## **Supplementary Information**

## Origin of the $\rho^{\gamma}/T$ scaling of conductivity relaxation and water relaxation times in a mixture of water with protic ionic liquid

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Fig. S1. Semilog Plot of relaxation times vs. reciprocal T of 26 wt.% fraction of water in PPG400. Close and open circles indicate  $\alpha$ - and v-processes, respectively. Asterisks are the relaxation times of the "effective" relaxation obtained from the convolution procedure indicated by the Williams ansatz. Black and red symbols indicate isobaric scan done at P=0.1 and 500 MPa, respectively. Dotted lines are Arrhenius fits to the data in the glassy state. Figure reproduced from Ref.[S1] by permission from Elsevier.



Fig. S2. Comparison of electric loss modulus spectra recorded at different temperature and pressure combinations and constant loss peak frequency for procainamide HCl with data from Ref.[S2] replotted.



Fig. S3. Normalized M''(f) spectra of [Si-MIm][BF4] at different combinations of P and T to show co-invariance of  $\tau_{\alpha}$ ,  $\tau_{\beta}$ , and n at constant  $\tau_{\alpha}$ . Red open triangles (P=600 MPa, T=253 K). Blue circles (P=0.1 MPa, T=213 K). Green open squares (P=0.1 MPa, T=253 K). Blue and red lines are fits by Fourier transform of stretched exponential correlation function with n=0.43. The inset show

co-invariance at two more constant values of  $\tau_{\alpha}$ . Blue triangles are data at ambient pressure and T=218 and 208 K from right to left. Red filled circles are data at constant T=253 K and P=300 MPa and 500 MPa from right to left. The arrows indicate the locations of the logarithm of the primitive conductivity relaxation frequencies,  $\log f_0$ , which agree with the most probable  $\beta$ -conductivity relaxation frequencies within a factor of about 2. Figure reproduced from Ref.[S3] by permission from ACS.



Fig. S4. *T-P* superposition of loss spectra for 10% QN in tristyrene measured for different *T* and *P* combinations but the same  $\tau_{\alpha} = 0.67$  s. The line is a Fourier transformed of the Kohlrausch function with  $\beta_{KWW} \equiv (1-n) = 0.53$ . The results demonstrate the co-invariance of three quantities,  $\tau_{\alpha}$ , *n*, and  $\tau_{JG}$ , to widely different combinations of *T* and *P*. Data of Kessaire et al. [S4] replotted.

## References

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