

Supporting Information

**Layered $\text{CrO}_2 \cdot n\text{H}_2\text{O}$ as cathode material for aqueous zinc-ion
batteries: Ab initio study**

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Supplementary Note1

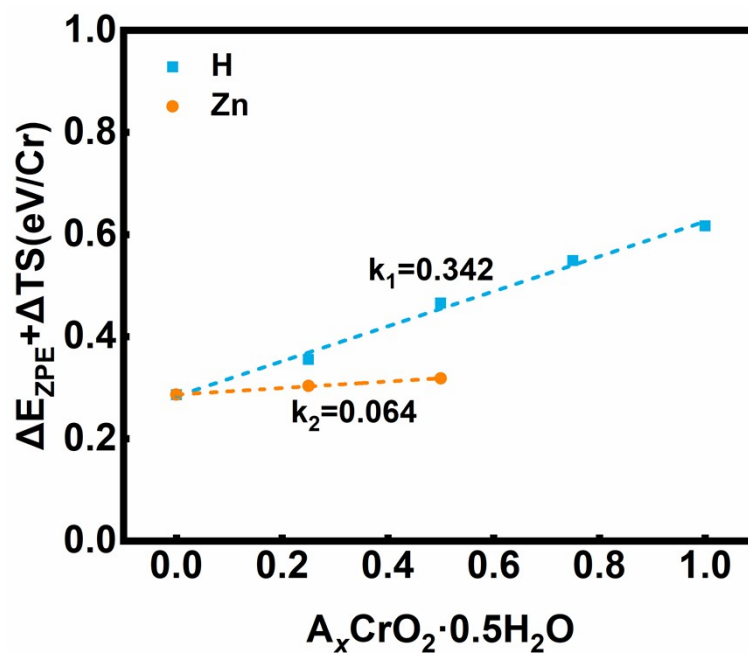


Fig. S1 The zero vibration energy (ΔE_{ZPE}) and entropy change (ΔS) of $A_x\text{CrO}_2 \cdot 0.5\text{H}_2\text{O}$ at 298.15 K

By comparing the energy added values (zero-point vibration energy (ΔE_{ZPE}) and entropy change (ΔS)) of the $A_x\text{CrO}_2 \cdot 0.5\text{H}_2\text{O}$ ($A=\text{H}/\text{Zn}$) structure at 298.15 K, it can be found that the slope corresponding to the H insertion process of the $\text{H}_y\text{CrO}_2 \cdot 0.5\text{H}_2\text{O}$ structure is 0.342, indicating that the additional value has a significant impact on H insertion mechanism. The slope of the $\text{Zn}_x\text{CrO}_2 \cdot 0.5\text{H}_2\text{O}$ structure during the Zn insertion process is only 0.064, indicating that the added value has a relatively small impact on the Zn insertion mechanism.

Supplementary Note1

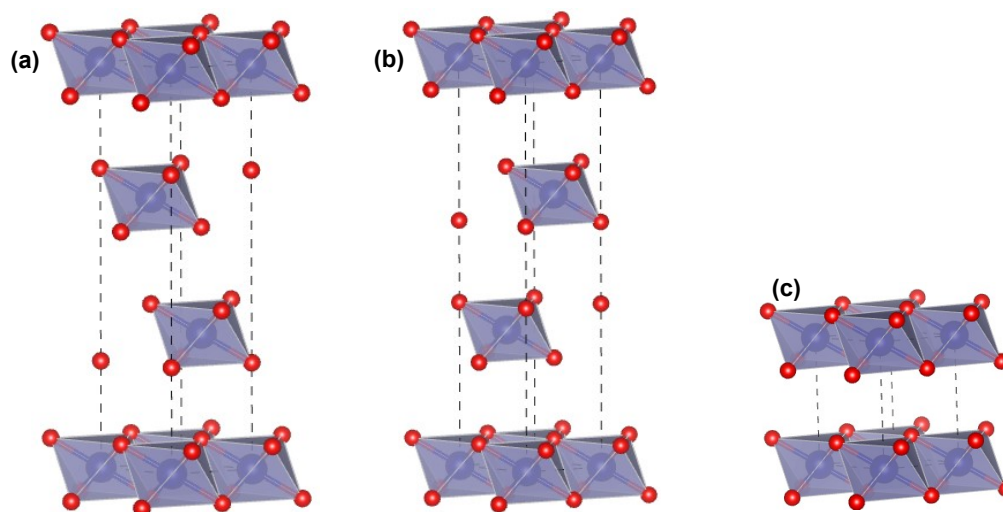


Fig. S2 Different stacking configurations of layered CrO_2 structures, (a) O3 stacking; (b) P3 stacking; (c) O1 stacking.

Table S1 The lattice parameters of different stacking structures under the interlayer interaction strategy are modified by DFT-D3(U)

Stacking type	Van der Waals	Lattice parameter (\AA)	E(meV/f.u.)
O1	DFT-D3(U)	$a=b=2.91, c=4.58$	—
	PBE	$a=b=2.92, c=14.90$	
	DFT-D3	$a=b=2.89, c=13.49$	
O3	DFT-D3(U)	$a=b=2.91, c=13.67$	$a=b=2.8797, c=14.169[1]$
	vdW-DF2(U)	$a=b=2.98, c=13.77$	
	opt86b-vdw(U)	$a=b=2.91, c=13.48$	
P3	DFT-D3(U)	$a=b=2.91, c=14.64$	$a=b=2.8578, c=14.002[2]$

The common stacking configurations of layered structures include O1, P3, and O3 stacking. The difference between the three structures is the lateral stacking displacement of the O-Cr-O layer, where oxygen atoms exhibit ABAB, ABBCA, and ABCABC stacking along the c-axis direction, respectively. By using different van der Waals correction methods to correct the interlayer spacing of O3- CrO_2 structure, it was found that the theoretical value was always smaller than the c-axis of the experimentally reported O3- CrO_2 structure, which may be related to the presence of a small amount of Na^+ between the CrO_2 layers ($\text{Na}_\delta\text{CrO}_2$)[1]. Therefore, the subsequent calculations were only optimized using the DFT-D3 (U) method.

Occupation site

For the Zn insertion mechanism, the non-equivalent sites occupied by Zn are the octahedral center (Zn_1) and tetrahedral center (Zn_2), with corresponding adsorption energies (E_{ad}) of -4.48 eV and -3.98 eV. Meanwhile, for the H insertion mechanism, the non-equivalent sites occupied by H in the O3-CrO₂ structure are lattice oxygen forming -OH bonds and pointing towards the octahedral center (H_1), octahedral center (H_2), and parallel tetrahedral center (H_3), respectively. The corresponding adsorption energies (E_{ad}) are -2.68 eV, 0.38 eV, and -2.39 eV. The non-equivalent sites occupied by H in the P3-CrO₂ structure are the interlayer hydrogen bonding (H_1), tetrahedral center (H_2), and hexagonal prism center (H_3) formed by H and lattice oxygen. The structural optimization of H located at the center of the hexagonal prism has not converged, and the corresponding adsorption energies (E_{ad}) for the latter two are -2.79 eV and 0.45 eV.

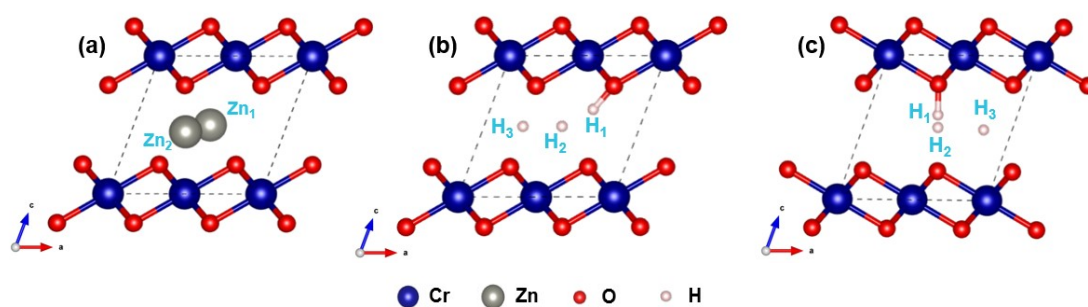


Fig. S3 For different reaction mechanisms, the non-equivalent sites occupied by the guest species in the CrO₂ structure, (a) Zn insertion; (b) H insertion (O3 stacking); (c) H insertion (P3 stacking)

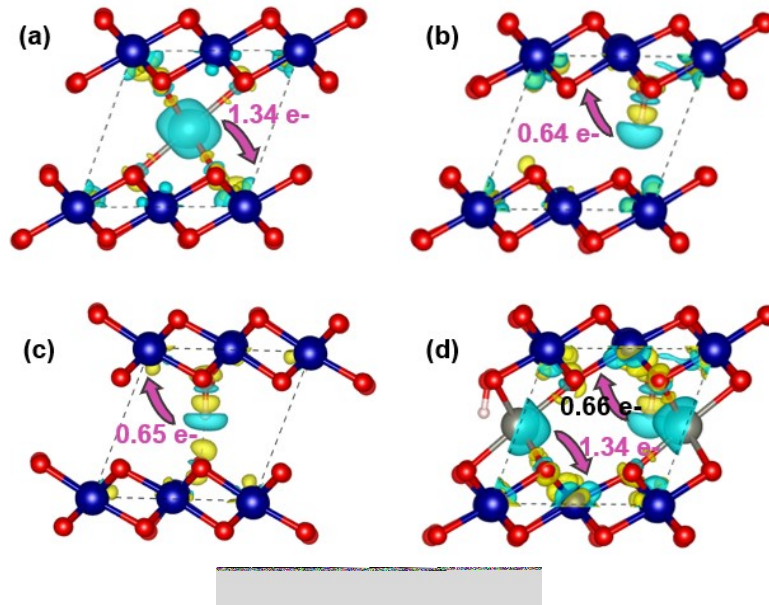


Fig. S4 The charge density differences between the guest ion and the substrate under different reaction mechanisms, (a) $\text{Zn}_{0.125}\text{CrO}_2$ (Zn insertion); (b) $\text{O}_3\text{-H}_{0.125}\text{CrO}_2$ (H insertion); (c) $\text{P}_3\text{-H}_{0.125}\text{CrO}_2$ (H insertion); (d) $\text{H}_{0.125}\text{Zn}_{0.125}\text{CrO}_2$ (H/Zn co-insertion). The green and yellow indicate electron depletion and aggregation, respectively, The isosurface is $0.01 \text{ electron}/\text{\AA}^3$.

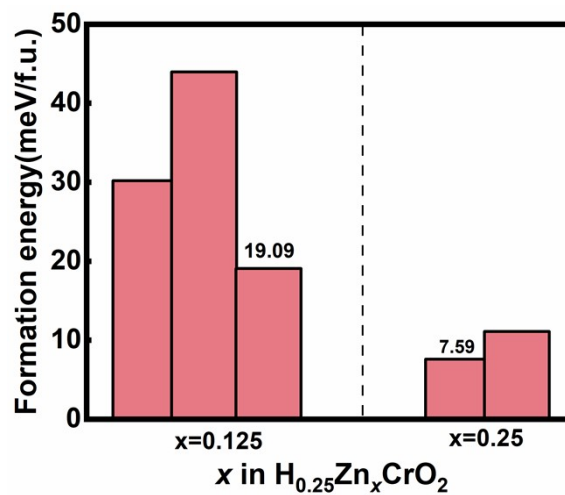


Fig. S5 The formation energy of different $\text{H}_{0.25}\text{Zn}_x\text{CrO}_2$ configurations

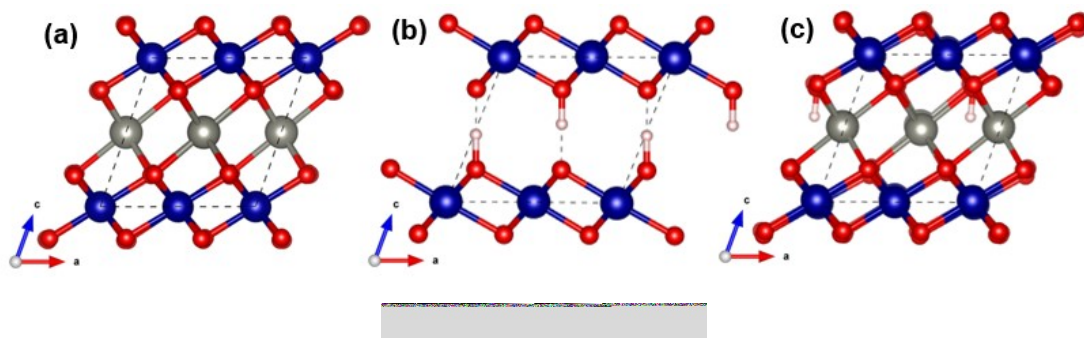


Fig. S6 The theoretical capacity of CrO₂ electrode is based on different reaction mechanisms, (a) Zn_{0.5}CrO₂ (Zn insertion); (b) P3-HCrO₂ (H insertion); (c) H_{0.125}Zn_{0.375}CrO₂ (H/Zn co-insertion).

H insertion mechanism

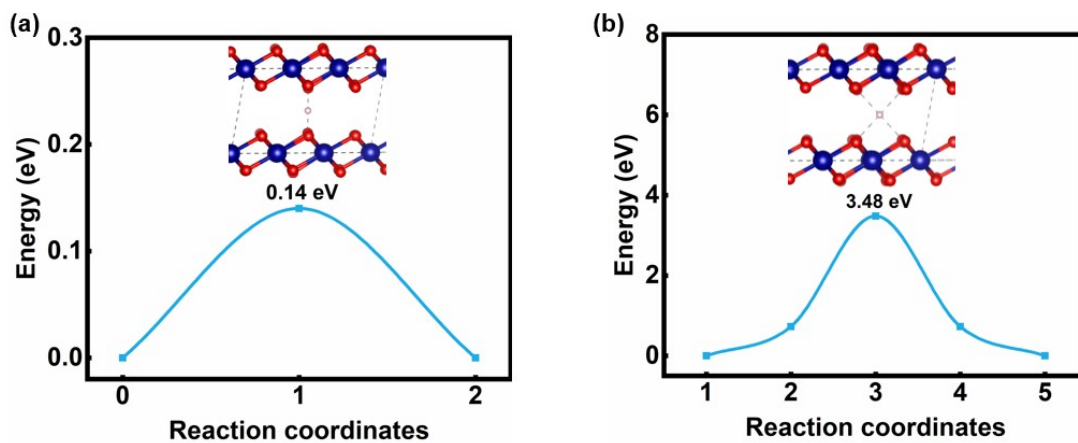


Fig. S7 The diffusion barrier and corresponding transition state model of H in P3-CrO₂ structure (a) Path 1 (Longitudinal jump); (b) Path 2 (Transverse diffusion)

H/Zn co-insertion mechanism

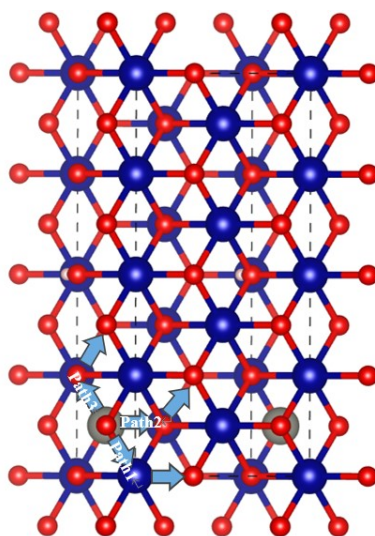


Fig. S8 The three diffusion paths of Zn at the CrO_2 electrode are under the H/Zn co-insertion mechanism

$\text{CrO}_2 \cdot n\text{H}_2\text{O}$ ($n=0.25\sim 1.0$)

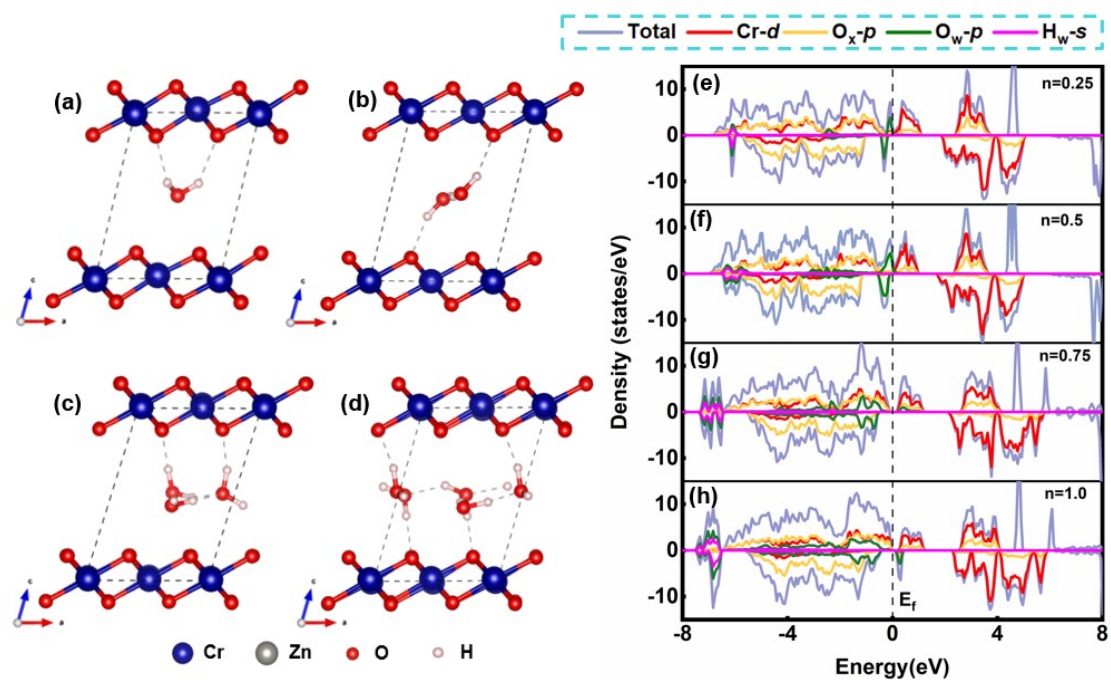


Fig. S9 The optimized pre-intercalation structure water model ($\text{CrO}_2 \cdot n\text{H}_2\text{O}$, (a-d)) and corresponding Density of states (e-h).

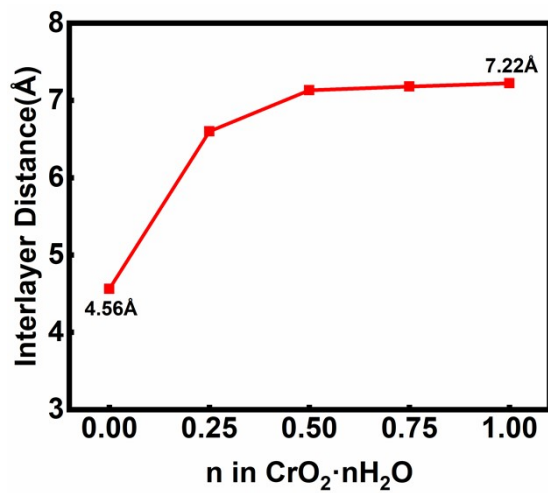


Fig. S10 The interlayer distance of CrO_2 electrodes after pre-intercalation into structural water ($n=0.25\sim 1.0$)

Zn insertion mechanism

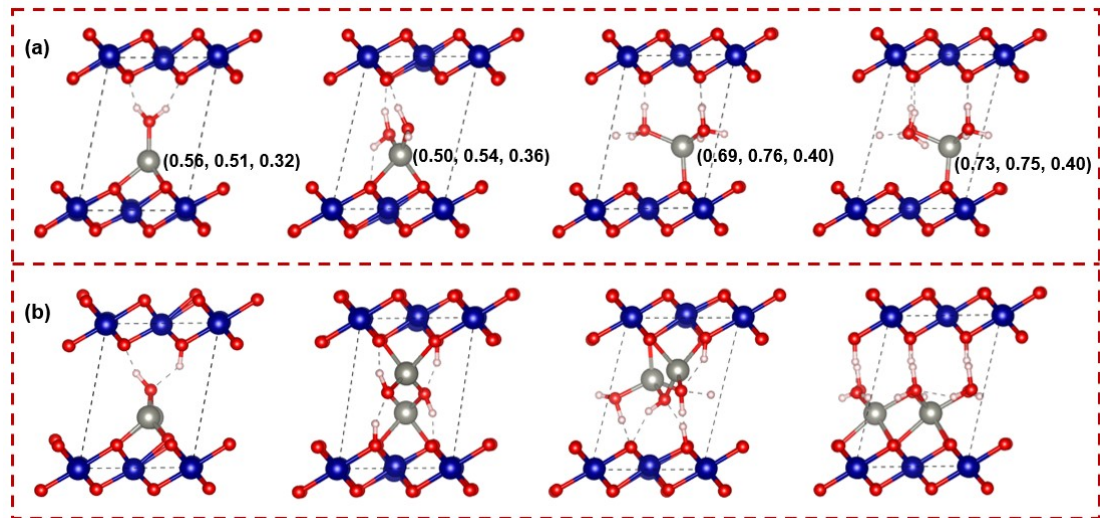


Fig. S11 The structural configurations for Zn intercalation in $(1 \times 2 \times 1)$ supercell of $\text{CrO}_2 \cdot n\text{H}_2\text{O}$ ($n=0.25, 0.5, 0.75, 1.0$) with different Zn concentrations (a) $c(\text{Zn})=0.25$; (b) $c(\text{Zn})=0.5$.

H insertion mechanism

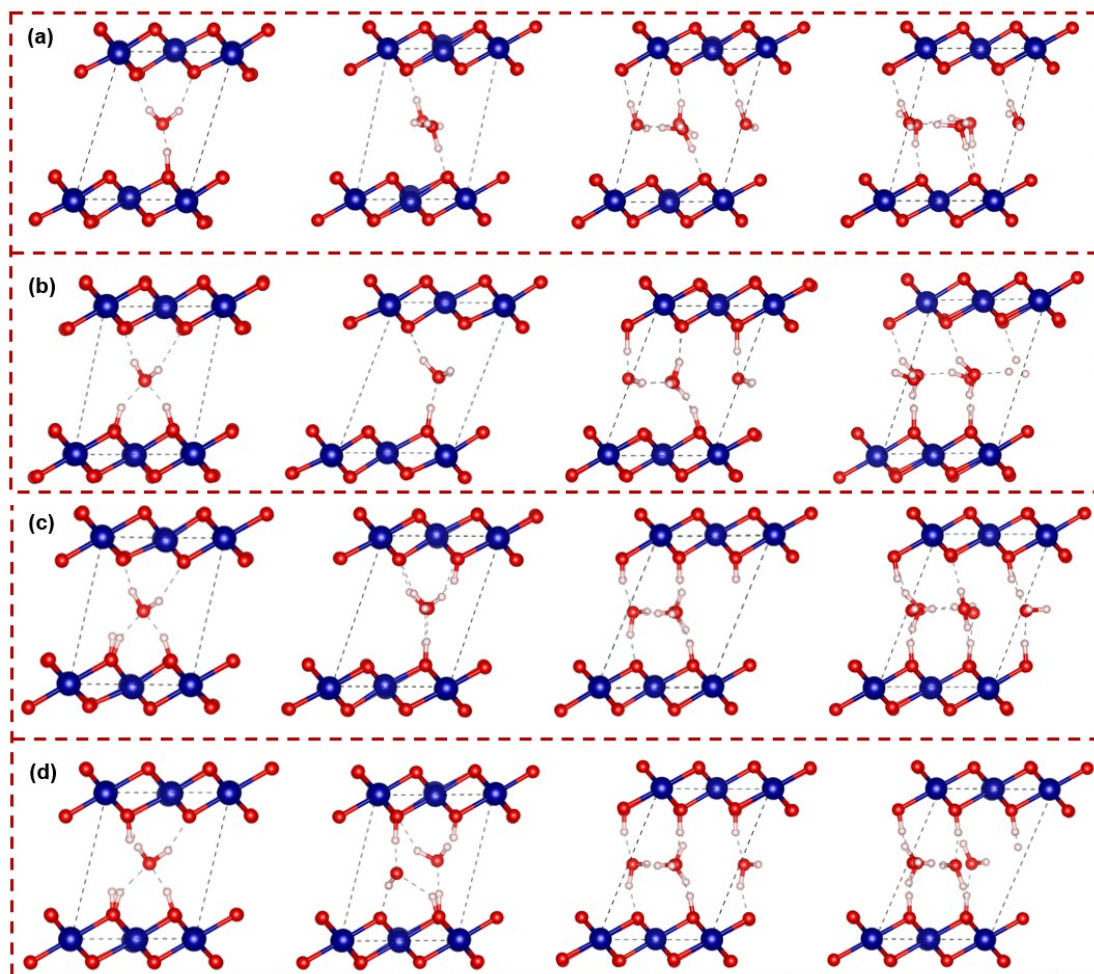


Fig. S12 The structural configurations for H inserted in $(1 \times 2 \times 1)$ supercell of $\text{CrO}_2 \cdot n\text{H}_2\text{O}$ ($n=0.25, 0.5, 0.75, 1.0$) with different H concentrations (a) $c(\text{H})=0.25$; (b) $c(\text{H})=0.5$; (c) $c(\text{H})=0.75$; (d) $c(\text{H})=1.0$.

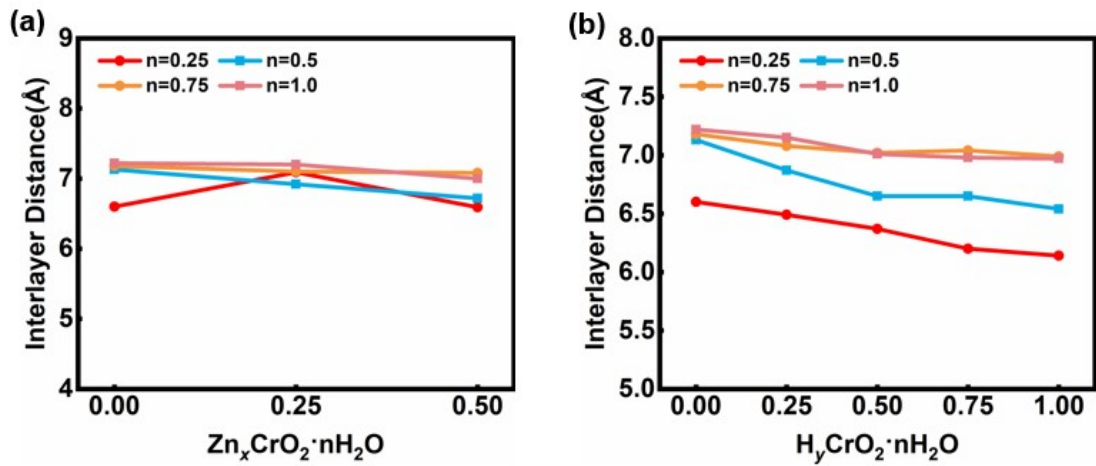


Fig. S13 The interlayer distance of $CrO_2 \cdot nH_2O$ at different insertion stages (a) Zn insertion mechanism; (b) H insertion mechanism.

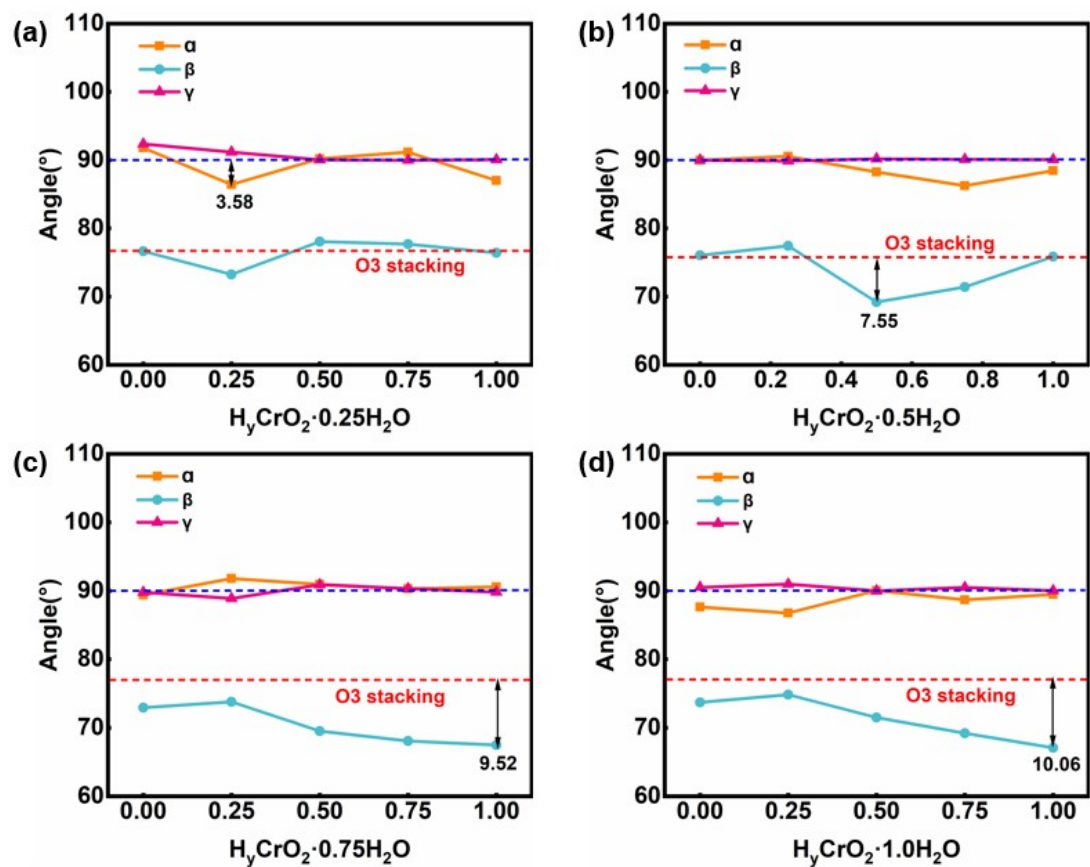


Fig. S14 The angle between the base vectors at different stages of H insertion in $H_yCrO_2 \cdot nH_2O$, (a) $n=0.25$; (b) $n=0.5$; (c) $n=0.75$; (d) $n=1.0$.

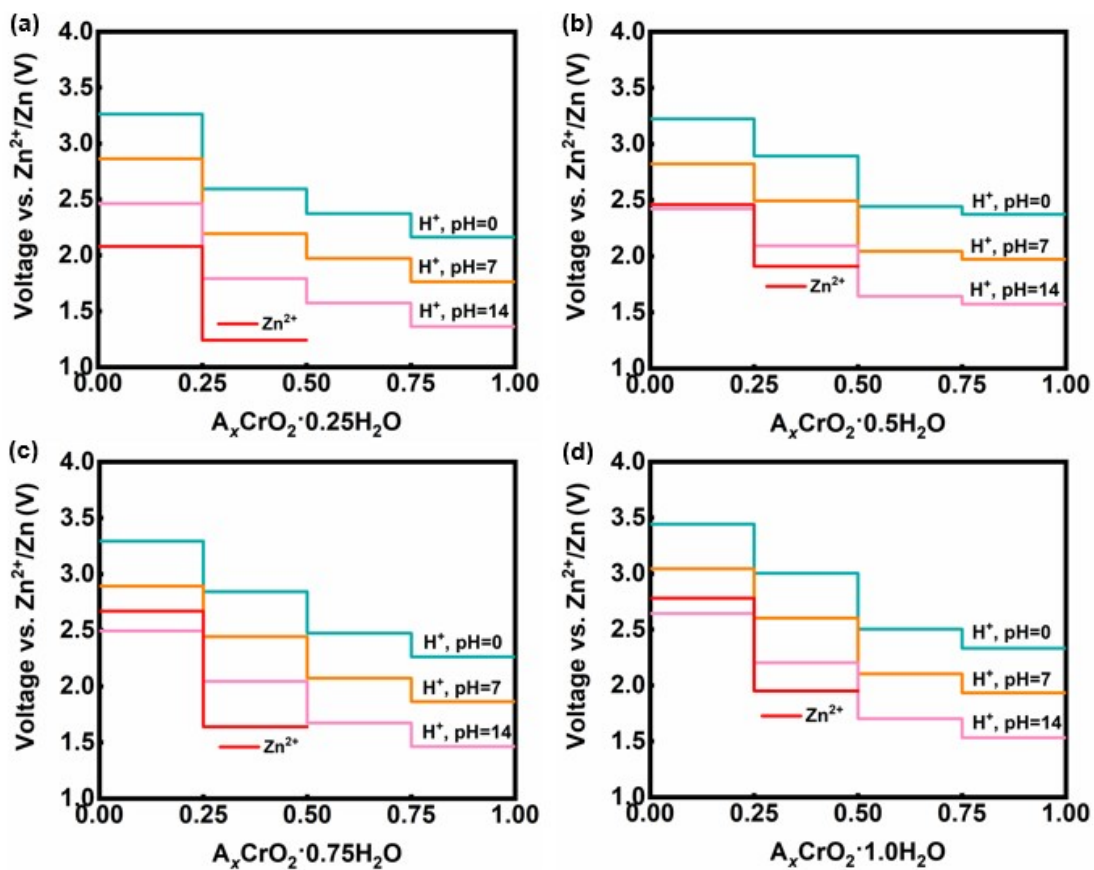


Fig. S15 Discharge curves of Zn^{2+} (red) and H^+ (based on different pH values) insertion/extraction process in $\text{CrO}_2 \cdot n\text{H}_2\text{O}$ ($n=0.0\sim 1.0$).

H/Zn co-insertion mechanism

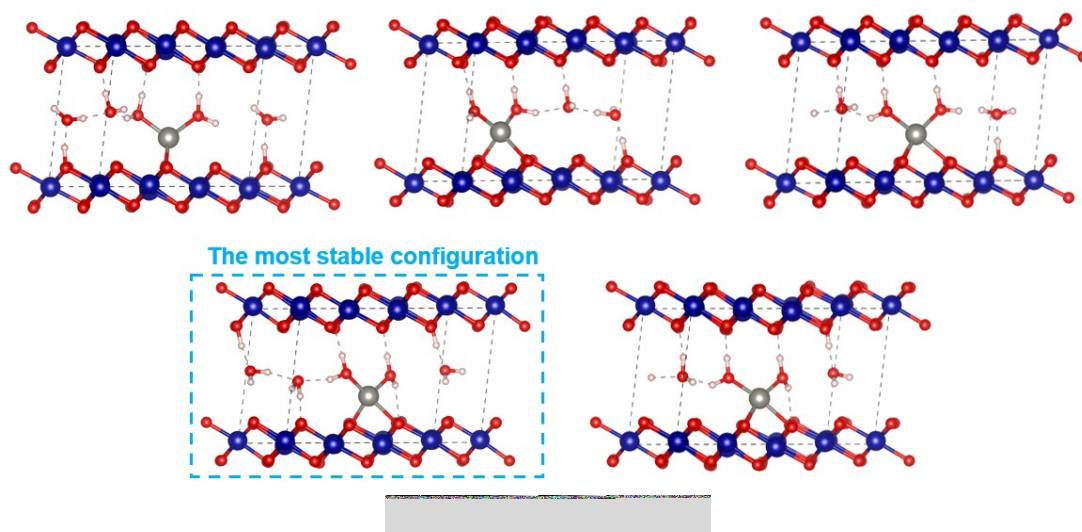


Fig. S16 The various optimized configurations of $\text{H}_{0.125}\text{Zn}_{0.125}\text{CrO}_2 \cdot 0.5\text{H}_2\text{O}$ (H/Zn co-insertion mechanism)

Table S2 Lattice parameters and volumes of $\text{CrO}_2 \cdot n\text{H}_2\text{O}$ and $\text{Zn}_x\text{CrO}_2 \cdot n\text{H}_2\text{O}$ configurations

c(H ₂ O)	lattice parameter						volume
	a	b	c	α	β	γ	
	Å			o			Å ³
0	5.048	5.828	4.853	90	69.72	90	133.929
0.25	5.004	5.924	6.836	91.79	76.64	92.36	196.962
x=0.25	5.143	5.92	7.372	93.65	78.01	89.83	219.075
x=0.5	5.214	6.012	6.828	84.43	78.66	89.77	208.820
0.5	5.184	5.677	7.45	90	76.055	90	212.807
x=0.25	5.133	5.909	7.192	84.94	76.55	90.96	211.188
x=0.5	5.183	6.058	6.853	90	82.44	90	213.344
0.75	5.145	5.832	7.52	89.39	72.93	89.78	215.576
x=0.25	5.107	5.954	7.336	88.70	77.07	89.42	217.417
x=0.5	5.241	6.051	7.317	86.63	76.24	91.55	224.818
1.0	5.207	5.821	7.560	87.63	73.69	90.50	219.693
x=0.25	5.137	5.955	7.308	87.95	78.23	91.53	221.476
x=0.5	5.235	6.061	7.235	90.03	76.47	89.99	223.186

Table S3 Lattice parameters and volumes of $\text{CrO}_2 \cdot n\text{H}_2\text{O}$ and $\text{H}_y\text{CrO}_2 \cdot n\text{H}_2\text{O}$ configurations

c(H ₂ O)	lattice parameter						volume
	a	b	c	α	β	γ	
	Å			o			Å ³
0	5.048	5.828	4.853	90	69.72	90	133.929
0.25	5.004	5.924	6.836	91.79	76.64	92.36	196.962
y=0.25	5.042	5.963	6.878	86.42	73.25	91.18	197.449
y=0.5	5.105	6.008	6.536	90.21	78.07	90.04	196.144
y=0.75	5.187	6.053	6.414	91.17	77.69	89.98	196.736
y=1.0	5.267	6.093	6.411	87.02	76.43	90.06	199.719
0.5	5.184	5.677	7.45	90	76.055	90	212.807
y=0.25	5.155	5.795	7.159	90.56	77.44	89.87	208.743
y=0.5	5.146	5.962	7.224	88.26	69.19	90.19	207.033
y=0.75	5.244	5.998	7.143	86.25	71.40	90.11	212.420
y=1.0	5.261	6.079	6.788	88.46	75.84	90.08	210.399
0.75	5.145	5.832	7.52	89.39	72.93	89.78	215.576
y=0.25	5.124	5.85	7.472	91.79	73.79	88.88	214.901
y=0.5	5.124	5.998	7.427	90.95	69.52	90.88	213.819
y=0.75	5.201	6.04	7.578	90.29	68.06	90.32	220.825
y=1.0	5.253	6.101	7.558	90.58	67.47	89.82	223.739
1.0	5.207	5.821	7.560	87.63	73.69	90.50	219.693
y=0.25	5.179	5.829	7.476	86.75	74.84	90.97	217.392
y=0.5	5.209	5.941	7.445	90.03	71.49	90.00	218.542
y=0.75	5.239	6.024	7.498	88.68	69.20	90.49	221.109
y=1.0	5.269	6.108	7.604	89.48	67.09	90.02	225.444

References

- [1] S.-H. Bo, X. Li, A.J. Toumar, and G. Ceder, *Chemistry of Materials*, 2016, 28, 1419-1429.
- [2] X. Xia, and J.R. Dahn, *Electrochemical and Solid-State Letters*, 2012, 15.