

Supplemental Materials for “Strain-engineering induced topological phase transitions and multiple valley states in Janus monolayer VCSiN₄”

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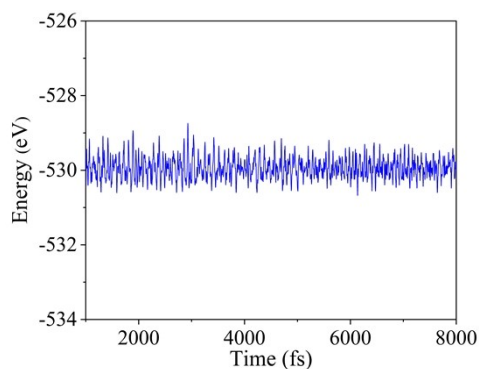


Fig. S1 The AIMD simulation of VCSiN₄ at 300 K.

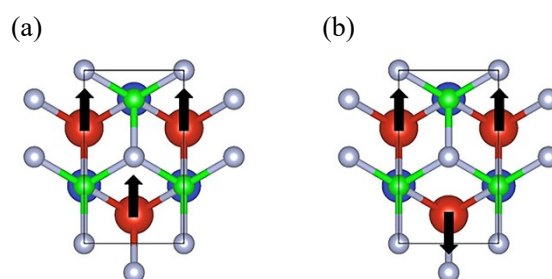


Fig. S2 The considered magnetic configurations: panel (a) is for the FM configuration, and panel (b) is for the AFM configuration.

Table S1 The equilibrium lattice constants (a), space group, crystal symmetry, magnetic ground state, and formation energy of monolayers VC₂N₄, VCSiN₄, and VSi₂N₄.

	VC ₂ N ₄	VCSiN ₄	VSi ₂ N ₄
a (Å)	2.57	2.77	2.89
space group	$P6m2$	$P3m1$	$P6m2$
crystal symmetry	D_{3h}	C_{3v}	D_{3h}
magnetic ground state	FM	FM	FM
formation energy (eV)	2.63	3.10	3.81

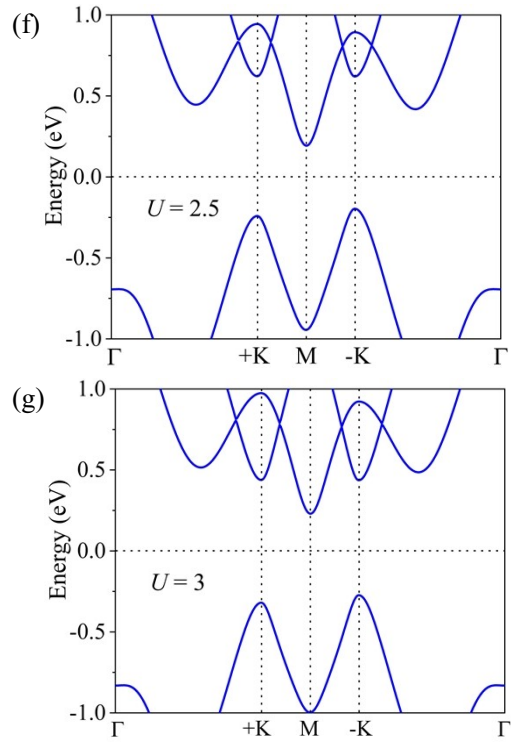
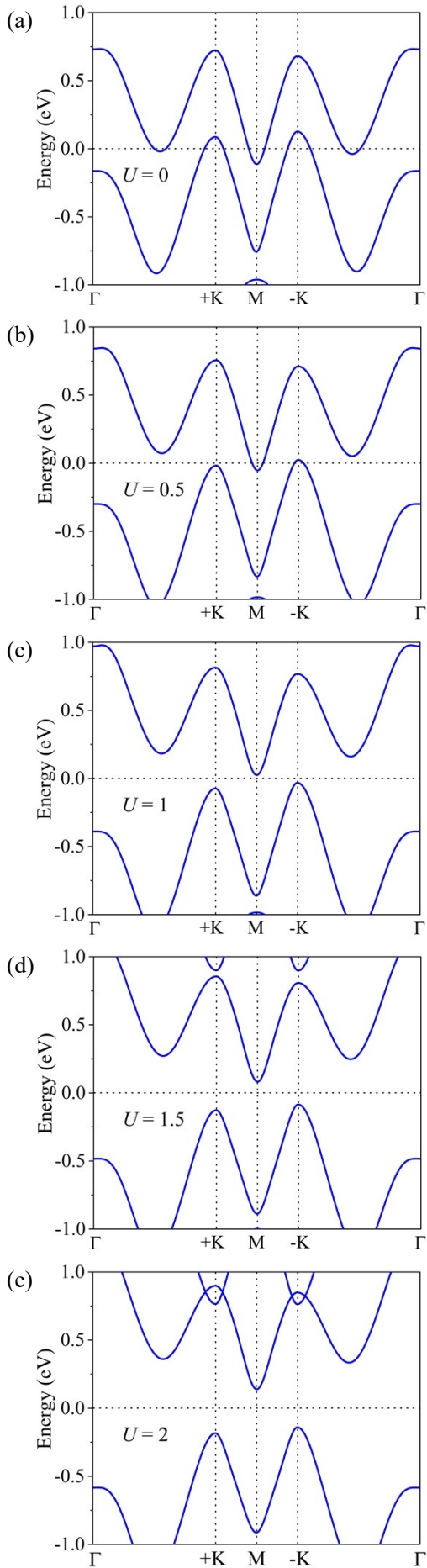


Fig. S3 The electronic band structures by using GGA+ U method with OOP magnetic anisotropy (U values vary from 0 to 3 eV).

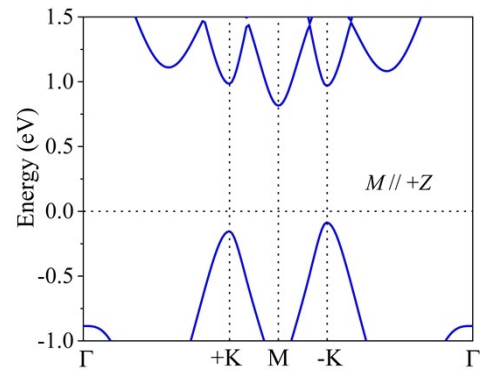
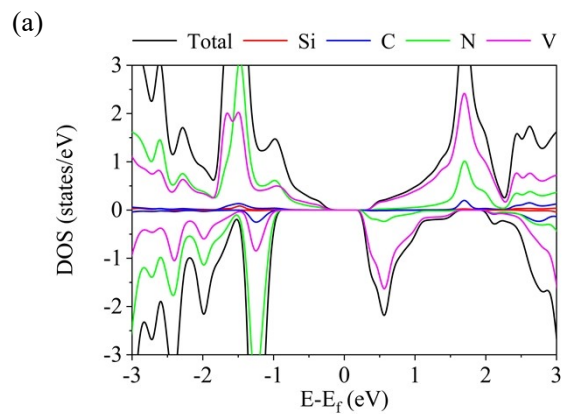


Fig. S4 The electronic band structures by using HSE06+SOC with OOP magnetic anisotropy.



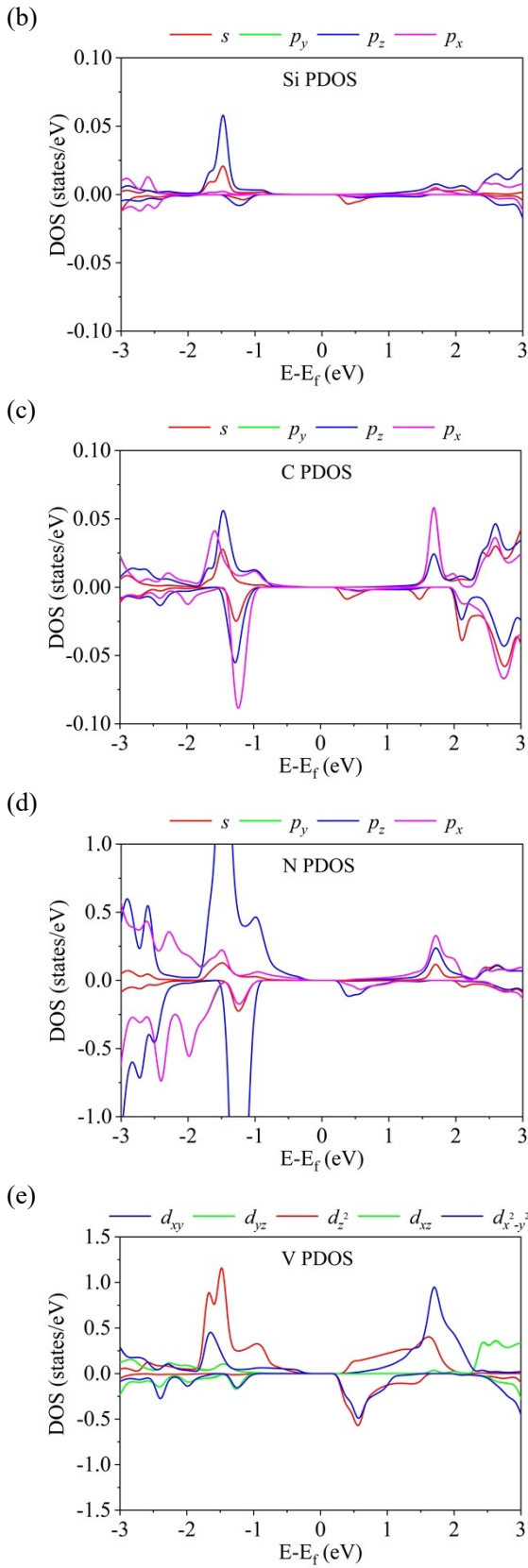
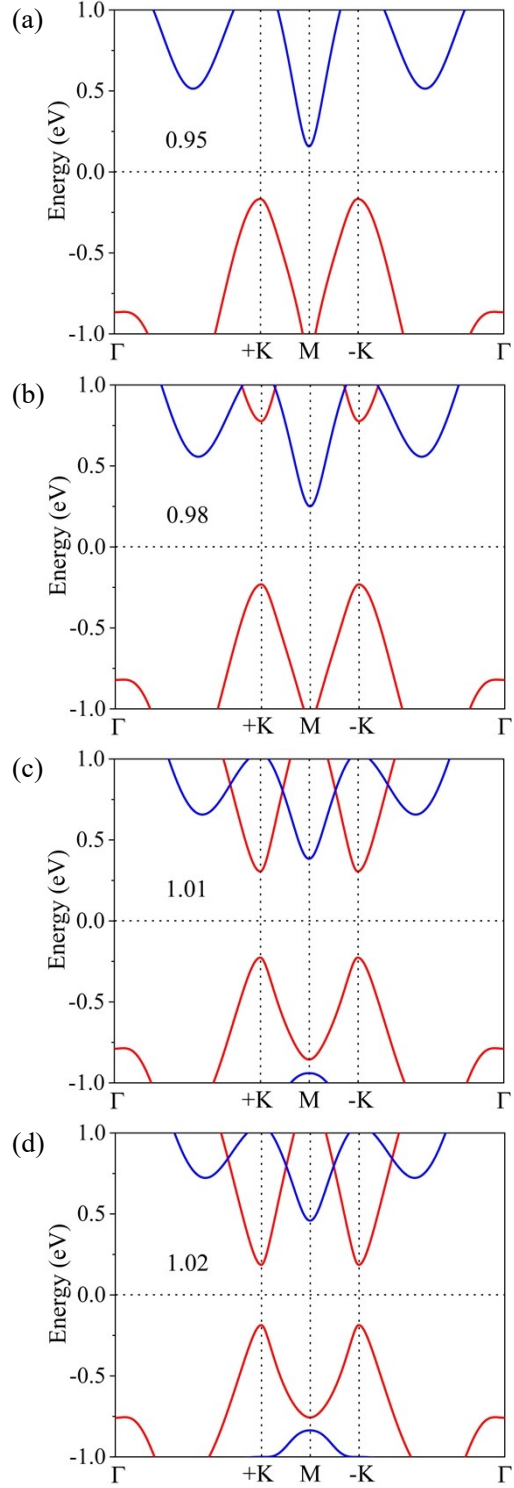


Fig. S5 (a) The total density of states (DOS) of the VCSiN₄. (b) The partial density of states (PDOS) of Si atoms. (c) The PDOS of C atoms. (d) The PDOS of N atoms. (e) The PDOS of V atoms.

The total and partial density of states (DOS) of the VCSiN₄ are calculated. As is exhibited in Fig. S5, we can observe that both CBM and VBM are mainly composed of $d_{x^2-y^2}/d_{xy}$ orbitals of V atoms and minority p_x/p_z orbitals of N atoms, which is consistent with that of orbital-resolved electronic band structure (see Fig. 3).



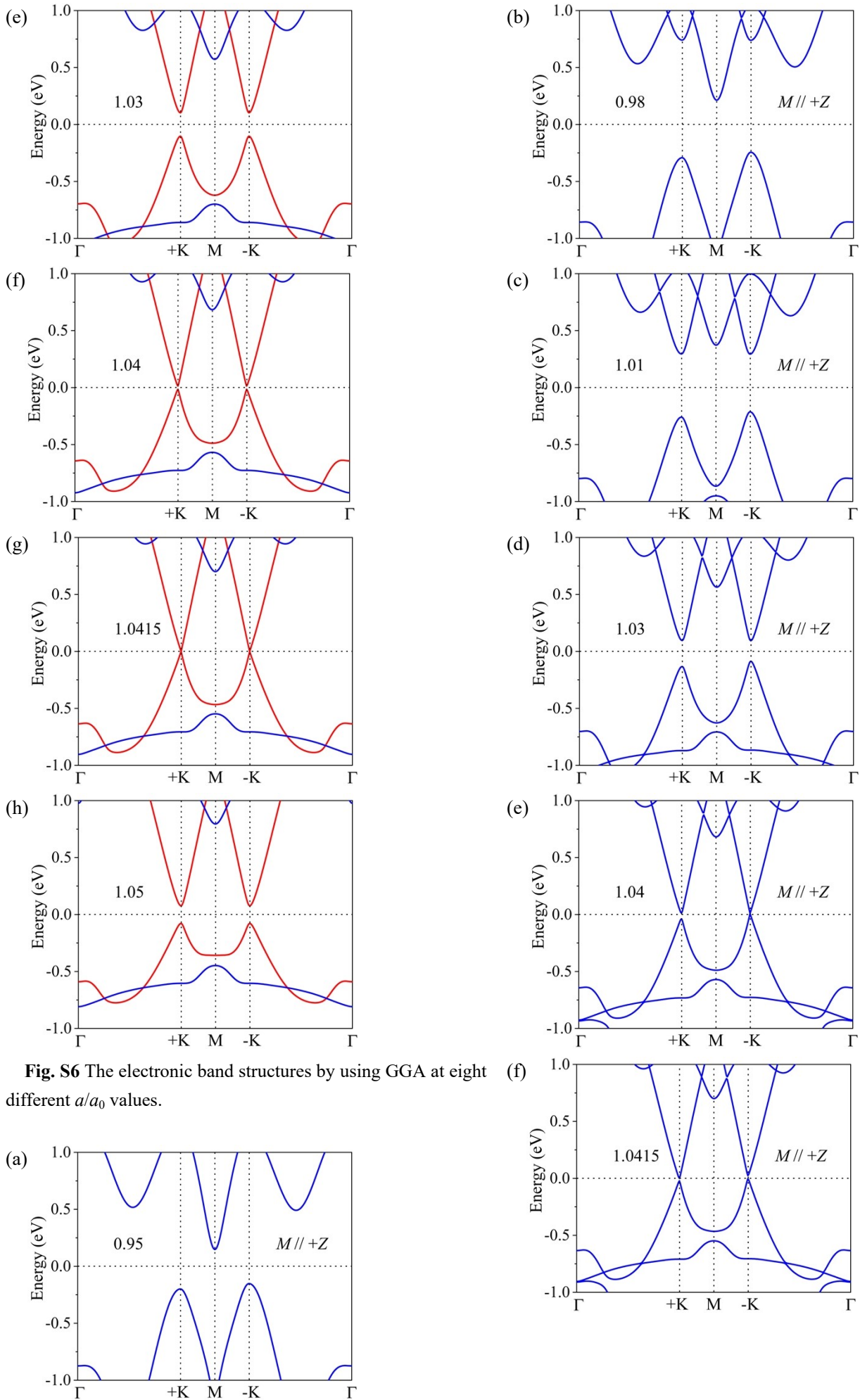


Fig. S6 The electronic band structures by using GGA at eight different a/a_0 values.

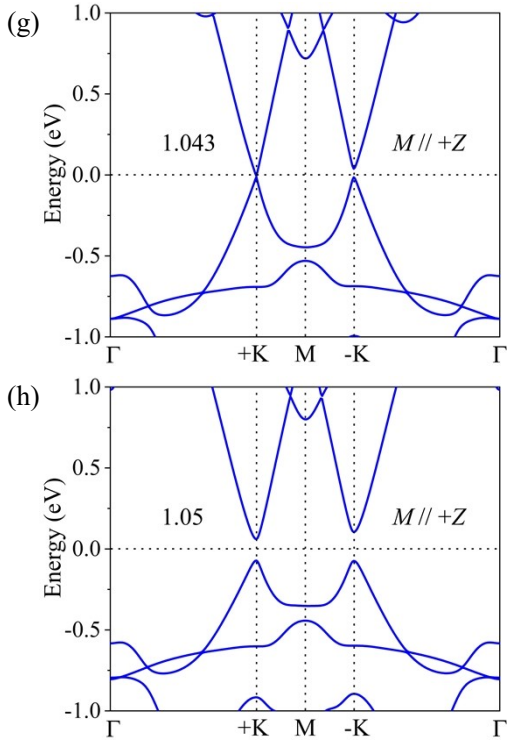


Fig. S7 The electronic band structures by using GGA+SOC with OOP magnetic anisotropy at eight different a/a_0 values.

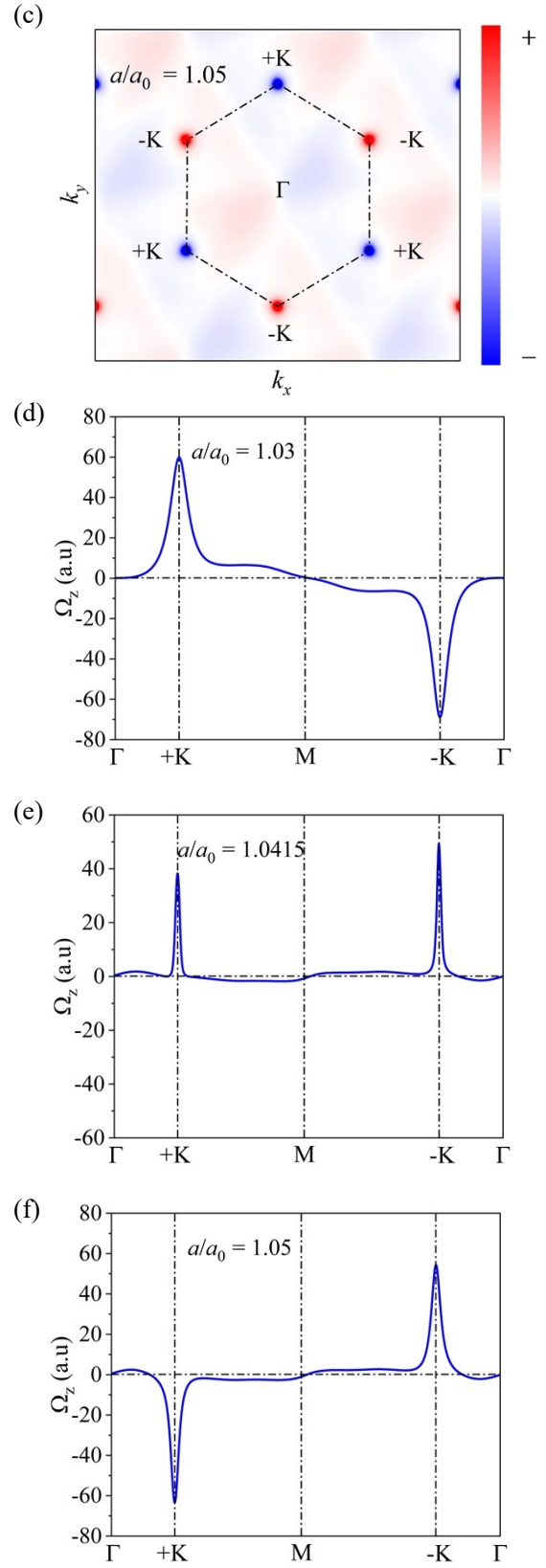


Fig. S8 The Berry curvature in the 2D BZ with (a) $a/a_0 = 1.03$, (b) $a/a_0 = 1.0415$, and (c) $a/a_0 = 1.05$. The Berry curvature along the high symmetry points with (d) $a/a_0 = 1.03$, (e) $a/a_0 = 1.0415$, and (f) $a/a_0 = 1.05$.

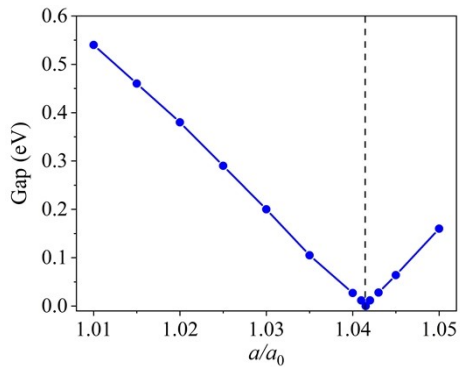


Fig. S9 The global band gaps with SOC (IP magnetic anisotropy) as a function of a/a_0 .

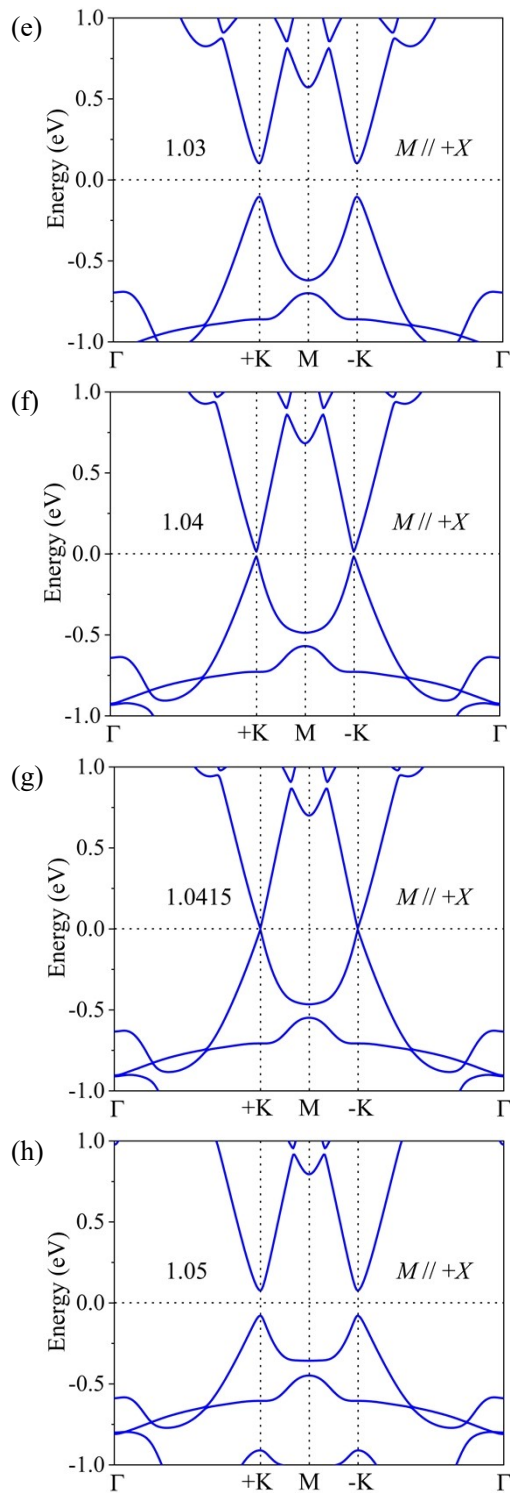
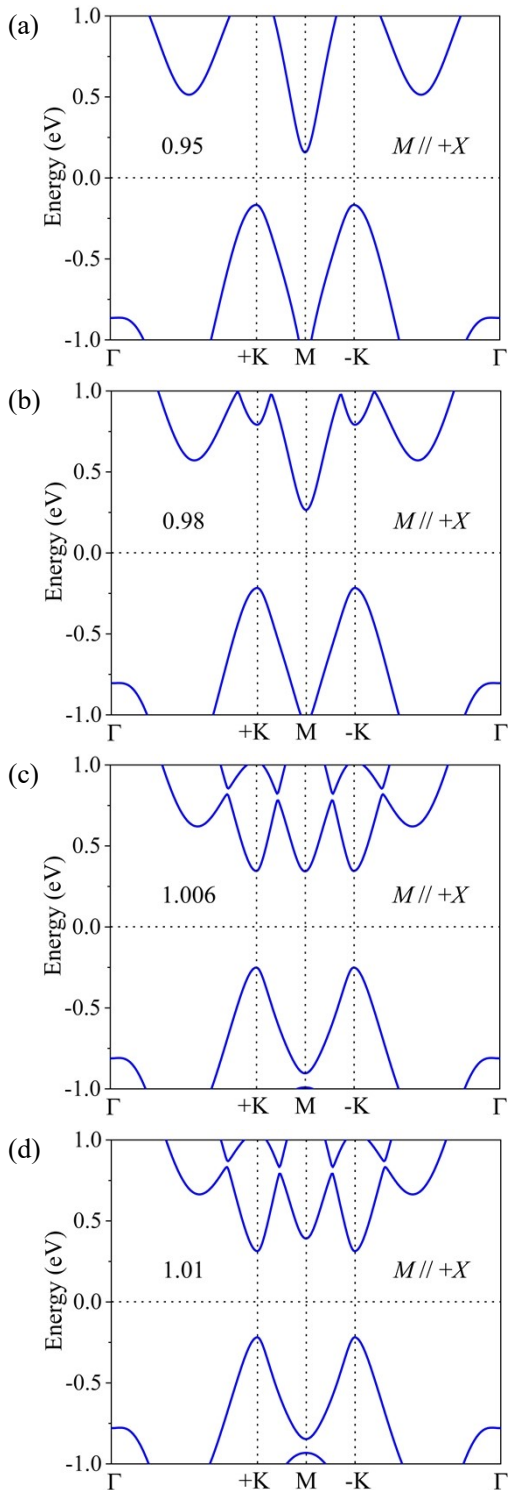


Fig. S10 The electronic band structures by using GGA+SOC with IP magnetic anisotropy at eight different a/a_0 values.