

Supplementary Information for

Electrophoretic propulsion of matchstick-shaped magnetodielectric particles in the presence of external magnetic fields in a nematic liquid crystal

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Table S1

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1. Brownian motion of dipoles and quadrupoles in ZLI-2293 NLC

Isolated elastic dipoles and quadrupoles in a planar cell are video recorded and the particle trajectories are obtained using a suitable particle tracking software. The mean square displacement (MSD) is calculated from the x - and y -position coordinates which vary linearly with time delay τ (Fig. S1). The translational diffusion equation is given by, $\langle(\Delta r_i)^2\rangle = 2D_i\tau$ where D_i is the diffusion coefficient, $i = \parallel$ or \perp to the director, r_i can be x or y . The difference in values of $\langle(\Delta x)^2\rangle$ and $\langle(\Delta y)^2\rangle$ is due to the anisotropy in motion of the particle (Fig. S1). Then the diffusion coefficients, D_{\parallel} and D_{\perp} are obtained from the slopes of linear fits of $\langle(\Delta x)^2\rangle$ and $\langle(\Delta y)^2\rangle$ as a function of τ and the corresponding drag coefficients, ζ_{\parallel} and ζ_{\perp} (Table S1) are obtained using the relation $\zeta_i = \frac{k_B T}{D_i}$ where T is the room temperature at which experiment is carried out.

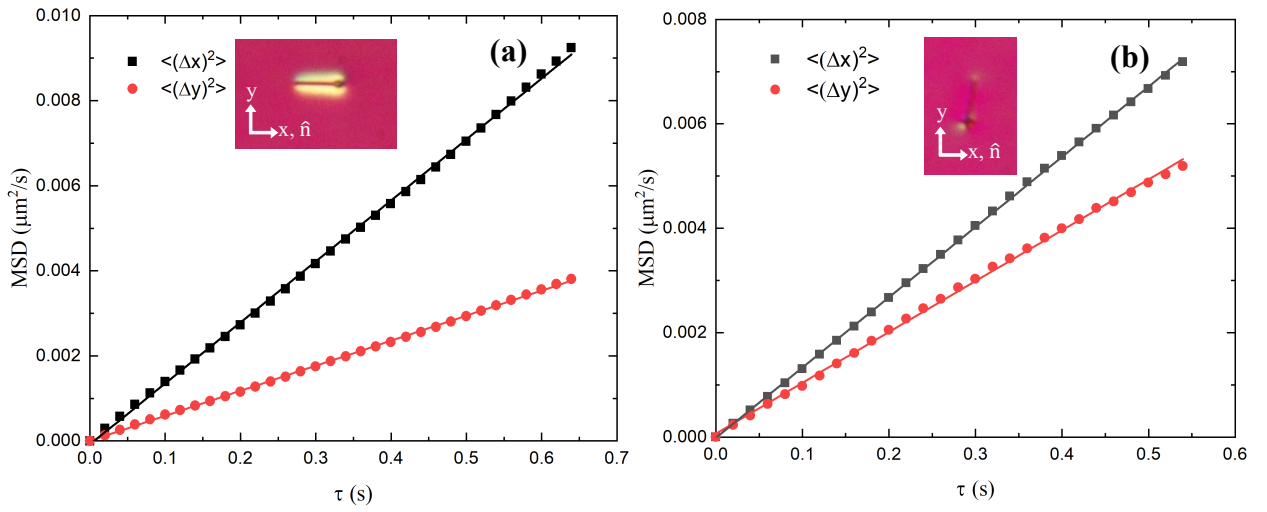


Figure S1: The position coordinates x and y of an elastic dipole and quadrupole. Mean square displacements along x - and y -axes in a planar cell as a function of τ for a (a) dipole and (b) quadrupole. POM images of both dipole and quadrupole are shown with director \hat{n} along the x -axis. Diffusion coefficients and drag coefficients are given in Table S1.

	$D_{\parallel}(10^{-2}\mu\text{m}^2/\text{s})$	$D_{\perp}(10^{-2}\mu\text{m}^2/\text{s})$	$\zeta_{\parallel}(10^{-6}\text{kg/s})$	$\zeta_{\perp}(10^{-6}\text{kg/s})$
Dipole	0.67 ± 0.1	0.49 ± 0.1	0.61 ± 0.1	0.84 ± 0.1
Quadrupole	0.71 ± 0.1	0.29 ± 0.1	0.58 ± 0.1	1.39 ± 0.1

Table S1: Diffusion coefficients (D_{\parallel} and D_{\perp}) and drag coefficients (ζ_{\parallel} and ζ_{\perp}) for dipoles and quadrupoles along parallel and perpendicular to the director.

2. Interaction energy of dipole and quadrupole pairs in ZLI-2293 NLC.

The particles experience long-range elastic interactions. Here elastic force (F_{el}) is balanced by the viscous drag force, $F_{drag} = -\zeta \frac{dR(t)}{dt}$ in a nematic medium where ζ is the drag coefficient, $R(t)$ is the interparticle separation and the equation of motion is given by, $F_{el} + F_{drag} = 0$. Elastic forces are given by $F_{el}^{dipole} = -\frac{k}{R^4}$ and $F_{el}^{quadrupole} = -\frac{k}{R^6}$ for dipoles and quadrupoles respectively. From these relations, we will get the interparticle separation, $R(t) = (R_0^5 - 5\alpha t)^{\frac{1}{5}}$ and $R(t) = (R_0^7 - 7\alpha t)^{\frac{1}{7}}$ for dipoles and quadrupoles, respectively, where $\alpha = \frac{k}{\zeta}$. The elastic interaction potential energy is given by, $W = \int F_{drag} \cdot dR$. The interactions of two colinear particles are attractive with minimum $W \approx -3400 k_B T$ and $\approx -120 k_B T$ for dipoles and quadrupoles, respectively (See Fig. S2).

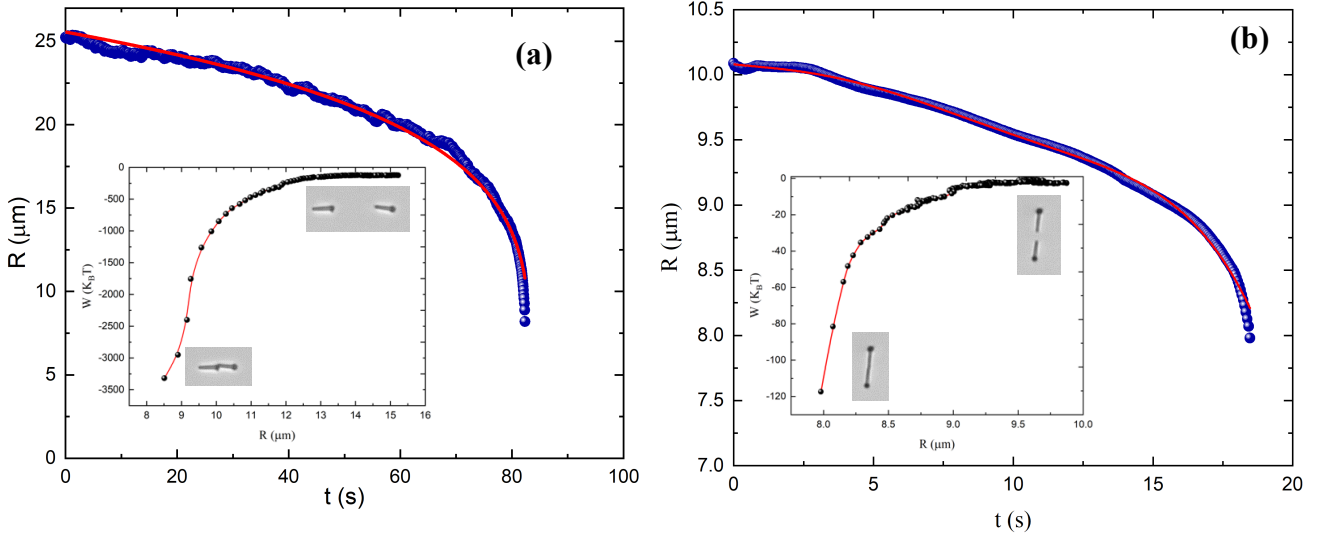


Figure S2: Variation of interparticle separation (R) with time (t) for (a) dipoles and (b) quadrupoles. The red curves show the nonlinear least square fit with the equations $R(t) = (R_0^5 - 5\alpha t)^{\frac{1}{5}}$ and $R(t) = (R_0^7 - 7\alpha t)^{\frac{1}{7}}$ for dipoles and quadrupoles, respectively. R_0 is the separation at time $t = 0$ and α is obtained as $(2.61 \pm 0.01) \times 10^4 \mu\text{m}^5/\text{s}$ and $(3.47 \pm 0.13) \times 10^4 \mu\text{m}^7/\text{s}$ for dipoles and quadrupoles, respectively. The inset shows the interaction potential energy (W) in units of $k_B T$ as a function of separation (R).

3. Dipolar assembly of match-stick shaped particles in NLC

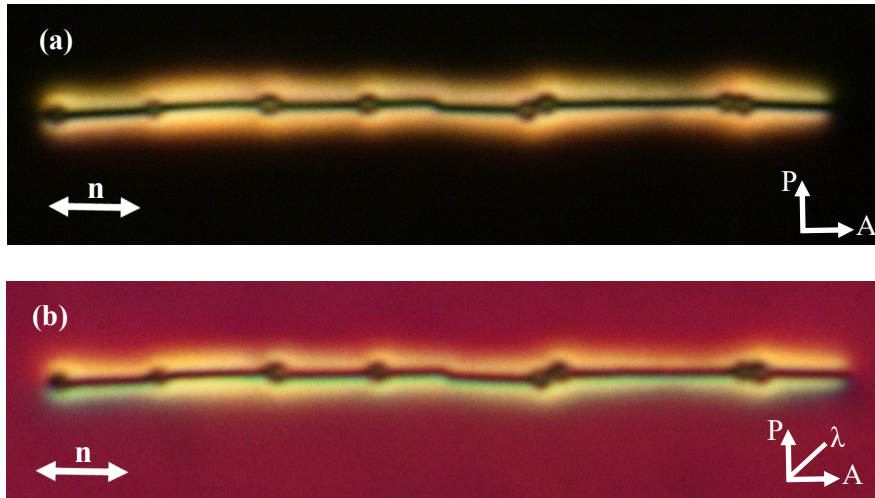


Figure S3: (a) POM and (b) full wave plate images of dipolar chains of matchstick-shaped particles. Double headed arrow shows the alignment direction of the director \mathbf{n} .

4. Motion of matchstick particles under in-plane transverse DC electric and magnetic fields in ZLI – 2293 NLC.

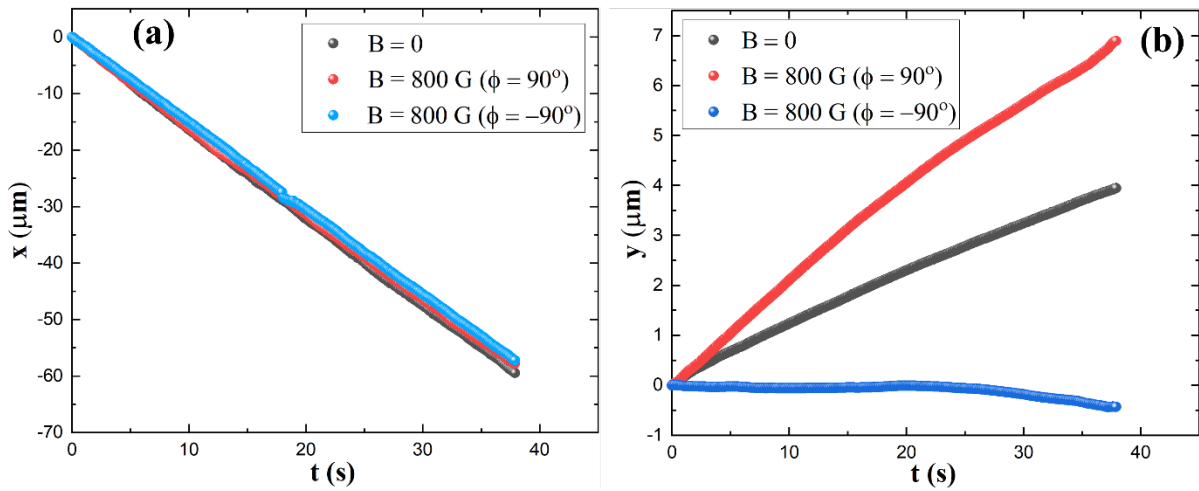


Figure S4: Variation in relative (a) x- and (b) y- coordinates with time for different values of \mathbf{B} for the particles under in-plane DC electric field ($7.5 \times 10^3 \text{V/m}$).

5. Motion of matchstick particles under in-plane transverse DC electric and magnetic fields in ZLI – 2293 NLC when the polarity of E is reversed.

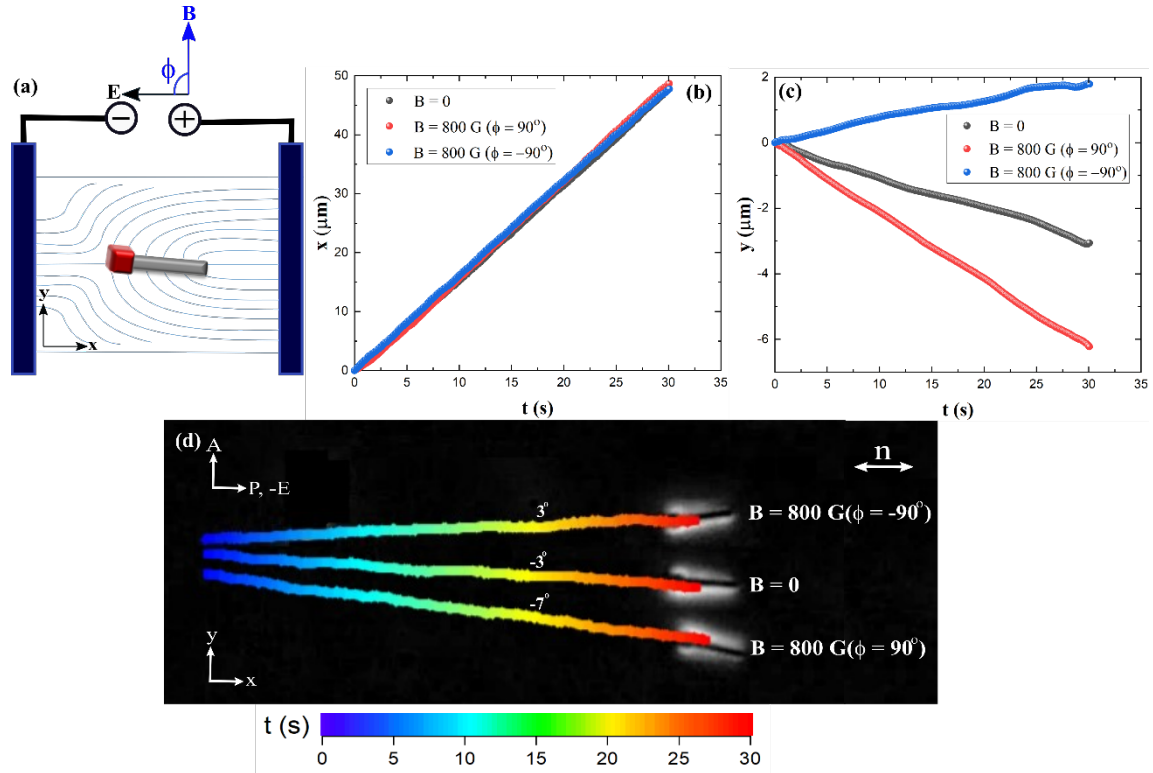


Figure S5: (a) Schematic of a planar cell with electric field E ($7.5 \text{ mV}/\mu\text{m}$) between in-plane electrodes and magnetic field B (800G) applied perpendicular to E . The director distortion and initial orientation of the matchstick is as shown. (b,c) Variation of x - and y - coordinates of the particle with time for different values of B . (d) Color coded trajectories depicting the motion of the particle when $B = 0$, and $B = 800\text{G}$ ($\phi = \pm 90^\circ$); $t_{min} = 0\text{s}$ and $t_{max} = 30\text{s}$ (see Movie S2). The angle subtended by B with the director is denoted by ϕ . The trajectory angles with respect to the director are mentioned in each case. Double-headed arrow denotes the director. The specified angles are accurate within $\pm 1.5^\circ$.

6. Variation of particle velocity with electric field and frequency in NLC (XV7039-200).

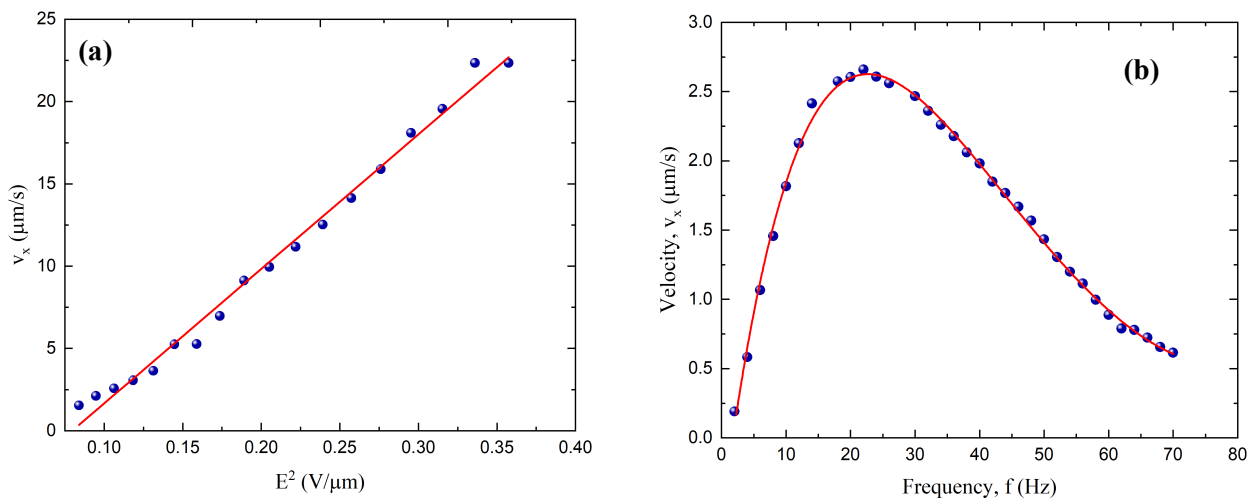


Figure S6: (a) Electric field dependent velocity (v_x) at a fixed frequency 30 Hz for E above a threshold. Red line shows the linear least square fit to $v_x = \beta E^2$ with slope $\beta = (81.7 \pm 1.9) \mu\text{m}^3\text{s}^{-1}\text{V}^{-2}$. (b) Variation of particle velocity with frequency at a fixed electric field ($0.38 \text{ V}/\mu\text{m}$). The red curve is a guide to the eye.

7. Motion of matchstick particles under out of plane transverse AC electric and magnetic fields in XV7039-200 NLC.

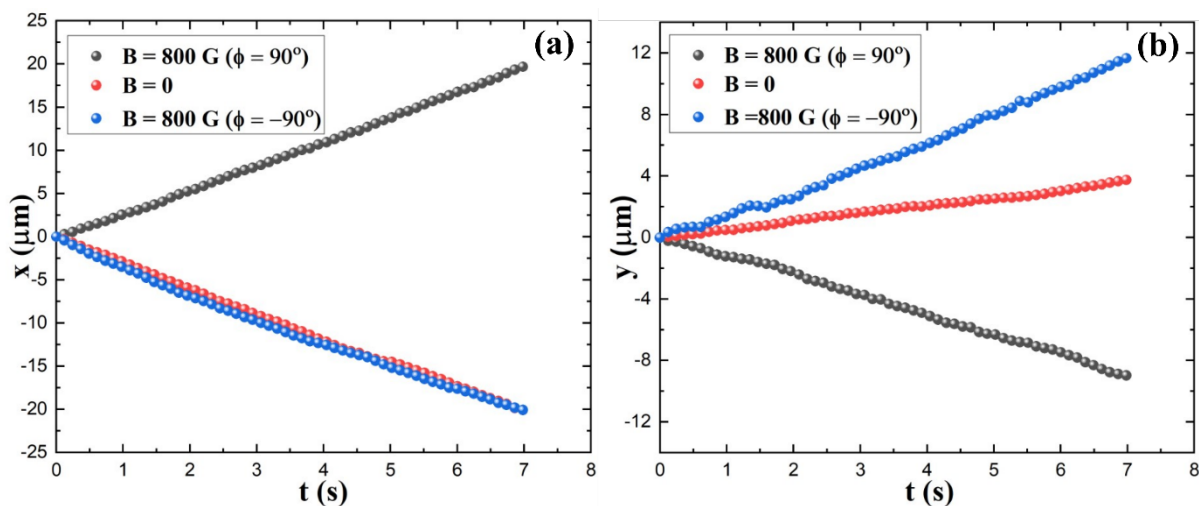


Figure S7: Variation in relative (a) x- and (b) y- coordinates with time for different values of B for the particles under out of plane AC electric field $E(0.38 \text{ V}/\mu\text{m}, 30 \text{ Hz})$.

8. Movies

Movie S1: Movie of a matchstick particle in ZLI-2293 with dipolar distortion moving under in-plane transverse DC electric and magnetic fields as shown in Fig.5a. The particle always moves towards the positive electrode. The value of the DC electric field, \mathbf{E} ($= 7.5 \text{ mV}/\mu\text{m}$), and the magnetic field, $\mathbf{B} = 800 \text{ G}$. The angle subtended by \mathbf{B} with the director is denoted by ϕ . (a) When $\phi = 90^\circ$, the trajectory makes an angle $\approx 7^\circ$ with the director; the x - component of velocity $v_x = -1.5 \text{ }\mu\text{m/s}$, and the y - component of velocity $v_y = 0.2 \text{ }\mu\text{m/s}$. (b) When $B = 0$, the trajectory makes an angle $\approx 4^\circ$ with the director; $v_x = -1.5 \text{ }\mu\text{m/s}$, and $v_y = 0.1 \text{ }\mu\text{m/s}$. (c) When $\phi = -90^\circ$, the trajectory makes an angle $\approx -1^\circ$ with the director; $v_x = -1.5 \text{ }\mu\text{m/s}$ and $v_y = -0.01 \text{ }\mu\text{m/s}$. The specified angles are accurate within $\pm 1.5^\circ$.

Movie S2: Movie of a matchstick particle in ZLI-2293 with dipolar distortion near the head of the matchstick moving under in-plane transverse DC electric and magnetic fields as shown in Fig. S4(a). The particle always moves towards the positive electrode. The value of the DC electric field, $\mathbf{E} = 7.5 \text{ mV}/\mu\text{m}$, and the magnetic field, $\mathbf{B} = 800 \text{ G}$. The angle subtended by \mathbf{B} with the director is denoted by ϕ . (a) When $\phi = -90^\circ$, the trajectory makes an angle $\approx 3^\circ$ with the director; the x - component of velocity $v_x = 1.6 \text{ }\mu\text{m/s}$, and the y - component of velocity $v_y = 0.1 \text{ }\mu\text{m/s}$. (b) When $B = 0$, the trajectory makes an angle $\approx -3^\circ$ with the director; $v_x = 1.6 \text{ }\mu\text{m/s}$, and $v_y = -0.1 \text{ }\mu\text{m/s}$. (c) When $\phi = 90^\circ$, the trajectory makes an angle $\approx -7^\circ$ with the director; $v_x = 1.6 \text{ }\mu\text{m/s}$ and $v_y = -0.2 \text{ }\mu\text{m/s}$. The specified angles are accurate within $\pm 1.5^\circ$.

Movie S3: Microscopic video recording of a matchstick particle in XV7039-200 with dipolar distortion near the head of the matchstick moving under out-of-plane AC electric field, \mathbf{E} ($0.38 \text{ V}/\mu\text{m}$, 30 Hz) and an in-plane orthogonal magnetic field, $\mathbf{B} = 800 \text{ G}$. The angle subtended by \mathbf{B} with the director is denoted by ϕ . Due to the AC electric field $E\hat{\mathbf{z}}$, the particle tilts in the z -direction and moves in the xy - plane. (a) When $\phi = 90^\circ$, the particle trajectory makes an angle $\approx -25^\circ$ with the director. The x - component of velocity $v_x = 2.8 \text{ }\mu\text{m/s}$, and y - component of velocity $v_y = -1.3 \text{ }\mu\text{m/s}$. (b) When $B = 0$, the trajectory makes an angle $\approx 10^\circ$ with the director; $v_x = -2.8 \text{ }\mu\text{m/s}$, and $v_y = 0.5 \text{ }\mu\text{m/s}$. (c) When $\phi = -90^\circ$, the trajectory makes an angle $\approx 37^\circ$ with the director; $v_x = -2.9 \text{ }\mu\text{m/s}$, and $v_y = 1.7 \text{ }\mu\text{m/s}$. The specified angles are accurate within $\pm 1.5^\circ$.