

Unraveling the Role of Single Atom Catalysts on the Charging Behavior of Nonaqueous Mg-CO₂ Batteries: A Combined Density Functional Theory and Machine Learning Approach

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Table S1. The computed lattice constants of 3d SACs doped N₄, N₃S and N₂S₂ substrates

SACs	TM-N ₄	TM-N ₃ S	TM-N ₂ S ₂
	Å	Å	Å
Sc	8.478	8.596	8.478
Ti	8.420	8.550	8.703
V	8.408	8.530	8.659
Cr	8.370	8.517	8.635
Mn	8.371	8.494	8.620
Fe	8.348	8.468	8.590
Co	8.329	8.449	8.577
Ni	8.327	8.417	8.622
Cu	8.380	8.459	8.486

Table S2. The computed lattice constants of 4d SACs doped N₄, N₃S and N₂S₂ substrates

SACs	TM-N ₄	TM-N ₃ S	TM-N ₂ S ₂
	Å	Å	Å
Y	8.464	8.504	8.527
Zr	8.500	8.497	8.555
Nb	8.465	8.605	8.559
Mo	8.437	8.561	8.702
Tc	8.422	8.528	8.678
Ru	8.390	8.512	8.646
Rh	8.382	8.510	8.646
Pd	8.388	8.518	8.491
Ag	8.432	8.500	8.581

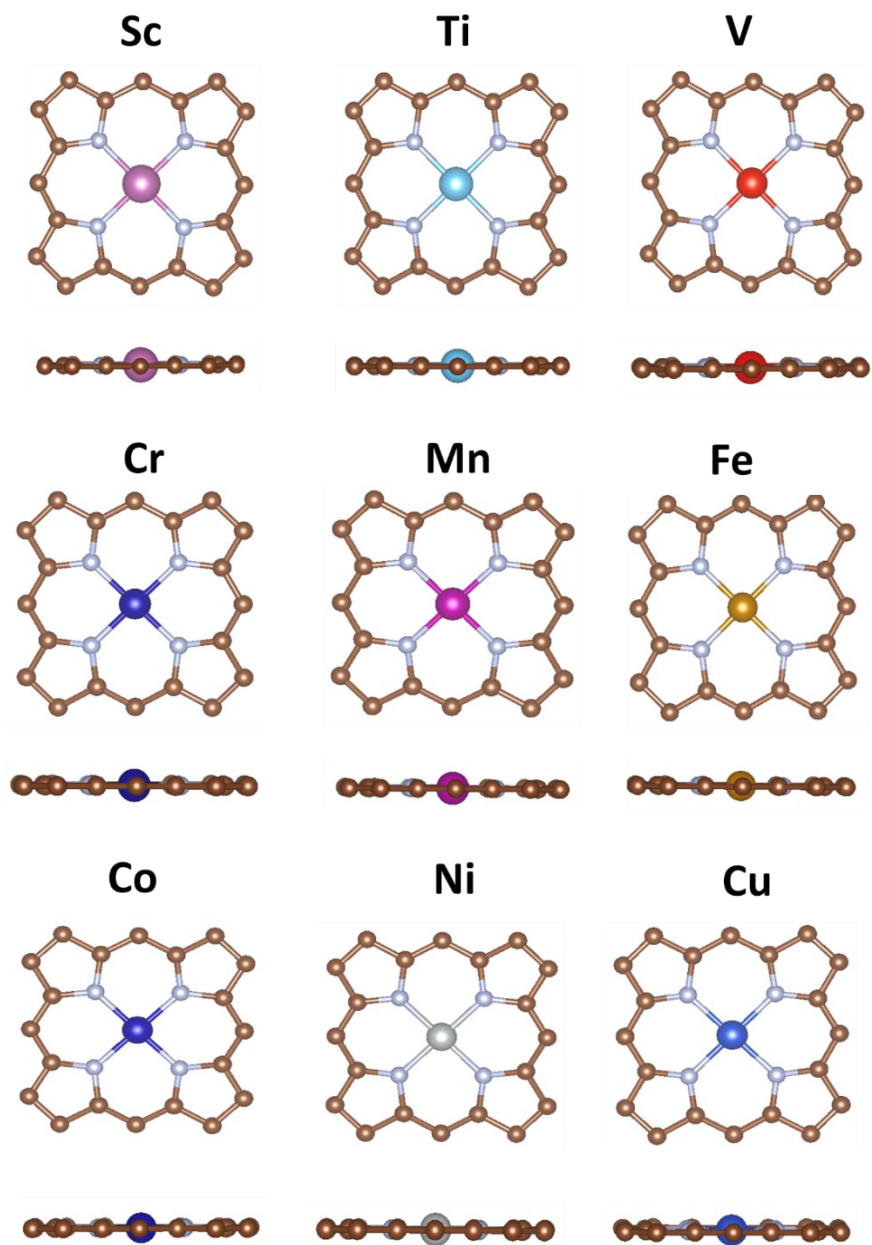


Figure S1. The top and side views of the optimized geometric configurations of 3d SACs doped N_4 environment

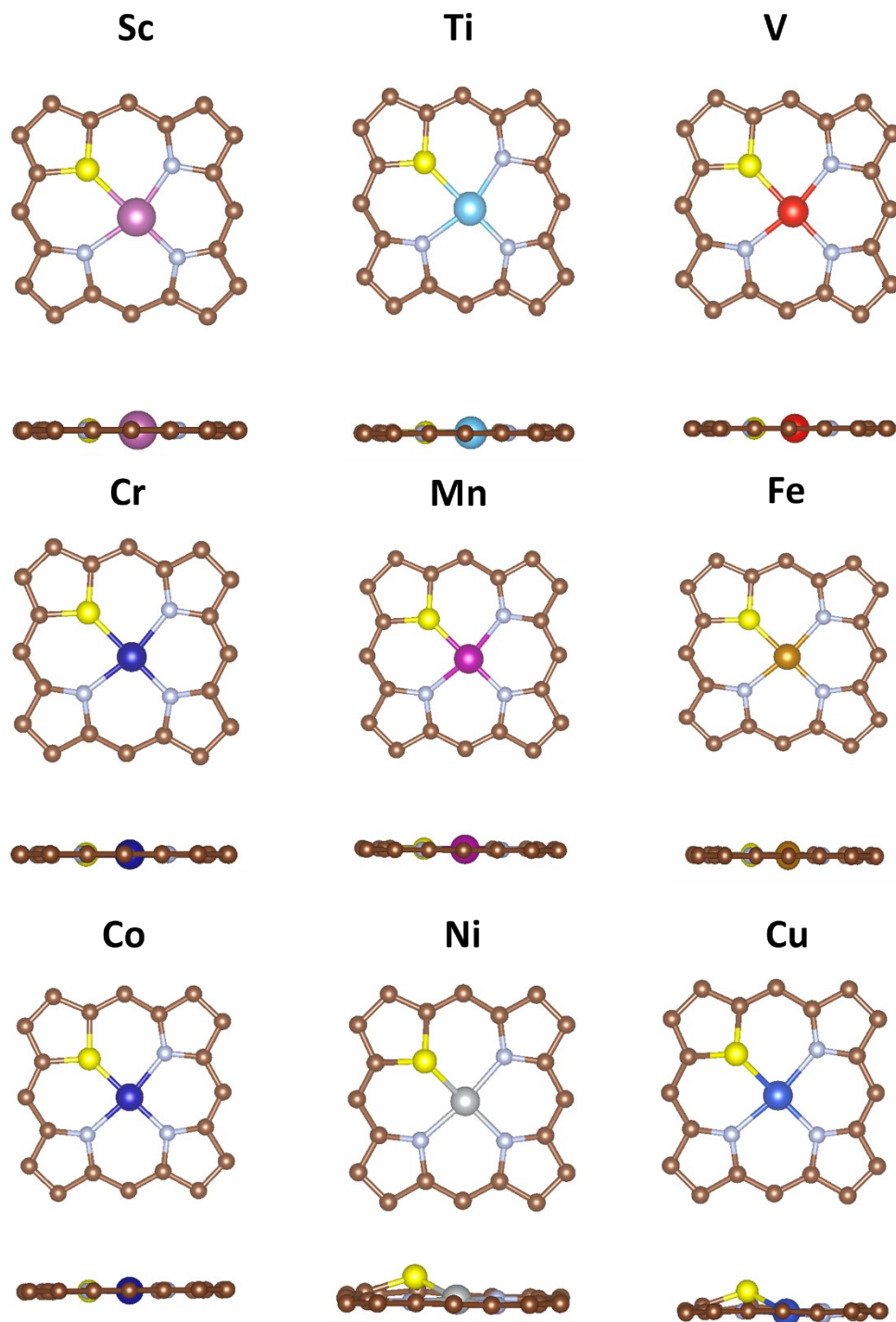


Figure S2. The top and side views of the optimized geometric configurations of 3d SACs doped N₃S environment

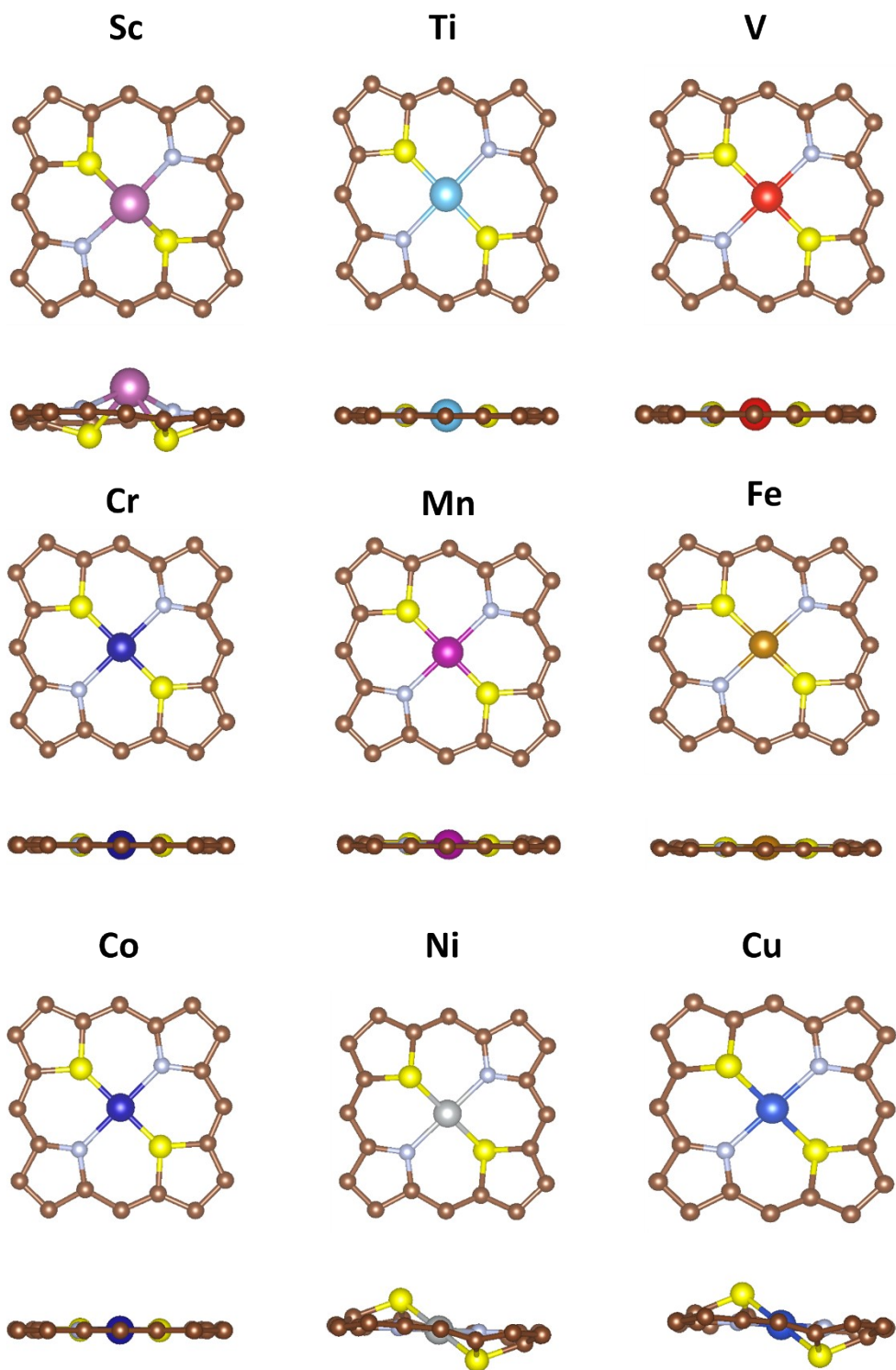


Figure S3. The top and side views of the optimized geometric configurations of 3d SACs doped N_2S_2 environment

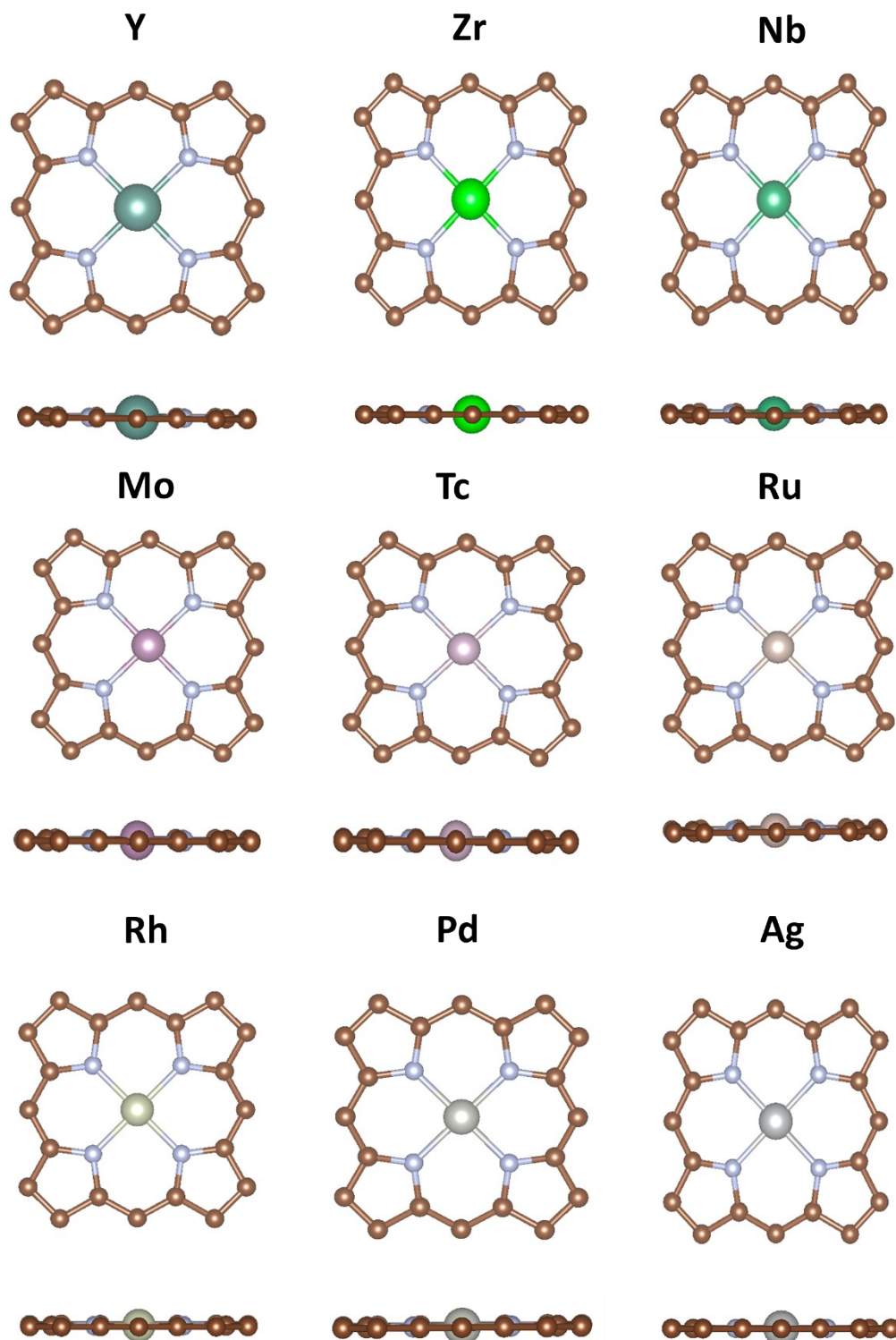


Figure S4. The top and side views of the optimized geometric configurations of 4d SACs doped N_4 environment

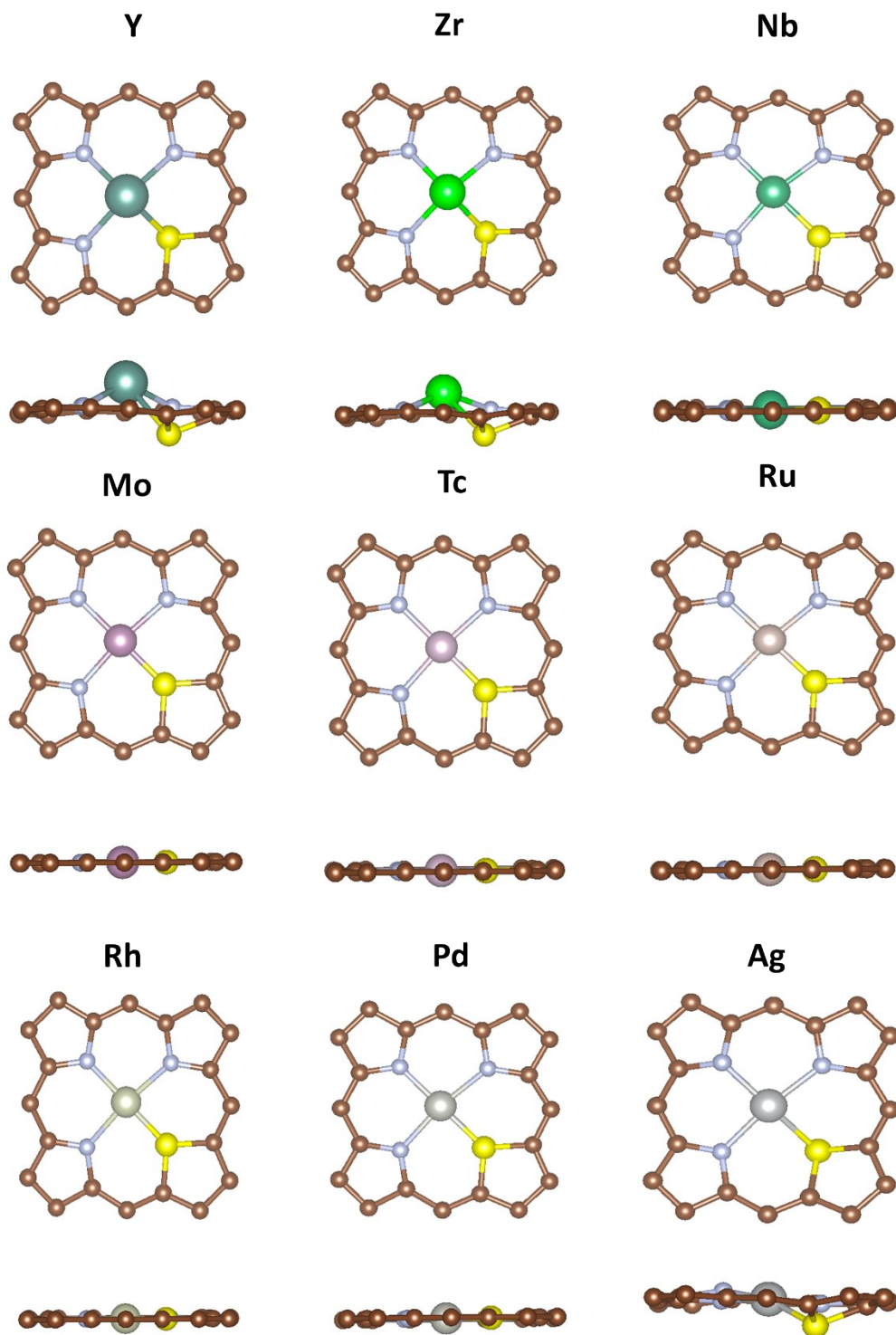


Figure S5. The top and side views of the optimized geometric configurations of 4d SACs doped N_3S environment

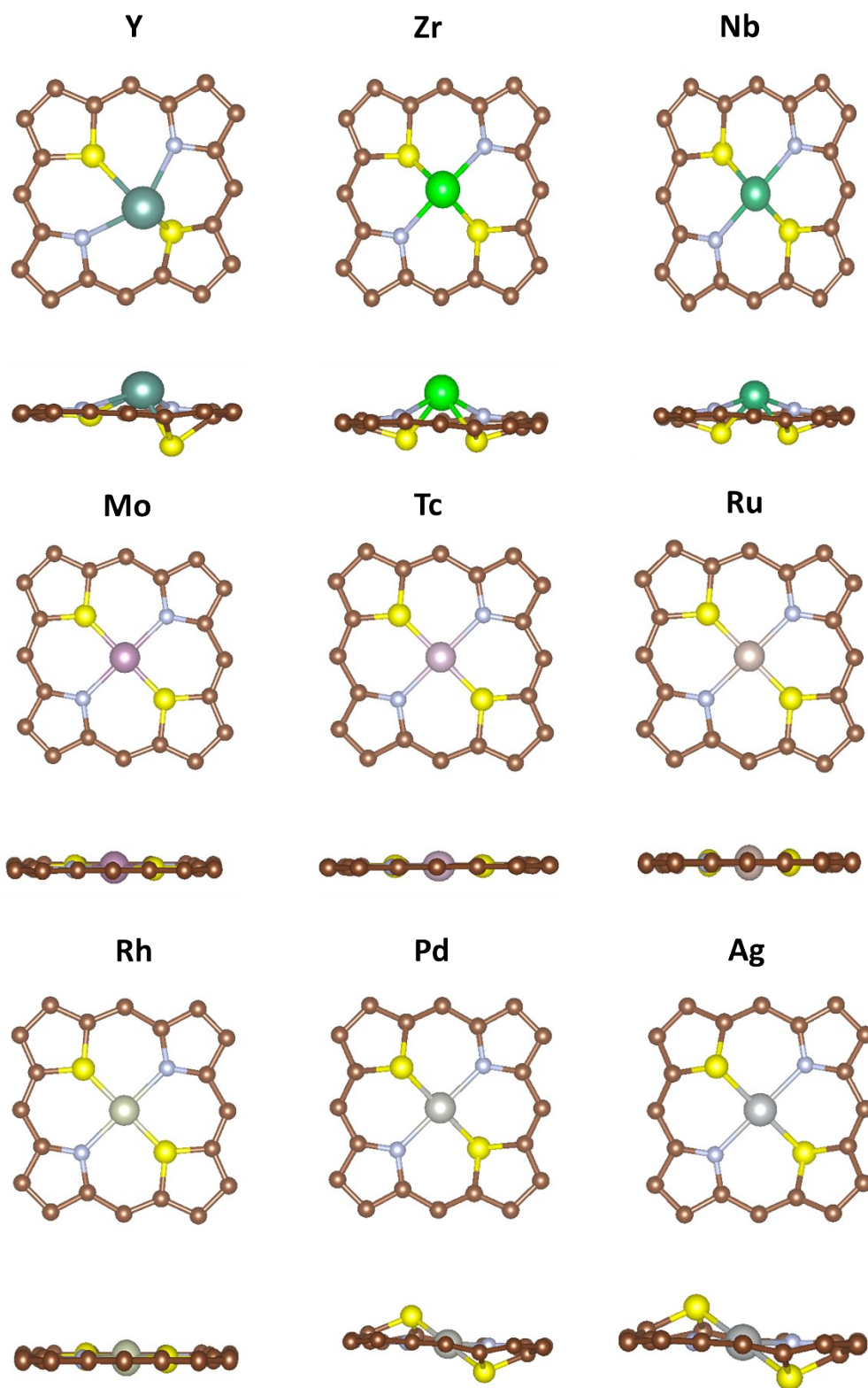


Figure S6. The top and side views of the optimized geometric configurations of 4d SACs doped N_2S_2 environment

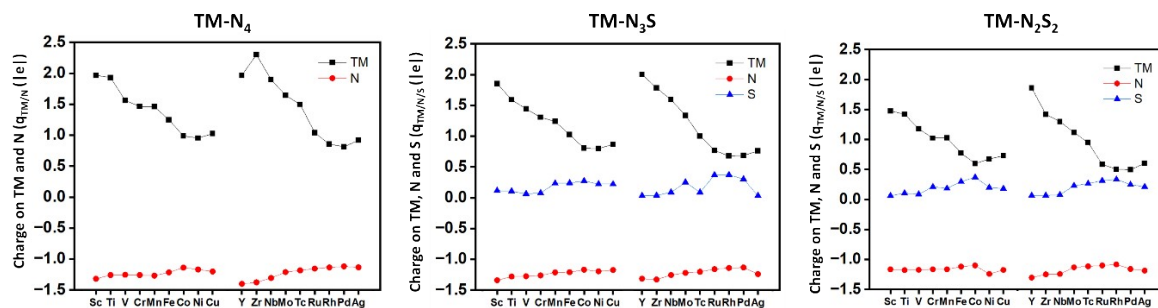


Figure S7. The computed charge transfer of TM, N and S on 3d and 4d SACs doped N_4 , N_3S and N_2S_2 substrates

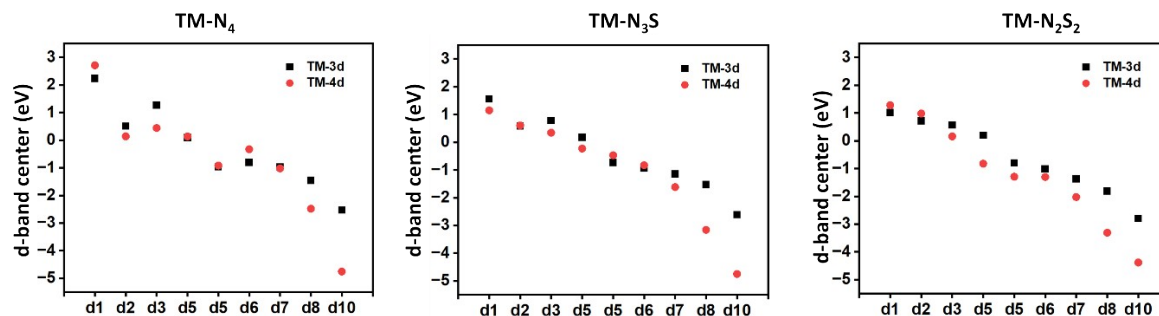


Figure S8. The calculated d-band center of both 3d and 4d SACs doped N_4 , N_3S and N_2S_2 substrates

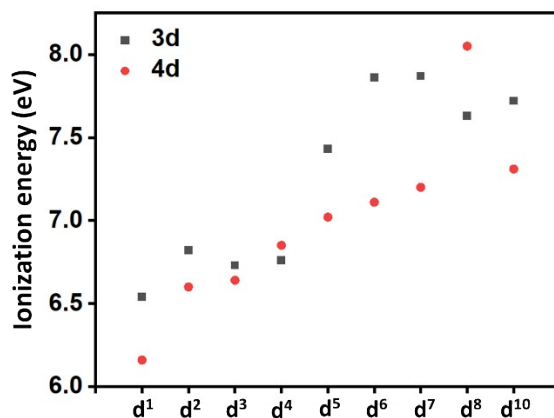
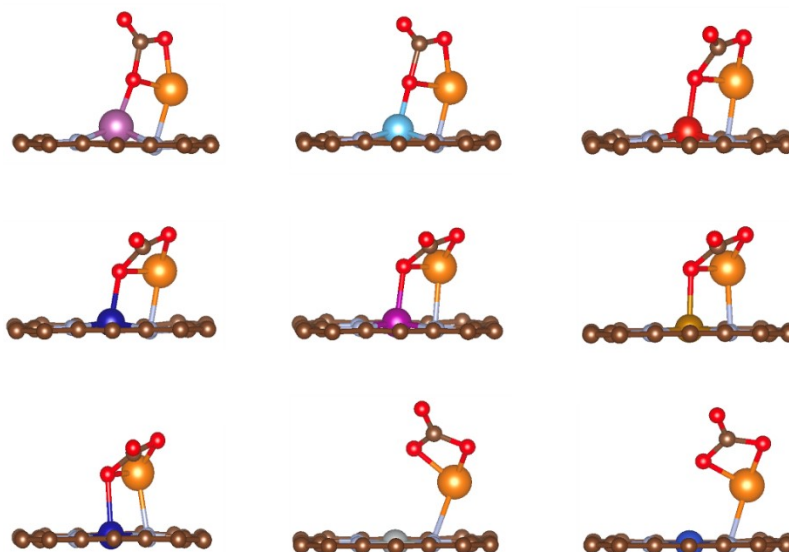


Figure S9. The correlation of ionization energy of both 3d and 4d SACs with the number of d-electrons

3d SACs@PP



4d SACs@PP

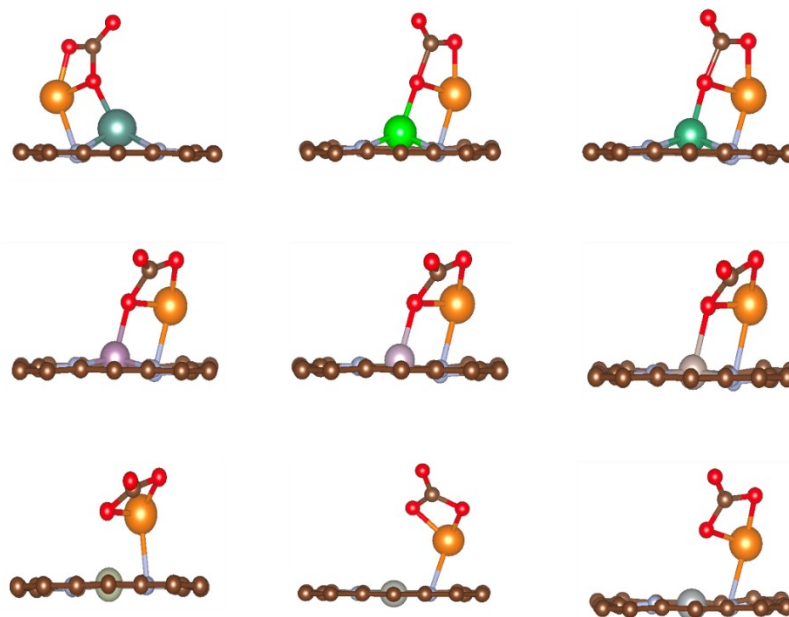
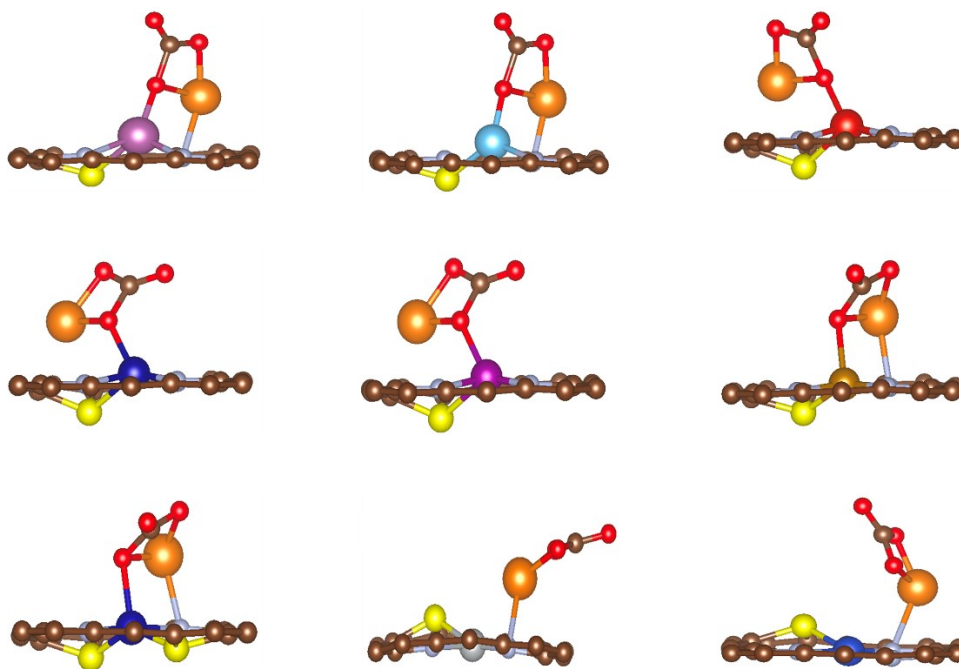


Figure S10. The side views of the optimized geometric configurations of MgCO₃ adsorbed on 3d and 4d SACs doped N₄ environment

3d SACs@PP



4d SACs@PP

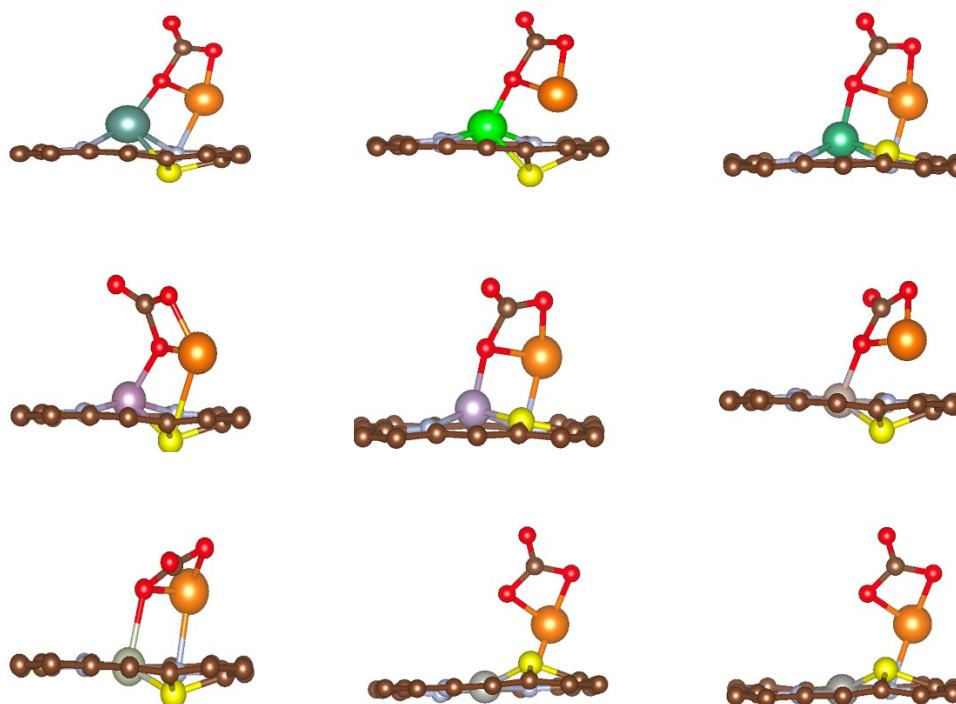
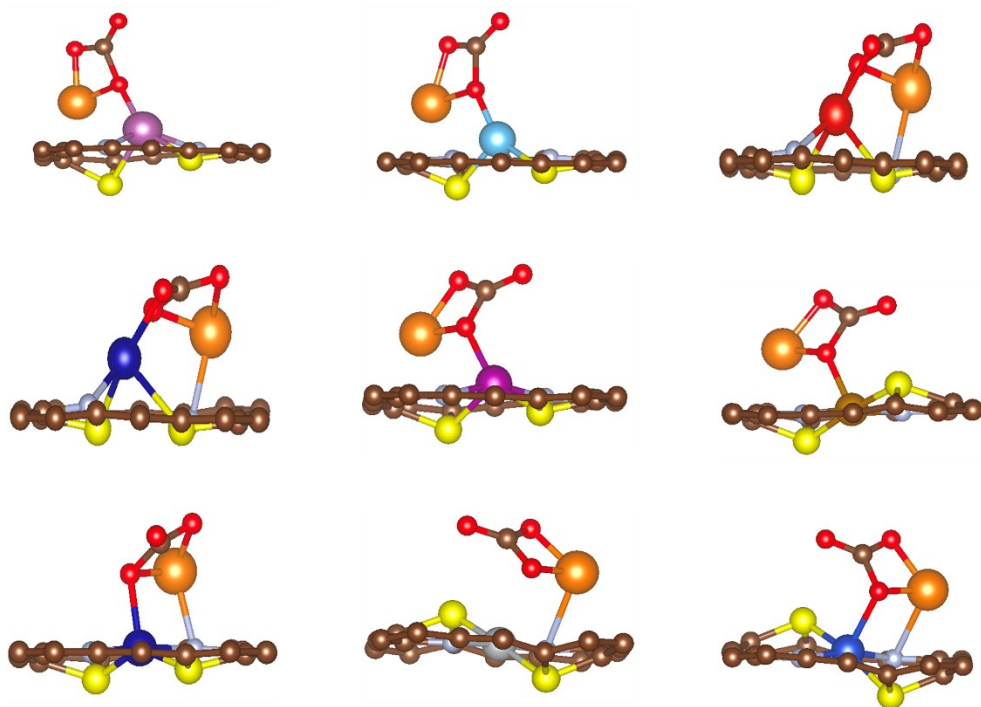


Figure S11. The side views of the optimized geometric configurations of MgCO_3 adsorbed on 3d and 4d SACs doped N_3S environment

3d SACs@PP



4d SACs@PP

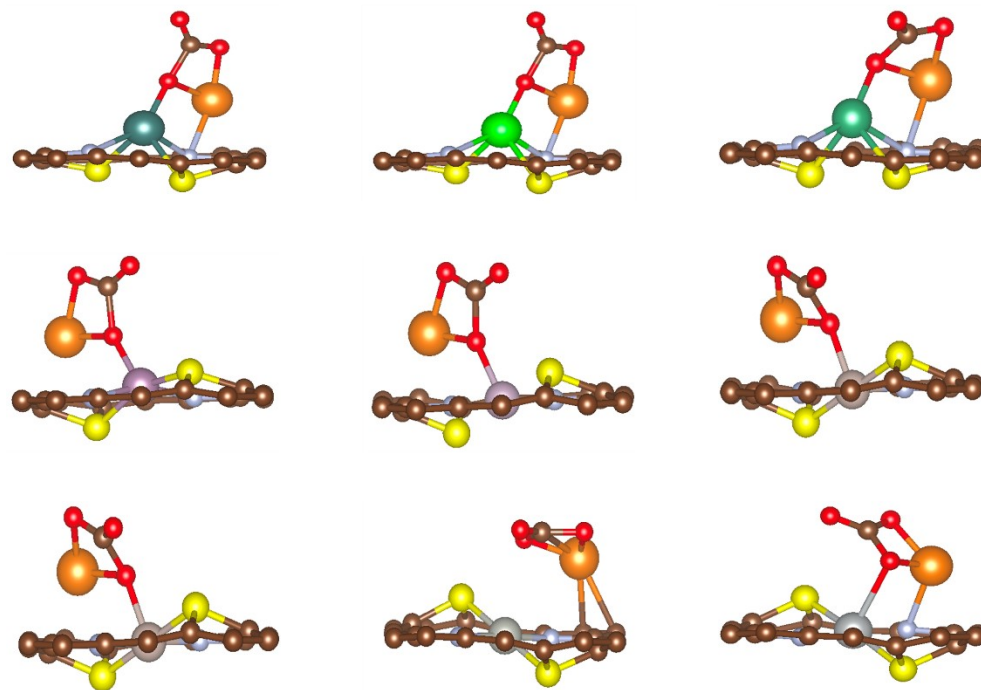


Figure S12. The side views of the optimized geometric configurations of MgCO_3 adsorbed on 3d and 4d SACs doped N_2S_2 environment

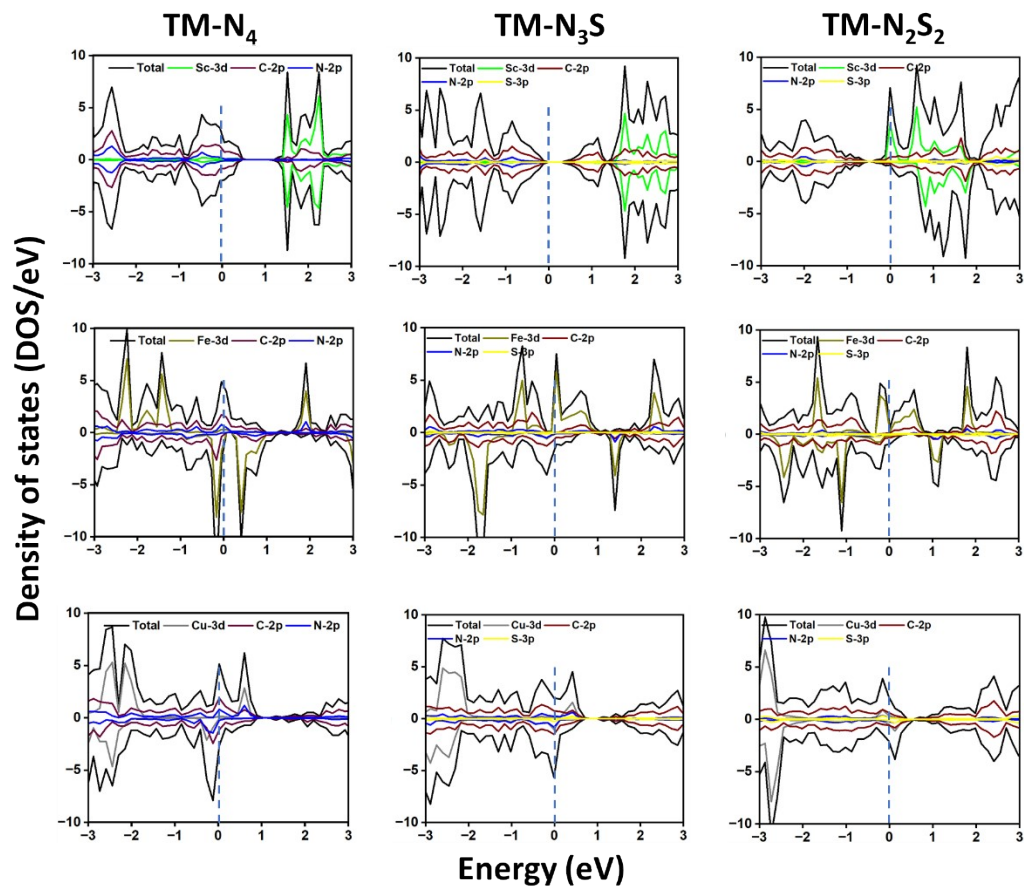


Figure S13. Projected density of states (PDOS) of representative early (Sc), mid (Fe) and late (Cu) 3d-TM doped N_4 , N_3S and N_2S_2 substrates

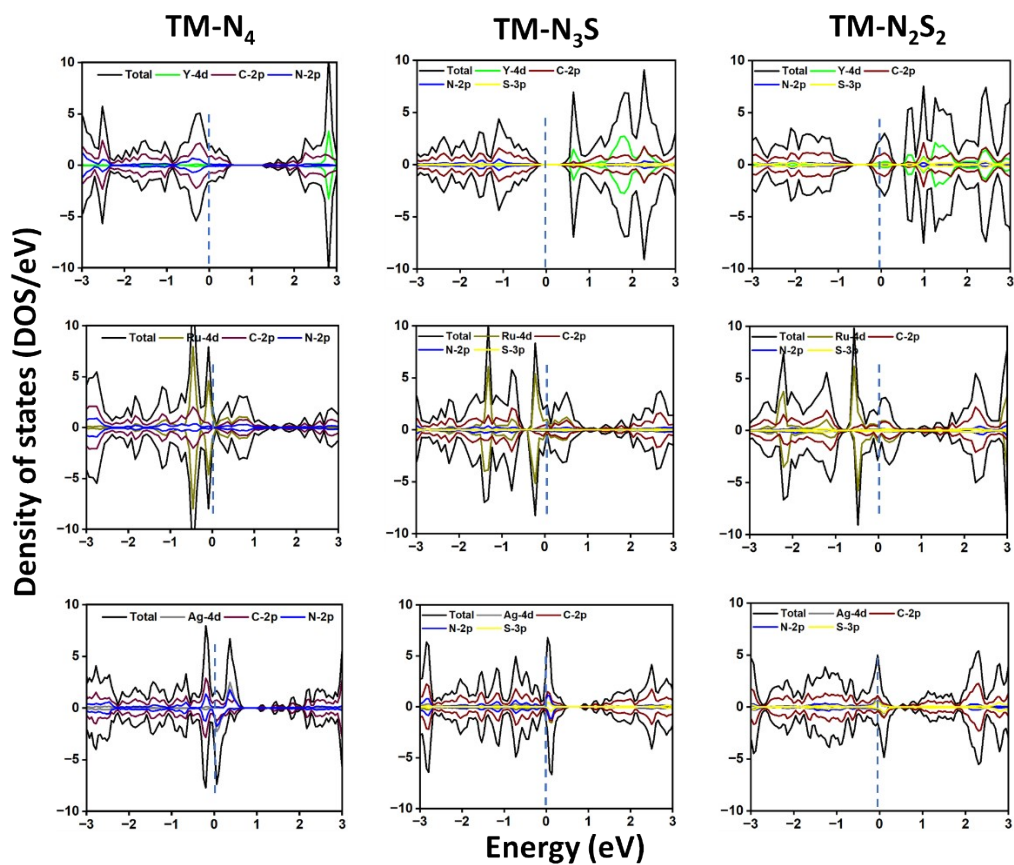


Figure S14. Projected density of states (PDOS) of representative early (Y), mid (Ru) and late (Ag) 4d-TM doped N_4 , N_3S and N_2S_2 substrates

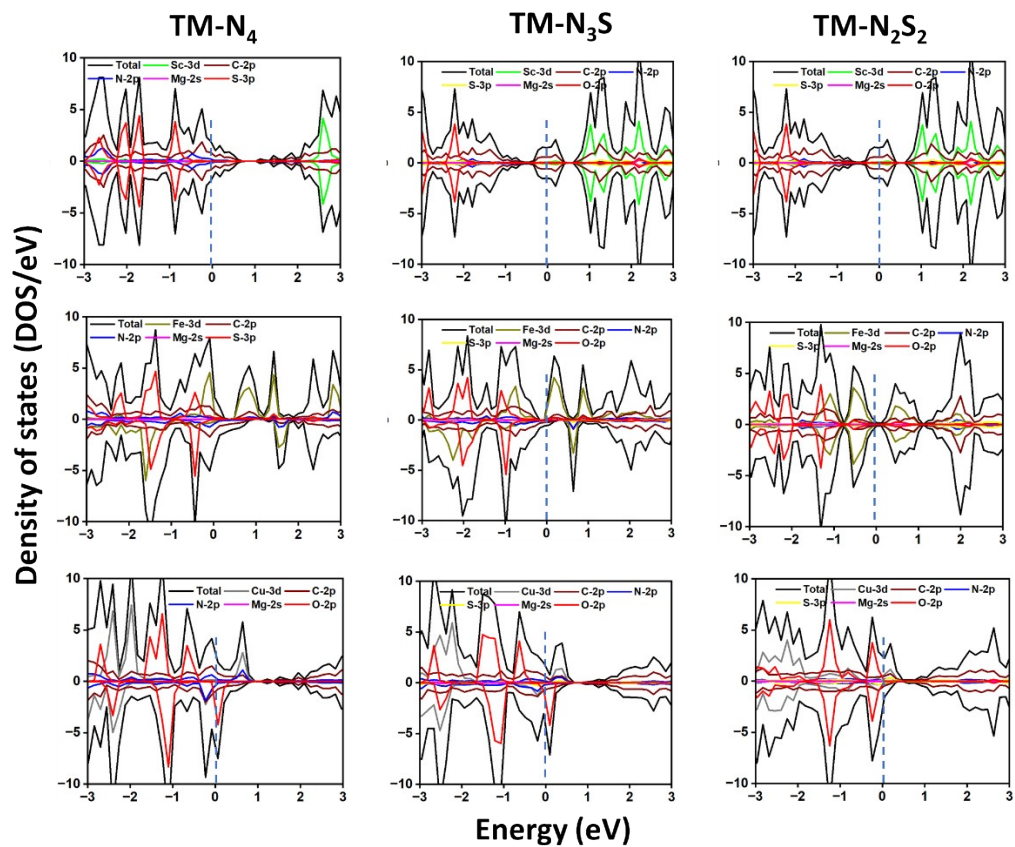


Figure S15. Projected density of states (PDOS) of MgCO₃ adsorbed Sc, Fe and Cu TM doped N₄, N₃S and N₂S₂ substrates.

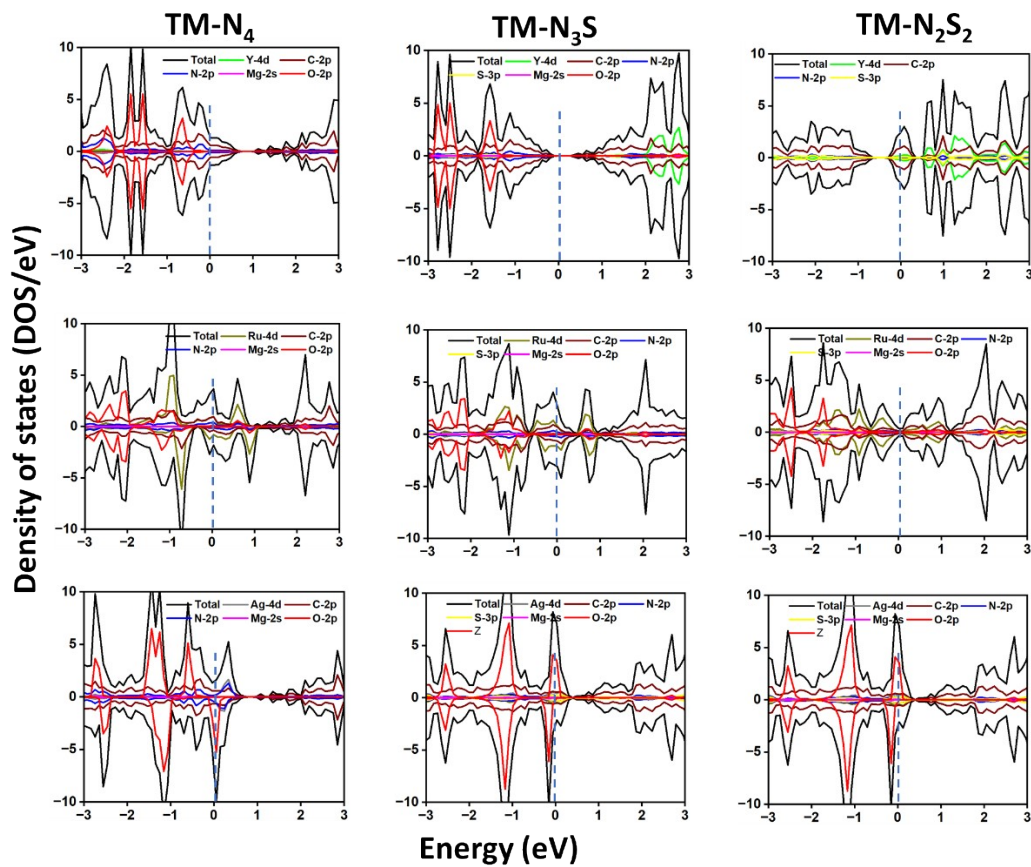


Figure S16. Projected density of states (PDOS) of MgCO_3 adsorbed Y, Ru and Ag TM doped N_4 , N_3S and N_2S_2 substrates.

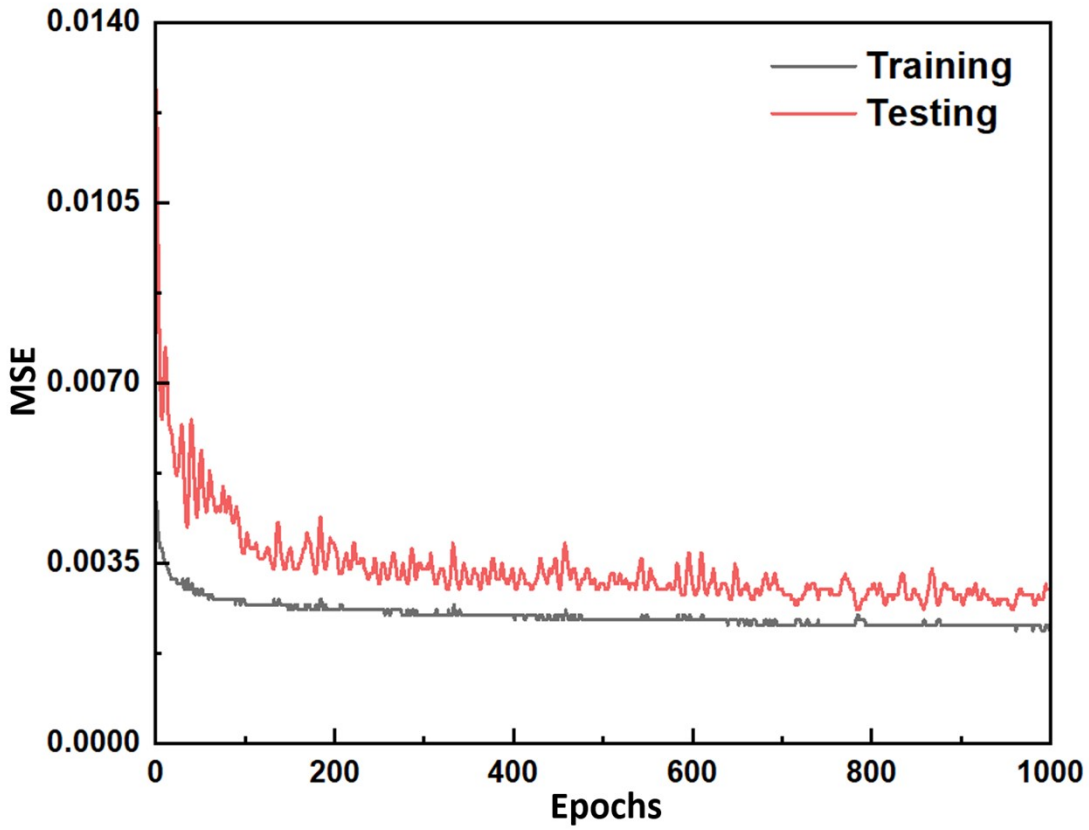


Figure S17. The evaluation of mean square error along with the number of iterations in ANN model

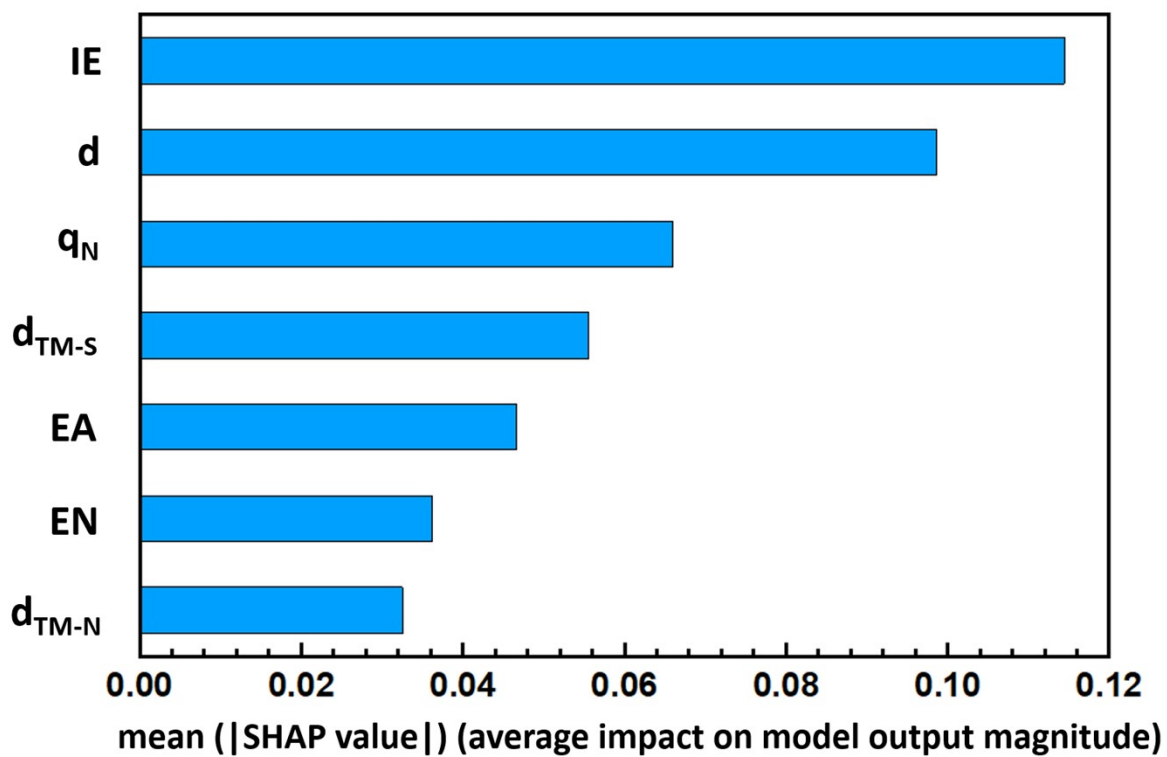


Figure S18. Comparison of SHAP values to analyze the feature importance of ANN model