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## Supplementary Material for "Area difference between monolayers facilitates budding of lipid droplets from vesicles" Meng Wang and Xin Yi Department of Mechanics and Engineering Science, College of Engineering, Peking University, Beijing 100871, China

Note 1. Budding of embedded lipid droplets (LDs) from vesicles with  $A_{out}^0 / A_{in}^0 \ge 1$ 



**Fig. S1** Selected LD-vesicle configurations for different values of  $\overline{\gamma}$  and  $\overline{p}$  with vesicle radius R = 5a and normalized osmotic pressure  $\overline{p} = 10$ .



**Fig. S2** Normalized total free energy variation  $\Delta E_{\text{tot}} = E_{\text{tot}} - 4\pi\gamma a^2$  and its components ( $E_{\text{bend}}, E_{\text{ten}}$ , and  $E_{\text{p-V}}$ ), and interfacial energy variation  $\Delta E_{\text{intf}} = E_{\text{intf}} - 4\pi\gamma a^2$  versus monolayer area ratio  $A_{\text{out}}^0 / A_{\text{in}}^0$  at R = 5a and  $\overline{p} = 10$  for  $\overline{\gamma} = 100$  (a), 1000 (b), and 5000 (c).



**Fig. S3** The LD-vesicle contact area  $A_c = A_1 + A_2$  (a) and outer  $(A_1)$  and inner  $(A_2)$  contact areas (b) versus monolayer area ratio  $A_{out}^0 / A_{in}^0$  for different values of  $\overline{\gamma}$  at R = 5a and  $\overline{p} = 10$ .



**Fig. S4** Selected LD-vesicle configurations for different values of  $\overline{\gamma}$  and  $\overline{p}$  with vesicle radius R = 5a and normalized osmotic pressure  $\overline{p} = 30$ .



**Fig. S5** Normalized total free energy  $E_{\text{tot}}$  and its components ( $E_{\text{bend}}$ ,  $E_{\text{ten}}$ , and  $E_{p-V}$ ), and interfacial energy variation  $\Delta E_{\text{intf}} = E_{\text{intf}} - 4\pi\gamma a^2$  versus monolayer area ratio  $A_{\text{out}}^0 / A_{\text{in}}^0$  at R = 5a and  $\overline{p} = 30$  for  $\overline{\gamma} = 300$  (a), 1000 (b), and 5000 (c).



**Fig. S6** The LD-vesicle contact area  $A_c = A_1 + A_2$  (a) and outer  $(A_1)$  and inner  $(A_2)$  contact areas (b) versus monolayer area ratio  $A_{out}^0 / A_{in}^0$  for different values of  $\overline{\gamma}$  at R = 5a and  $\overline{p} = 30$ .



Note 2. Budding of embedded LDs from vesicles with  $A_{\rm out}^0 / A_{\rm in}^0 \le 1$ 

**Fig. S7** The LD-vesicle contact area  $A_c=A_1+A_2$  (a) and outer  $(A_1)$  and inner  $(A_2)$  contact areas (b) versus monolayer area ratio  $A_{out}^0 / A_{in}^0$  for different values of  $\overline{\gamma}$  at R=5a and  $\overline{p}=0$ .



**Fig. S8** Total free energy variations  $\Delta E_{\text{tot}} = E_{\text{tot}} - 4\pi\gamma a^2$  versus distance *d* between two poles of the LD-vesicle complex for outward and inward budding at  $\overline{\gamma} = 5000$ ,  $A_{\text{out}}^0 / A_{\text{in}}^0 = 0.995$ , R = 5a, and  $\overline{p} = 0$ . Local minimum values of  $E_{\text{tot}}$  in the outward and inward budding states can be well determined by Eqs. (5) and (7), respectively.