Supporting Information

Enhanced Electron Transport and Optical Properties of Experimentally Synthesized Monolayer Si₉C₁₅: A Comprehensive DFT Study for Nanoelectronics and Photocatalytic Applications

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Fig.S1 Evolution of band-edge positions of Si_9C_{15} as a function of applied uniaxial strain in -5%~5% in the direction a and b, respectively. The redox potentials for water oxidation and hydrogen reduction from pH = 0 to pH = 7 are marked as red and blue lines, respectively. The various symbols in the legend represent the positions of CBM and VBM at different strains, respectively.

OER and HER free energy theory

To calculate the Gibbs free energy ΔG in the OER and HER reaction processes, we have utilized the Gibbs free energy theory proposed by Nørskov et al., as follows^[1-4]:

$$\Delta G = \Delta E + \Delta E_{\rm ZPE} - T\Delta S + \Delta G_{\rm pH} + \Delta G_U$$

 ΔE represents the adsorption energy, while ΔE_{ZPE} and ΔS correspond to the differences in zero-point energy and entropy between the adsorbed state and the gas phase. All the E_{ZPE} and S results can be obtained from the reference^[5] and are shown in Table S1. $\Delta G_{\text{pH}}=0.059 \times$ pH is the free energy at different pH values, and $\Delta G_{\text{U}} = -eU$ represents an extra potential bias provided by an electron or hole relative to the normal hydrogen electrode.

The equation for HER is as follows:

$$* + \mathrm{H}^{+} + + \mathrm{e}^{-} \to \mathrm{H}^{*} \tag{S1}$$

$$^{*}H + H^{+} + +e^{-} \rightarrow * +H_{2}(g)$$
 (S2)

There are four steps involved in the conversion of H_2O into O_2 molecules in OER reaction:

$$H_20 + * \to 0H^* + H + +e^-$$
 (S3)

$$OH^* \to O^* + H + +e^- \tag{S4}$$

$$0^* + H_2 0 \to 00H^* + H + +e^-$$
 (S5)

$$00H^* \to *+0_2(g) + H + +e^-$$
 (S6)

where * denotes an adsorbed species, and OH*, O*, OOH*, and H* are the adsorbed intermediates.

The change in free energy of HER as a function of electrolyte pH can be expressed as:

$$\Delta G_1 = G_{\mathrm{H}^*} - \frac{1}{2}G_{\mathrm{H}_2} - G^* + 0.059 \times \mathrm{pH} - \mathrm{e}U \tag{S7}$$

$$\Delta G_2 = G^* + \frac{1}{2}G_{H_2} - G_{H^*} + 0.059 \times pH - eU$$
 (S8)

The potential of the photogenerated electrons for HER (U_e) is defined as the energy difference between the hydrogen reduction potential and the CBM of hydrogen evolution photocatalyst, thus U_e = eU-0.059×pH. For OER:

$$\Delta G_3 = G_{\text{OH}^*} + \frac{1}{2}G_{\text{H}_2} - G_{\text{H}_2\text{O}} - G^* - 0.059 \times \text{pH} - \text{eU}$$
(S9)

$$\Delta G_4 = G_{0^*} + \frac{1}{2}G_{H_2} - G_{OH^*} - 0.059 \times \text{pH} - eU$$
 (S10)

$$\Delta G_5 = G_{\text{OOH}^*} + \frac{1}{2}G_{\text{H}_2} - G_{\text{H}_2\text{O}} - G_{\text{O}^*} - 0.059 \times \text{pH} - \text{eU}$$
(S11)

$$\Delta G_6 = 2G_{\rm H_2O} + G^* - \frac{3}{2}G_{\rm H_2} - G_{\rm OOH^*} + 4.92 - 0.059 \times \rm{pH} - eU \ (S12)$$

The potential of the photogenerated holes for OER (U_h) is defined as the energy difference between the VBM of oxygen evolution photocatalyst and the hydrogen reduction potential, thus $U_h=eU+0.059 \times pH$. The term 0.059 \times pH denotes the energetic contribution resulting from changes in the concentration of H^+ ions, while eU accounts for the impact of potential bias on all states. This involves the transfer of energy through the movement of an electron or a hole within the electrode, with *U* representing the electrode potential relative to the normal hydrogen electrode (NHE).

Table S1 The entropy and zero-point energy corrections are utilized to determine the free energy of reactants, products, and intermediate species that are adsorbed on catalysts^[5]. In the case of adsorbates, the ZPE values are averaged across all single atom catalyst systems as they exhibit a rather similar value.

Species	<i>T×S</i> (eV) (298K)	ZPE (eV)
H^{*}	0	0.17
O*	0	0.07
OH*	0	0.33
OOH*	0	0.43
$H_2(g)$	0.41	0.27
$H_2O(g)$	0.58	0.57

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