

analytical grade and ordered from Shanghai Aladdin Biochemical Technology Co., Ltd.

23 (Shanghai, China). Zinc acetate dihydrate $(C_4H_6O_4Zn.2H_2O, 99\%)$, zinc sulfate 24 heptahydrate $(ZnSO_4.7H_2O, 99.5\%)$, N, N-dimethylformamide $(C_3H_7NO, 99.5\%)$, 25 acetonitrile (C₂H₃N, 99.5%), isopropanol (C₃H₈O, 99.7%), dichloromethane (CH₂Cl₂, 26 99.5%), potassium carbonate $(K_2CO_3, 99.0\%)$, hydrochloric acid (HCl, 36.0-38.0%), 27 and toluene $(C_7H_8, 99.5\%)$ were of analytical grade and purchased from Sinopharm 28 Chemical Reagent Co., Ltd. (Shanghai, China). Piperazine $(C_4H_{10}N_2, 97%)$ and 29 1,4,8,11-tetraazacyclotetradecane $(C_{10}H_{24}N_4, 98\%)$ were obtained from Shanghai 30 Tensus Biotech Co., Ltd. (Shanghai, China). 1,4,7-Triazacyclononane $(C_6H_15N_3, 98\%)$ 31 was received from Shanghai Macklin Biochemical Co., Ltd. (Shanghai, China). High 32 purity H₂ (\geq 99.999%) CO₂ (\geq 99.999%), N₂ (\geq 99.999%) and CH₄ (\geq 99.999%) were 33 purchased from Nanjing Shangyuan Industrial Gas Factory. Air source was acquired 34 from Nanjing Special Gas Co. Ltd. 5,5',6,6'-Tetrahydroxy-3,3,3',3'-tetramethyl-1,1'- 35 spirobisindane (TTSBI, 97%, Alfa Aesar), 2,3,5,6-Tetrafluoroterephthalonitrile 36 (TFTPN, 99%, Sigma-Aldrich) was purified via sublimation.

37 **1.2 DAC experiments**

38 First, 10 mL MeCN and 1 mmol HC_4 -N₂ were placed in a round-bottom flask and 39 homogenized by a magnetic stirrer at 200 r/min. Then, the round-bottomed flask was 40 loaded into the DAC testing system. The nondispersive infrared $CO₂$ meter, for 41 detecting $CO₂$ concentration in the downstream of the reactor, was turned on. The air 42 source was turned on, and the flow rate was adjusted to 60 mL min-1 for the DAC 43 experiments.

44 **1.3 Fabrication of HCx-Ny-CO2-Zn MOFs**

45 **1.3.1 Synthesis of HC4-N2-CO²**

46 The synthesis strategy of $HC_x-N_y-CO_2$ powders was carried out with slight 47 modifications based on the previous literature ^{S1}. The specific preparation method was 48 as follows: 0.75 mmol (51.68 mg) piperazine (HC_4-N_2) was dissolved in 20 mL IPA 49 and ultrasonicated for 10 minutes in a 50 mL round-bottom flask filled with an agitator 50 and rubber stopper. A clear and transparent colorless solution was obtained. N_2 was 51 added and swept for 10 minutes to remove air in the aqueous solvent and round-bottom 52 flask. Rapidly, CO_2 was introduced into the bottom of the round-bottom flask using a 53 catheter at room temperature and pressure, accompanied by bubbles in the solvent. In 54 this process, continuous magnetic stirring (960 r/min) made the distribution of starting 55 materials and $CO₂$ more uniform. After 1 minute, a white precipitate was produced. As 56 the reaction proceed, more CO_2 reacted with the secondary amine groups of HC_4 -N₂, 57 resulting in an increasing number of products until the reaction was completed after 3 58 hours. The white precipitate was centrifugally washed with isopropanol 3 times and 59 dried in a vacuum drying oven at 25 °C for 10 h. Finally, a white powder was obtained 60 by grinding.

61 **1.3.2 Synthesis of HC6-N3-CO²**

62 The HC_6 -N₃-CO₂ powder synthesis strategy was similar to that of HC_4 -N₂-CO₂ with 63 slight modifications. The specific preparation method was as follows: First, 0.75 mmol 64 96.91 mg 1,4,7-triazacyclononane (HC_6-N_3) was dissolved in 20 mL MeCN organic 65 solvent. As reported in the previous literature S2 , MeCN is more conducive to the 66 dissolution of $CO₂$ due to the presence of nitrogenous groups with a strong affinity for $CO₂$ and is more conducive to realizing a high yield. A clear and transparent colorless solution was obtained in a 50 mL round-bottom flask with a rubber stopper and agitator 69 for 10 min by ultrasound. Thereafter, N_2 was injected for 10 minutes to remove air from 70 the solvent and round-bottomed flask. Promptly, $CO₂$ was introduced into the bottom of the round-bottomed flask using a catheter at room temperature and pressure, accompanied by bubbles in the solvent. During this process, magnetic stirring (960 r/min) was carried out continuously to make the distribution of starting materials and $CO₂$ more uniform. A white precipitate was generated after 5 s, indicating that the 75 reactive activation of HC_6-N_3 was higher than that of HC_4-N_2 due to the special 76 chemical structure. As the reaction progressed, more $CO₂$ reacted with the secondary 77 amine group of HC_6-N_3 , resulting in an increasing number of products until the reaction ended 2 hours later. The white precipitate was washed 3 times by centrifugation with the MeCN solvent and dried in a vacuum drying oven for 10 hours. After grinding, white powders were also obtained.

81 **1.3.3 Synthesis of HC10-N4-CO²**

82 The synthesis strategy of HC_{10} -N₄-CO₂ powders was similar to that of HC_{4} -N₂-CO₂ 83 with only slight modifications. The specific preparation method was as follows: First, 84 1.50 mmol 300.50 mg needle-like 1,4,8,11-tetraazacyclotetradecane (HC_{10} - N_4) as the 85 starting material was dissolved in a 30 mL MeCN organic solvent of 30 mL. A clear 86 and transparent colorless solution was obtained in a 50 mL round-bottom flask with a 87 rubber stopper and agitator for 10 min by ultrasound. Similarly, N_2 was injected for 10 88 minutes to remove air from the solvent and round-bottomed flask. Rapidly, $CO₂$ was

 introduced into the bottom of the round-bottomed flask using a catheter at room temperature and pressure, accompanied by bubbles in the solvent. During this process, magnetic stirring (960 r/min) was carried out continuously to make the distribution of 92 starting materials and $CO₂$ more uniform. After 30 min, a white precipitate was 93 produced, indicating that the reactive activation of HC_{10} -N₄ was lower than that of HC_{4} - N₂ and HC₆-N₃ due to the more complex chemical structure. As the reaction progressed, 95 more CO_2 reacted with the secondary amine groups of HC_{10} -N₄, resulting in an increasing number of products until the reaction ended after 5 hours. The white precipitate was washed 3 times by centrifugation with MeCN and dried in a vacuum drying oven for 10 h. After grinding, white powders were also obtained.

99 **1.3.4 Synthesis of HC4-N2-CO2-ZnX (X=OAC- , NO³ - , SO⁴ 2-)**

100 The synthesis strategy of HC_4 -N₂-CO₂-ZnX powders was carried out as follows: 101 Initially, 0.8 mmol 175.6 mg Zn(OAC)₂·2H₂O [0.8 mmol 237.99 mg Zn(NO₃)₂·6H₂O 102 or 0.8 mmol 230.05 mg $ZnSO_4$ ⁻⁷H₂O] and 0.75 mmol (51.68 mg) HC₄-N₂ were 103 dissolved in 20 mL N,N-dimethylformamide (DMF) and 20 mL IPA solvent, 104 respectively. The clear and transparent colorless solution was obtained by ultrasound 105 for 10 min. N_2 bubbling was carried out and purged for 10 min to remove the air in the 106 metal solution and round-bottom flask. $Zn(OAC)_{2}$:2H₂O, $Zn(NO_{3})_{2}$:6H₂O or 107 $ZnSO_4$ $7H_2O$ and HC_4 -N₂ solution were placed in a 100 mL round-bottom flask filled 108 with an agitator and rubber stopper. Promptly, $CO₂$ was introduced into the bottom of 109 the round-bottom flask using a catheter at room temperature and pressure, accompanied 110 by bubbles in the solvent. During this process, magnetic stirring (960 r/min) was carried

111 out continuously to make the distribution of starting materials and $CO₂$ more uniform. 112 After 10 s, a white precipitate occurred. As the reaction proceeded, CO_2 reacted with 113 the secondary amine groups of HC_4 -N₂ to form HC_4 -N₂-CO₂, which acted as the ligands 114 of the MOFs. Ultimately, the resulting ligands reacted with six-coordinated zinc 115 clusters to form Zn-MOFs. As the reaction progressed, an increasing number of white 116 products were produced until the reaction was over three hours later. The final white 117 precipitates, $HC_4 - N_2 - CO_2 - Zn(OAC)_2$, $HC_4 - N_2 - CO_2 - Zn(NO_3)_2$, and $HC_4 - N_2 - CO_2 - Zn(NO_3)_2$ 118 ZnSO4, were centrifugally washed with DMF and IPA 3 times and dried in a vacuum 119 oven for 10 hours. The white powders were ground, sealed and preserved under 120 vacuum.

121 **1.3.5 Synthesis of HC6-N3-CO2-ZnY (Y=OAC- , NO³ -)**

122 The synthesis strategy of HC_6 -N₃-CO₂-ZnY powders was similar to that of HC_4 -N₂-123 $CO₂$ -ZnX. The specific method was carried out as follows: First, 0.9 mmol 197.56 mg 124 Zn(OAC)₂·2H₂O [0.9 mmol 267.74 mg Zn(NO₃)₂·6H₂O] and 0.75 mmol 96.91 mg 125 HC_6-N_3 were dissolved in 20 mL DMF and 20 mL MeCN, respectively. Thereafter, the 126 solutions were fully dissolved by ultrasound for 10 min to obtain clear and transparent 127 colorless solutions. A N_2 bubble was added and purged for 10 minutes to remove the 128 air in the solvent. The $Zn(OAC)_2$ ²H₂O [Zn(NO₃)₂·6H₂O] and HC₆-N₃ solutions were 129 placed in a 100 mL round-bottom flask with a rubber stopper filled with an agitator. 130 Rapidly, $CO₂$ was introduced into the bottom of the round-bottom flask using a catheter 131 at room temperature and pressure, accompanied by bubbles in the solvent and round-132 bottomed flask. A white precipitate was formed immediately with the entry of $CO₂$.

133 During this process, magnetic stirring (960 r/min) was carried out continuously to make 134 the distribution of starting materials and the $CO₂$ system more uniform. In this reaction 135 system, CO_2 reacted with the secondary amine groups of HC_6 -N₃ to form HC_6 -N₃-CO₂ 136 as the ligands of MOFs. Furthermore, the resulting ligands reacted with six-coordinated 137 zinc clusters to form Zn-MOFs. As the reaction progressed, an increasing number of 138 white products was produced until the reaction was conducted over 2 hours. The white 139 precipitate was centrifugally washed with DMF and MeCN 3 times and dried in a 140 vacuum oven for 10 h. Fine HC_6 -N₃-CO₂-Zn(OAC)₂ and HC_6 -N₃-CO₂-ZnNO₃ white 141 powders were obtained by grinding, which were sealed and stored in vacuum for later 142 use.

143 **1.3.6 Synthesis of HC10-N4-CO2-Zn(OAC)²**

144 The synthesis strategy of HC_{10} -N₄-CO₂-Zn(OAC)₂ powders was as follows: 1.5 mmol 145 329.27 mg $Zn(OAC)_2$: $2H_2O$ and a certain amount of HC_{10} -N₄-CO₂ powder were dissolved in 20 mL DMF and 20 mL IPA, respectively. Two clear and transparent 147 colorless solutions were obtained by ultrasound for 10 min. N_2 was added and purged for 10 min to remove the air in the solvents and round-bottomed flask. The $Zn(OAC)_2$ ²H₂O and HC₁₀-N₄-CO₂ solutions were placed in a 100 mL round-bottom 150 flask with a rubber stopper filled with an agitator. Rapidly, $CO₂$ was introduced into the bottom of the round-bottom flask using a catheter at room temperature and pressure, accompanied by bubbles in the solvent. During this process, magnetic stirring (960 r/min) was carried out continuously to make the distribution of starting materials and CO_2 more uniform. In the process, HC_{10} -N₄-CO₂, as the ligand, reacted with six coordinated zinc clusters to form Zn-MOFs. After 6 hours of reaction, the liquid was 156 heated to 80 °C to precipitate the crystal powders. The white HC_{10} -N₄-CO₂-Zn(OAC)₂

powders obtained by grinding were sealed and stored in vacuum for later use.

1.4 Fabrication of PIM-1-based mixed-matrix membranes

1.4.1 TTSBI and TFTPN purification

 5,5',6,6'-Tetrahydroxy-3,3,3',3'-tetramethyl-1,1'-spirobisindane (TTSBI) powders (26 g) and methanol (MeOH, 140 g) were mixed into a conical flask with a stirrer. Then 163 the bottle was placed on a 65 \degree C heater and stirred for 4 hours. After finishing above process, the heater was turned off. Dichloromethane (DCM, 40 g) was added into the bottle. After 30 min, the bottle was placed in a refrigerator for 2 hours. Finally, the mixture was filtered and rinsed by methanol to obtain purified TTSBI. 2,3,5,6- Tetrafluoroterephthalonitrile (TFTPN) was purified via sublimation using a homemade equipment.

1.4.2 synthesis of PIM-1 powders

 The typical procedure for synthesis of PIM-1 was carried out as follows: TTSBI (1.55 171 g, 4.5 mmol), TFTPN (0.91 g, 4.5 mmol), and K_2CO_3 (2.51 g, 18.0 mmol), and freshly distilled DMF (30 mL) were added to a 50 mL round-bottomed flask equipped with a magnetic stirrer, a nitrogen inlet and a reflux condenser. The system was purged with N_2 and then the N_2 inlet was removed and the mixture was placed on a hot stirring plate 175 and stirred at 600 rpm. The mixture was heated to 100 $^{\circ}$ C and 1.0 mL toluene was added to the system and maintained at this temperature for 24 h to ensure high molecular

 polymers. With the polymerization process, a yellowish suspension was gradually obtained. Then the solution was cooled down to room temperature and carefully poured into 300 mL deionized water with a vigorously stirred magnetic stirrer to yield a 180 powder-like precipitate. The residual K_2CO_3 was removed by adding 1M HCl until CO₂ evolution stopped and pH was about 5. The recovered precipitate was filtered, then washed thoroughly with deionized water for several times until pH was about 7. After 183 that, the orange precipitate was washed several times with methanol at 60 \degree C to remove the organic solvent. Finally, the orange solid dried at 80 °C under high vacuum for 12 h.

1.4.3 Fabrication of mixed-matrix membranes

 PIM-1-based MMMs were fabricated by a priming process. PIM-1 (0.2 g) was 188 dissolved in $CH_2Cl_2(9.8 g)$ to obtain a 2 wt% solution. MOF nanoparticles (2 mg) were dispersed in the above PIM-1 solution and violently stirred for 12 h to obtain a uniform dispersion. Finally, the casting solution was poured into a homemade mold with a glass lid to slow down its evaporation rate, and the evaporation process was controlled for 12 h. The obtained membranes were dried for 12 h before the tests.

1.4 Separation performance tests

 Separation performance tests were carried out by using a home-made gas permeability 195 analyzer at 298 K. The prepared membrane with an effective area of 0.28 cm² was sealed and placed in the permeation cell by using an O-ring. Pure gas was used as the feed gas. The inlet pressure was regulated through an upstream vacuum pump, while the permeate side was vacuum-treated. Finally, the feed gas would pass through the 1 %

 HC_6 -N₃-CO₂-Zn(NO)₃ mixed matrix membranes into the permeate side. Gas permeability (P) was calculated based on the membrane thickness, permeate time, permeate volume, transmembrane pressure, and effective membrane area. Selectivity 202 (α) was calculated by the permeability of different gases (Pi and Pi):

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203 \qquad \qquad \alpha = P_i/P_j
$$

1.5 Characterizations of HCx-Ny-CO2-Zn MOFs

 Powder X-ray diffraction (PXRD, Bruker D8 Advance) was employed to investigate 206 the crystalline structure of MOFs powders in a 2 θ range of 5-50° utilizing Cu K- α 207 (λ =1.54 Å) as the X-ray radiation source. The chemical structures of the synthesized $HC_x-N_y-CO_2-Zn$ MOFs were identified using a Bruker Tensor II Fourier transform 209 infrared spectrometer with a wavenumber range of 400-4000 cm⁻¹. X-ray photoelectron spectroscopy (XPS, Kratos AXIS SUPRA+) equipped with an Al Kα X-ray source (1486.6 eV) was used to analyze the chemical structure and element composition of MOFs. The morphology of the starting material and MOFs were further determined by field emission scanning electron microscopy (FESEM, Quanta FEG 250). The dispersion of samples was of great importance for SEM characterizations to obtain the desired morphology. A variety of MOFs powders were uniformly dispersed by ultrasonication for a certain time using different organic solvents before being dripped onto a silicon wafer. All samples were sprayed with Pt/Pd alloy for 40 s using an auto fine coater (208 HR, TED PELLA, INC.) and operating at a 20 mA current to enhance the definition of SEM images. The thermal stability of different MOFs was evaluated by a thermogravimetric analyzer (DTG-60H, SHIMADZU) in the temperature range of

221 25-800 °C with a heating ramp of 10 °C min⁻¹ under a flowing N₂ atmosphere 222 accompanying a flow of 50 mL min⁻¹. Field emission transmission electron microscopy images were obtained by a Talos F200X field emission transmission electron microscope at an accelerating voltage of 200 kV. Solvent-dispersed MOFs powders were loaded on copper grids for FE-TEM imaging. 1H NMR spectra were recorded on a Bruker Avance-600 (600 MHz) spectrometer. Chemical shifts were expressed in 227 p.p.m. downfield from tetramethylsilane (TMS) at $d \delta = 0$ p.p.m. and J values are given in Hz. The free volume size and distribution of the membranes were detected by positron annihilation lifetime spectroscopy (PALS). ²²Na isotope was employed as positron and g-ray (1275 keV) sources. The membrane samples were cut into pieces of 1×1 cm, and the thickness of each sample was stacked into a total thickness of approximately 1 mm.

236 **Figure S1**. Measurements of CO₂ concentration in the atmosphere by using a

- 237 nondispersive infrared CO_2 meter (GMP252, Vaisala GmbH). The testing result was
- 408 ppm.
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243 **Figure S2. Visible DAC capacity analysis of HCx-Ny**. (a) Model diagram and (b) 244 Digital images after HC_4 -N₂ and HC_6 -N₃ adsorbents absorbing CO_2 exhaled by a human 245 body. (c) Model diagram of the experimental apparatus to capture $CO₂$ existing in the 246 atmosphere. (d) Changes in the form of HC_6 -N₃ before (left side) and after (right side) 247 CO_2 captured in the atmosphere by comparing their digital images. (e) The CO_2 248 absorption testing system including air source, absorption reactor and detection system. 249 (f) The CO_2 removal efficiency of HC_4 -N₂, MEA, and KOH as a function of time. 250

252 **Figure S3.** a, b, FESEM pictures and **C**, Size distribution of HC₄-N₂-CO₂ obtained in

- the atmosphere at different magnifications. d, e, FESEM pictures and f, Size
- 254 distribution of HC_6 -N₃-CO₂ obtained in the atmosphere at different magnifications.
- Size distributions in c and f were measured by a software.
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259 **Figure S4**. Schematic diagram of the CO₂ absorption testing system for the DAC

- process.
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Figure S5. Photographs of the DAC process by using HC4-N² in MeCN solutions

under air sources. a, 0.00 h. b, 0.50 h. c, 1.00 h. d, 3.15 h. e, 6.00 h. f, 12.00 h. The

265 downstream CO_2 concentration was monitored by using a nondispersive infrared CO_2

meter (GMP252, Vaisala GmbH).

Material class	Material	P_{CO2} (mbar)	$T (^{\circ}C)$	g/kg	mol/Kg	Reference
Metal-organic frameworks	Te-Mg ₂ (dobpdc)	50	90	149.6	3.4	[S3]
	Mg ₂ (dobdc)	50	95	35.2	0.8	[S4]
	CALF-20	1200	20	179.1	4.1	[_S 5]
	13X-IO10	900	30	46.2	1.1	[S6]
Zeolites	13X-IO20	900	30	65.1	1.5	[S6]
	$Na-GIS-3.0$	200	25	162.8	3.7	[S7]
	Graphene/IL	1000	25	374.0	8.5	[^S 8]
Ionic liquid	[DEEA][Pent]	4000	60	10.6	0.2	[^{S9}]
	P-DVB-AEImOH	1000	25	43.6	1.0	[S10]
	Mesoporous Silica	50	60	143.0	3.3	[S11]
Amine-decorated	TEPA-MCM-41	129	75	140.8	3.2	[S12]
mesoporous solid	SWIRL-TEPA	50	95	176.0	4.0	[S13]
		100	106	176.0	4.0	[S14]
	CTF-1-500	÷,	25	98.1	2.2	[S15]
Aza-fused π - conjugated	Bipy-CTF600		25	129.8	3.0	[S15]
networks	O-Doped CTFs	1000	24	211.2	4.8	[S16]
	IPDA	\blacksquare	25	279.0	6.3	[S17]
Amine adsorbent	MEA		25	446.6	10.2	[S17]
	HC_4 -N ₂	100	25	1048.0	23.8	This work
HC_x-N_v	HC_6 -N ₃	100	25	1047.6	23.8	This work
	$HC_{10} - N_4$	100	25	898.0	20.4	This work

273 **Table S1**. Comparison of CO_2 absorption performance of HC_x-N_y and other high

274 performing adsorbents reported in the literature.

275 -: not available

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- **Figure S6.** Diagram of the experimental device and the schematic diagram to prepare
- 282 MOFs from CO_2 , Zn clusters and HC_x-N_y .

291 **Figure S7.** Flow diagrams of the preparation process for HC_4 - N_2 - CO_2 - $Zn(OAC)_2$.

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- 297 **Figure S8.** Flow diagrams of the preparation process for HC_6 -N₃-CO₂-Zn(OAC)₂.
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303 **Figure S10.** (a) Digital picture and (b-e) SEM images of HC_{10} -N₄ at different

magnifications.

- **Figure S11.** Digital images of reaction at reaction durations of 0 s, 5 s and 2 h in the
- 308 HC_6-N_3 reaction system.

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Figure S12. FESEM images of HC4-N2-CO2-ZnSO4. FESEM images were colored

red for visual effect.

Entry	Name	Structure	N content a	Reference
$\mathbf{1}$	MEA	NH ₂ HO.	0.229	[S18]
$\overline{2}$	IPDA	NH ₂ NH ₂	0.165	[S18]
3	Cyclohexane-1, 3- diamine	NH ₂ NH ₂	0.246	[S18]
$\overline{4}$	DMAPA	NH ₂ N	0.159	[S19]
5	Lysine	Î NH ₂ OН NH ₂	0.171	[S20]
6	2-methylpiperidine		0.141	[S21]
τ	MMEA	H N CH ₃ HO.	0.237	$[$ 22]
8	DEAB	HO.	0.097	$[$ S22 $]$
9	MDEA	CH ₃ HO OH	0.118	$[$ 23]
10	HC_4 - N_2	NH HN	0.326	In this work
11	HC_6 -N ₃	nh hn, H -N	0.326	In this work
12	HC_{10} - N_4	-HN NH- NH HN-	0.280	In this work

315 **Table S2.** A comparison of N content of different amines reported in the state-of-the-

316 art literature.

317 **a** represent the mass ratio of N to the molecular mass

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321

324 **Figure S13** BET surface areas and pore sizes of the synthesized (a, d) HC₄-N₂-CO₂-

325 $Zn(OAC)_2$, (b, e) $HC_6-N_3-CO_2-Zn(NO_3)_2$, (c, f) $HC_{10}-N_4-CO_2-Zn(OAC)_2$ MOFs.

Notice: Aperture of MOFs is mainly less than 2 nm (micropore), so we choose the

327 $CO₂$ isotherm. The temperature of $CO₂$ isotherm was 195 K. Horvath-Kawazoe (HK)

method was used to test the micropores of MOFs.

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337 **Figure S14.** FT-IR spectra of HC_4 -N₂ and HC_4 -N₂-CO₂-ZnSO₄.

341 **Figure S15.** FT-IR spectra of HC₁₀-N₄.

343 **Figure S16.** ¹H NMR spectrum of HC_6 -N₃-CO₂-Zn(OAC)₂ dissolved in CDCl₃ at T =

298 K.

346 **Figure S17.** ¹H NMR spectrum of HC_{10} -N₄-CO₂-Zn(OAC)₂ dissolved in CDCl₃ at T

350 HC₄-N₂-CO₂-Zn(OAC)₂. **b**-**b2**, HC₆-N₃-CO₂-Zn(OAC)₂. **c-c2**, HC₁₀-N₄-CO₂-

Figure S19. Pie charts of different atomic ratios in different MOFs.

Figure S20. Synthesis and SEM pictures of PIM-1.

- TTSBI: 5,5′,6,6′-tetrahydroxy-3,3,3′,3′ tetramethylspirobisindane; TTFPN: 2,3,5,6-
- tetrafluoroterephthalonitrile; Solvent was dimethylformamide.

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377 **Figure S21** Preparation diagram of PIM-1/HC₆-N₃-CO₂-Zn(NO₃)₂ (1%) MMMs

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387 **Figure S23.** XPS survey spectra of the pure PIM-1 membrane and PIM-1/HC₆-N₃-CO₂-

Zn(NO3)2.

383 **Figure S22.** FTIR spectra of the pure PIM-1 and PIM- $1/HC_6$ -N₃-CO₂-Zn(NO₃)₂ (1%) MMMs.

390 **Figure S24.** Fine Zn 2p XPS spectra of PIM-1/HC₆-N₃-CO₂-Zn(NO₃)₂ (1%) MMMs.

394 **Figure S25.** TGA of the pure PIM-1 membrane and PIM- $1/HC_6$ -N₃-CO₂-Zn(NO₃)₂

(1%) MMMs.

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- **Figure S27.** Schematic diagram of positron annihilation lifetime spectroscopy
- (PALS).
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Figure S28. Peak-normalized positron lifetime spectra measured for the PIM-1 and

413 PIM-1/HC₆-N₃-CO₂-Zn(NO₃)₂ (1 %) membranes.

Figure S29. The illustration of the home-made apparatus including gas sources,

membrane modules, vacuum and detecting system for gas permeation tests.

- of the gas permeation apparatus.
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Figure S32. Digital picture of the PIM-1 membrane.

membranes.

Time (h)	Permeability (Barrer)		Selectivity	
	CO ₂	N_2	CO ₂ /N ₂	
$\mathbf{0}$	13343±520	601 ± 64	20.02 ± 0.32	
12	10925±516	589±35	18.08 ± 1.17	
18	10860±526	583±32	18.08 ± 1.07	
24	10467±532	580±34	17.76 ± 0.82	
36	10568±422	556±23	18.14 ± 0.86	
48	10681 ± 462	551±24	18.42 ± 0.75	
60	9928±450	546±26	17.85 ± 0.67	
66	9758±396	537±25	17.70 ± 0.75	
72	10058±385	504 ± 26	18.42 ± 0.56	
96	9569±366	483±25	17.82 ± 0.11	
108	9822±371	423 ± 26	19.50 ± 0.23	
120	9354±322	391±25	19.36 ± 0.31	
144	9060±316	365 ± 21	21.43 ± 0.71	
168	8784±268	583±19	22.48 ± 0.55	
192	9264±296	580±26	25.41 ± 0.67	

MMMs at 2 bar and 298 K during long-term tests.

494 **Table S7** Gas permeability and selectivity of PIM-1/HC₆-N₃-CO₂-Zn(NO₃)₂(1 %)

MMMs at 298 K and different pressures

Pressures (bars) Permeability (Barrer) Selectivity

507 **Table S8** Comparison of CO₂ permeability and CO₂/gases selectivity between PIM-

508 $1/HC_6$ -N₃-CO₂-Zn(NO₃)₂ (1 %) MMMs in this work and other reported PIM-1/MOF

509 MMMs.

524 **Figure S34.** Selectivity versus permeability for $CO₂/CH₄$, where gas separation performance of the MMMs prepared in this work (pentacles) and various MOF-based MMMs from literatures plotted against the Robeson plot of 2008. A fully detailed comparison of the data in this plot could be found in the Table S7.

- [S4] K. Sumida, D. L. Rogow, J. A. Mason, T. M. McDonald, E. D. Bloch, Z. R.
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