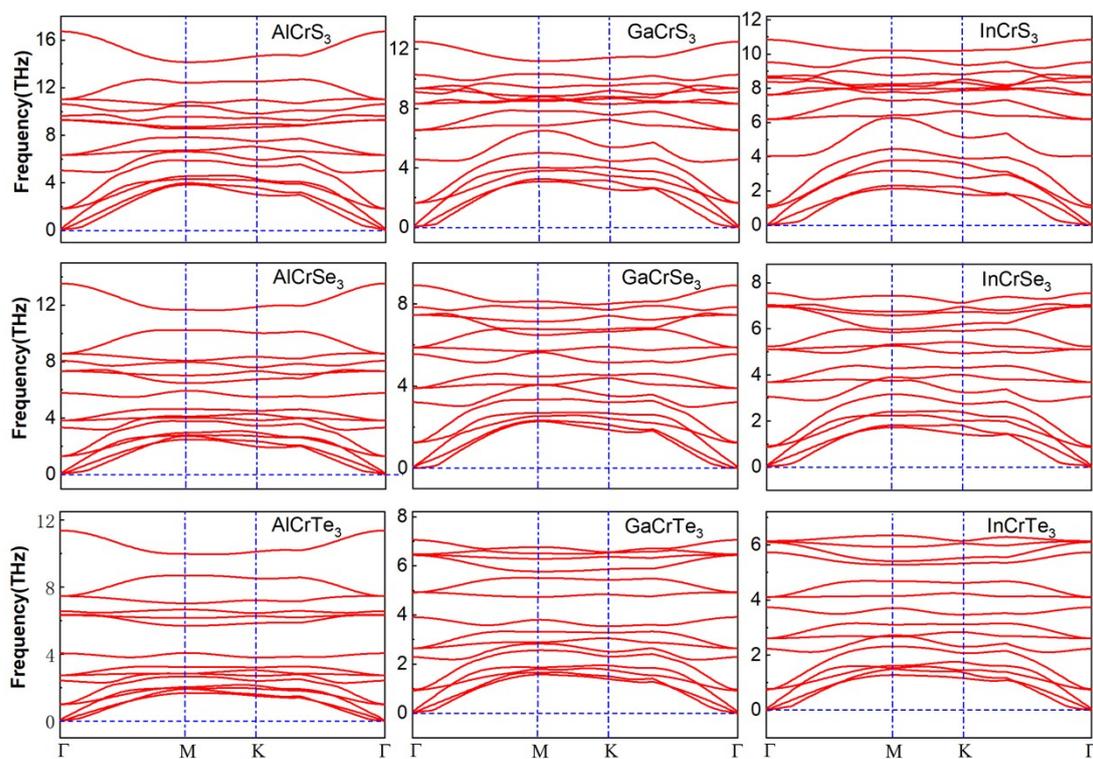


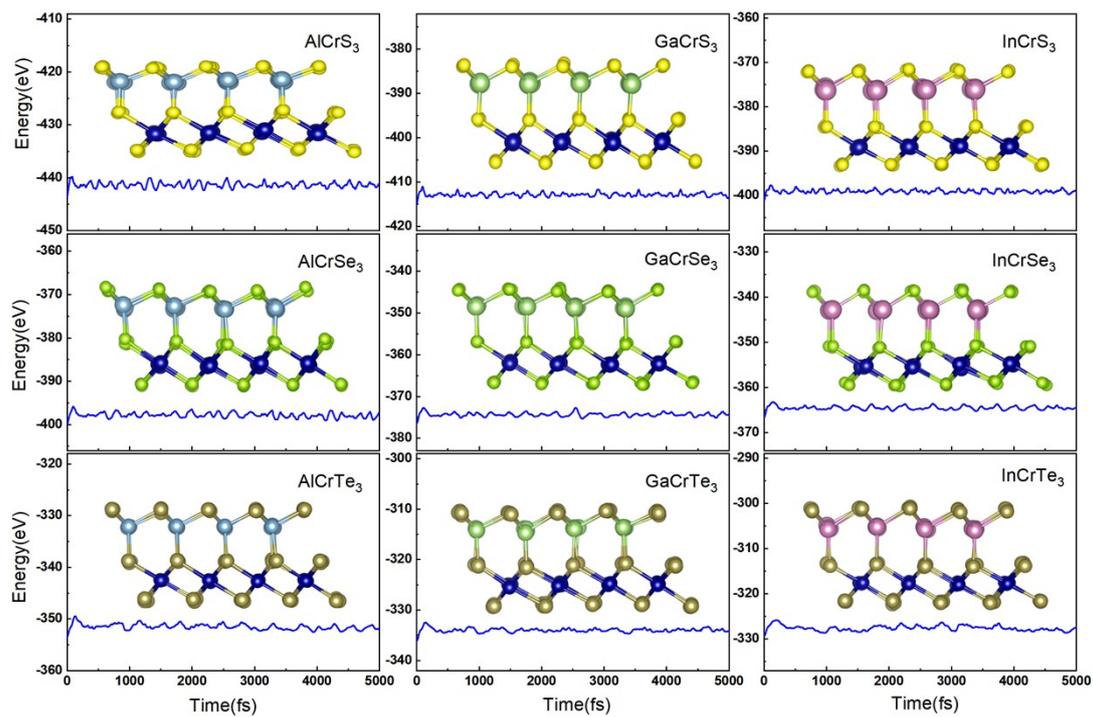
Supplemental materials for **“Intrinsic Ferromagnetism with High Curie Temperature in Two Dimensional  $XCrY_3$  ( $X = Al, Ga, In; Y = S, Se, Te$ ) Monolayers.”**

In this Supplemental Material we provide (1) the phonon spectra and the MD simulation results for all  $XCrY_3$  ( $X=Al, Ga, In$ ;  $Y=S, Se, Te$ ) monolayers, (2) the electronic band structures and PDOSs of all  $XCrY_3$  monolayers, (3) the top and side view of deformation charge density distribution of the  $AlCrS_3$  monolayer, (4) the orbital-projected contribution to MAE from the SOC interaction, (5) Magnetic moment and specific heat capacity as a function of temperature by Monte Carlo simulations, and (6) the total energies per cell of monolayer  $XCrY_3$  with different magnetic configurations at the GGA+ U level.

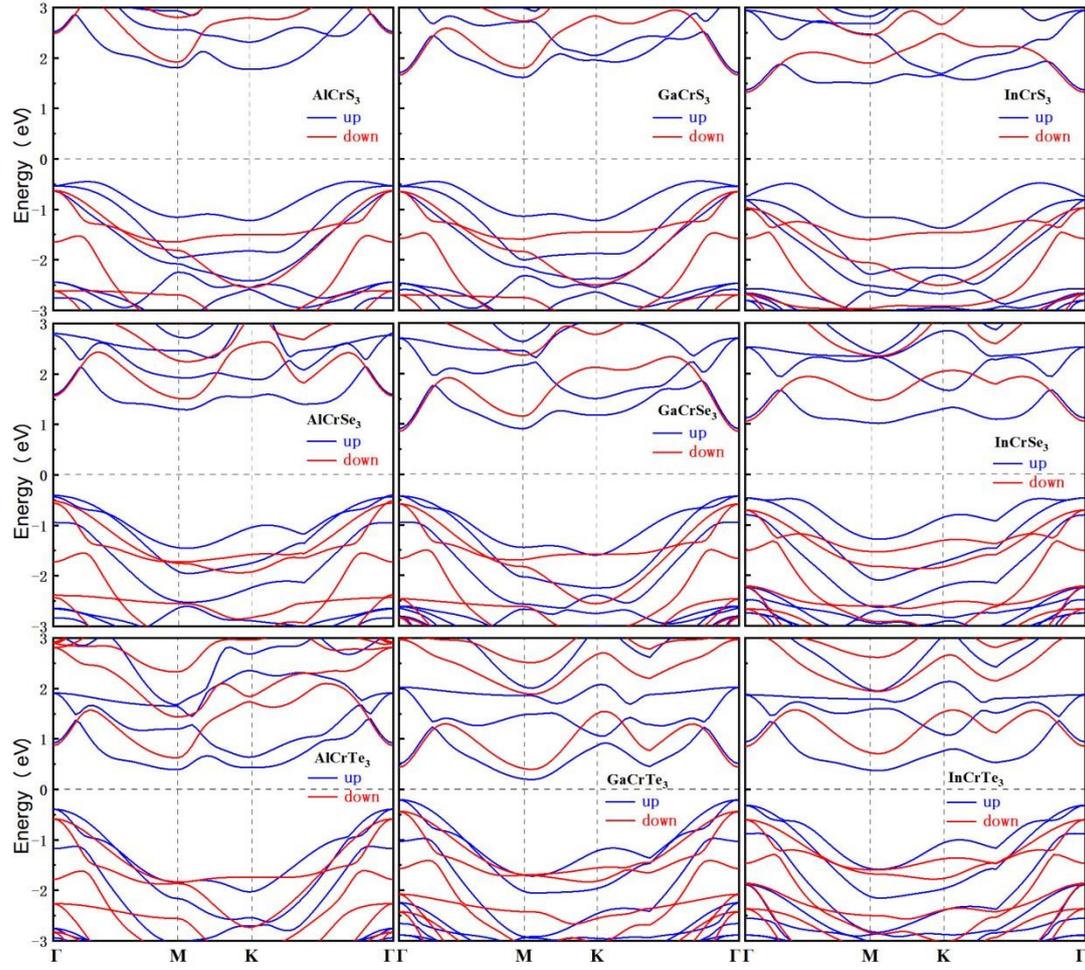
Figures S1 and S2 shows that the studied  $XCrY_3$  monolayers are kinetically and dynamically stable.



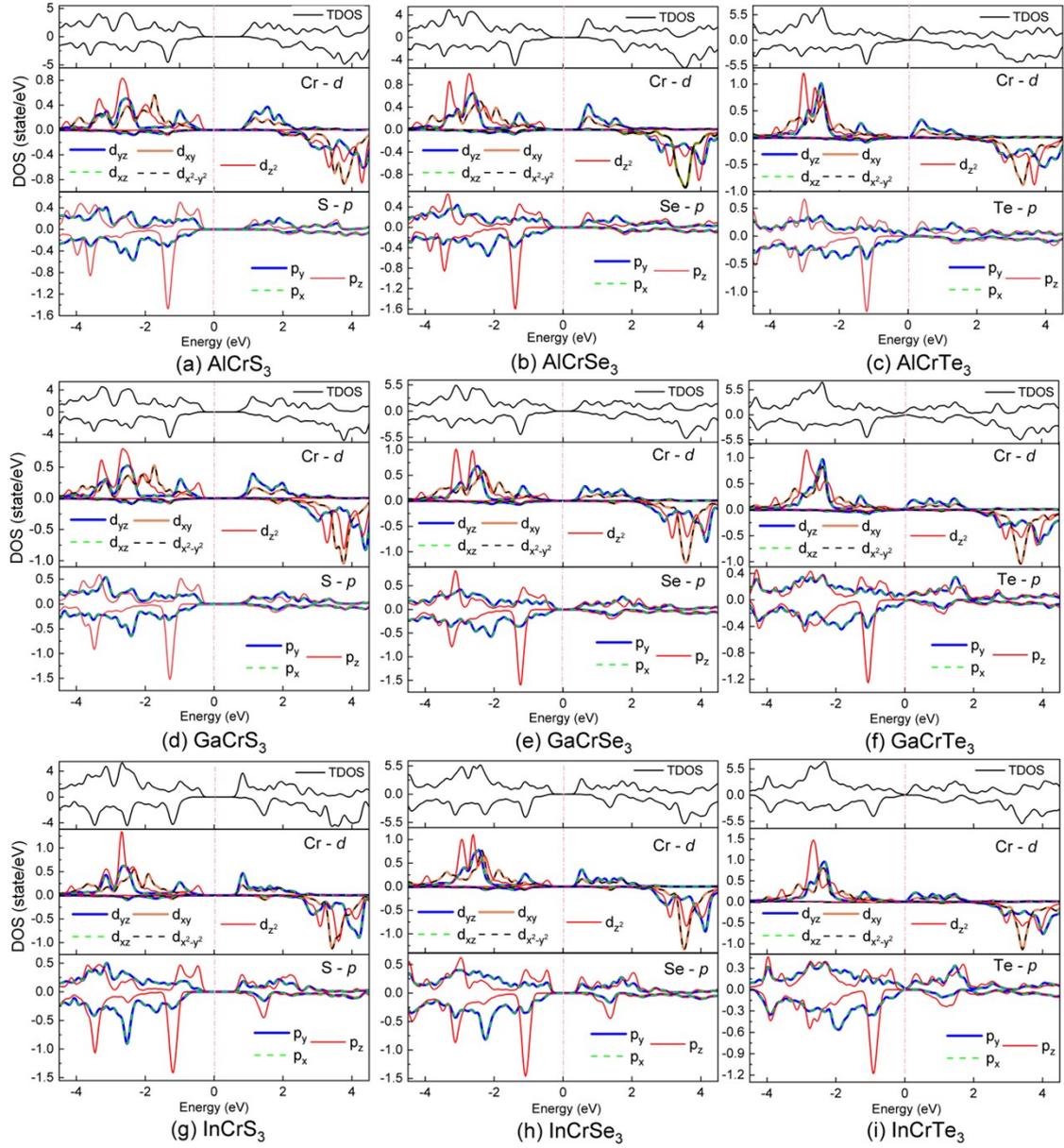
**Figure S1.** The phonon spectra of all  $XCrY_3$  ( $X=Al, Ga, In$ ;  $Y=S, Se, Te$ ) monolayers.



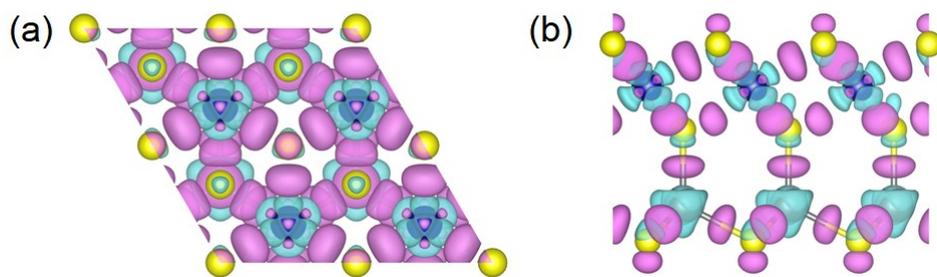
**Figure S2.** Results of molecular dynamics simulations of all  $X\text{CrY}_3$  ( $X=\text{Al, Ga, In}$ ;  $Y=\text{S, Se, Te}$ ) monolayers, as well as the final structures after being heated at 300K for 5ps inserted.



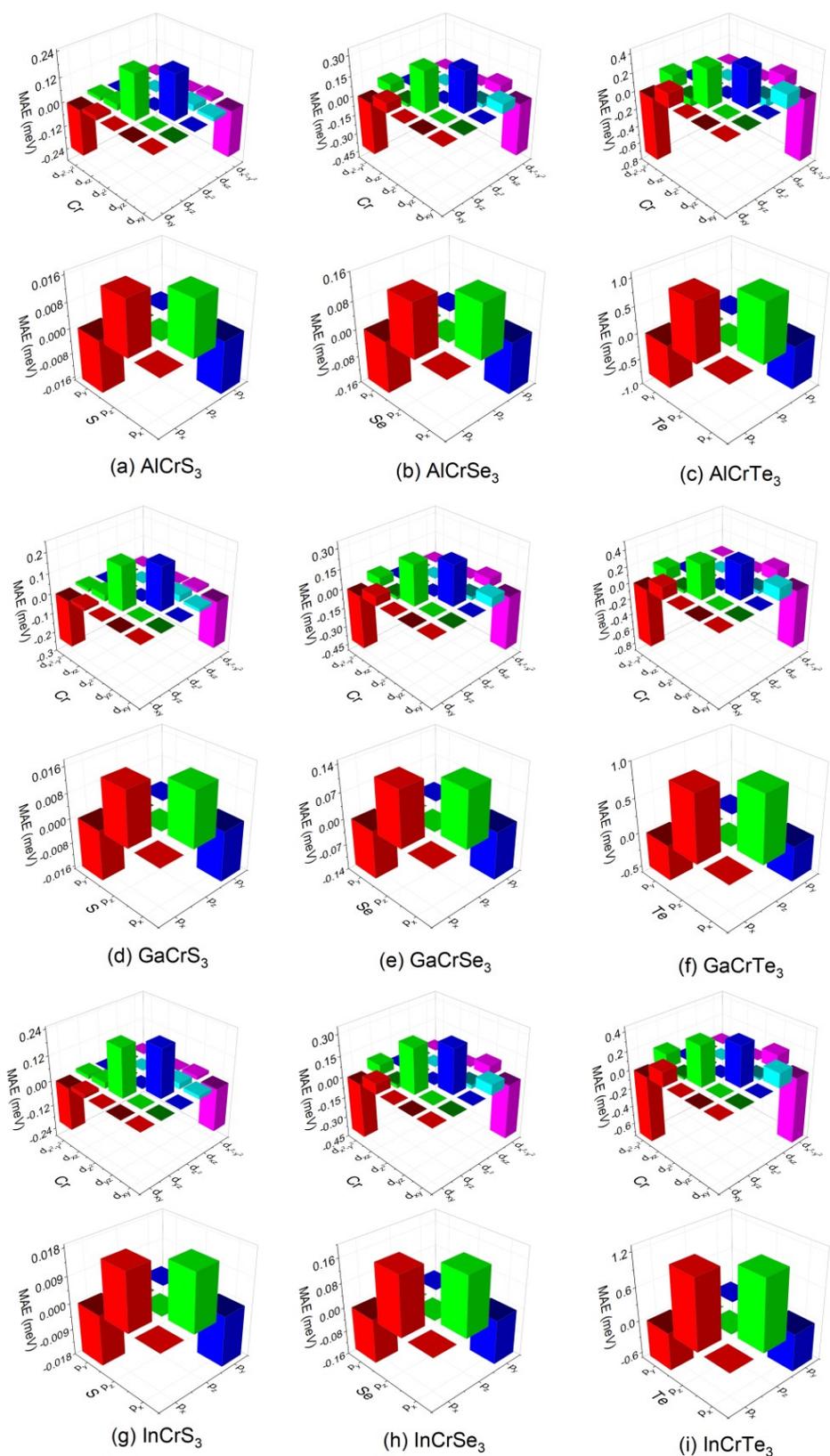
**Figure S3.** Band structures of all  $XCrY_3$  ( $X=Al, Ga, In; Y=S, Se, Te$ ) monolayers under HSE06 calculation methods. Blue and red lines represent up and down spin, respectively.



**Figure S4.** Total DOS and corresponding PDOS of monolayer AlCrS<sub>3</sub>, AlCrSe<sub>3</sub>, AlCrTe<sub>3</sub>, GaCrS<sub>3</sub>, GaCrSe<sub>3</sub>, GaCrTe<sub>3</sub>, InCrS<sub>3</sub>, InCrSe<sub>3</sub>, InCrTe<sub>3</sub>, respectively. The vertical dashed line represents the Fermi level which is set as zero.

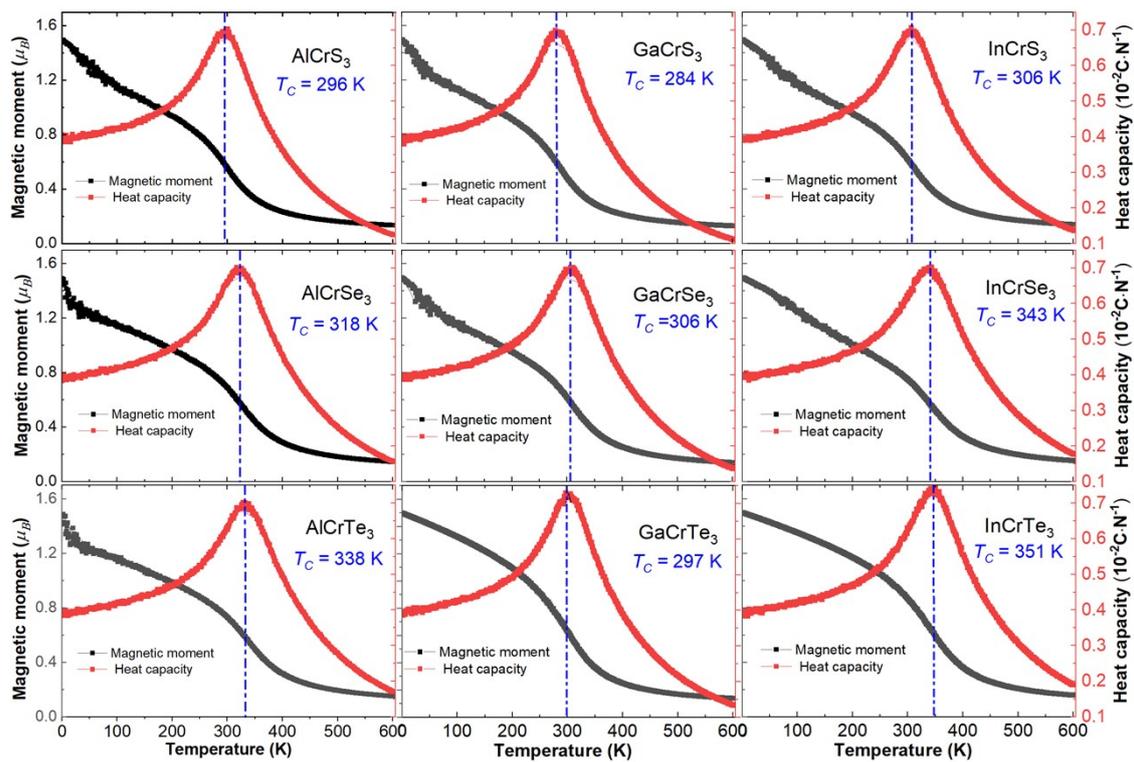


**Figure S5.** The (a) top and (b) side view of deformation charge density distribution of the AlCrS<sub>3</sub> monolayer. The value of the isosurface is 0.003 e/bohr<sup>3</sup>. The silver, blue and yellow balls represent Al, Cr and S atoms, respectively.



**Figure S6.** (a)-(i) are the orbital-projected contribution to MAE from the SOC interaction for AlCrS<sub>3</sub>, AlCrSe<sub>3</sub>, AlCrTe<sub>3</sub>, GaCrS<sub>3</sub>, GaCrSe<sub>3</sub>, GaCrTe<sub>3</sub>, InCrS<sub>3</sub>, InCrSe<sub>3</sub>, InCrTe<sub>3</sub>, respectively.





**Figure S7.** Magnetic moment and specific heat capacity as a function of temperature by Monte Carlo simulations.

**Table S1.** The total energies per cellof monolayer  $XCrY_3$  with different magnetic configurations at the GGA+ U level, including FM, zigzag AFM (z-AFM), stripe AFM (s-AFM), and  $120^\circ$  noncollinear AFM (n-AFM).

$XCrY_3$	$E_{\text{FM}}/e$ V	$E_{z\text{-AFM}}$ /eV	$E_{s\text{-AFM}}$ /eV	$E_{n\text{-AFM}}$ /eV
AlCrS <sub>3</sub>	-27.72	-27.62	-27.61	-27.60
AlCrSe <sub>3</sub>	-24.99	-24.87	-24.86	-24.85
AlCrTe <sub>3</sub>	-22.09	-22.05	-22.02	-22.03
GaCrS <sub>3</sub>	-25.94	-25.85	-25.84	-25.83
GaCrSe <sub>3</sub>	-23.53	-23.47	-23.44	-23.43
GaCrTe <sub>3</sub>	-21.01	-20.99	-20.97	-20.98
InCrS <sub>3</sub>	-25.07	-24.90	-24.90	-24.89
InCrSe <sub>3</sub>	-22.92	-22.78	-22.77	-22.76
InCrTe <sub>3</sub>	-20.59	-20.52	-20.50	-20.50