

Supplementary materials

Migration paths of the Na⁺-ion diffusion for minerals of the lovozerite group: crystallochemical and DFT modeling

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Table S1. Topological characteristics of the atomic nets for lovozerite group of minerals.

Mineral	Space group	Topological classification	Type of atoms coordination	Point symbol		Transitivity	Tiling	ICSD
Combeite Litvinskite Lovozerite Townendite Zolotarevite	$R\bar{3}m$ Cm $C2_1$ $R\bar{3}m$ $R\bar{3}m$	sqc962	3,6-c	$\{6^3\}6\{6^6.8^6.12^3\}$	2-nodal net	[4 2 3 1]	$[6^4.8^3]$	62827 57042 30389 168092 137779
Kapustinite Kazakovite Zirsinalite	$R\bar{3}m$ $C2/m$ $R\bar{3}cr$	New topology	3,4,6 ² -c net	$\{4.8^2\}2\{4^3.8^3\}2\{4^6.8^6.10^3\}$	4-nodal net	[10 10 9 8]	2t-kzd + 6t-jnt-1 + 3t-kds+t-cub+3t-ste	250170 200602 200800
Imandrite	$Pmnn$	New topology	3 ² ,4 ² ,6 ² -c net	$\{4.5.7\}2\{4.5^2.6^2.8\}2\{4.5^2.7^2.8\}$ $4\{4.7.8\}4\{4^4.5^2.6^2.7^4.8^2.9\}$ $2\{4^6.7^2.8^4.9^2.10\}$	6-nodal net	[9 10 9 7]	2t-kzd + 2t-ukc + 4t-jnt-1 + t-lov + 4[4.5.7.8 ²] + t-bru + t-ste	200805
Tisinalite	$P\bar{3}$	New topology	3,4,6-c net	$\{4.5.7\}2\{4.5^2.6^2.8\}2\{4.5^2.7^2.8\}$ $4\{4.7.8\}4\{4^4.5^2.6^2.7^4.8^2.9\}$ $2\{4^6.7^2.8^4.9^2.10\}$	6-nodal net	[10 9 8 7]	3t-kds + t-cub+2[6 ³ .8 ³]	250068
Koashvite	$Pmnb$	New topology	3 ⁴ ,4 ⁴ ,6 ³ -c net	$\{4.5.7\}\{4.5^2.7^2.8\}\{4.7.8\}$ $5\{4^2.5.7.8^2\}4\{4^3.7^2.8\}$ $\{4^4.5^2.7^6.8^2.10\}\{4^6.7^2.8^4.9^2.10\}$ $\{4^6.7^2.8^4.9^3\}$	11-nodal net	[16 19 16 10]	2t-kzd + 4t-jnt-1 +[4 ² .7 ²]+t-kds + 2[4.5.7.8 ²]+ t-csv-1 + t-ste+[4 ² .7 ⁴ .8 ²]	86517

Table S2. Tiles for atomic net of the combeite, litvinskite, lovozerite, townendite, zolotarevite minerals with **sqc962** topology.

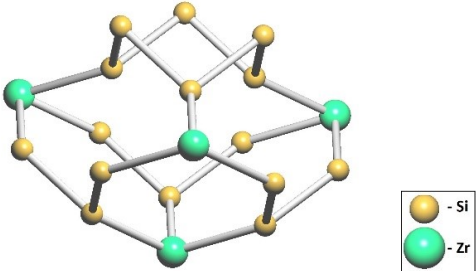
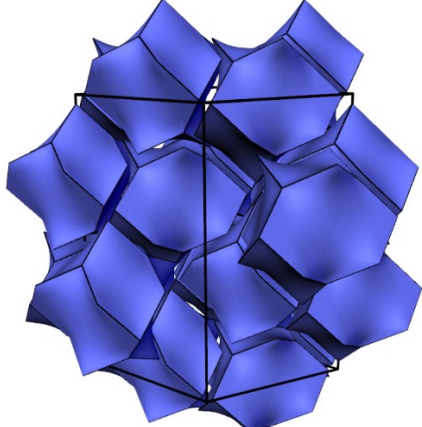
sqc962 (Combeite, Lovozerite, Litvinskite, Townendite, Zolotarevite)	
Face symbol:	[6⁴.8³]
	
V, E, F:	(19, 24, 7)
Label:	t-unknown
	<p style="text-align: center;">TILING</p> 

Table S3. Tiles for atomic net of the tisinallite mineral with new topology obtained by means the geometrically-topological analysis.

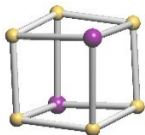
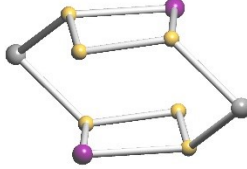
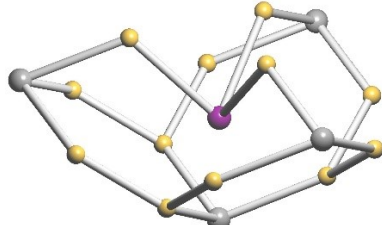
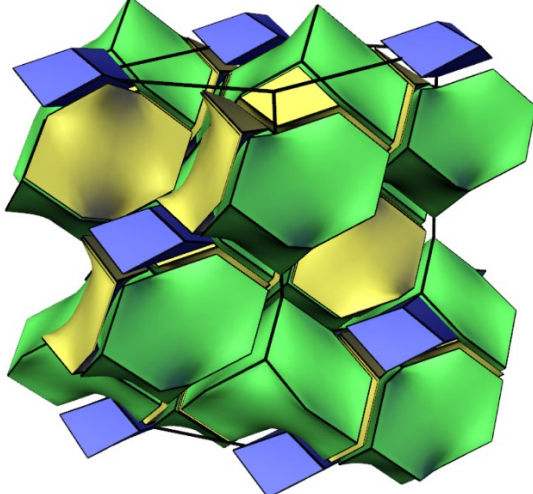
3,4,6-c net New topology (Tisinallite)			
Face symbol:	[4⁶]	[4².8²]	[6³.8³]
			
V, E, F:	(8, 12, 6)	(10, 12, 4)	(17, 21, 6)
Label:	t-cub	t-kds	t-unknown1
			<p style="text-align: center;">TILING</p> 

Table S4. Tiles for atomic net of the kapustinite, kazakovite, zirsinalite minerals with new topology obtained by means the geometrically-topological analysis.

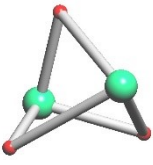
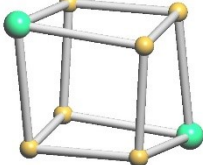
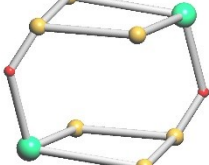



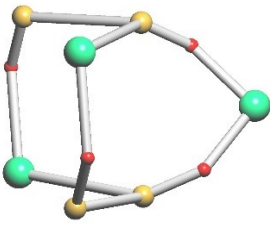
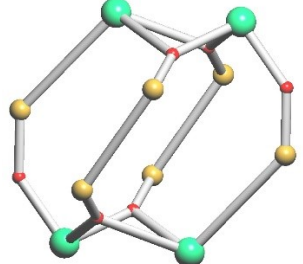





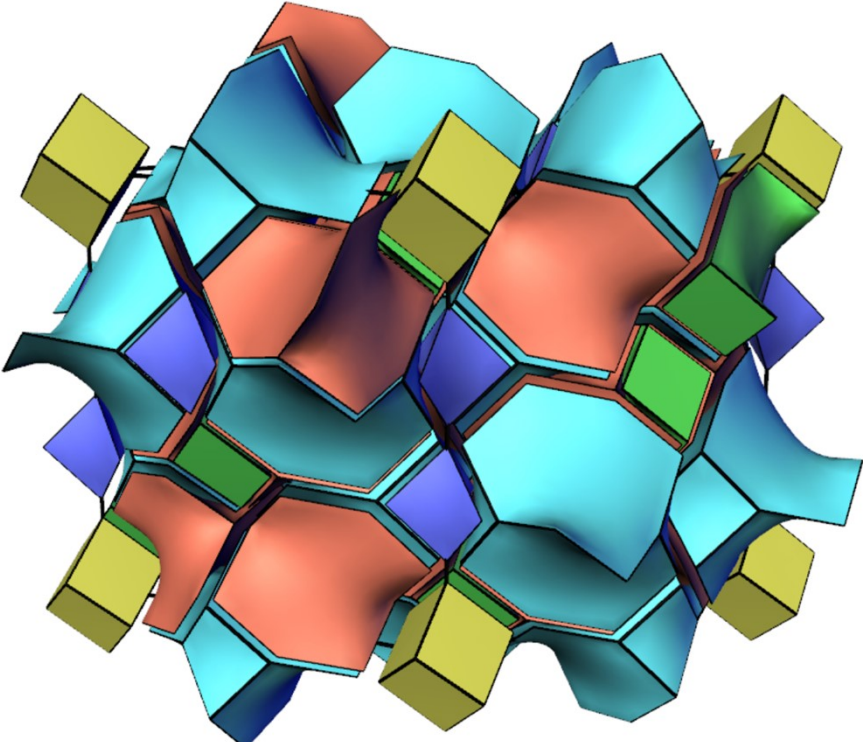
3,4,6²-c net New topology (Kapustinite, Kazakovite, Zirsinalite)			
Face symbol:	[4³]	[4⁶]	[4².8²]
			
V, E, F:	(5, 6, 3)	(8, 12, 6)	(10, 12, 4)
Label:	t-kzd 	t-cub 	t-kds 
Face symbol:	[8³]	[4².8⁴]	
		 <div style="display: inline-block; vertical-align: middle; margin-left: 10px;">  - O  - Si  - Zr </div>	
V, E, F:	(11, 12, 3)	(16, 20, 6)	
Label:	t-jnt-1 	t-ste 	
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Table S5. Tiles for atomic net of the imandrite mineral with $3^2,4^2,6^2T18$ topology obtained by means the geometrically-topological analysis.


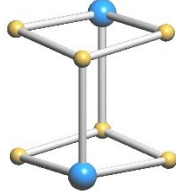
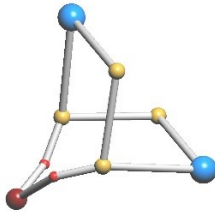
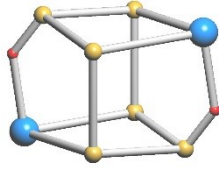




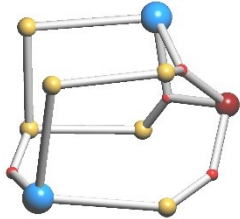
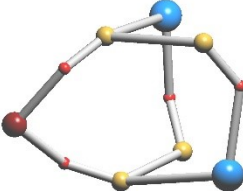
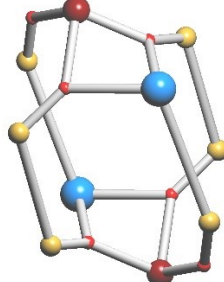
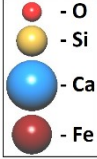



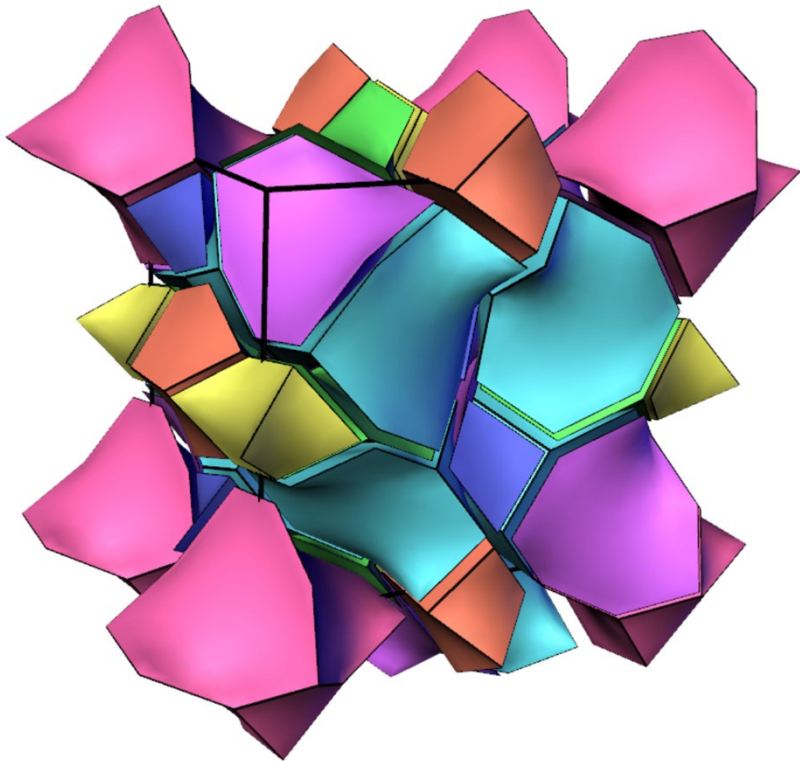
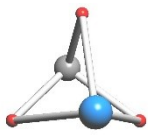
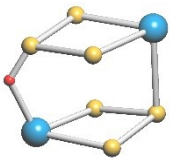
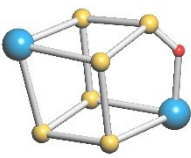
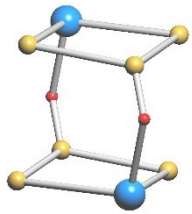




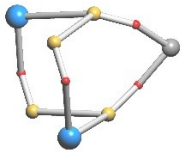
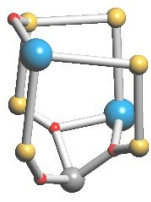
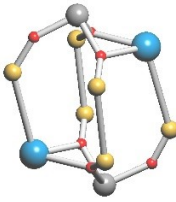
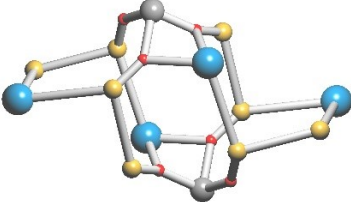




$3^2,4^2,6^2T18$ (Imandrite)				
Face symbol:	$[4^3]$	$[4^2.6^2]$	$[6.7^2]$	$[4^2.5^4]$
				
V, E, F: Label:	(5, 6, 3) t-kzd 	(8, 10, 4) t-lov 	(9, 10, 3) t-ukc 	(10, 14, 6) t-bru 
Face symbol:	$[4.5.7.8^2]$	$[8^3]$	$[4^2.8^4]$	
				
V, E, F: Label:	(13, 16, 5) t-unknown1 	(11, 12, 3) t-jnt-1 	(16, 20, 6) t-ste 	
TILING				
				

Table S6. Tiles for atomic net of the koashvite mineral with new topology obtained by means the geometrically-topological analysis.

$3^4,4^4,6^3$-c net New topology (Koashvite)				
Face symbol:	$[4^3]$	$[4^2.7^2]$	$[4^4.5^2]$	$[4^2.8^2]$
				
V, E, F: Label:	(5, 6, 3) t-kzd 	(9, 11, 4) t-unknown1 	(9, 13, 6) t-csv-1 	(10, 12, 4) t-kds 
Face symbol:	$[8^3]$	$[4.5.7.8^2]$	$[4^2.8^4]$	$[4^2.7^4.8^2]$
				
V, E, F: Label:	(11, 12, 3) t-jnt-1 	(13, 16, 5) t-unknown2 	(16, 20, 6) t-ste 	(20, 26, 8) t-unknown3 

TILING

