

*Supporting Information for*

**High-Throughput Computational Discovery of 3,218 Ultralow Thermal Conductivity and Dynamically Stable Materials by Dual Machine Learning Models**

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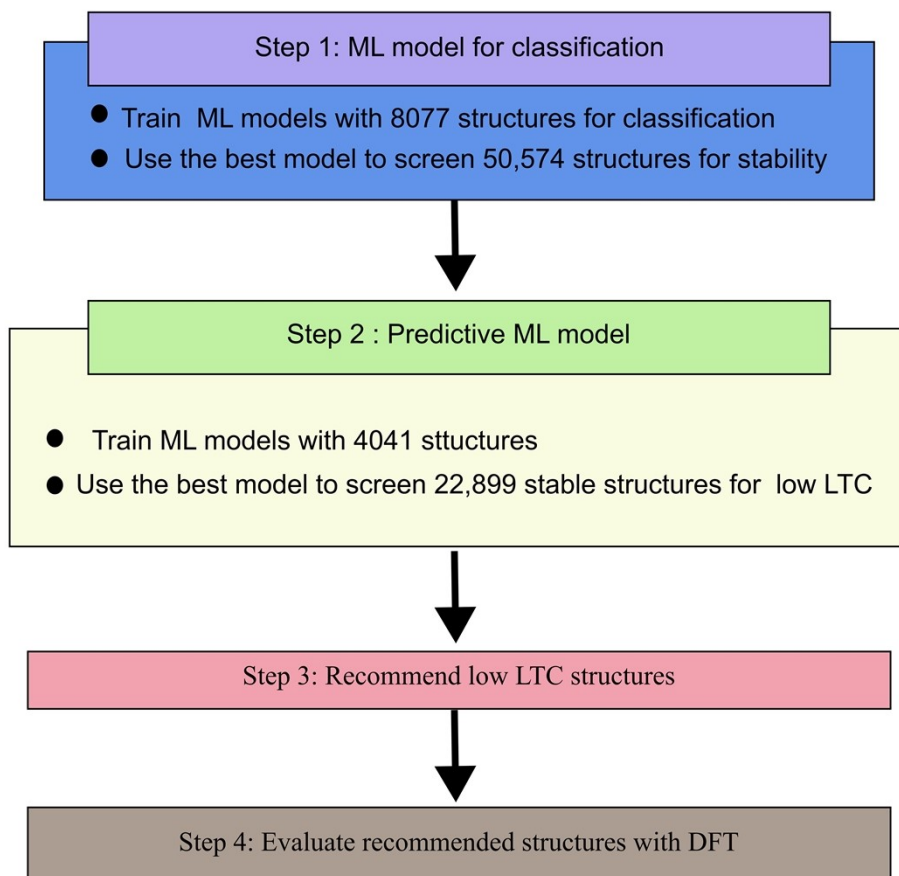
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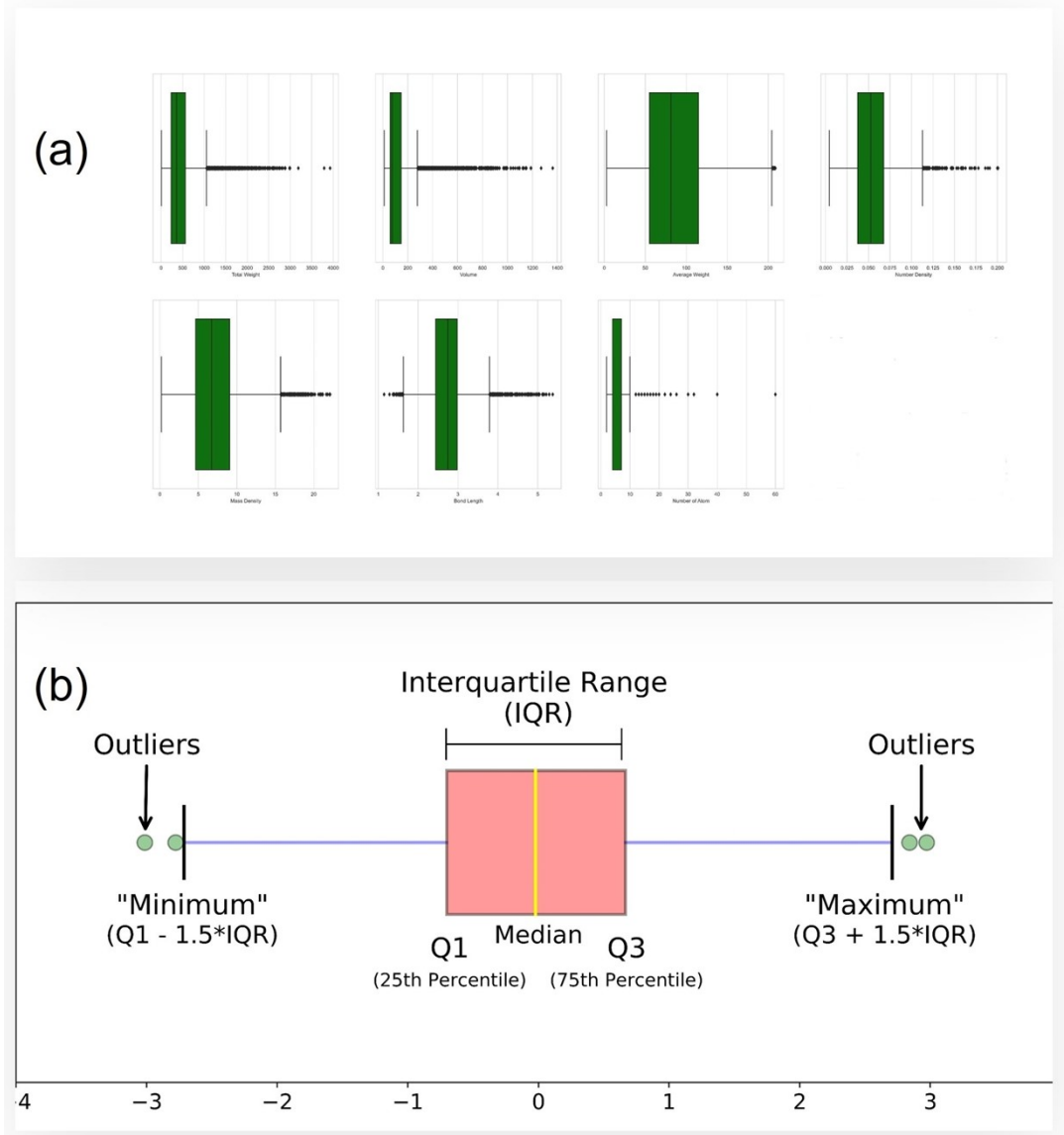
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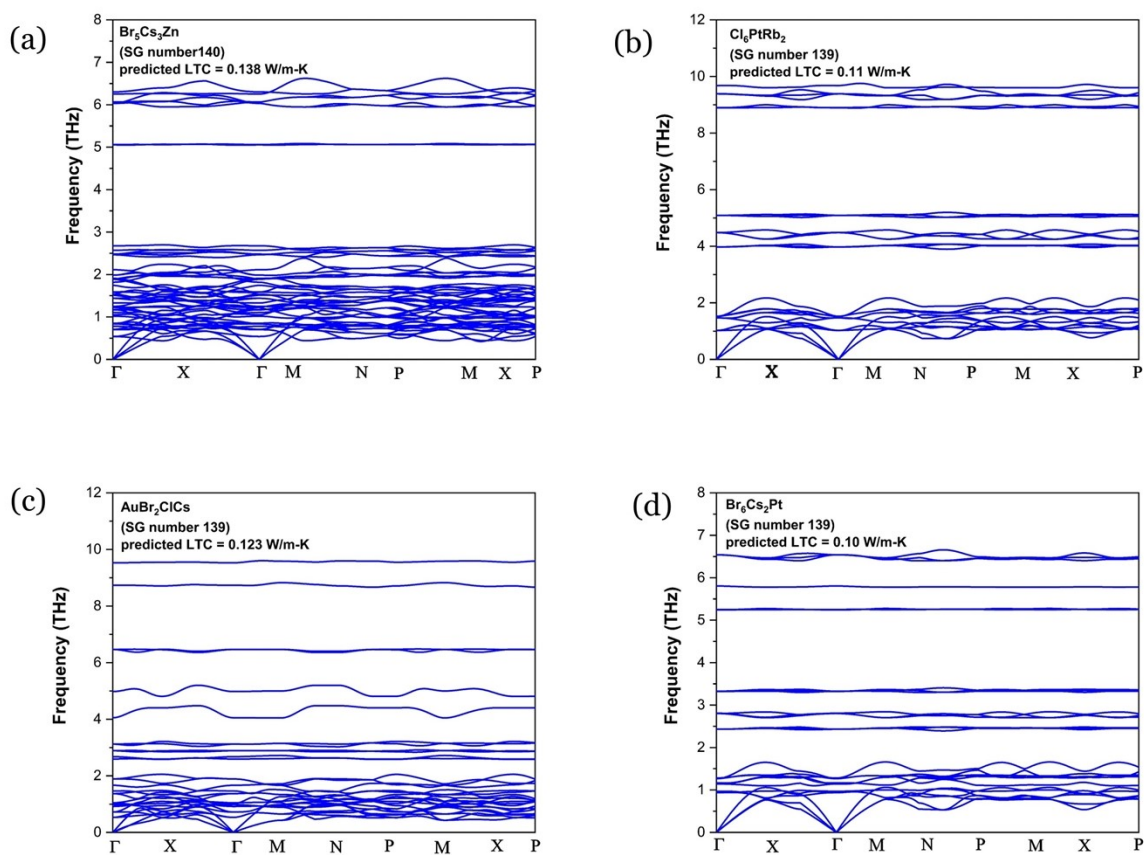
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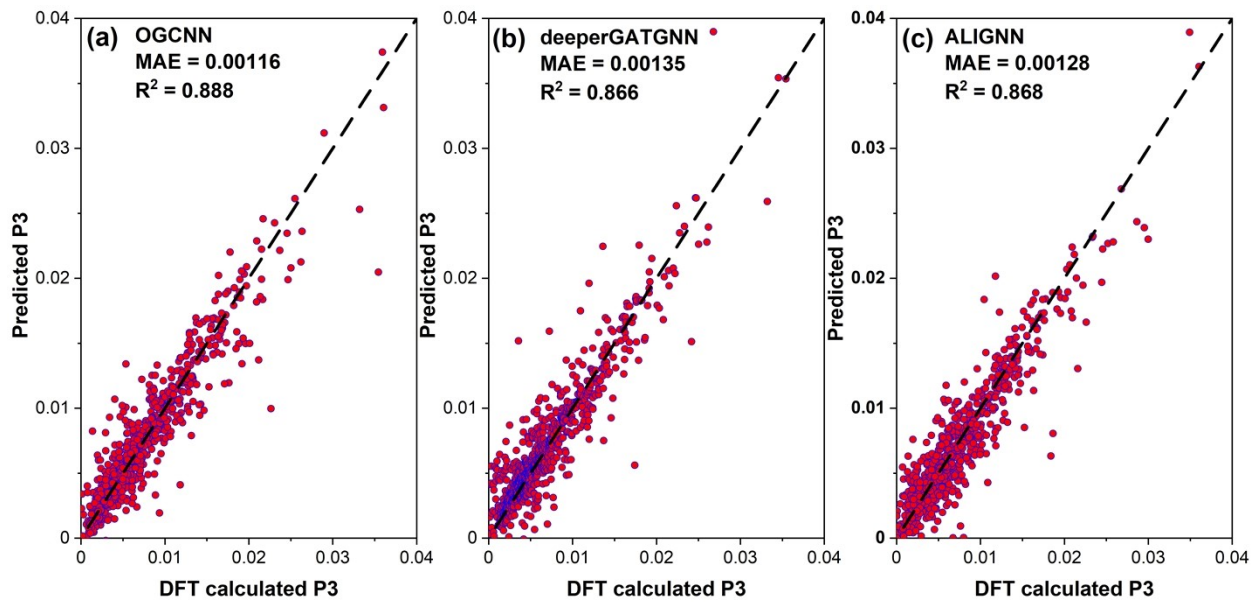
**Figure S1:** Overview of the workflow. After training classification model and predicting stable structures (Step 1), step 2 is to train and screen the stable structures for low LTC. Step 3 and step 4 are recommendation and verification of low LTC structures, respectively.



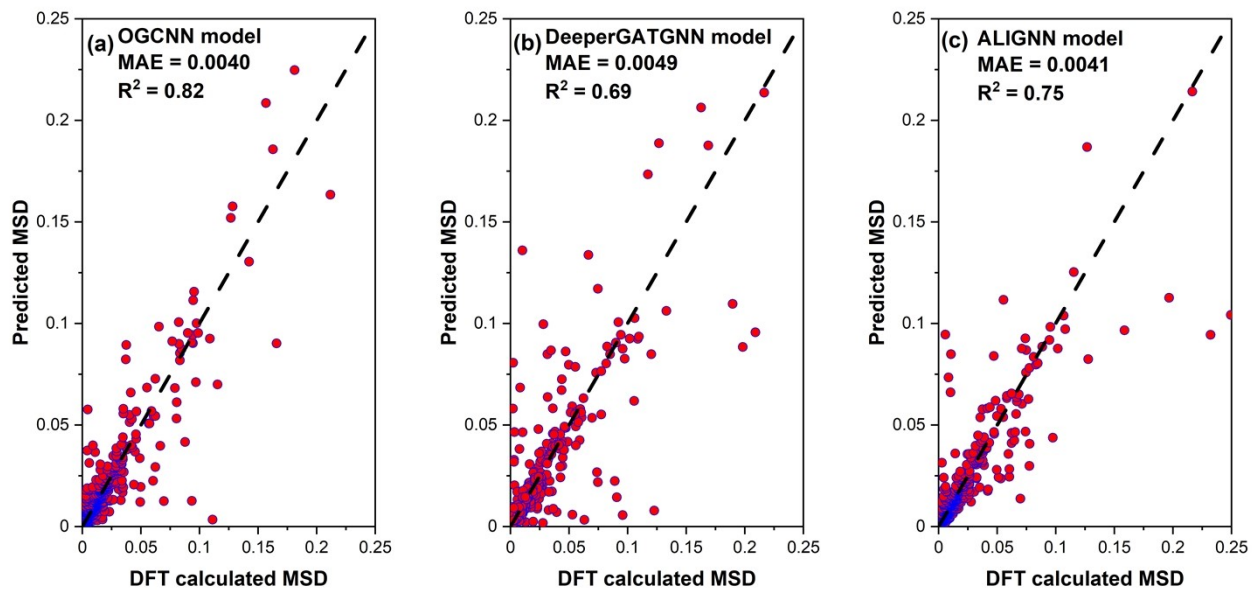
**Figure S2:** (a) Outliers within the independent variables for the machine learning classification models. Panel (b) explains the boxplot, showing the outliers.



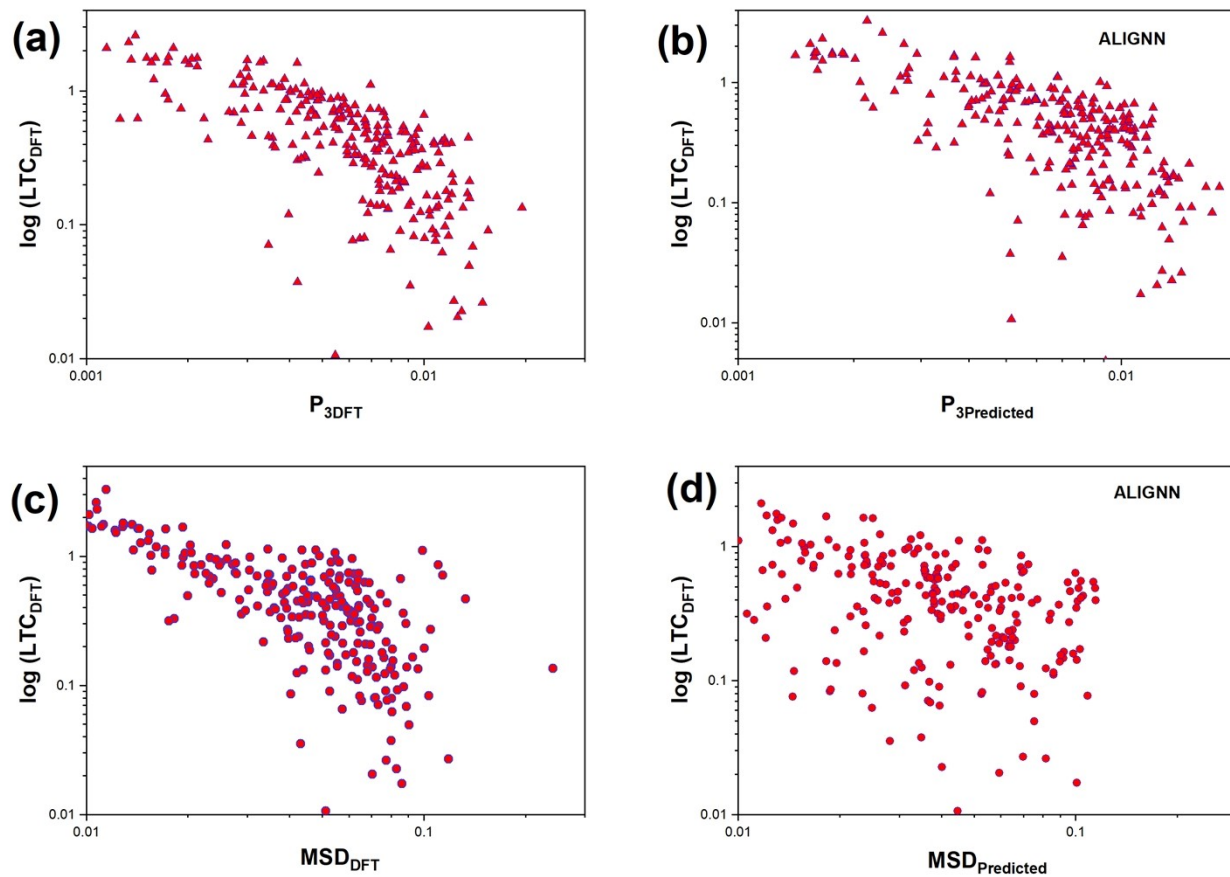
**Figure S3:** Phonon dispersions of selected structures (a)  $\text{Br}_5\text{Cs}_3\text{Zn}$ , (b)  $\text{Cl}_6\text{PtRb}_2$ , (c)  $\text{AuBr}_2\text{ClCs}$ , and (d)  $\text{Br}_6\text{Cs}_2\text{Pt}$  along high symmetry paths. The non-negative phonon dispersions prove the thermodynamic stability of the structures. The low-lying acoustic phonon frequencies are also clearly seen, which is partially responsible for their ultralow lattice thermal conductivity.



**Figure S4:** Testing results of  $P_3$  parameter for the three GNN predictive models for 808 structures: (a) OGCNN, (b) deeperGATGNN, and (c) ALIGNN.



**Figure S5:** Testing results of mean squared displacement (MSD) of three GNN predictive models for 808 structures: (a) OGCNN, (b) deeperGATGNN, and (c) ALIGNN.



**Figure S6:** (a) DFT calculated  $P_3$  parameter versus LTC, (b) ALIGNN model predicted  $P_3$  parameter versus LTC, (c) DFT calculated MSD versus LTC, (d) ALIGNN model predicted MSD versus LTC.