp^{tt} (1.298 g, 6 mmol). The reaction mixture was allowed to reflux for 16 hours. The bright yellow solvent was removed *in vacuo* and toluene (30 mL) was added. The reaction mixture was allowed to reflux for 40 hours. The resultant suspension was allowed to settle for 3 hours and filtered. The orange solution was concentrated to 2 mL and stored at 8 °C to afford **1-Sm** as orange crystals (0.716 g, 52%). ¹H NMR (C₆D₆, 400 MHz, 298 K): $\delta = -1.58$ (s, 54H, C(CH₃)₃), 18.66 (s, 6H, Cp-*H*), 21.19 (s, 3H, Cp-*H*). The paramagnetism of **1-Sm** precluded assignment of its ¹³C{¹H} NMR spectrum. FTIR (ATR, microcrystalline): $\tilde{v} = 2952$ (s), 2901 (m), 2864 (w), 1460 (s), 1390 (s), 1366 (s), 1298 (s), 1250 (s), 1199 (s), 1164 (s), 1085 (w), 1060 (w), 1022 (m), 927 (s), 807 (s), 741 (s), 700 (s), 661 (s), 606 (m), 560 (m), 519 (w), 483 (w), 426 (s) cm⁻¹.

2. NMR Spectroscopy



Figure S1. ¹H NMR spectrum of complex **1-La** in C_6D_6 zoomed in the region 1 and 7.5 ppm. Solvent residual marked.



Figure S2. ¹³C{¹H} NMR spectrum of complex **1-La** in C₆D₆. Solvent residual marked.



Figure S3. ¹H NMR spectrum of complex **1-Ce** in C_6D_6 zoomed in the region –7 and 28 ppm. Solvent residual marked; minor diamagnetic impurities can be seen between 0 and 4 ppm.



Figure S4. ¹H NMR spectrum of complex **1-Nd** in C_6D_6 zoomed in the region –20 and 40 ppm. Solvent residual marked; minor diamagnetic impurities can be seen between 0 and 7 ppm.



Figure S5. ¹H NMR spectrum of complex **1-Sm** in C_6D_6 zoomed in the region –4 and 22. Solvent residual marked; minor diamagnetic impurities can be seen between –1 and 7 ppm.

3. ATR-IR spectroscopy



Figure S6. ATR-IR spectrum of 1-La recorded as a microcrystalline powder.



Figure S7. ATR-IR spectrum of 1-Ce recorded as a microcrystalline powder.



Figure S8. ATR-IR spectrum of 1-Nd recorded as a microcrystalline powder.



Figure S9. ATR-IR spectrum of 1-Sm recorded as a microcrystalline powder.



Figure S10. ATR-IR spectra of **1-La**, **1-Ce**, **1-Nd**, **1-Sm** in the region 1600–400 cm⁻¹ intended to show the similarities between both spectra.

4. Crystallography

The crystal data for complexes **1-La** and **1-Nd** are compiled in **Table S1**, and are depicted in Figures S11 and S12, respectively. Crystals of **1-La** and **1-Nd** were examined using an Oxford Diffraction Supernova diffractometer with a CCD area detector and a mirror-monochromated Mo K α radiation ($\lambda = 0.71073$ Å). Intensities were integrated from data recorded on 1° frames by ω rotation. Cell parameters were refined from the observed positions of all strong reflections in each data set. A Gaussian grid face-indexed (**1-Nd**) or multi-scan (**1-La**) absorption correction with a beam profile was applied.¹ The structures were solved using SHELXS;² the datasets were refined by full-matrix least-squares on all unique F^2 values,³ with anisotropic displacement parameters for all non-hydrogen atoms, and with constrained riding hydrogen geometries; U_{iso} (H) was set at 1.2 (1.5 for methyl groups) times U_{eq} of the parent atom. The largest features in final difference syntheses were close to heavy atoms and were of no chemical significance. CrysAlisPro¹ was used for control and integration, and SHELX^{2.3} was employed through OLEX2⁴ for structure solution and refinement. ORTEP-3⁵ and POV-Ray⁶ were employed for molecular graphics. CCDC 2271676 and 2271677 contain the supplementary crystal data for this article. These data can be obtained free of charge from the Cambridge Crystallographic Data Centre via <u>www.ccdc.cam.ac.uk/data request/cif</u>.

Powder XRD data of microcrystalline samples of **1-Ln** mounted with a minimum amount of fomblin were collected at 100(2) K using a Rigaku FR-X rotating anode single crystal X-ray diffractometer using Cu K α radiation ($\lambda = 1.5418$ Å) with a Hypix-6000HE detector and an Oxford Cryosystems nitrogen flow gas system (Figures S13-S16). Data were collected between 2–70 ° θ with a detector distance of 150 mm and a beam divergence of 1.5 mRad using CrysAlisPro.¹ For data processing, the instrument was calibrated using silver behenate as standard, then the data were reduced and integrated using CrysAlisPro.¹

Table S1. Crystallographic data for 1-La and 1-Nd.

	1-La	1-Nd
Formula	$C_{39}H_{63}La$	C ₃₉ H ₆₃ Nd
Formula weight	670.80	676.13
Crystal size, mm	$0.05\times0.06\times0.07$	$0.24 \times 0.31 \times 0.44$
Crystal system	triclinic	monoclinic
Space group	<i>P</i> -1	$P2_{1}/n$
a, Å	10.7001(8)	10.7938(3)
b, Å	18.4935(9)	19.4422(5)
c, Å	19.7113(13)	17.8596(5)
α, °	83.299(5)	90
β, °	77.365(6)	104.394(3)
γ, °	74.640(5)	90
$V, Å^3$	3663.0(4)	3630.25(18)
Z	4	4
$\rho_{\rm calc}, {\rm g} {\rm cm}^3$	1.216	1.237
μ , mm ⁻¹	1.189	1.453
F(000)	1416	1428
No. of reflections (unique)	21453(13284)	15912 (6631)
S ^a	1.00	1.06
$R_1(wR_2) (F^2 > 2\sigma(F^2))$	0.0559 (0.0926)	0.0451 (0.0968)
R _{int}	0.050	0.042
Min./max. diff map, Å ⁻³	-1.01, 1.06	-0.44, 1.74

^{*a*}Conventional $R = \Sigma ||Fo| - |Fc|| / \Sigma |Fo|$; $Rw = [\Sigma w (Fo^2 - Fc^2)^2 / \Sigma w (Fo^2)^2]^{1/2}$; $S = [\Sigma w (Fo^2 - Fc^2)^2 / no.$ data – no. params)]^{1/2} for all data.

4.1 Molecular structures of 1-La and 1-Nd



Figure S11. Molecular structure of $[La(Cp^t)_3]$ (1-La) with selected labelling. Displacement ellipsoidsset at 30 % probability level and hydrogen atoms are omitted for clarity. Selected distances and angles:La1…Cp_{centroid1}, 2.657(2) Å; La1…Cp_{centroid2}, 2.623(2) Å; La1…Cp_{centroid3}, 2.625(3) Å;Cp_{centroid1}…La1…Cp_{centroid2}, 120.38(7)°; Cp_{centroid1}…La1…Cp_{centroid3}, 118.74(8)°;Cp_{centroid2}...La1…Cp_{centroid3}, 120.88(8)°.



Figure S12. Molecular structure of $[Nd(Cp^{tt})_3]$ (1-Nd) with selected labelling. Displacement ellipsoidsset at 30 % probability level and hydrogen atoms are omitted for clarity. Selected distances and angles:Nd1...Cp_{centroid1}, 2.558(18) Å; Nd1...Cp_{centroid2}, 2.558(16) Å; Nd1...Cp_{centroid3}, 2.567(15) Å;Cp_{centroid1}...Nd1...Cp_{centroid2}, 119.68(5)°; Cp_{centroid1}...Nd1...Cp_{centroid3}, 120.60(6)°;Cp_{centroid2}...Nd1...Cp_{centroid3}, 119.71(6)°.



Figure S13. Simulated X-ray diffraction pattern from single crystal X-ray diffraction at 150 K (red) compared to experimental powder XRD pattern at 100 K (black) for **1-La** (arbitrary intensities).



Figure S14. Simulated X-ray diffraction pattern from single crystal X-ray diffraction at 150 K (red) compared to experimental powder XRD pattern at 100 K (black) for **1-Ce** (arbitrary intensities).



Figure S15. Simulated X-ray diffraction pattern from single crystal X-ray diffraction at 150 K (red) compared to experimental powder XRD pattern at 100 K (black) for **1-Nd** (arbitrary intensities).



Figure S16. Simulated X-ray diffraction pattern from single crystal X-ray diffraction at 130 K (red) compared to experimental powder XRD pattern at 100 K (black) for **1-Sm** (arbitrary intensities).

5. UV/vis/NIR Spectroscopy



Figure S17. UV-vis-NIR spectrum of **1-La** between 36000–6000 cm⁻¹ (278–1650 nm) recorded as a 0.5 mM solution in toluene.



Figure S18. UV-vis-NIR spectrum of **1-Ce** between 34000–6000 cm⁻¹ (295–1650 nm) recorded as a 0.5 mM solution in toluene. Inset shows the region 22000–14000 cm⁻¹ (455–714 nm).



Figure S19. UV-vis-NIR spectrum of **1-Nd** between 34000–6000 cm⁻¹ (295–1650 nm) recorded as a 0.5 mM solution in toluene. Inset shows the region 18000–12000 cm⁻¹ (555–833 nm).



Figure S20. UV-vis-NIR spectrum of **1-Sm** between 34000–6000 cm⁻¹ (295–1650 nm) recorded as a 0.5 mM solution in toluene. Inset shows the region 8000–6000 cm⁻¹ (1250–1667 nm).



Figure S21. UV-vis-NIR spectrum of **1-La**, **1-Ce**, **1-Nd**, **1-Sm**, in the region 6000–30000 cm⁻¹ (inset 6000–20000 cm⁻¹) recorded as 0.5 mM solutions in toluene at room temperature.

6. Magnetic Studies

Magnetic measurements were performed on solid-state polycrystalline samples restrained in a known amount of eicosane (to prevent orientation of the crystallites with the applied magnetic field) and flamesealed under vacuum in a borosilicate glass NMR tube. The ampoule was mounted in the centre of a drinking straw by wrapping in Kapton tape and using friction, and the straw was fixed to the end of the sample rod. Data for 1-Nd and 1-Ce were collected with a Quantum Design MPMS3 SQUID magnetometer. Measurements were performed in dc scan mode with a scan length of 30 mm and scan time of 4 s. Equilibrium susceptibility measurements on 1-Ce and 1-Nd were performed under a dc magnetic field of 0.1 T upon cooling from 300 to 1.8 K. Complex 1-Ce was found to slowly thermally equilibrate; for each temperature below 100 K the moment was measured continually until an equilibrium value was obtained. For compound 1-Nd, waits were employed at each temperature to ensure equilibration: 300-100 K: 10 min, 90-5 K: 30 min; 5-2 K: 10 mins, 1.8 K: 18 min. Isothermal magnetization measurements were performed at 2 and 4 K, 0-7 T with a minimum of 10 min waits at each field point. Measurements for 1-Sm were performed on a Quantum Design MPMS-XL7 using dc scans. Susceptibility measurements were performed between 2–300 K in a 0.5 T dc field and isothermal magnetization measurements were performed at 2 and 4 K, 0–7 T. Experimental data were corrected for the diamagnetism of the sample, using Pascal's constants, for the shape of the sample using the Quantum Design Geometry Simulator (MPMS3 data), and for the contribution of the sample holder and eicosane using calibrated blanks.



Figure S22. Field dependence of the magnetization for **1-Nd** at 2 and 4 K. Solid lines from CASSCF-SO calculations using the XRD geometry.



Figure S23. Field dependence of the magnetization for **1-Ce** at 2 and 4 K. Solid lines from CASSCF-SO calculations on molecule 1 using the XRD geometry (there are two independent molecules with different metrical parameters in the unit cell of **1-Ce**, so both were computed; see Section 8 for details).



Figure S24. Field dependence of the magnetization for **1-Sm** at 2 and 4 K. Solid lines from CASSCF-SO calculations using the XRD geometry.

7. EPR Spectroscopy

7.1 Continuous-wave EPR Measurements

Continuous-wave (CW) electron paramagnetic resonance (EPR) spectra of **1-Ln** (Figs. S26-S28) were recorded on Bruker EMX 300 and Bruker ElexSys E580 EPR spectrometers operating at either X-band (*ca.* 9.4-9.8 GHz) or Q-band (*ca.* 34 GHz) mw frequencies and variable temperatures. Spectra were simulated using the EasySpin software.⁷



Figure S25. Experimental (black) and simulated (red) CW X-band EPR spectra of **1-Nd** (a) 10 mM toluene-hexane (9:1) solution at 8 K; (b) powder at 5 K. We observe polycrystallinity effects, previously reported for similar complexes.⁸ Simulation parameters are given in Table S2.



Figure S26. Experimental (black) and simulated (red) CW X-band EPR spectra of **1-Ce** (a) 20 mM toluene-hexane (9:1) solution at 10 K; (b) powder at 10 K. We observe polycrystallinity effects, previously reported for similar complexes.⁸ Simulation parameters are given in Table S2.



Figure S27. Experimental (black) and simulated (red) CW X-band EPR spectra of **1-Sm** (left) 20 mM toluene-hexane (9:1) solution at 20 K; (right) powder at 15 K. We observe polycrystallinity effects, previously reported for similar complexes.⁸ Simulation parameters are given in Table S2.

Compound	Τ	g	A (MHz)
	(K)		
1-Nd (10 mM, Tol/Hex)	8	$g_{\rm x/y/z} = 3.332/1.22/0.56$	$ A_{\rm x/y/z}{}^{\rm Nd} = 1280/700/200$
1-Nd (powder)	5	$g_{\rm x/y/z} = 2.70/1.92/0.714$	$ A_{x/y/z}^{\rm Nd} = 980/350/100$
1-Ce (10 mM, Tol/Hex)	10	$g_{\rm x/y/z} = 3.15/1.88/0.636$	-
1-Ce (powder)	10	$g_{x/y/z} = 3.24/1.92-1.81/0.588$	-
1-Sm (10 mM, Tol/Hex)	20	$g_{\rm x/y/z} = 0.917/0.917/0.477$	$ A_{\rm x/y/z}{}^{\rm Sm} = 180/180/955$
1-Sm (powder)	15	$g_{\rm x/y/z} = 0.917/0.917/0.477$	$ A_{x/y/z}^{Sm} = 180/180/955$

Table S2. Hamiltonian parameters obtained from the CW simulation of 1-Ce, 1-Nd and 1-Sm.

7.2 Pulsed EPR Measurements

Pulsed EPR spectra were recorded with a Bruker ElexSys E580 instrument equipped with either a MD5 or a MD4 resonator, and operating at *ca*. 9.7 GHz and various temperatures. Solution samples of different concentrations (2, 5 and 10 mM in toluene/hexane) were investigated to check reproducibility and to achieve an acceptable signal-to-noise response in HYSCORE experiments. Data were simulated with the Easy Spin software package.⁷

7.2.1. Echo-detected EPR

The echo-detected field–swept (EDFS) spectra recorded at 9.7 GHz (X-band) (Figures 5, S28 and S29) were recorded with a two-pulse primary Hahn-echo sequence $(\pi/2 - \tau - \pi - \tau - echo)$,⁹ with microwave π pulses of 32 or 64 ns, a fixed delay time $\tau = 300$ ns, and with the variation of the static B_0 magnetic field. Those measurements at 34 GHz (Q-band; Figure S30) were recorded with microwave π pulses of 40 ns, and a fixed delay time $\tau = 300$ ns.



Figure S28. Calculated derivative of the X-band (9.7 GHz) EDFS spectra in Figure 5, for frozen solutions of **1-Nd** and **1-Ce** at 5 K.



Figure S29. (left) X-band (9.7 GHz) EDFS spectrum of a frozen solution (10 mM in 9:1 toluene-hexane at 5 K) of **1-Sm**. Arrows indicate the observer field positions where T_1 and T_m were measured. (right) Calculated derivative for the same EDFS spectrum.



Figure S30. Q-band (34 GHz) EDFS spectra of frozen solutions (10 mM in 9:1 toluene-hexane) of (a) **1-Nd** at 3 K and (b) **1-Ce** at 5 K. Arrows indicate the observer positions at which T_1 (blue) and T_m (green) were measured.

7.2.2. Phase Memory Time (T_m)

Electron spin echo envelope modulation (ESEEM) measurements involved monitoring the echo intensity generated with a primary Hahn-echo sequence as a function of τ . A similar pulse sequence was used to measure the phase memory time, T_m , with the difference that longer pulse durations (up to 128 ns) were necessary to suppress possible ¹H nuclear modulation effects in the echo decays (Figures S31-S33). T_m was determined by least squares fitting of the experimental echo decay data using a stretched exponential function with a solver based on the Levenberg-Marquardt algorithm. The fitting function used was:

$$Y(2\tau) = Y(0)e^{(-2\tau/T_m)X}$$
 (Equation 1)

or, for strongly modulated data,

$$Y(2\tau) = Y(0)e^{(-2\tau/T_m)X}(1 + k\sin(\omega t + \Phi)) \quad \text{(Equation 2)}$$

where *k* is the modulation depth, ω is the Larmor angular frequency of a nucleus *I* coupled to the electron spin, ϕ is the phase correction, *X* is the stretching parameter, *Y*(2 τ) is the echo integral for a pulse separation τ , and *Y*(0) is the echo intensity extrapolated to $\tau = 0.^{10-13}$ The extracted *T*_m times are given in Tables S3-S7.



Figure S31. Normalized Hahn echo signal intensities of **1-Nd** as a function of the inter-pulse delay 2τ at different magnetic fields at 5 K, measured with π/τ (ns) of (a) 32/200; (b) 64/300, and (c) 128/400.



Figure S32. Normalized Hahn echo signal intensities of **1-Ce** and **1-Sm** as a function of the inter-pulse delay 2τ at different magnetic fields at 5 K, measured with π/τ (ns) of (left) 128/500 and (right) 32/200.



Figure S33. Normalized Hahn echo signal intensities at Q-band of (left) **1-Nd** and (right) **1-Ce** as a function of the inter-pulse delay 2τ at different magnetic fields at 5 K, measured with π/τ (ns) of 40/400.

<u>7.2.3. Spin–lattice Relaxation Time (T_1) </u>

Spin-lattice relaxation time data (Figures S34-S35) were acquired with a standard magnetization inversion recovery sequence, $\pi - t - \pi/2 - \tau - \pi - \tau - echo$,⁹ with $t\pi = 32$ ns and $\tau = 300$ ns for X-band and with $t\pi = 40$ ns and $\tau = 400$ ns for Q-band, and variable *t*. The spin-lattice relaxation time constant, T_1 , was determined by fitting the experimental data to the following biexponential decay function:

$$Y(t) = Y(0) + Y_1 e^{(-t/T_1)} + Y_{SD} e^{(-t/T_{SD})}$$
 (Equation 3)

where Y_1 and Y_{SD} are the amplitudes, and T_{SD} is the spectral diffusion time constant,¹² giving the results presented in Tables S3-S7. The presence of two decays is commonly attributed to the occurrence of both spectral diffusion (SD) and spin-lattice relaxation (T_1) of which the latter is usually assigned as being the slower process.¹³ We notice that the magnetization recovery curves do not reach full saturation below 15 K, indicating that the T_1 spin-lattice relaxation time is very long. Fitting such curves to an exponential model is likely to introduce some inaccuracy in the determination of the T_1 values at these temperatures.



Figure S34. Inversion recovery data for (a) 1-Nd, (b) 1-Ce and (c) 1-Sm measured at 5 K.



Figure S35. Inversion recovery data at Q-band of (left) **1-Nd** and (right) **1-Ce** measured at 3 and 5 K with π/τ (ns) of 40/400.

Field (G)	T ₁ (ns)	T _{SD} (ns)	T _m (ns)	X (eqn1)
2534	4084±126	1715±65	254±75°	1.031±0.167
3632	3660±62	1501±47	313±9 ^b 246±42 ^c	1.139±0.024 1.002±0.090
4819	4052±84	1706±28	362±6 ^b 316±29 ^c	1.201±0.015 1.113±0.065
5793	3501±54	1579±30	454 ± 2^{a} 410 ± 4^{b} 379 ± 21^{c}	1.315±0.007 1.232±0.011 1.219±0.050
6040	4964±46	2181±31	535±1ª	1.367±0.005
6655	4060±79	1756±28	463 ± 2^{a} 419 ± 5^{b} 373 ± 24^{c}	1.295±0.005 1.225±0.013 1.138±0.051
8500	5771±107	2270±33	520±2ª	1.281±0.005
11500	9864±245	2648±24	670±3ª	1.303±0.006
11719			619±3ª 567±9 ^b 537±31°	1.283±0.008 1.248±0.021 1.207±0.059
12360	12097±332	3215±40	678 ± 5^{a} 643 ± 13^{b} 581 ± 40^{c}	1.239±0.010 1.223±0.025 1.166±0.068

Table S3. Extracted spin lattice (T_1) and phase memory (T_m) times and the stretching parameter X for **1-Nd** at 5 K (10 mM tol-hex). T_m was recorded with π/τ (ns) of 32/200,^a 64/300^b and 128/400.^c

Table S4. Extracted spin lattice (T_1) and phase memory (T_m) times and the stretching parameter X for **1-Ce** at 5 K (10 mM tol-hex). T_m was recorded with π/τ (ns) of 128/500.

Field (G)	T ₁ (ns)	T _{SD} (ns)	T _m (ns)	X (eqn1)
2498	85458±287	28041±146	494±14	0.796±0.011
3482	78130±160	24613±74	538±6	0.863 ± 0.005
4380	77178±159	23574±80	664±6	0.988±0.006
5463	81614±236	25262±110	-	
11228	89414±838	27081±469	1077±35	1.195±0.040

Table S5. Extracted spin lattice (T_1) and phase memory (T_m) times and the stretching parameter X for **1-Sm** at 5 K (10 mM tol-hex). T_m measured with π/τ (ns) of 32/200.

Field (G)	T ₁ (ns)	T _{SD} (ns)	T _m (ns)	X (eqn1)
6936	149245±9106	38586±2934	1882±18	1.457±0.026
7211	155023±4426	38261±1436	1732±9	1.394±0.012
7675	117638±518	29498±224	1597±4	1.304±0.005
12424	125845±4849	30153±1518	1745±16	1.066±0.011

Table S6. Extracted spin lattice (T_1) and phase memory (T_m) times and the stretching parameter X for **1-Nd** at 3 K (10 mM tol-hex) measured at Q-band.

Field (G)	T ₁ (ns)	T _{SD} (ns)	T _m (ns)	X (eqn1)
0			1155±2	1 016±0 002
U	-	-	1155±2	1.010±0.002
70	-	-	235±4	0.8 ± 0.006
2401	241755 1624	76010 405		
3491	541755±1054	70010±403	-	-
7350	135475±689	28923±163	618±1	1.193±0.001
8364	135575±1113	26677±264	1153±3	1.457 ± 0.005
9521	87113±831	19079±351	481±1	1.125 ± 0.002
13280	65100±733	15655±216	482±1	1.210 ± 0.002
14000	-	-	657±1	1.114±0.002

Table S7. Extracted spin lattice (T_1) and phase memory (T_m) times and the stretching parameter X for **1-Ce** at 3 and 5 K (10 mM tol-hex) measured at Q-band.

Field (G)	T ₁ (ns)		T_{1} (ns) T_{SD} (ns) T_{m} (ns		(ns)	X (eqn1)		
	3 K	5 K	3 K	5 K	3 K	5K	3 K	5K
7913	406922 ±3494	49273	116122	15191	582±3	527±2	0.860	1.021
		±373	±2114	±208			±0.003	±0.003
12803	165852 ±2720	28959	42824	8322	761±2	579±1	1.153	1.205
		±232	±1175	±124			±0.003	±0.002

7.2.4 HYSCORE (Hyperfine sub-level correlation) Measurements

The HYSCORE spectra were recorded at X-band with a four–pulse sequence, $\pi/2 - \tau - \pi/2 - t_1 - \pi - t_2 - \pi/2 - echo$,⁹ with pulses $\pi/2$ and π of 16 and 32 ns, respectively, and fixed τ (136, 200 or 400 ns). Times t_1 and t_2 were varied from 100 to 5200 ns in increments of 20 ns. 256 data points were collected in both dimensions. A four-step phase-cycle procedure was used to eliminate unwanted echo contributions. Fourier transformation of the data in both directions yielded 2D (v_1 , v_2) spectra in which the nuclear cross-peaks (i.e. peaks that correlate nuclear frequencies from opposite spin-manifolds) of the ¹H and ¹³C nuclei appeared in the (+,+) quadrant of the (v_1 , v_2) map, at separations equivalent with the corresponding hyperfine coupling frequencies (weak coupling regime: $2|v_n| > |A|$).⁹ The contour line-shape of the cross peaks, and their displacement from the anti-diagonal about the nuclear Larmor frequency (v_n), relate to the magnitude and anisotropy of the hyperfine couplings, and thus analysis of the HYSCORE spectra allows to determine such parameters.

Spectra modelling using EasySpin assumed that the hyperfine coupling matrix (*A*) for a given 13 C nucleus *n* is determined by the point dipole (through space) interaction with spin density at the metal ion, given by Equation (4):

$$A^{\rm dip} = \frac{\mu_0 \beta_e \beta_n}{4\pi h} \frac{3(\bar{g} \cdot \mathbf{n}) (\tilde{\mathbf{n}} \cdot g_n \bar{l}) - \bar{g} \cdot g_n \bar{l}}{r^3}$$

where g_n is the scalar isotropic nuclear *g*-value, \overline{I} is the identity matrix, *r* is the distance of the nucleus from the Ln³⁺ ion (in m), n is the Ln-n unit vector expressed in the molecular frame (and ñ is its transpose), β_e and β_n are the electron and nuclear magnetons, *h* is Plank's constant, and μ_0 is the vacuum permittivity. It is also assumed that g_z lies along the pseudo- C_3 axis (Figure 6), and that the electron spin density is located at the lanthanide ion. A^{dip} is then calculated for each unique carbon position in the Cp^{tt} ligands, using the crystallographic coordinates of the atoms. Simulations considering only A^{dip} reproduce the experimental data satisfactorily for **1-Nd** and **1-Ce** (Figure 6).

Modelling of the ¹H HYSCORE data involved a similar approach, including the point dipolar ¹H hyperfine (A^{dip}) for the protons of the cyclopentadienyl rings (H^2 , H^4 , H^5), and all protons of the methyl groups supposed to be close to the Ln(III) ion. Again, good agreement is found with the experimental data for **1-Nd** and **1-Ce** (Figure 6).

1-Nd	A _{xx}	A _{xy}	A _{xz}	A _{yx}	A _{yy}	A _{yz}	A _{zx}	A _{zy}	A _{zz}
C1	2.05	0.52	-1.49	0.19	-0.47	-0.08	-0.25	-0.04	-0.12
C2	2.02	1.45	0.025	-0.53	-0.25	0.004	0.004	0.002	-0.22
C3	2.03	0.47	1.52	-0.17	-0.48	0.08	0.255	0.03	-0.12
C4	2.34	-1.58	1.10	-0.58	-0.37	-0.16	0.19	-0.07	-0.22
C5	2.30	-1.52	-1.16	-0.555	-0.38	-0.165	-0.2	0.08	-0.21
H2	2.87	-4.59	0.08	-1.68	0.11	0.02	0.01	0.01	-0.53
H4	2.75	-1.04	0.73	-1.85	-0.03	-0.195	0.12	-0.09	-0.08
H5	2.71	-2.30	-1.76	-1.78	-0.11	0.46	-0.295	0.21	-0.17

7.2.5 HYSCORE Simulation (simple dipolar model)

Table S8. Calculated dipolar interactions of 1-Nd used for HYSCORE simulations.

1-Ce	A _{xx}	A _{xy}	A _{xz}	A _{yx}	A _{yy}	A _{yz}	A _{zx}	A _{zy}	A _{zz}
C1	-0.05	0.86	1.57	0.51	-0.40	0.66	0.32	0.22	0.15
C2	1.10	0.04	1.81	0.02	-0.75	0.02	0.37	0.006	0.03
C3	-0.02	-0.825	1.49	-0.49	-0.38	-0.62	0.30	-0.21	0.13
C4	-1.39	-0.17	0.64	-0.10	-0.71	-0.655	-0.13	-0.22	0.52
C5	-1.38	0.13	0.50	0.08	-0.69	0.63	0.10	0.21	0.51
H2	4.67	0.16	3.37	0.09	-1.83	0.04	0.68	0.01	-0.32
H4	-3.77	0.40	-0.90	0.24	-1.19	-2.53	-0.18	-0.85	1.17
H5	-3.47	-0.45	-1.09	-0.27	-1.21	2.26	-0.22	0.76	1.11

 Table S9. Calculated dipolar interactions of 1-Ce used for HYSCORE simulations.

8. Computational Studies

8.1 Methods

Density functional theory (DFT) optimizations were performed with the PBE¹⁴ functional and Grimme's D3 dispersion correction¹⁵ with Gaussian 16 Rev. C.01.¹⁶ The Stuttgart effective f-in-core pseudopotentials¹⁷ were used for the lanthanide ions and the cc-pVDZ¹⁸ basis set was used to treat the remaining C and H atoms.

Complete active space self-consistent field with spin-orbit coupling (CASSCF-SO)^{19,20} calculations with an active space containing all 4f electrons and seven 4f orbitals were performed to compute the magnetic properties of **1-Ce**, **1-Sm**, and **1-Nd**; for **1-Ce** there are two molecules in the unit cell with different metrics so both were calculated. The relativistic atomic natural orbital (ANO-RCC)²¹⁻²⁵ basis sets were used in the CASSCF-SO calculations and the valence orbital treatment was varied based on the distance from the paramagnetic centre: Ln - VTZP; C(Cp), H(Cp), C(tbu1) - VDZP; all other C and H - VDZ. The CASSCF-SO calculations were performed using OpenMolcas version 22.06.²⁶

The ¹H and ¹³C HYSCORE simulations of **1-Ce** and **1-Nd** were obtained by calculating relativistic hyperfine coupling constants using DFT-optimized geometries and the above CASSCF-SO methods, feeding into the Hyperion²⁷ package. The hyperion2easyspin utility was then used to generate EasySpin²⁸ input files, and the EPR parameters were used to simulate HYSCORE spectra with saffron.⁷ Here, using five C(Cp) atoms from one ligand and using three H(Cp) atoms (one H2-, H4- and H5-type atom from one Cp ligand), accurately reproduced the experimental ¹³C and ¹H spectra, respectively.

8.2	Calculated	properties	of 1-Nd	, 1-Ce and	d 1-Sm
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g _x	$\mathbf{g}_{\mathbf{y}}$	gz
2.20	2.38	1.08
0.23	0.02	0.96
3.74	3.50	0.55
0.05	0.02	5.48
2.49	2.57	2.71
	g x 2.20 0.23 3.74 0.05 2.49	gx gy 2.20 2.38 0.23 0.02 3.74 3.50 0.05 0.02 2.49 2.57

Table S10. Energies (in cm⁻¹) and g-values for 1-Nd.

	$ m_j angle$ wavefunction contributions (%)									
Energy (cm ⁻¹)	-9/2	-7/2	-5/2	-3/2	-1/2	1/2	3/2	5/2	7/2	9/2
0	0.1	27.3	1.8	0.0	0.0	0.0	0.5	69.8	0.4	0.0
26.44	4.2	0	0.4	53.3	0.5	0.2	34.7	0.1	0.1	6.5
126.77	0.0	0.	0.0	0.7	93.6	5.6	0.1	0.0	0.0	0.0
516.77	12.7	0.0	0.0	9.1	0.1	0.0	1.5	0.0	0.1	76.4
612.72	0.1	56.3	6.9	0.0	0.0	0.0	0.1	20.8	15.8	0.0

Table S11. Crystal field states of 1-Nd.

Table S12. Energies, g-values and crystal field states of 1-Ce, molecule 1.

				$ m_j angle$ wavefunction contributions (%)					
Energy (cm ⁻¹)	g _x	\mathbf{g}_{y}	gz	-5/2	-3/2	-1/2	1/2	3/2	5/2
0	2.09	3.03	0.71	0.0	0.7	39.6	59.3	0.4	0.0
134.61	0.47	0.44	2.65	0.0	8.1	0.9	0.1	90.7	0.2
859.51	0.16	0.19	3.94	88.4	0.2	0.0	0.0	0.0	11.4

Table S12. cont. Energies, g-values and crystal field states of 1-Ce, molecule 2.

					$ m_j angle$ wavefunction contributions (%)					
Energy (cm ⁻¹)	g _x	$\mathbf{g}_{\mathbf{y}}$	$\mathbf{g}_{\mathbf{z}}$	-5/2	-3/2	-1/2	1/2	3/2	5/2	
0	2.92	2.21	0.73	0.0	0.1	85.5	13.6	0.7	0.0	
105.15	0.36	0.31	2.67	0.3	60.3	0.0	0.8	38.3	0.3	
800.55	0.21	0.15	3.95	93.1	0.6	0.0	0.0	0.0	6.3	

					$ m_j\rangle$ wavefunction contributions (%)					
Energy (cm ⁻¹)	g _x	gy	gz	-5/2	-3/2	-1/2	1/2	3/2	5/2	
0	0.42	0.42	0.61	0.0	49.4	0.0	0.0	50.6	0.0	
400.89	0.003	0.02	0.33	0.0	0.0	58.3	41.7	0.0	0.0	
699.23	1.18	1.15	0.85	71.8	0.0	0.0	0.0	0.0	28.2	

Table S13. Energies, g-values and crystal field states of 1-Sm.

8.3 Simulated HYSCORE spectra



Figure S36. X-Band HYSCORE spectra at a static field of (a), (b) $B_0 = 353.0 \text{ mT}$ and (c), (d) $B_0 = 348.2 \text{ mT}$ at 5 K. (a) **1-Nd** ¹³C region (blue) and CASSCF(3,7)-SO calculated spectrum (red) including C1-C5; (b) **1-Nd** ¹H region (blue) with CASSCF(3,7)-SO simulated spectrum (red) with H2, H4, and H5 protons from one ligand; (c) **1-Ce** ¹³C region (blue) and CASSCF-(1,7)-SO simulated spectrum (red) including C1-C5; (d) **1-Ce** ¹H region (blue) and CASSCF(1,7)-SO simulated spectrum (red) with H2, H4, and H5 protons from one ligand.

Table S14. CASSCF-SO hyperfine couplings of 1-Ce used for HYSCORE simulations, obtained using optimized structure.

1-Ce	A _{xx}	A _{xy}	A _{xz}	A _{yx}	A _{yy}	A _{yz}	A _{zx}	A _{zy}	A _{zz}
C1	-0.007	-0.897	0.136	-0.897	-1.847	0.500	0.136	0.500	1.172
C2	-0.007	0.897	-0.136	0.897	-1.847	0.500	-0.136	0.500	1.172
C3	-0.008	0.333	-0.847	0.333	0.844	1.059	-0.847	1.059	-1.531
C4	-0.008	-0.333	0.847	-0.333	0.844	1.059	0.847	1.059	-1.531
C5	-0.007	0.570	0.705	0.570	-0.034	-1.558	0.705	-1.558	-0.648
H2	0.592	0.000	0.000	0.000	1.364	2.054	0.000	2.054	-3.435
H4	-0.843	-2.734	0.164	-2.734	-2.954	-0.889	0.164	-0.889	2.349
H5	-0.843	2.734	-0.164	2.734	-2.954	-0.889	-0.164	-0.889	2.349

Table S15. CASSCF-SO hyperfine couplings of **1-Nd** used for HYSCORE simulations, obtained using optimized structure.

1-Nd	A _{xx}	A _{xy}	A _{xz}	A _{yx}	A _{yy}	A _{yz}	A _{zx}	A _{zy}	A _{zz}
C1	0.283	-0.833	0.194	-0.833	-1.578	0.640	0.194	0.640	0.999
C2	0.285	0.831	-0.194	0.831	-1.580	0.641	-0.194	0.641	0.999
C3	0.269	-0.251	0.851	-0.251	0.876	0.785	0.851	0.785	-1.558
C4	0.271	0.250	0.840	0.250	0.876	0.786	0.840	0.786	1 562
04	0.271	0.230	-0.049	0.230	0.870	0.780	-0.049	0.780	-1.302
C5	0.278	0.633	0.595	0.633	-0.385	-1.442	0.595	-1.442	-0.241
H2	0.904	0.001	0.001	0.001	-1.093	-2.795	0.001	-2.795	-0.729
H4	-0.448	-2.211	1.266	-2.211	-1.422	2.268	1.266	2.268	1.101
H5	-0.442	2.209	-1.265	2.209	-1.427	2.272	-1.265	2.272	1.098

Table S16. Average CASSCF(n,7)-SO Mulliken spin populations of **1-Ce**, **1-Sm**, **and 1-Nd**, obtained using optimized structures.

1-M	М	Cp(C1)	Cp(C2)	Cp(C3)	Cp(C4)	Cp(C5)	% spin density on Cp ligands
Ce	0.9988	0.0000	0.0000	0.0001	0.0001	0.0001	0.09
Nd	2.9972	0.0002	0.0002	0.0002	0.0002	0.0002	0.10
Sm	4.9923	0.0005	0.0005	0.0005	0.0005	0.0005	0.15

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