## **Supporting Information**

## Two-dimensional Mo<sub>1-x</sub>B<sub>2</sub> with ordered metal vacancies obtained for

## advanced thermoelectric applications based on first-principles

## calculations

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**Table S1.** Lattice Constants and bonds length of Mo<sub>1-x</sub>B<sub>2</sub> (x=0, 0.05, 0.10, 0.125, 0.15).

	a=b(Å)	c(Å)	B-B	Mo-Mo	Mo-B
$MoB_2$	10.271	23.720	1.708	2.986	2.221
$Mo_{0.95}B_2$	10.271	23.720	1.712	2.890	2.264
$Mo_{0.9}B_2$	10.271	23.720	1.701	2.830	2.178
$Mo_{0.875}B_2$	10.271	23.720	1.717	2.786	2.222
$Mo_{0.85}B_2$	10.271	23.720	1.728	2.774	2.123



Figure S1. Phonon spectra of  $MoB_2$  (a) and  $Mo_{0.9}B_2$  (b).



**Figure S2.** The orbital projection energy bands and the density of projected states of Mo in Mo<sub>1-</sub>  $_xB_2$ , with (a) x = 0.000, (b) x = 0.050, (c) x = 0.100, (d) x = 0.125, (e) x = 0.150 calculated by PBE.



Figure S3. Bonding analysis of Mo atoms. Partial orbitals diagram comparisons between MoB<sub>2</sub> and Mo<sub>0.9</sub>B<sub>2</sub>.



Figure S4. (a) The total energy of  $MoB_2$  is fitted along the a-axis direction, (b) the energy changes of electrons at valence band maximum (VBM), (c) the energy changes of holes at the conduction band minimum (CBM).



**Figure S5.** Thermoelectric parameters of *n*-type and *p*-type monolayer  $MoB_2$  varied with carrier concentration. (a) *n*-type ZT value, (b) *n*-type Seebeck coefficient, (c) *n*-type conductivity, (d) *n*-type power factor, (e) *p*-type ZT value, (f) *p*-type Seebeck coefficient, (g) *p*-type conductivity, (h) *p*-type power factor.



**Figure S6.** Thermoelectric parameters of *n*-type and *p*-type monolayer  $Mo_{0.95}B_2$  varied with carrier concentration. (a) *n*-type ZT value, (b) *n*-type Seebeck coefficient, (c) *n*-type conductivity, (d) *n*-type power factor, (e) *p*-type ZT value, (f) *p*-type Seebeck coefficient, (g) *p*-type conductivity, (h) *p*-type power factor.



**Figure S7.** Thermoelectric parameters of *n*-type and *p*-type monolayer  $Mo_{0.9}B_2$  varied with carrier concentration. (a) *n*-type ZT value, (b) *n*-type Seebeck coefficient, (c) *n*-type conductivity, (d) *n*-type power factor, (e) *p*-type ZT value, (f) *p*-type Seebeck coefficient, (g) *p*-type conductivity, (h) *p*-type power factor.



**Figure S8.** Thermoelectric parameters of *n*-type and *p*-type monolayer  $Mo_{0.875}B_2$  varied with carrier concentration. (a) *n*-type ZT value, (b) *n*-type Seebeck coefficient, (c) *n*-type conductivity, (d) *n*-type power factor, (e) *p*-type ZT value, (f) *p*-type Seebeck coefficient, (g) *p*-type conductivity, (h) *p*-type power factor.



**Figure S9.** Thermoelectric parameters of *n*-type and *p*-type monolayer  $Mo_{0.85}B_2$  varied with carrier concentration. (a) *n*-type ZT value, (b) *n*-type Seebeck coefficient, (c) *n*-type conductivity, (d) *n*-type power factor, (e) *p*-type ZT value, (f) *p*-type Seebeck coefficient, (g) *p*-type conductivity, (h) *p*-type power factor.