

Supporting Information

Superconducting Be₂SH₃ with hydrogen kagome lattice at high pressure

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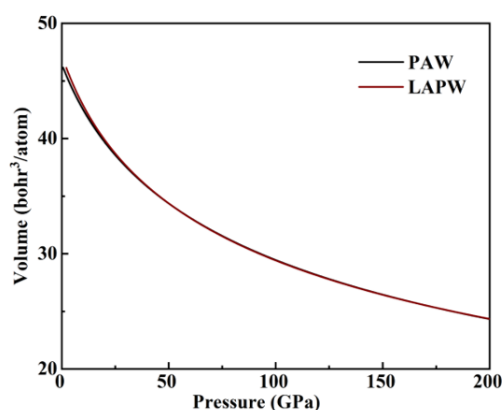


Fig. S00 Comparison of the fitted Birch-Murnaghan equation of states for *P6/mmm* Be₂SH₃ using calculated results with the PAW pseudopotentials and full-potential LAPW methods.

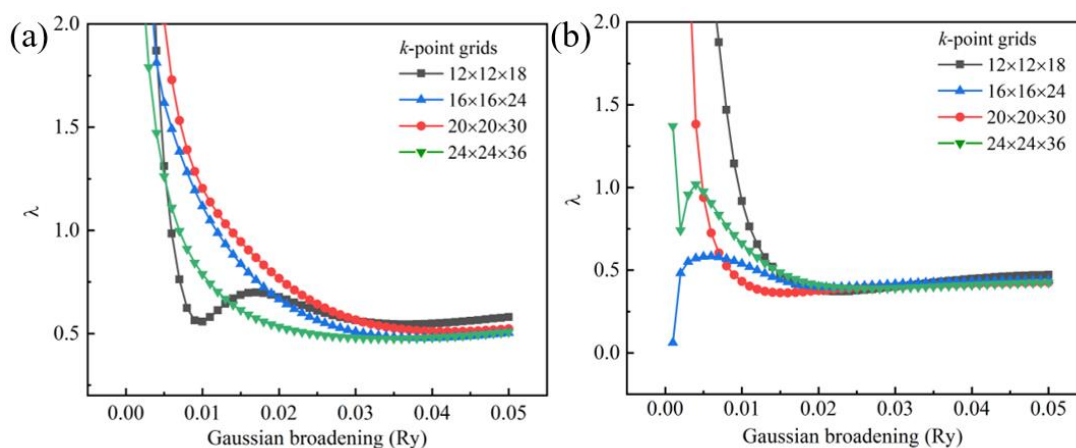


Fig. S01 Electron-phonon coupling constant, λ , versus Gaussian broadening, σ , for *P6/mmm* Be₂SH₃ at 200 GPa at $q = (0, 0, 0)$ (a) and $q = (0, 0, 0.554628)$ (b) using various k -grids. In (a) and (b) the k -meshes $16 \times 16 \times 24$ are considered to be converged for acquiring an accurate λ .

Table. S1. Superconducting parameters for $P6/mmm$ Be_2SH_3 at 200 GPa: electron-phonon coupling parameter (λ), logarithmic average of phonon frequencies (ω_{\log}) and estimated superconducting critical temperature (T_c) for values of the Coulomb pseudopotential, using the listed q-grids.

q -meshes	λ	ω_{\log} (K)	T_c (K)
$4 \times 4 \times 6$	0.53	1161.28	18
$6 \times 6 \times 9$	0.58	1029.08	22

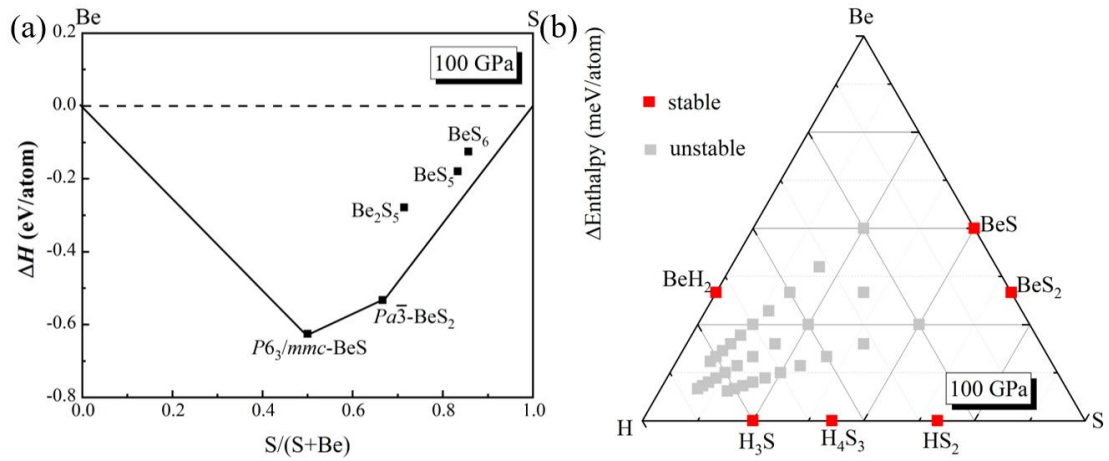


Fig. S1 (a) Convex hull of Be-S system and (b) Phase diagram of Be-S-H system at 100 GPa.

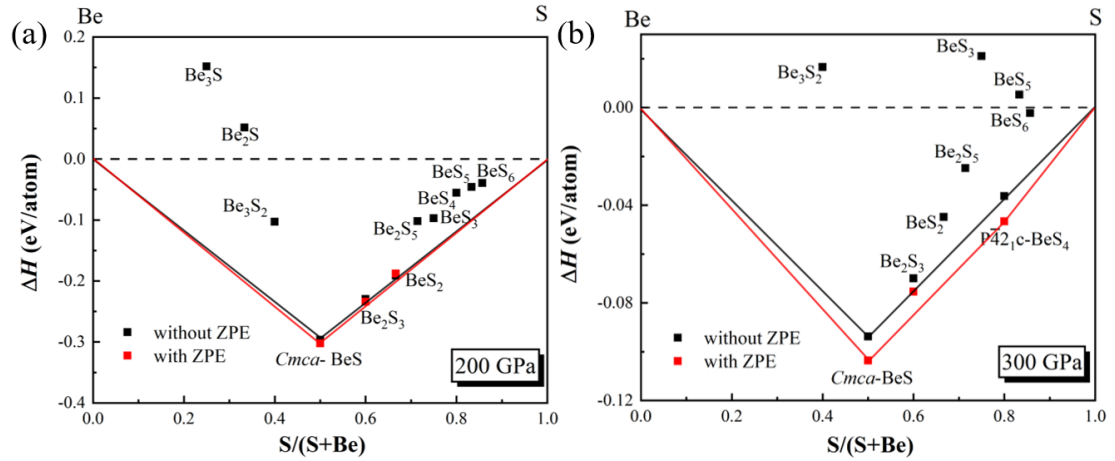


Fig. S2 Phase diagram of Be-S system at (a) 200 GPa, (b) 300 GPa. Convex hulls are shown as continuous lines, with (red) and without (black) the inclusion of zero-point vibrational enthalpy (ZPE).

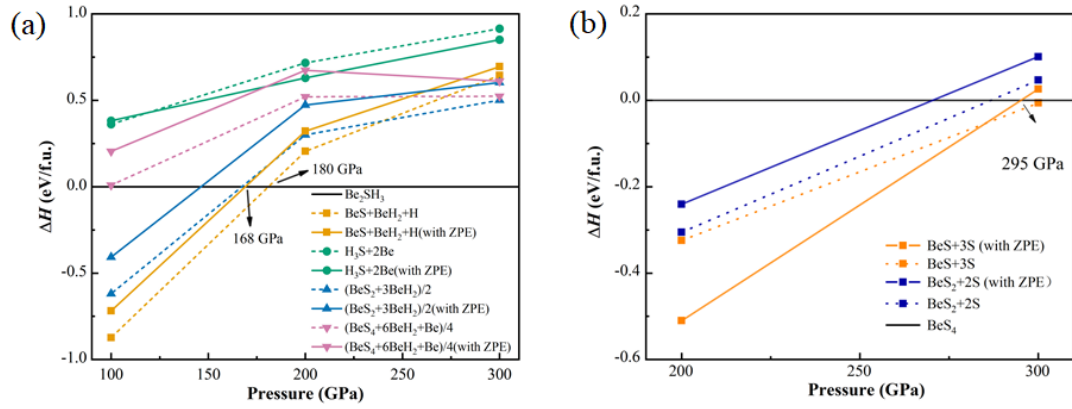


Fig. S3 The calculated formation enthalpy of (a) $P6/mmm$ Be_2SH_3 and (b) $P\bar{4}2_1c$ BeS_4 and crystal as a function of pressure relative to the competing element and binary compounds.

Table. S2. Charge transfer of Be, S and H atoms in one unit cell. The negative and positive signs indicate electron gain and loss, respectively.

Phases	Pressure (GPa)	Atoms	Charge (e)
$P\bar{4}2_1c$ BeS_4	180	Be (2a)	-1.63
		S (8e)	0.41
$P\bar{4}2_1c$ BeS_4	300	Be (2a)	-1.62
		S (8e)	0.41
$P6/mmm$ Be_2SH_3	100	Be (2d)	-1.65
		S (1b)	0.97
		H (3f)	0.78
$P6/mmm$ Be_2SH_3	200	Be (2d)	-1.65
		S (1b)	1.11
		H (3f)	0.73
$P6/mmm$ Be_2SH_3	300	Be (2d)	-1.64
		S (1b)	1.17
		H (3f)	0.70

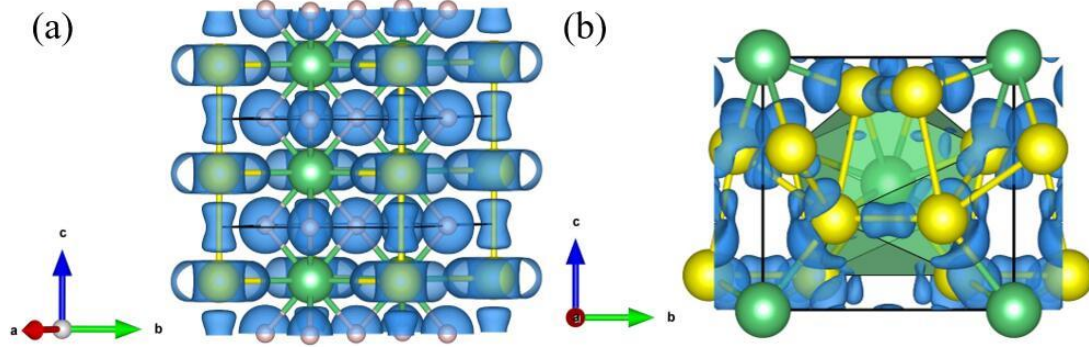


Fig. S4 The ELF of (a) $P6/mmm$ Be_2SH_3 at 200 GPa and (b) $P42_1c$ BeS_4 at 300 GPa, the ELF isosurfaces with a value of 0.75.

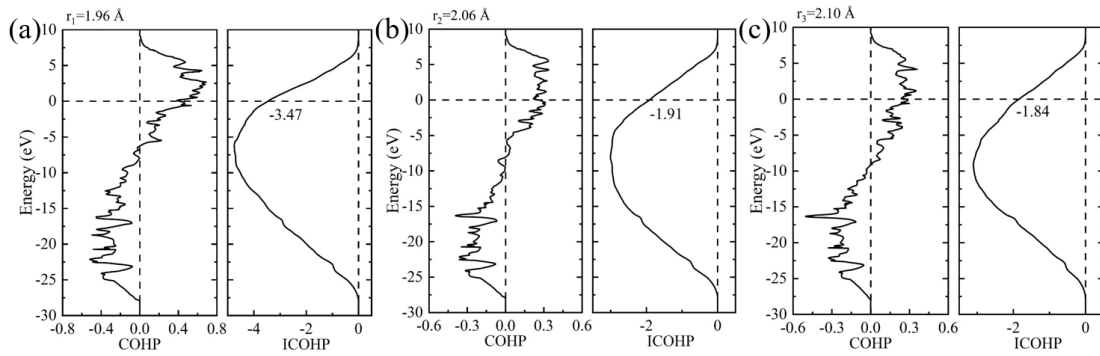


Fig. S5 The calculated Crystalline Orbital Hamiltonian Population (COHP) and Integrated Crystalline Orbital Hamiltonian Population (ICOHP) of BeS_4 with S-S distances of (a) 1.96, (b) 2.06 and (c) 2.10 Å at 300 GPa. The horizontal lines present the Fermi levels. The negative COHP indicates bonding and positive COHP indicates antibonding and the negative ICOHP values represent the bonding interactions between the S atoms.

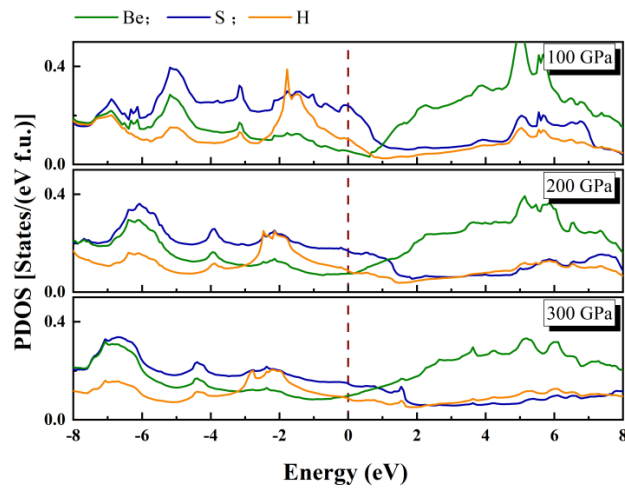


Fig. S6 Atom-projected density of states near the Fermi level for $P6/mmm$ Be_2SH_3 at 100 GPa, 200 GPa and 300 GPa.

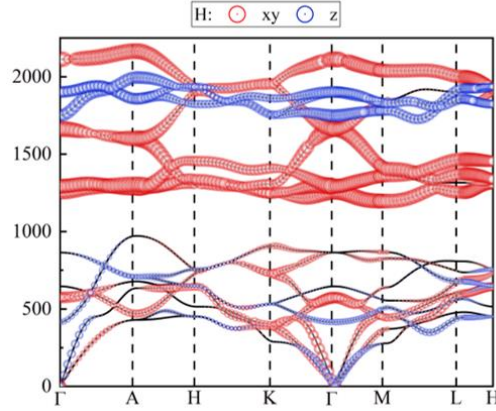


Fig. S7. Calculated phonon spectra for $P6/mmm$ Be_2SH_3 at 200 GPa highlighting the primary nature of the different modes. xy shown as red are in-plane vibrations and z shown as blue are out-of-plane vibrations.

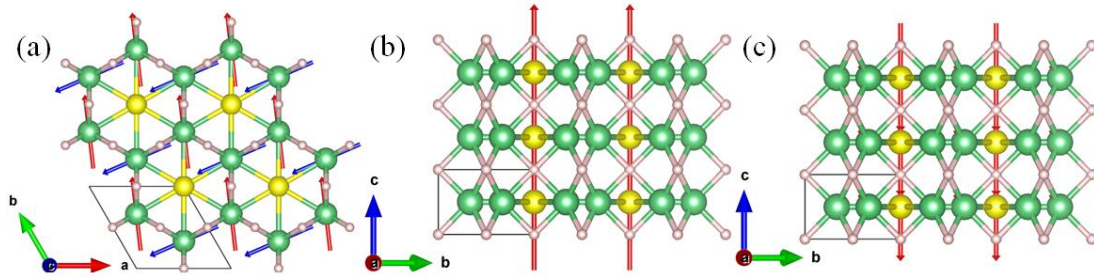


Fig. S8 The vibrational modes at (a) Γ -A (b) H-K and (c) M-L of $P6/mmm$ Be_2SH_3 at 100 GPa. The arrows represent the direction of atomic vibration.

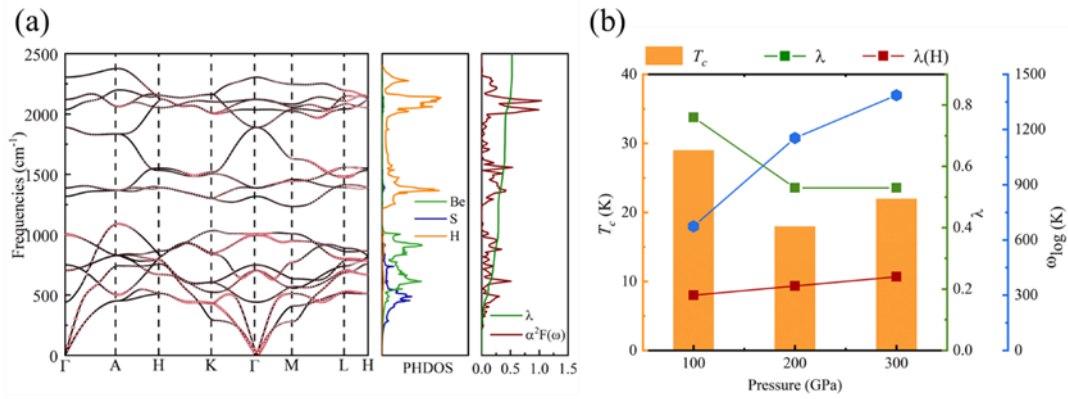


Fig. S9 (a) Phonon-dispersion curves, PHDOS, projected on the Be, S, and H atoms, Eliashberg spectral function, $\alpha^2F(\omega)$ and λ for $P6/mmm$ Be_2SH_3 at 300 GPa. (b) Pressure dependence of T_c , the logarithmic average phonon frequency ω_{\log} , the total EPC parameter λ and the contribution of H atoms to the total λ , namely $\lambda(\text{H})$, for $P6/mmm$ Be_2SH_3 .

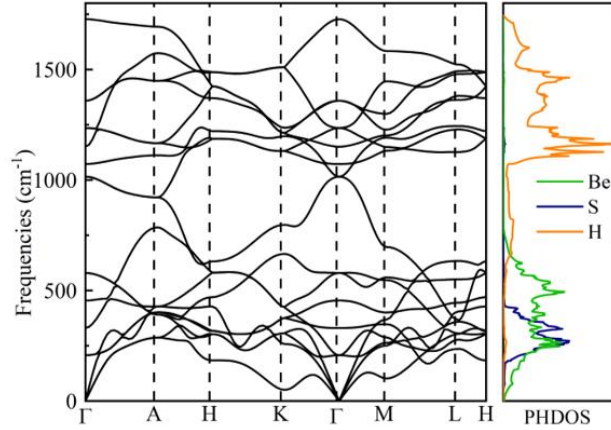


Fig. S10 Phonon dispersion curves of $P6/mmm$ Be_2SH_3 at the pressure of 60 GPa, PHDOS, projected on the Be, S, and H atoms.

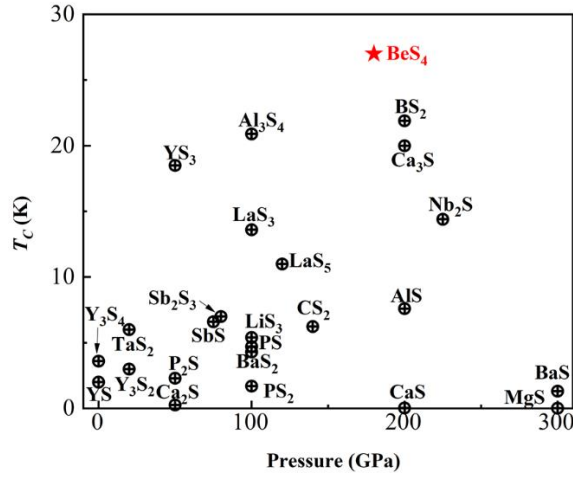


Fig. S11 T_c values of the reported binary chalcogenides at high pressure.

Table S3. The structure information of $P6/mmm$ Be_2SH_3 at 200 GPa and $\bar{P}42_1c$ BeS_4 at 300 GPa.

Space group	Lattice parameters	Atomic coordinates			Sites	
Pressure	(Å)					
$P6/mmm$ Be_2SH_3	a=3.48	Be	0.33333	0.66667	0.50000	2d
200 GPa	c=2.06	S	0.00000	-0.00000	0.50000	1b
		H	0.50000	-0.00000	0.00000	3f
$\bar{P}42_1c$ BeS_4	a=4.21	Be	0.00000	0.00000	0.00000	2a
300 GPa	c=4.37	S	0.88184	0.70802	0.37436	8e