

1 **Super-Hydrophobic and Resilient Hybrid Silica Aerogels for Thermal Insulation, Energy**
2 **Harvesting, and Electrical Applications in Harsh Environments**

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10 ***Morphological analysis:***

11 The Density Functional Theory (DFT) method stands as a potent tool for determining pore
12 size distributions in nanoporous solid materials. It has demonstrated its efficacy in providing a
13 quantitative description of low-temperature N₂ adsorption on various materials. For accurately
14 assessing pore size and pore size distribution (PSD) in materials featuring nanopores (those with
15 widths smaller than 100 nm), methods grounded in statistical mechanics and molecular simulation,
16 such as DFT, represent the current state-of-the-art. DFT-based techniques are widely embraced
17 and commercially available across numerous gas adsorption systems used for measurement
18 purposes. They offer a reliable means to estimate PSD over a range encompassing micro and
19 mesopores. In contrast, classic methods like Barrett-Joyner-Halenda (BJH), Horvath-Kawazoe
20 (HK), Saito-Foley (SF), and Dubinin-Radushkevich (DR) may not be suitable for the entire
21 nanopore spectrum and have the potential to underestimate pore sizes below 10 nm in width.
22 Considering these factors, and in alignment with the recommendations of the International
23 Standard Organization (ISO), we have chosen to implement DFT as the preferred method for PSD
24 measurements in this paper^{1,2}.

25 During gas adsorption, a monolayer is formed on the sorbent's structure in low relative
26 pressure. As the relative pressure is increased, fine pores are filled first, followed by the gas
27 condensation and saturation of all pores. Consequently, the isotherm required for pore structure
28 analysis is obtained. The DFT model considers the properties of the condensed gas on the pores
29 such as the gas density to study the pore properties. The DFT, considers a specific geometry for
30 each material type (i.e., slit for carbon-based, cylinder for silica based, etc.) and fits its theoretical
31 isotherm to the data obtained from the experimental nitrogen adsorption isotherm using
32 complicated fitting and regression procedures. The DFT model can be explained using Equation
33 (1):

34
$$N_{exp}(P/P_0) = \int_{D_m}^{D_M} N_{DFT}(P/P_0, D) \times F(D) dD \quad (1)$$

35 where $N_{exp}(P/P_0)$ is the experimental adsorption isotherm, $f(D)$ is a pore diameter distribution
36 function, and D_m and D_M are minimum and maximum pore diameters in our model². The basic
37 formulations of the DFT approach can be found elsewhere^{3,4}.

1 It is also worth mentioning that there is no distinct relationship between the pore width,
2 pore volume and specific surface area. By assuming all pores having a cylindrical shape, the
3 following equation can be used to estimate the pore size⁵:

$$D_{pore} \approx \frac{V_{pore}}{4S_{BET}} \quad (2)$$

4
5 Equation 2 shows that pore width is a function of both pore volume and specific surface
6 area. Hence, improvement of surface area or pore volume will not necessarily affect the pore width.
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8 ***Thermal imaging experiments:***

9 To conduct thermal imaging experiments, a thick insulation material with tubular hole was
10 affixed to the hot plate to control heat convection. Subsequently, the samples were placed within
11 this hole, and temperature at the center of each sample was recorded. In thermal images, the red
12 circle is the visible portion of the hot plate. This circle served as a visual indicator for the reference
13 temperature.

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Figure S1. The optical images of the samples depict the diverse degrees of contraction.

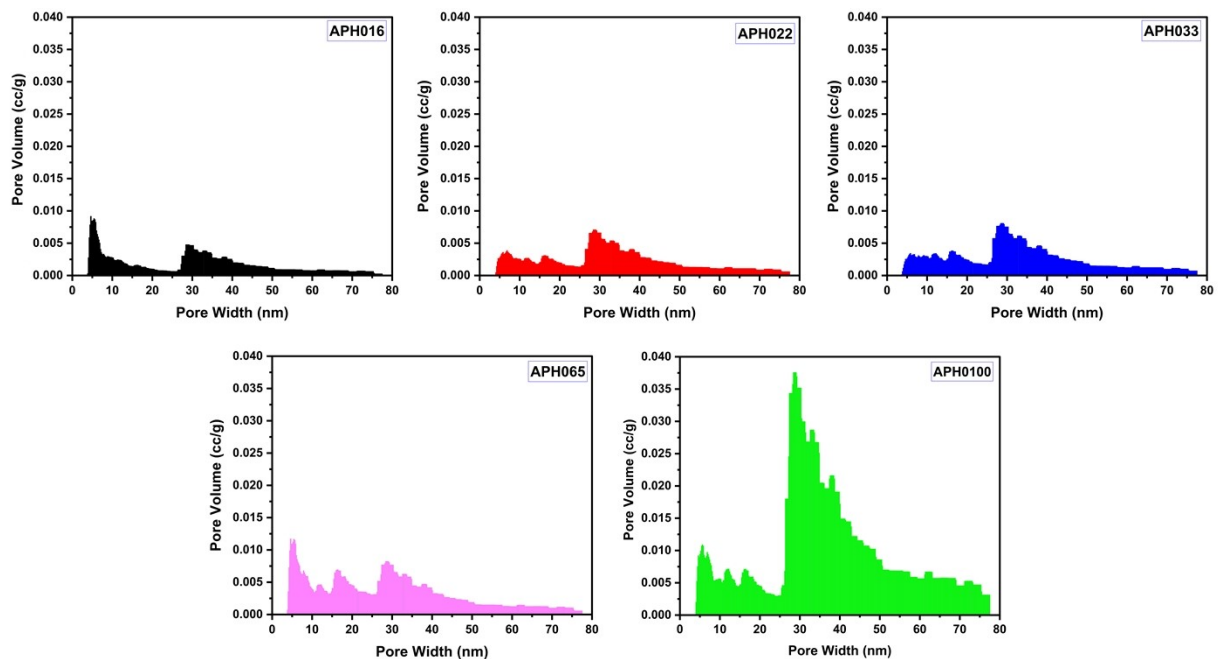


Figure S2: Linear pore size distribution and related pore volume for all samples.

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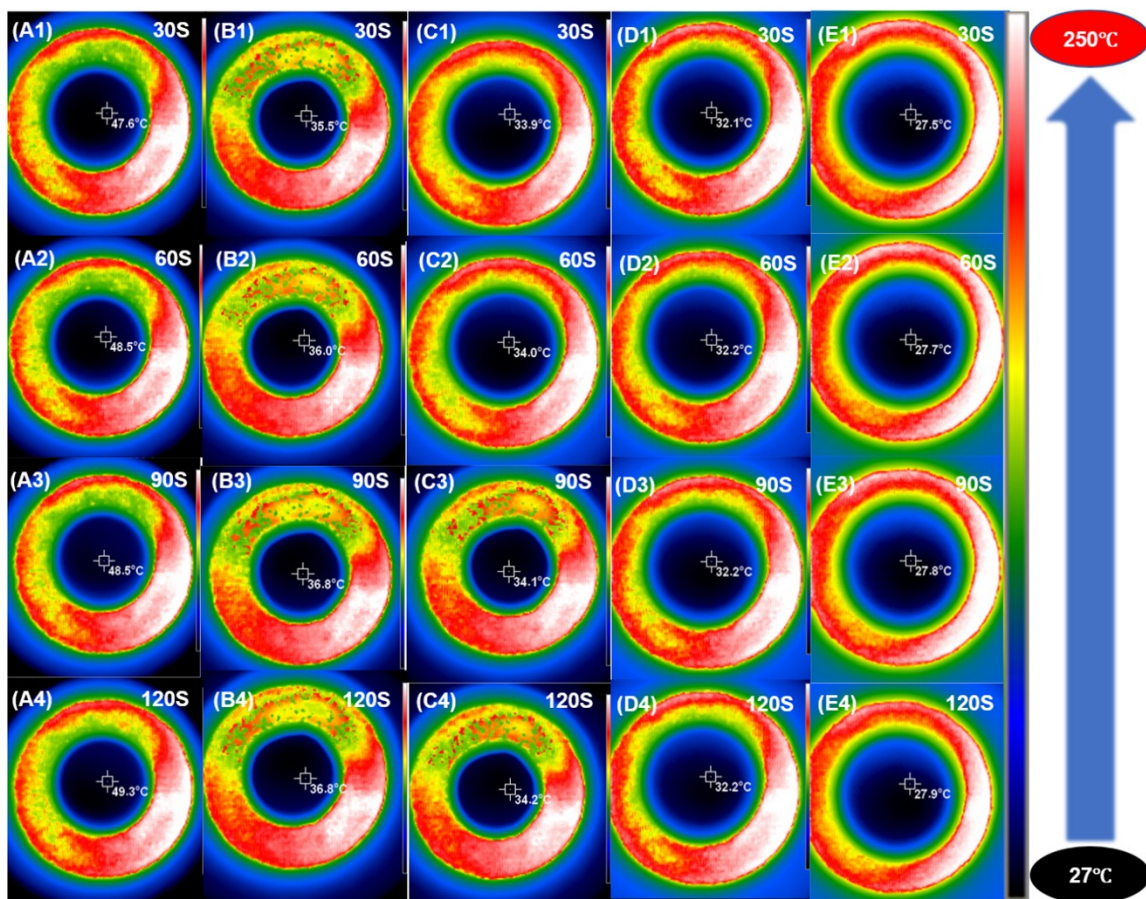


Figure S3. Thermal images of the samples captured at 30-second intervals, APH016 (A1-A4), APH022 (B1-B4), APH033 (C1-C4), APH065 (D1-D4), APH100 (E1-E4)

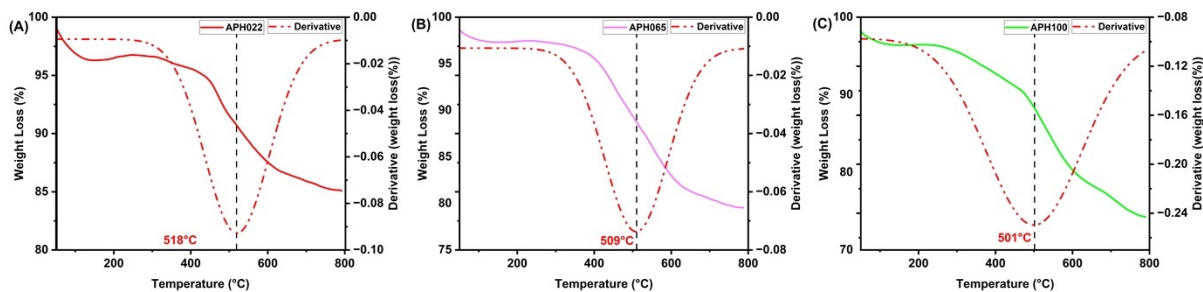


Figure S4. Thermal stability analyzed using TGA curves and their derivatives.

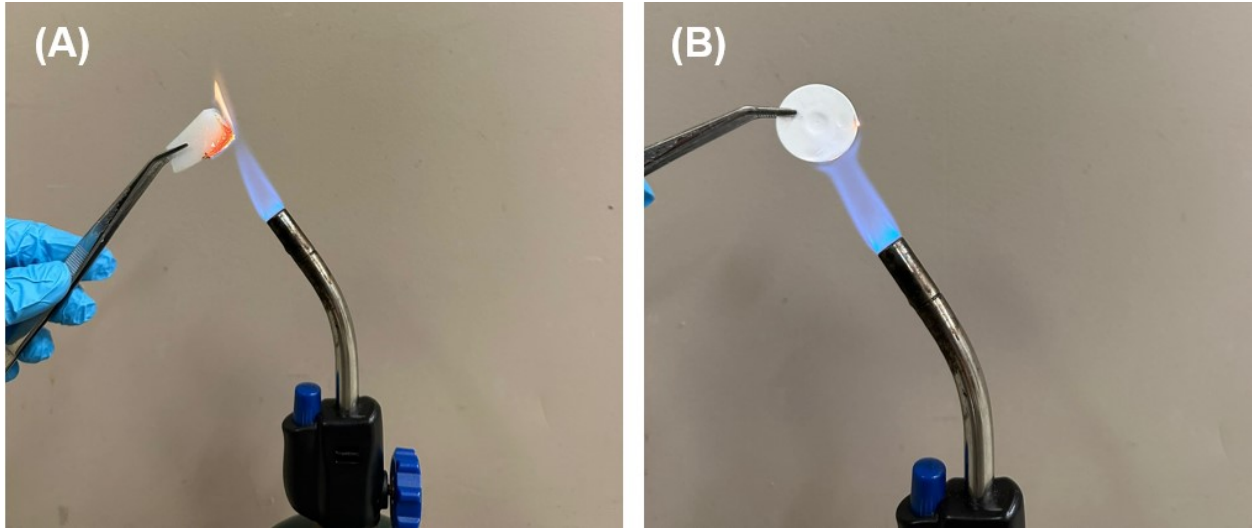


Figure S5. (A) PVTMS sample burns in fire, while (B) APH016 is more fire resistant.

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Densification Modulus:

6 The densification modulus was computed for all specimens following the curvature point
7 of the diagrams. In order to maintain consistency in the measurement procedure, reference points
8 of 1 and 3.3 MPa were selected, except for sample APH022HC, where the maximum point is at
9 2.12 MPa.

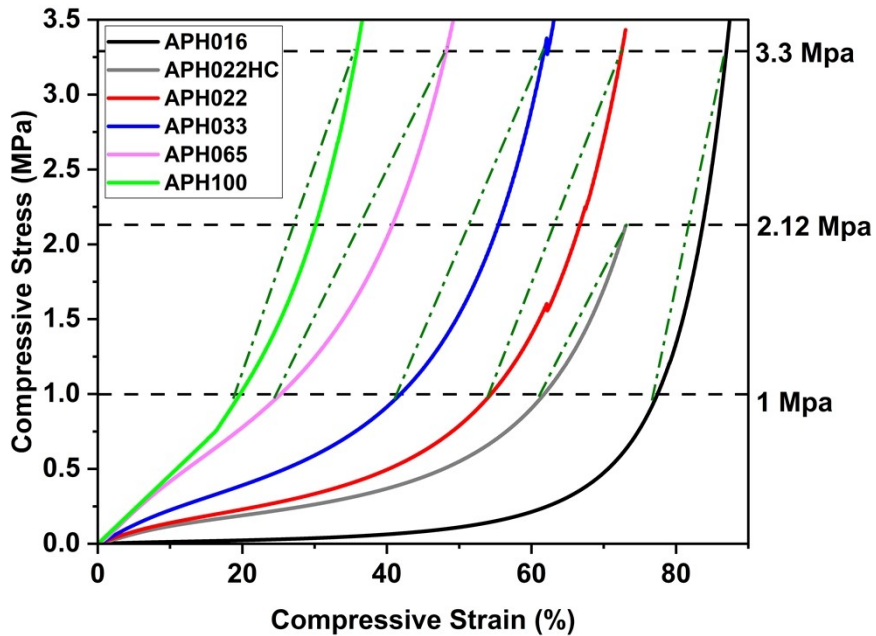


Figure S6. Densification modulus for specimens.

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1 Table S1: Stress-strain values for calculating young and densification modulus and data points for comparing samples
 2 at 15, 25, and 35 % strain.

APH016		APH022HC		APH022		APH033		APH065		APH100	
Strain (%)	Stress (Mpa)	Strain (%)	Stress (Mpa)	Strain (%)	Stress (Mpa)	Strain (%)	Stress (Mpa)	Strain (%)	Stress (Mpa)	Strain (%)	Stress (Mpa)
0	0	0	0	0	0	0	0	0	0	0	0
0.99	0.00	1.00	0.01	0.99	0.02	0.99	0.02	0.99	0.03	0.99	0.04
1.00	0.00	1.02	0.01	1.01	0.02	1.01	0.02	1.01	0.03	1.01	0.05
15.00	0.02	15.01	0.16	15.01	0.19	15.01	0.31	15.01	0.59	15.01	0.69
25.00	0.03	25.01	0.22	25.00	0.28	25.00	0.48	25.00	0.99	25.01	1.47
35.00	0.05	35.01	0.31	35.01	0.40	35.01	0.73	35.01	1.58	35.00	3.09
77.45	1.00	61.77	1.00	54.40	1.00	41.90	1.00	25.32	1.00	19.69	1.00
86.99	3.30	73.04	2.12	72.55	3.30	61.79	3.30	48.30	3.30	35.87	3.30

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1 References:

- 2 1 ISO 15901-2:2022 - Pore size distribution and porosity of solid materials by mercury porosimetry and gas
3 adsorption — Part 2: Analysis of nanopores by gas adsorption, <https://www.iso.org/standard/67586.html>.
- 4 2 R. Bardestani, G. S. Patience and S. Kaliaguine, *Can J Chem Eng*, 2019, **97**, 2781–2791.
- 5 3 J. Landers, G. Y. Gor and A. V. Neimark, *Colloids Surf A Physicochem Eng Asp*, 2013, **437**, 3–32.
- 6 4 P. I. Ravikovitch, G. L. Haller and A. V. Neimark, *Adv Colloid Interface Sci*, 1998, **76–77**, 203–226.
- 7 5 H. Maleki, S. Montes, N. Hayati-Roodbari, F. Putz and N. Huesing, *ACS Appl Mater Interfaces*, 2018, **10**,
8 22718–22730.

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