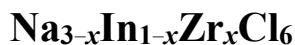


Supporting Information

On the influence of the coherence length on the ionic conductivity in mechanochimically synthesized sodium-conducting halides,



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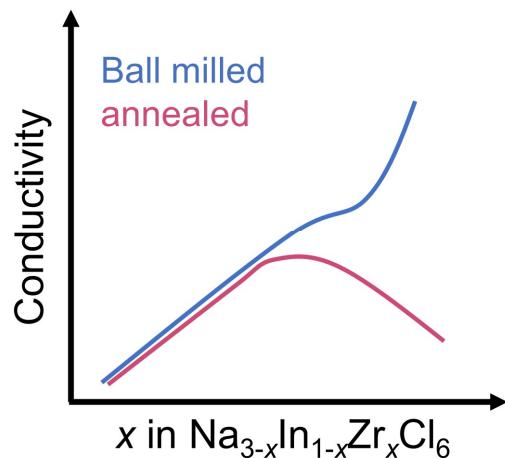


Fig. S1. Schematic of the differing trends of ionic conductivity against Zr content between ball milled and subsequently annealed $\text{Na}_{3-x}\text{In}_{1-x}\text{Zr}_x\text{Cl}_6$.

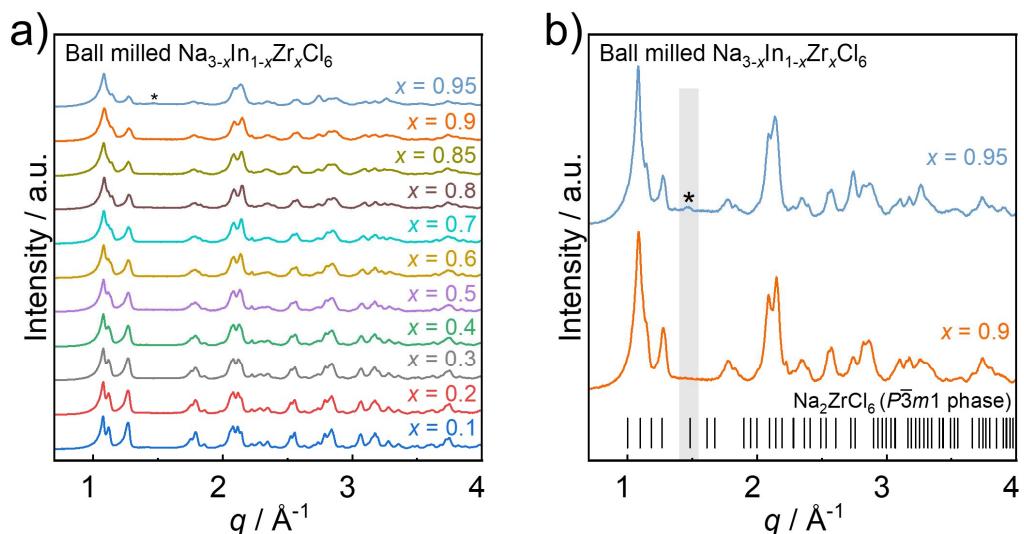


Fig. S2. a) X-ray diffraction patterns under $\text{Ag K}\alpha_1$ radiation of the ball milled $\text{Na}_{3-x}\text{In}_{1-x}\text{Zr}_x\text{Cl}_6$ series. b) Comparison of X-ray diffraction patterns of $\text{Na}_{2.05}\text{In}_{0.05}\text{Zr}_{0.95}\text{Cl}_6$ and $\text{Na}_{2.1}\text{In}_{0.1}\text{Zr}_{0.9}\text{Cl}_6$ with reflections of the trigonal phase of Na_2ZrCl_6 (space group $P\bar{3}m1$). The dominant additional side-phase reflection ($\sim 1.47 \text{\AA}^{-1}$) is marked with an asterisk (*).

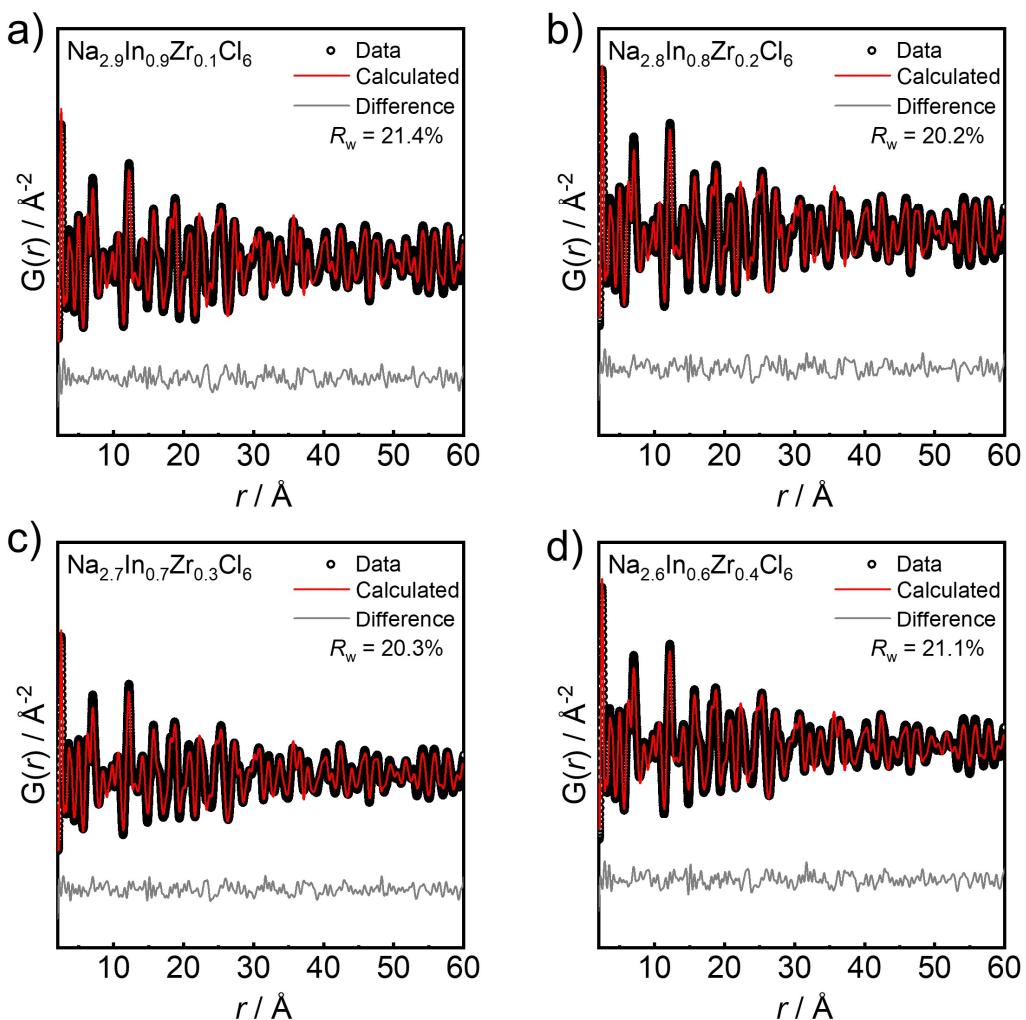


Fig. S3. Summary of pair distribution function fitting results of ball milled **a)** $\text{Na}_{2.9}\text{In}_{0.9}\text{Zr}_{0.1}\text{Cl}_6$, **b)** $\text{Na}_{2.8}\text{In}_{0.8}\text{Zr}_{0.2}\text{Cl}_6$, **c)** $\text{Na}_{2.7}\text{In}_{0.7}\text{Zr}_{0.3}\text{Cl}_6$, **d)** $\text{Na}_{2.6}\text{In}_{0.6}\text{Zr}_{0.4}\text{Cl}_6$.

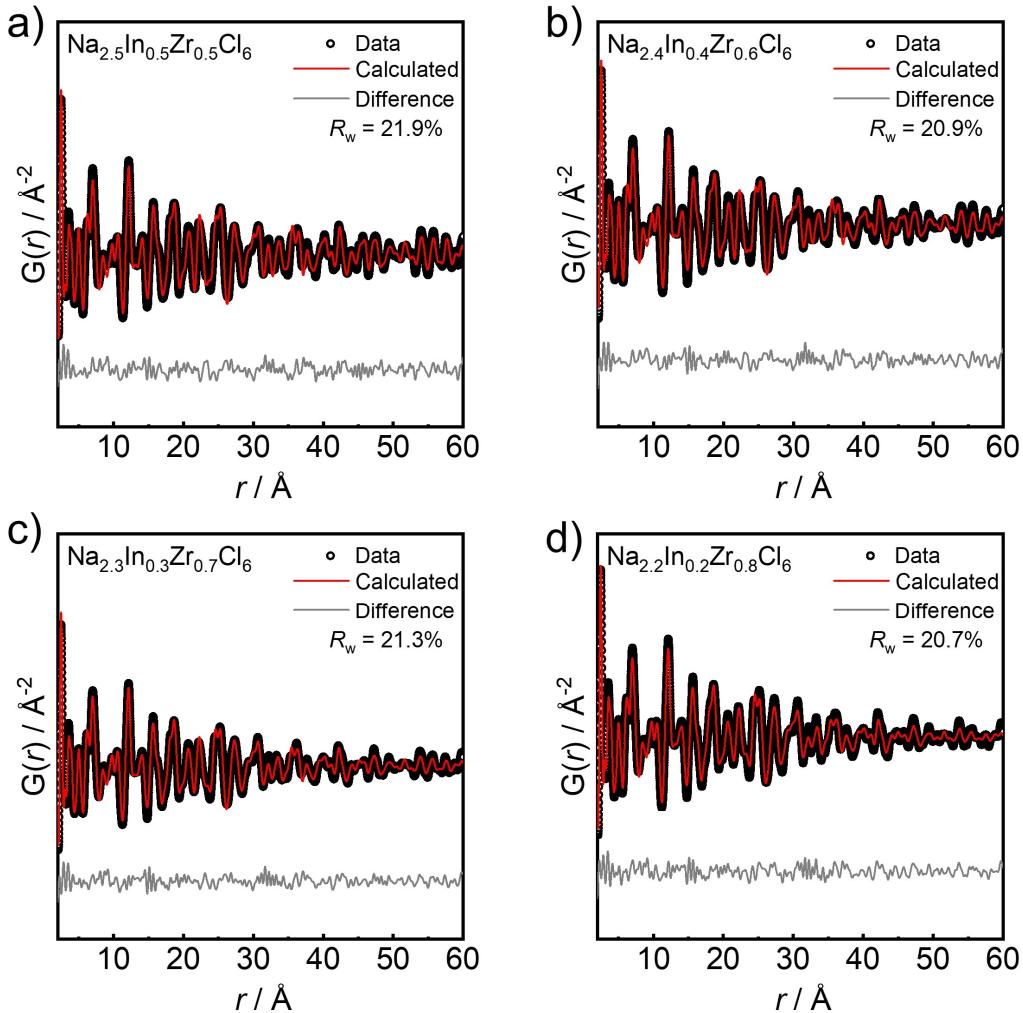


Fig. S4. Summary of pair distribution function fitting results of ball milled **a)** $\text{Na}_{2.5}\text{In}_{0.5}\text{Zr}_{0.5}\text{Cl}_6$, **b)** $\text{Na}_{2.4}\text{In}_{0.4}\text{Zr}_{0.6}\text{Cl}_6$, **c)** $\text{Na}_{2.3}\text{In}_{0.3}\text{Zr}_{0.7}\text{Cl}_6$, **d)** $\text{Na}_{2.2}\text{In}_{0.2}\text{Zr}_{0.8}\text{Cl}_6$.

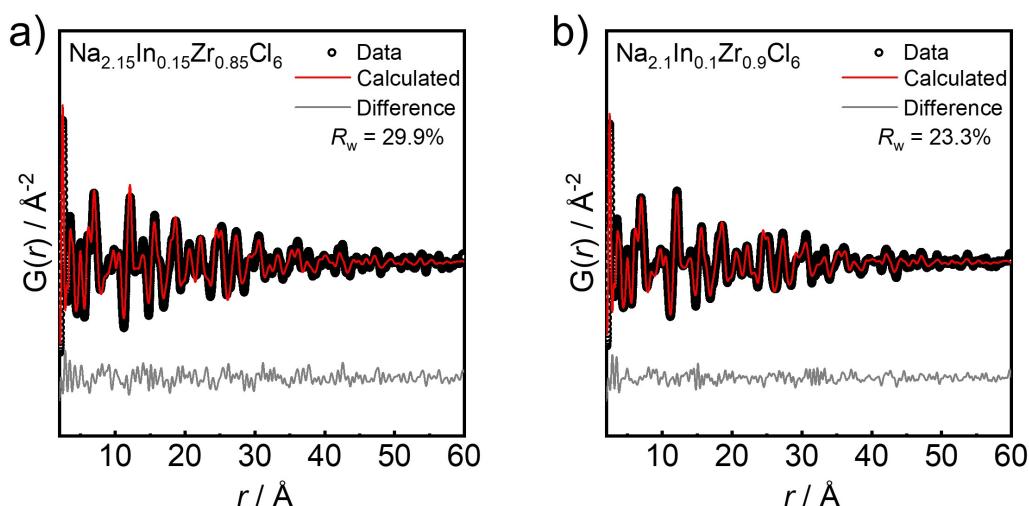


Fig. S5. Summary of pair distribution function fitting results of ball milled **a)** $\text{Na}_{2.15}\text{In}_{0.15}\text{Zr}_{0.85}\text{Cl}_6$,

b) $\text{Na}_{2.1}\text{In}_{0.1}\text{Zr}_{0.9}\text{Cl}_6$.

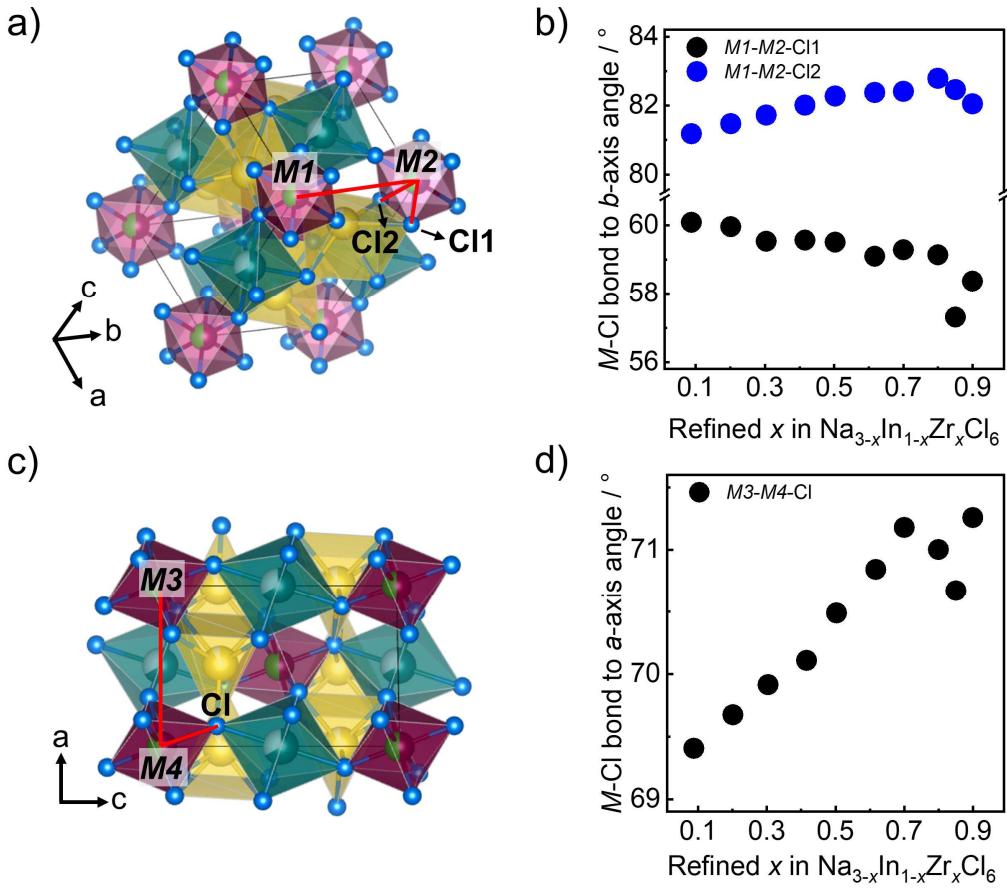


Fig. S6. **a)** Schematic of the angles between b axis (parallel to $M1\text{-}M2$ direction) and $M\text{-Cl}$ bond ($M, M1, M2 = \text{In; Zr}$). **b)** Angles between the b axis and $M\text{-Cl}$ bond as a function of refined Zr content. **c)** Schematic of the angles between a axis (parallel to $M3\text{-}M4$ direction) and $M\text{-Cl}$ bond ($M, M3, M4 = \text{In; Zr}$). **d)** Angles between a axis and $M\text{-Cl}$ bond as a function of refined Zr content.

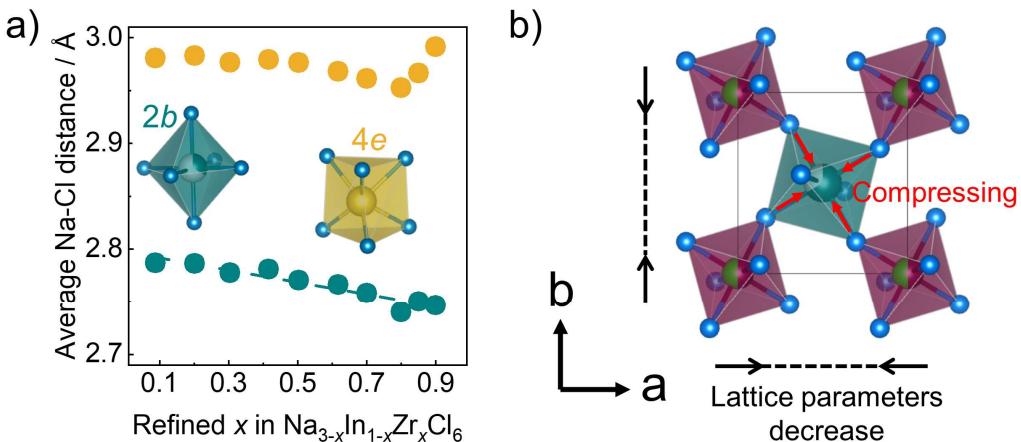


Fig. S7. **a)** Average Na-Cl distances of NaCl_6^{5-} octahedra (Na^+ at Wyckoff $2b$ site) and prism (Na^+ at Wyckoff $4e$ site). Dashed lines correspond to linear behavior as guides-to-the-eye. **b)** Schematics of NaCl_6^{5-} octahedra compressing upon decreased lattice parameters.

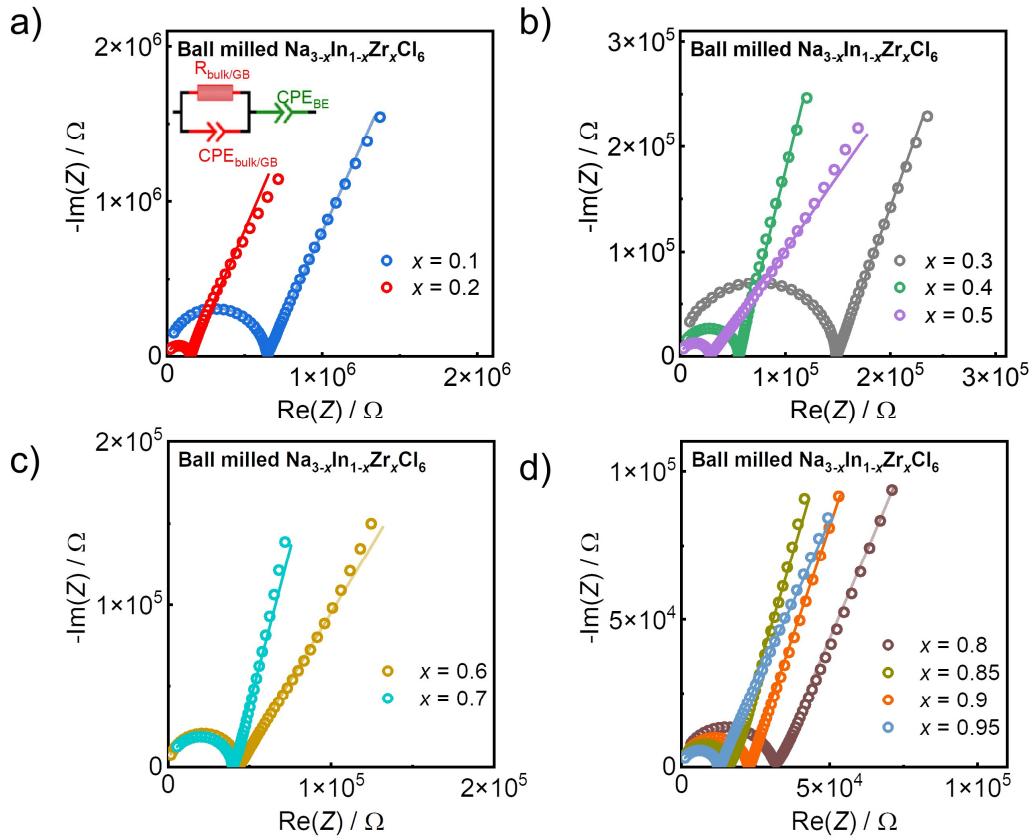


Fig. S8. **a)** Nyquist plots of ball milled $\text{Na}_{3-x}\text{In}_{1-x}\text{Zr}_x\text{Cl}_6$ ($x = 0.1; 0.2$). Inset: equivalent circuit model used for fitting the measured impedance spectra. **b)** Nyquist plots of ball milled $\text{Na}_{3-x}\text{In}_{1-x}\text{Zr}_x\text{Cl}_6$ ($x = 0.3; 0.4; 0.5$). **c)** Nyquist plots of ball milled $\text{Na}_{3-x}\text{In}_{1-x}\text{Zr}_x\text{Cl}_6$ ($x = 0.6; 0.7$). **d)** Nyquist plots of ball milled $\text{Na}_{3-x}\text{In}_{1-x}\text{Zr}_x\text{Cl}_6$ ($x = 0.8; 0.85; 0.9; 0.95$). These impedances were measured at room temperature (25 °C).

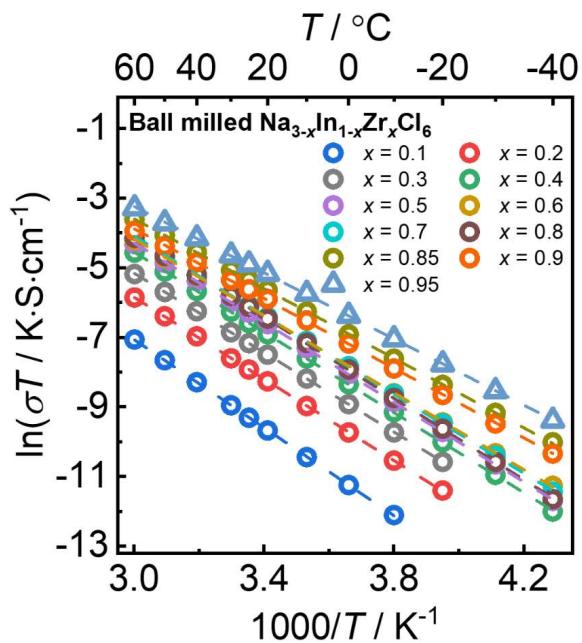


Fig. S9. Arrhenius plots from the temperature dependent impedance of ball milled $\text{Na}_{3-x}\text{In}_{1-x}\text{Zr}_x\text{Cl}_6$ series.

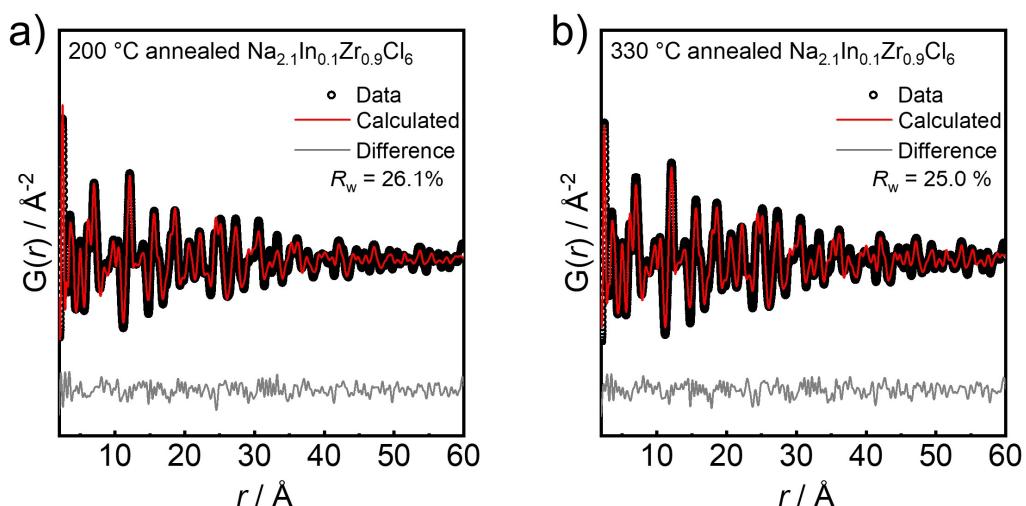


Fig. S10. Summary of pair distribution function fitting results of $\text{Na}_{2.1}\text{In}_{0.1}\text{Zr}_{0.9}\text{Cl}_6$ annealed at a) $200 \text{ } ^\circ\text{C}$ and b) $330 \text{ } ^\circ\text{C}$ for 1 hour.

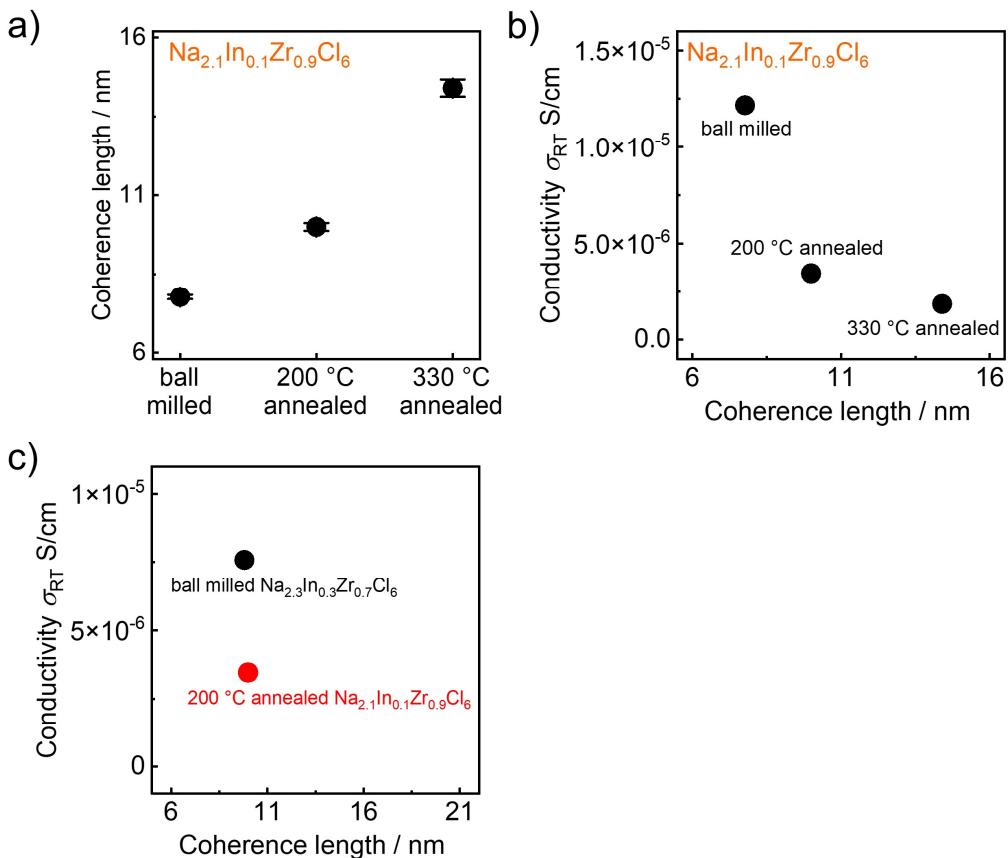


Fig. S11. **a)** Coherence lengths of ball milled, 200 °C annealed and 330 °C annealed $\text{Na}_{2.1}\text{In}_{0.1}\text{Zr}_{0.9}\text{Cl}_6$. The uncertainties, where shown, correspond to 1σ . **b)** Room-temperature ionic conductivities of $\text{Na}_{2.1}\text{In}_{0.1}\text{Zr}_{0.9}\text{Cl}_6$ synthesized by different procedures against coherence length. **c)** Room-temperature ionic conductivities of 200 °C annealed $\text{Na}_{2.1}\text{In}_{0.1}\text{Zr}_{0.9}\text{Cl}_6$ and ball milled $\text{Na}_{2.3}\text{In}_{0.3}\text{Zr}_{0.7}\text{Cl}_6$ against coherence length. The ionic conductivities of annealed $\text{Na}_{2.1}\text{In}_{0.1}\text{Zr}_{0.9}\text{Cl}_6$ were extracted from Ref. 31.

Table S1: Used constraints for pair distribution function fitting of ball milled $\text{Na}_{3-x}\text{In}_{1-x}\text{Zr}_x\text{Cl}_6$.

$\text{Na}_{3-x}\text{In}_{1-x}\text{Zr}_x\text{Cl}_6$
Lattice Parameter: $\alpha = \gamma = 90^\circ$
Space group: $P2_1/n$

Atom	Wyckoff Position	Atomic coordinates			<i>Occ.</i>	$U_{iso} / \text{\AA}^2$
		x	y	z		
Na1	4e	Pos1	Pos2	Pos3	$(3-x-\text{Occ}_{\text{Na}})/2$	Th1
Na2	2b	0	0	0.5	Occ_{Na}	Th1
Zr1	2a	0	0	0	x	Th2
In1	2a	0	0	0	$1-x$	Th2
Cl1	4e	Pos4	Pos5	Pos6	1	Th3
Cl2	4e	Pos7	Pos8	Pos9	1	Th3
Cl3	4e	Pos10	Pos11	Pos12	1	Th3

Table S2: Pair distribution function fitting result of ball milled $\text{Na}_{2.9}\text{In}_{0.9}\text{Zr}_{0.1}\text{Cl}_6$. Fitting range: 2 - 60 Å.

$\text{Na}_{2.9}\text{In}_{0.9}\text{Zr}_{0.1}\text{Cl}_6$
Lattice Parameter: $a = 6.7631(5)$ Å, $b = 7.1722(7)$ Å, $c = 9.9708(10)$ Å, $\beta = 90.537(13)^\circ$
Space group: $P2_1/n$

Atom	Wyckoff	Atomic coordinates	<i>Occ.</i>	$U_{iso} / \text{\AA}^2$
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Position	<i>x</i>	<i>y</i>	<i>z</i>		
Na1	4e	0.506(2)	-0.0752(7)	0.2474(11)	0.967(11)
Na2	2b	0	0	0.5	0.98(3)
Zr1	2a	0	0	0	0.09(2)
In1	2a	0	0	0	0.91(2)
Cl1	4e	0.1610(8)	0.3082(6)	-0.0765(6)	1
Cl2	4e	0.1339(6)	0.0537(6)	0.2327(6)	1
Cl3	4e	-0.3071(6)	0.1724(7)	0.0536(5)	1

Table S3: Pair distribution function fitting result of ball milled $\text{Na}_{2.8}\text{In}_{0.8}\text{Zr}_{0.2}\text{Cl}_6$. Fitting range: 2 - 60 Å.

Na_{2.8}In_{0.8}Zr_{0.2}Cl₆

Lattice Parameter: $a = 6.7598(5)$ Å, $b = 7.1698(7)$ Å, $c = 9.9693(10)$ Å, $\beta = 90.631(13)^\circ$

Space group: $P2_1/n$

Atom	Wyckoff Position	Atomic coordinates			<i>Occ.</i>	$U_{\text{iso}} / \text{\AA}^2$
		<i>x</i>	<i>y</i>	<i>z</i>		
Na1	4e	0.507(2)	-0.0767(7)	0.2480(11)	0.947(10)	0.067(2)
Na2	2b	0	0	0.5	0.90(3)	0.067(2)
Zr1	2a	0	0	0	0.20(2)	0.0201(4)
In1	2a	0	0	0	0.80(2)	0.0201(4)
Cl1	4e	0.1607(8)	0.3072(6)	-0.0770(6)	1	0.0457(7)
Cl2	4e	0.1324(6)	0.0517(6)	0.2324(6)	1	0.0457(7)
Cl3	4e	-0.3064(7)	0.1727(7)	0.0523(5)	1	0.0457(7)

Table S4: Pair distribution function fitting result of ball milled $\text{Na}_{2.7}\text{In}_{0.7}\text{Zr}_{0.3}\text{Cl}_6$. Fitting range: 2 - 60 Å.

Na_{2.7}In_{0.7}Zr_{0.3}Cl₆

Lattice Parameter: $a = 6.7563(6)$ Å, $b = 7.1656(8)$ Å, $c = 9.9670(11)$ Å, $\beta = 90.750(14)^\circ$

Space group: $P2_1/n$

Atom	Wyckoff Position	Atomic coordinates			<i>Occ.</i>	$U_{\text{iso}} / \text{\AA}^2$
		<i>x</i>	<i>y</i>	<i>z</i>		
Na1	4e	0.507(2)	-0.0783(8)	0.2487(11)	0.960(11)	0.079(3)
Na2	2b	0	0	0.5	0.78(3)	0.079(3)
Zr1	2a	0	0	0	0.30(2)	0.0226(3)
In1	2a	0	0	0	0.70(2)	0.0226(3)
Cl1	4e	0.1612(8)	0.3092(6)	-0.0781(6)	1	0.0472(4)
Cl2	4e	0.1328(7)	0.0507(6)	0.2350(5)	1	0.0472(4)
Cl3	4e	-0.3023(3)	0.1736(4)	0.0523(4)	1	0.0472(4)

Table S5: Pair distribution function fitting result of ball milled $\text{Na}_{2.6}\text{In}_{0.6}\text{Zr}_{0.4}\text{Cl}_6$. Fitting range: 2 - 60 Å.

Na_{2.6}In_{0.6}Zr_{0.4}Cl₆

Lattice Parameter: $a = 6.7529(7)$ Å, $b = 7.1611(9)$ Å, $c = 9.9609(13)$ Å, $\beta = 90.88(2)^\circ$

Space group: $P2_1/n$

Atom	Wyckoff Position	Atomic coordinates			<i>Occ.</i>	$U_{\text{iso}} / \text{\AA}^2$
		<i>x</i>	<i>y</i>	<i>z</i>		
Na1	4e	0.508(2)	-0.0774(8)	0.2437(13)	0.927(11)	0.083(3)
Na2	2b	0	0	0.5	0.73(3)	0.083(3)
Zr1	2a	0	0	0	0.42(2)	0.0254(6)
In1	2a	0	0	0	0.58(2)	0.0254(6)
Cl1	4e	0.1619(9)	0.3064(6)	-0.0797(6)	1	0.0517(8)
Cl2	4e	0.1306(7)	0.0483(7)	0.2323(6)	1	0.0517(8)
Cl3	4e	-0.3044(7)	0.1743(4)	0.0510(5)	1	0.0517(8)

Table S6: Pair distribution function fitting result of ball milled $\text{Na}_{2.5}\text{In}_{0.5}\text{Zr}_{0.5}\text{Cl}_6$. Fitting range: 2 - 60 Å.

Na_{2.5}In_{0.5}Zr_{0.5}Cl₆

Lattice Parameter: $a = 6.7463(7)$ Å, $b = 7.1544(11)$ Å, $c = 9.952(2)$ Å, $\beta = 91.05(2)^\circ$
Space group: $P2_1/n$

Atom	Wyckoff Position	Atomic coordinates			Occ.	$U_{\text{iso}} / \text{\AA}^2$
		x	y	z		
Na1	4e	0.511(2)	-0.0792(8)	0.2516(13)	0.924(11)	0.091(4)
Na2	2b	0	0	0.5	0.65(3)	0.091(4)
Zr1	2a	0	0	0	0.50(2)	0.0287(6)
In1	2a	0	0	0	0.50(2)	0.0287(6)
Cl1	4e	0.1649(9)	0.3080(7)	-0.0793(7)	1	0.0572(9)
Cl2	4e	0.1287(8)	0.0464(7)	0.2319(6)	1	0.0572(9)
Cl3	4e	-0.3035(7)	0.1741(8)	0.0500(5)	1	0.0572(9)

Table S7: Pair distribution function fitting result of ball milled $\text{Na}_{2.4}\text{In}_{0.4}\text{Zr}_{0.6}\text{Cl}_6$. Fitting range: 2 - 60 Å.

Na_{2.4}In_{0.4}Zr_{0.6}Cl₆

Lattice Parameter: $a = 6.7395(8)$ Å, $b = 7.1475(11)$ Å, $c = 9.937(2)$ Å, $\beta = 91.24(2)^\circ$
Space group: $P2_1/n$

Atom	Wyckoff Position	Atomic coordinates			Occ.	$U_{\text{iso}} / \text{\AA}^2$
		x	y	z		
Na1	4e	0.515(2)	-0.0797(9)	0.2439(12)	0.932(11)	0.092(4)
Na2	2b	0	0	0.5	0.52(3)	0.092(4)
Zr1	2a	0	0	0	0.62(2)	0.0287(6)
In1	2a	0	0	0	0.38(2)	0.0287(6)
Cl1	4e	0.1648(8)	0.3043(6)	-0.0799(6)	1	0.0573(9)
Cl2	4e	0.1279(8)	0.0459(7)	0.2329(6)	1	0.0573(9)
Cl3	4e	-0.3018(7)	0.1765(8)	0.0514(5)	1	0.0573(9)

Table S8: Pair distribution function fitting result of ball milled $\text{Na}_{2.3}\text{In}_{0.3}\text{Zr}_{0.7}\text{Cl}_6$. Fitting range: 2 - 60 Å.

Na_{2.3}In_{0.3}Zr_{0.7}Cl₆

Lattice Parameter: $a = 6.7308(9)$ Å, $b = 7.1387(11)$ Å, $c = 9.918(2)$ Å, $\beta = 91.51(2)^\circ$
Space group: $P2_1/n$

Atom	Wyckoff Position	Atomic coordinates			Occ.	$U_{\text{iso}} / \text{\AA}^2$
		x	y	z		
Na1	4e	0.517(2)	-0.0813(9)	0.2461(12)	0.932(11)	0.094(4)
Na2	2b	0	0	0.5	0.44(3)	0.094(4)
Zr1	2a	0	0	0	0.70(2)	0.02862(13)
In1	2a	0	0	0	0.30(2)	0.02862(13)
Cl1	4e	0.1671(9)	0.3023(7)	-0.0784(6)	1	0.05863(14)
Cl2	4e	0.1286(9)	0.0461(7)	0.2357(4)	1	0.05863(14)
Cl3	4e	-0.2996(3)	0.1742(4)	0.0517(4)	1	0.05863(14)

Table S9: Pair distribution function fitting result of ball milled $\text{Na}_{2.2}\text{In}_{0.2}\text{Zr}_{0.8}\text{Cl}_6$. Fitting range: 2 - 60 Å.

Na_{2.2}In_{0.2}Zr_{0.8}Cl₆

Lattice Parameter: $a = 6.7182(10)$ Å, $b = 7.1300(12)$ Å, $c = 9.894(2)$ Å, $\beta = 91.781(15)^\circ$
Space group: $P2_1/n$

Atom	Wyckoff Position	Atomic coordinates			Occ.	$U_{\text{iso}} / \text{\AA}^2$
		x	y	z		
Na1	4e	0.520(2)	-0.0863(9)	0.2487(12)	0.978(13)	0.099(4)
Na2	2b	0	0	0.5	0.24(3)	0.099(4)
Zr1	2a	0	0	0	0.80(2)	0.0282(3)
In1	2a	0	0	0	0.20(2)	0.0282(3)
Cl1	4e	0.1733(9)	0.3012(7)	-0.0759(7)	1	0.0587(3)
Cl2	4e	0.1319(10)	0.0440(7)	0.2367(5)	1	0.0587(3)
Cl3	4e	-0.2985(1)	0.1749(3)	0.0522(4)	1	0.0587(3)

Table S10: Pair distribution function fitting result of ball milled $\text{Na}_{2.15}\text{In}_{0.15}\text{Zr}_{0.85}\text{Cl}_6$. Fitting

range: 2 - 60 Å.

Na_{2.15}In_{0.15}Zr_{0.85}Cl₆

Lattice Parameter: $a = 6.710(2)$ Å, $b = 7.121(2)$ Å, $c = 9.883(3)$ Å, $\beta = 91.91(2)^\circ$

Space group: $P2_1/n$

Atom	Wyckoff Position	Atomic coordinates			Occ.	$U_{\text{iso}} / \text{\AA}^2$
		x	y	z		
Na1	4e	0.513(3)	-0.0814(13)	0.247(2)	0.95(2)	0.100(6)
Na2	2b	0	0	0.5	0.25(2)	0.100(6)
Zr1	2a	0	0	0	0.85(3)	0.0288(7)
In1	2a	0	0	0	0.15(3)	0.0288(7)
Cl1	4e	0.1576(12)	0.2993(10)	-0.0797(10)	1	0.0599(9)
Cl2	4e	0.1306(10)	0.0446(10)	0.2290(3)	1	0.0599(9)
Cl3	4e	-0.3061(9)	0.1918(12)	0.0497(8)	1	0.0599(9)

Table S11: Pair distribution function fitting result of ball milled Na_{2.1}In_{0.1}Zr_{0.9}Cl₆. Fitting range: 2 - 60 Å.

Na_{2.1}In_{0.1}Zr_{0.9}Cl₆

Lattice Parameter: $a = 6.7067(14)$ Å, $b = 7.116(2)$ Å, $c = 9.873(2)$ Å, $\beta = 92.05(2)^\circ$

Space group: $P2_1/n$

Atom	Wyckoff Position	Atomic coordinates			Occ.	$U_{\text{iso}} / \text{\AA}^2$
		x	y	z		
Na1	4e	0.498(2)	-0.0690(13)	0.2142(13)	0.96(2)	0.100(5)
Na2	2b	0	0	0.5	0.18(4)	0.100(5)
Zr1	2a	0	0	0	0.90(3)	0.0300(10)
In1	2a	0	0	0	0.10(3)	0.0300(10)
Cl1	4e	0.1664(10)	0.2967(8)	-0.0761(8)	1	0.0636(11)
Cl2	4e	0.1290(9)	0.0474(9)	0.2315(4)	1	0.0636(11)
Cl3	4e	-0.3030(8)	0.1834(11)	0.0539(6)	1	0.0636(11)

Table S12: Pair distribution function fitting result of ball milled Na_{2.5}In_{0.5}Zr_{0.5}Cl₆. Fitting range: 2 - 20 Å.

Na_{2.5}In_{0.5}Zr_{0.5}Cl₆

Lattice Parameter: $a = 6.746(3)$ Å, $b = 7.150(3)$ Å, $c = 9.952(6)$ Å, $\beta = 91.17(7)^\circ$

Space group: $P2_1/n$

Atom	Wyckoff Position	Atomic coordinates			Occ.	$U_{\text{iso}} / \text{\AA}^2$
		x	y	z		
Na1	4e	0.515(2)	-0.0817(10)	0.259(2)	1.00(2)	0.075(5)
Na2	2b	0	0	0.5	0.48(5)	0.075(5)
Zr1	2a	0	0	0	0.52(3)	0.027(2)
In1	2a	0	0	0	0.48(3)	0.027(2)
Cl1	4e	0.1642(14)	0.3157(12)	-0.0845(11)	1	0.055(2)
Cl2	4e	0.126(2)	0.0429(13)	0.2333(7)	1	0.055(2)
Cl3	4e	-0.3019(4)	0.177(2)	0.052(2)	1	0.055(2)

Table S13: Pair distribution function fitting result of ball milled Na_{2.5}In_{0.5}Zr_{0.5}Cl₆. Fitting range: 2 - 40 Å.

Na_{2.5}In_{0.5}Zr_{0.5}Cl₆

Lattice Parameter: $a = 6.7472(11)$ Å, $b = 7.156(2)$ Å, $c = 9.952(2)$ Å, $\beta = 91.18(2)^\circ$

Space group: $P2_1/n$

Atom	Wyckoff Position	Atomic coordinates			Occ.	$U_{\text{iso}} / \text{\AA}^2$
		x	y	z		
Na1	4e	0.514(2)	-0.0840(9)	0.2584(12)	0.946(13)	0.074(4)
Na2	2b	0	0	0.5	0.58(4)	0.074(4)
Zr1	2a	0	0	0	0.52(3)	0.0262(6)
In1	2a	0	0	0	0.48(3)	0.0262(6)
Cl1	4e	0.1678(10)	0.3107(8)	-0.0838(8)	1	0.0543(9)
Cl2	4e	0.1287(9)	0.0417(8)	0.2321(6)	1	0.0543(9)
Cl3	4e	-0.3039(6)	0.1745(9)	0.0500(6)	1	0.0543(9)

Table S14. Fitted parameters of room-temperature impedance spectra of ball milled $\text{Na}_{3-x}\text{In}_{1-x}\text{Zr}_x\text{Cl}_6$, where x represents nominal Zr content; $R_{\text{bulk}/\text{GB}}$ and $\text{CPE}_{\text{bulk}/\text{GB}}$ represent the resistance and CPE capacitance of $\text{Na}_{3-x}\text{In}_{1-x}\text{Zr}_x\text{Cl}_6$ pellets respectively; $\alpha_{\text{bulk}/\text{GB}}$ is the ideal indicator of $\text{CPE}_{\text{bulk}/\text{GB}}$; CPE_{BE} represent the CPE capacitance of blocking electrode; α_{BE} is the ideal indicator of CPE_{BE} .

x in $\text{Na}_{3-x}\text{In}_{1-x}\text{Zr}_x\text{Cl}_6$	$R_{\text{bulk}/\text{GB}}$	$\text{CPE}_{\text{bulk}/\text{GB}}$	$\alpha_{\text{bulk}/\text{GB}}$	CPE_{BE}	α_{BE}
0.1	6.37×10^5	7.56×10^{-11}	0.98	7.37×10^{-7}	0.73
0.2	1.46×10^5	4.33×10^{-11}	0.97	4.43×10^{-7}	0.74
0.3	1.48×10^5	3.75×10^{-11}	0.97	5.90×10^{-6}	0.78
0.4	5.56×10^4	5.00×10^{-11}	0.98	2.07×10^{-6}	0.84
0.5	2.81×10^4	8.04×10^{-11}	0.94	2.42×10^{-6}	0.61
0.6	4.32×10^4	5.79×10^{-11}	0.97	2.59×10^{-6}	0.66
0.7	3.97×10^4	4.06×10^{-11}	0.96	2.52×10^{-6}	0.84
0.8	3.18×10^4	2.17×10^{-10}	0.88	1.38×10^{-6}	0.75
0.85	1.61×10^4	1.11×10^{-10}	0.97	5.51×10^{-6}	0.82
0.9	2.27×10^4	9.56×10^{-11}	0.91	2.10×10^{-6}	0.79
0.95	1.25×10^4	8.88×10^{-11}	0.93	4.73×10^{-6}	0.73

Table S15: Pair distribution function fitting result of 200 °C annealed $\text{Na}_{2.1}\text{In}_{0.1}\text{Zr}_{0.9}\text{Cl}_6$. Fitting range: 2 - 60 Å.

$\text{Na}_{2.1}\text{In}_{0.1}\text{Zr}_{0.9}\text{Cl}_6$

Lattice Parameter: $a = 6.7117(11)$ Å, $b = 7.1204(12)$ Å, $c = 9.880(2)$ Å, $\beta = 91.907(14)^\circ$

Space group: $P2_1/n$

Atom	Wyckoff Position	Atomic coordinates			Occ.	$U_{\text{iso}} / \text{\AA}^2$
		x	y	z		
Na1	4e	0.505(2)	-0.0757(12)	0.2256(15)	0.949(15)	0.100(5)
Na2	2b	0	0	0.5	0.19(4)	0.100(5)
Zr1	2a	0	0	0	0.91(3)	0.0216(8)
In1	2a	0	0	0	0.09(3)	0.0216(8)
Cl1	4e	0.1693(10)	0.2984(8)	-0.0782(8)	1	0.0216(8)
Cl2	4e	0.1285(9)	0.0470(9)	0.2315(4)	1	0.0566(10)
Cl3	4e	-0.3044(8)	0.1858(10)	0.0525(6)	1	0.0566(10)

Table S16: Pair distribution function fitting result of 330 °C annealed $\text{Na}_{2.1}\text{In}_{0.1}\text{Zr}_{0.9}\text{Cl}_6$. Fitting range: 2 - 60 Å.

$\text{Na}_{2.1}\text{In}_{0.1}\text{Zr}_{0.9}\text{Cl}_6$

Lattice Parameter: $a = 6.7058(9)$ Å, $b = 7.1113(9)$ Å, $c = 9.8744(12)$ Å, $\beta = 91.908(10)^\circ$

Space group: $P2_1/n$

Atom	Wyckoff Position	Atomic coordinates			Occ.	$U_{\text{iso}} / \text{\AA}^2$
		x	y	z		
Na1	4e	0.511(2)	-0.0853(10)	0.2451(13)	0.955(14)	0.090(4)
Na2	2b	0	0	0.5	0.20(4)	0.090(4)
Zr1	2a	0	0	0	0.89(3)	0.0205(7)
In1	2a	0	0	0	0.11(3)	0.0205(7)
Cl1	4e	0.1692(8)	0.2990(6)	-0.0722(6)	1	0.0452(8)
Cl2	4e	0.1266(8)	0.0424(7)	0.2289(3)	1	0.0452(8)
Cl3	4e	-0.3098(7)	0.1821(8)	0.0532(5)	1	0.0452(8)

The uncertainties shown in the tables correspond to 1σ .