Intermolecular interaction potential maps from energy decomposition for interpreting reactivity and intermolecular interactions

Amin Kiani,^{†,‡} Wentong Zhou,^{†,‡} and Lawrence M. Wolf^{*,†}

†Department of Chemistry, University of Massachusetts, Lowell, MA, 01854,

United States

 \ddagger These authors contributed equally to this work

E-mail: lawrence_wolf@uml.edu

List of Figures

Figure S1. $\Delta E_{\rm orb}$ surfaces of aniline generated using	a $\mathrm{CH_3}^+$ probe within the
(a) NOCV-ETS EDA and (b) LMO-EDA framework	ork framework (r ² -SCAN);
(c) The ball-stick model of the Barnase-Barstar pro	tein complex (left) and its
corresponding $\Delta E_{\rm int}$ surface generated with Li ⁺ p	probe within the xTB-iFF
framework (right).	
Figure S2. Probes and their geometries. Blue arrows ind	licate the alignment/orientation
of probes toward the surface	
Figure S3. Spherical grid generated around benzene u	sing the Fibonacci sphere
algorithm.	
Figure S4. Overview of methodology for IMIP map ge	neration (a) structure op-
timization (b) grid generation (c) preliminary isode	ensity selection (d) volume
element construction (e) volume element search (f) final filtration (g) probe
positioning and orientation (h) EDA calculation (i)	surface generation (units:
kcal/mol)	
Figure S5. $\Delta E_{\text{int}}, \Delta E_{\text{elec}}, \text{ and } \Delta E_{\text{orb}} \text{ surfaces of aniline g}$	cenerated at the r^2 SCAN/def2-
SVP, r^2 SCAN/def2-TZVP, and B3LYP/def2-SVP	level of theory, within the
LMO-EDA framework	
Figure S6. ΔE_{int} , ΔE_{elec} , and ΔE_{orb} surfaces of aniling	ne (first and second rows)
with $\mathrm{CH_3}^+$ probe, and benzene (third and fourth	rows) with stacked C_6H_6
probe. xTB scans (first and third rows), DFT scan	s (second and fourth rows). 16
Figure S7. $\Delta E_{\text{int}}, \Delta E_{\text{elec}}, \Delta E_{\text{orb}}, \Delta E_{\text{ex-rep}}, \text{ and } \Delta E_{\text{dis}}$	
	$_{\rm p-corr}$ surfaces of benzene,
naphthalene, anthracene, phenanthrene, and tetrac	$_{p-corr}$ surfaces of benzene, ene; Ag ⁺ probe 19
naphthalene, anthracene, phenanthrene, and tetrac Figure S8. $\Delta E_{\text{int}}, \Delta E_{\text{elec}}, \Delta E_{\text{orb}}, \Delta E_{\text{ex-rep}}, \text{ and } \Delta E_{\text{dis}}$	$_{p-corr}$ surfaces of benzene, ene; Ag ⁺ probe
naphthalene, anthracene, phenanthrene, and tetrac Figure S8. $\Delta E_{\text{int}}, \Delta E_{\text{elec}}, \Delta E_{\text{orb}}, \Delta E_{\text{ex-rep}}, \text{ and } \Delta E_{\text{dis}}$ naphthalene, anthracene, phenanthrene, and tetrac	$_{p-corr}$ surfaces of benzene, eene; Ag ⁺ probe 19 $_{p-corr}$ surfaces of benzene, eene; Be ²⁺ probe 20
naphthalene, anthracene, phenanthrene, and tetrac Figure S8. $\Delta E_{\text{int}}, \Delta E_{\text{elec}}, \Delta E_{\text{orb}}, \Delta E_{\text{ex-rep}}, \text{ and } \Delta E_{\text{dis}}$ naphthalene, anthracene, phenanthrene, and tetrac Figure S9. $\Delta E_{\text{int}}, \Delta E_{\text{elec}}, \Delta E_{\text{orb}}, \Delta E_{\text{ex-rep}}, \text{ and } \Delta E_{\text{dis}}$	$_{p-corr}$ surfaces of benzene, eene; Ag ⁺ probe

Figure S10. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of benzene,	
naphthalene, anthracene, phenanthrene, and tetracene; \mathbf{K}^+ probe. $\ .$	22
Figure S11. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of benzene,	
naphthalene, anthracene, phenanthrene, and tetracene; Li^+ probe	23
Figure S12. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of benzene,	
naphthalene, anthracene, phenanthrene, and tetracene; ${\rm Mg}^{2+}$ probe	24
Figure S13. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of benzene,	
naphthalene, anthracene, phenanthrene, and tetracene; Na $^+$ probe	25
Figure S14. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of benzene,	
naphthalene, anthracene, phenanthrene, and tetracene; Zn^{2+} probe	26
Figure S15. $\Delta E_{\text{int}}, \Delta E_{\text{elec}}, \Delta E_{\text{orb}}, \Delta E_{\text{ex-rep}}, \text{ and } \Delta E_{\text{disp-corr}}$ surfaces of bromoben-	
zene with Li^+ , Na^+ , K^+ , Be^{2+} probes.	28
Figure S16. $\Delta E_{\text{int}}, \Delta E_{\text{elec}}, \Delta E_{\text{orb}}, \Delta E_{\text{ex-rep}}, \text{ and } \Delta E_{\text{disp-corr}}$ surfaces of bromoben-	
zene with Mg^{2+} , Ca^{2+} , Ag^+ , Zn^{2+} probes	29
Figure S17. $\Delta E_{\text{int}}, \Delta E_{\text{elec}}, \Delta E_{\text{orb}}, \Delta E_{\text{ex-rep}}, \text{ and } \Delta E_{\text{disp-corr}}$ surfaces of trifluorotoluene	ļ
with Li^+ , Na^+ , K^+ , Be^{2+} probes	30
Figure S18. $\Delta E_{\text{int}}, \Delta E_{\text{elec}}, \Delta E_{\text{orb}}, \Delta E_{\text{ex-rep}}, \text{ and } \Delta E_{\text{disp-corr}} \text{ surfaces of trifluorotoluene}$	ļ
with Mg^{2+} , Ca^{2+} , Ag^+ , Zn^{2+} probes	31
Figure S19. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of toluene	
with Li^+ , Na^+ , K^+ , Be^{2+} probes	32
Figure S20. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of toluene	
with Mg^{2+} , Ca^{2+} , Ag^+ , Zn^{2+} probes	33
Figure S21. $\Delta E_{\text{int}}, \Delta E_{\text{elec}}, \Delta E_{\text{orb}}, \Delta E_{\text{ex-rep}}, \text{ and } \Delta E_{\text{disp-corr}}$ surfaces of chlorobenzene	
with Li^+ , Na^+ , K^+ , Be^{2+} probes	34
Figure S22. $\Delta E_{\text{int}}, \Delta E_{\text{elec}}, \Delta E_{\text{orb}}, \Delta E_{\text{ex-rep}}, \text{ and } \Delta E_{\text{disp-corr}} \text{ surfaces of chlorobenzene}$	
with Mg^{2+} , Ca^{2+} , Ag^+ , Zn^{2+} probes	35

Figure S23. $\Delta E_{\text{int}}, \Delta E_{\text{elec}}, \Delta E_{\text{orb}}, \Delta E_{\text{ex-rep}}, \text{ and } \Delta E_{\text{disp-corr}}$ surfaces of benzaldehyde	
with Li^+ , Na^+ , K^+ , Be^{2+} probes	36
Figure S24. $\Delta E_{\text{int}}, \Delta E_{\text{elec}}, \Delta E_{\text{orb}}, \Delta E_{\text{ex-rep}}, \text{ and } \Delta E_{\text{disp-corr}}$ surfaces of benzaldehyde	
with Mg^{2+} , Ca^{2+} , Ag^+ , Zn^{2+} probes	37
Figure S25. $\Delta E_{\text{int}}, \Delta E_{\text{elec}}, \Delta E_{\text{orb}}, \Delta E_{\text{ex-rep}}, \text{ and } \Delta E_{\text{disp-corr}}$ surfaces of benzonitrile	
with Li^+ , Na^+ , K^+ , Be^{2+} probes.	38
Figure S26. $\Delta E_{\text{int}}, \Delta E_{\text{elec}}, \Delta E_{\text{orb}}, \Delta E_{\text{ex-rep}}, \text{ and } \Delta E_{\text{disp-corr}}$ surfaces of benzonitrile	
with Mg^{2+} , Ca^{2+} , Ag^+ , Zn^{2+} probes	39
Figure S27. $\Delta E_{\text{int}}, \Delta E_{\text{elec}}, \Delta E_{\text{orb}}, \Delta E_{\text{ex-rep}}, \text{ and } \Delta E_{\text{disp-corr}}$ surfaces of ethylbenzene	
with Li^+ , Na^+ , K^+ , Be^{2+} probes	40
Figure S28. $\Delta E_{\text{int}}, \Delta E_{\text{elec}}, \Delta E_{\text{orb}}, \Delta E_{\text{ex-rep}}, \text{ and } \Delta E_{\text{disp-corr}}$ surfaces of ethylbenzene	
with Mg^{2+} , Ca^{2+} , Ag^+ , Zn^{2+} probes	41
Figure S29. $\Delta E_{\text{int}}, \Delta E_{\text{elec}}, \Delta E_{\text{orb}}, \Delta E_{\text{ex-rep}}, \text{ and } \Delta E_{\text{disp-corr}}$ surfaces of fluorobenzene	
with Li^+ , Na^+ , K^+ , Be^{2+} probes.	42
Figure S30. $\Delta E_{\text{int}}, \Delta E_{\text{elec}}, \Delta E_{\text{orb}}, \Delta E_{\text{ex-rep}}, \text{ and } \Delta E_{\text{disp-corr}}$ surfaces of fluorobenzene	
with Mg^{2+} , Ca^{2+} , Ag^+ , Zn^{2+} probes	43
Figure S31. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of cumene	
with Li^+ , Na^+ , K^+ , Be^{2+} probes	44
Figure S32. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of cumene	
with Mg^{2+} , Ca^{2+} , Ag^+ , Zn^{2+} probes	45
Figure S33. $\Delta E_{\text{int}}, \Delta E_{\text{elec}}, \Delta E_{\text{orb}}, \Delta E_{\text{ex-rep}}, \text{ and } \Delta E_{\text{disp-corr}}$ surfaces of acetanilide	
with Li^+ , Na^+ , K^+ , Be^{2+} probes	46
Figure S34. $\Delta E_{\text{int}}, \Delta E_{\text{elec}}, \Delta E_{\text{orb}}, \Delta E_{\text{ex-rep}}, \text{ and } \Delta E_{\text{disp-corr}}$ surfaces of acetanilide	
with Mg^{2+} , Ca^{2+} , Ag^+ , Zn^{2+} probes	47
Figure S35. $\Delta E_{\text{int}}, \Delta E_{\text{elec}}, \Delta E_{\text{orb}}, \Delta E_{\text{ex-rep}}, \text{ and } \Delta E_{\text{disp-corr}}$ surfaces of aniline with	
Li^+, Na^+, K^+, Be^{2+} probes	48

Figure S36. $\Delta E_{\text{int}}, \Delta E_{\text{elec}}, \Delta E_{\text{orb}}, \Delta E_{\text{ex-rep}}, \text{ and } \Delta E_{\text{disp-corr}}$ surfaces of aniline with	
$Mg^{2+}, Ca^{2+}, Ag^+, Zn^{2+}$ probes	49
Figure S37. $\Delta E_{\text{int}}, \Delta E_{\text{elec}}, \Delta E_{\text{orb}}, \Delta E_{\text{ex-rep}}, \text{ and } \Delta E_{\text{disp-corr}}$ surfaces of nitrobenzene	
with Li^+ , Na^+ , K^+ , Be^{2+} probes	50
Figure S38. $\Delta E_{\text{int}}, \Delta E_{\text{elec}}, \Delta E_{\text{orb}}, \Delta E_{\text{ex-rep}}, \text{ and } \Delta E_{\text{disp-corr}}$ surfaces of nitrobenzene	
with Mg^{2+} , Ca^{2+} , Ag^+ , Zn^{2+} probes	51
Figure S39. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of anisole	
with Li^+ , Na^+ , K^+ , Be^{2+} probes	52
Figure S40. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of anisole	
with Mg^{2+} , Ca^{2+} , Ag^+ , Zn^{2+} probes	53
Figure S41. $\Delta E_{\text{int}}, \Delta E_{\text{elec}}, \Delta E_{\text{orb}}, \Delta E_{\text{ex-rep}}, \text{ and } \Delta E_{\text{disp-corr}} \text{ surfaces of phenyl-acetate}$	е
with Li^+ , Na^+ , K^+ , Be^{2+} probes	54
Figure S42. $\Delta E_{\text{int}}, \Delta E_{\text{elec}}, \Delta E_{\text{orb}}, \Delta E_{\text{ex-rep}}, \text{ and } \Delta E_{\text{disp-corr}} \text{ surfaces of phenyl-acetated}$	е
with Mg^{2+} , Ca^{2+} , Ag^+ , Zn^{2+} probes	55
Figure S43. $\Delta E_{\text{int}}, \Delta E_{\text{elec}}, \Delta E_{\text{orb}}, \Delta E_{\text{ex-rep}}, \text{ and } \Delta E_{\text{disp-corr}} \text{ surfaces of phenol with}$	
Li^+, Na^+, K^+, Be^{2+} probes	56
Figure S44. $\Delta E_{\text{int}}, \Delta E_{\text{elec}}, \Delta E_{\text{orb}}, \Delta E_{\text{ex-rep}}, \text{ and } \Delta E_{\text{disp-corr}}$ surfaces of phenol with	
$Mg^{2+}, Ca^{2+}, Ag^+, Zn^{2+}$ probes	57
Figure S45. $\Delta E_{\text{int}}, \Delta E_{\text{elec}}, \Delta E_{\text{orb}}, \Delta E_{\text{ex-rep}}, \text{ and } \Delta E_{\text{disp-corr}}$ surfaces of n-propylbenzer	ne
with Li^+ , Na^+ , K^+ , Be^{2+} probes	58
Figure S46. $\Delta E_{\text{int}}, \Delta E_{\text{elec}}, \Delta E_{\text{orb}}, \Delta E_{\text{ex-rep}}, \text{ and } \Delta E_{\text{disp-corr}}$ surfaces of n-propylbenzer	ne
with Mg^{2+} , Ca^{2+} , Ag^+ , Zn^{2+} probes	59
Figure S47. $\Delta E_{\text{int}}, \Delta E_{\text{elec}}, \Delta E_{\text{orb}}, \Delta E_{\text{ex-rep}}, \text{ and } \Delta E_{\text{disp-corr}}$ surfaces of benzenesulfonial	c acid
with Li^+ , Na^+ , K^+ , Be^{2+} probes	60
Figure S48. $\Delta E_{\text{int}}, \Delta E_{\text{elec}}, \Delta E_{\text{orb}}, \Delta E_{\text{ex-rep}}, \text{ and } \Delta E_{\text{disp-corr}}$ surfaces of benzenesulfonial	c acid
with Mg^{2+} , Ca^{2+} , Ag^+ , Zn^{2+} probes	61

Figure S49. $\Delta E_{\text{int}}, \Delta E_{\text{elec}}, \Delta E_{\text{orb}}, \Delta E_{\text{ex-rep}}, \text{ and } \Delta E_{\text{disp-corr}} \text{ surfaces of tert-butylben}$	zene
with Li^+ , Na^+ , K^+ , Be^{2+} probes	62
Figure S50. $\Delta E_{\text{int}}, \Delta E_{\text{elec}}, \Delta E_{\text{orb}}, \Delta E_{\text{ex-rep}}, \text{ and } \Delta E_{\text{disp-corr}} \text{ surfaces of tert-butylben}$	zene
with Mg^{2+} , Ca^{2+} , Ag^+ , Zn^{2+} probes	63
Figure S51. ΔE_{int} , ΔE_{elec} , and ΔE_{orb} surfaces of variable benzene derivatives with	
Na^+ probes. A constant scale is used to demonstrate substituent effects on	
energetics.	64
Figure S52. Hammett plots of benzene derivatives illustrating the relationships	
between different energy terms and σ_{total} : (1) ΔE_{elec} vs. σ_{total} and (2) ΔE_{int}	
vs. σ_{total}	66
Figure S53. $\Delta E_{\text{int}}, \Delta E_{\text{elec}}, \Delta E_{\text{orb}}, \Delta E_{\text{ex-rep}}, \text{ and } \Delta E_{\text{disp-corr}}$ surfaces of hexflouroben-	
zene with F^-, Cl^-, Br^-, I^- probes	68
Figure S54. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of 1,2,4,5-	
tetracyanobenzene with F^-, Cl^-, Br^-, I^- probes	69
Figure S55. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of 1,3,5-	
trinitrobenzene with F^-, Cl^-, Br^-, I^- probes.	70
Figure S56. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of triazine	
with F^- , Cl^- , Br^- , I^- probes	71
Figure S57. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of trifluo-	
roazine with F^- , Cl^- , Br^- , I^- probes.	72
Figure S58. Most favorable interaction energies mapped onto each atom within	
the allyl portion of the Pd-allyl transition metal complexes, selecting and	
mapping the most favorable interaction within the region of each atom for:	
(a) unsubstituted, (b) methoxy-substituted, (c) methyl-substituted, and (d)	
1-methoxy-3-methyl configurations.	73

List of Tables

Table S1. ΔE_{int} , ΔE_{elec} , and ΔE_{orb} (kcal/mol) and σ^+ values of variable mono-	
substituted benzene derivatives (and benzene). Energies were obtained at the	
para-positions of the π systems	17
Table S2. Isodensities of various cation probes based on optimized interactions	
with benzene	18
Table S3. σ_{para} , σ_{meta} , and σ_{total} values for various benzene derivatives	65
Table S4. Isodensities of various anion probes based on optimized interactions	
with benzene	67

1. IMIP surfaces generated using NOCV-ETS and xTB-iff EDA

Depicted in **Figure S1** are surfaces generated using the NOCV-ETS EDA and xTB-IFF EDA schemes for comparison. The provided surfaces are of aniline using a CH_3^+ probe. The ortho- and para-regions of aniline (excluding the amino nitrogen) are identified as the most favorable interaction sites on both surfaces. This aligns with experimental observations and demonstrates qualitative consistency between the two EDA methods. As expected, some minor quantitative differences can be traced to differences in the two decomposition schemes. Furthermore, a brief introduction to both these methods is presented here:

Within the xTB-IFF EDA scheme, the total interaction energy (ΔE_{int}) of two systems can be divided into repulsion (ΔE_{rep}) , electrostatic (ΔE_{elec}) , dispersion (ΔE_{disp}) , induction (ΔE_{ind}) , and charge transfer (ΔE_{CT}) energies.

In the NOCV-ETS EDA scheme implemented in Orca, the total interaction energy can be divided into distortion(ΔE_{dist}), electrostatic (ΔE_{elec}), Pauli repulsion (ΔE_{rep}), and orbital interaction (ΔE_{orb}). The orbital interaction can be further decomposed using eigenvalue pairs derived from the deformed density matrix. This analysis offers insights into the nature of bonding, revealing regions of electron density depletion and gain. From this gain or depletion of electron density, the degree and energetics of bonding and back-bonding interactions between the fragments can be determined.



Figure S1. $\Delta E_{\rm orb}$ surfaces of aniline generated using a CH₃⁺ probe within the (a) NOCV-ETS EDA and (b) LMO-EDA framework framework (r²-SCAN); (c) The ball-stick model of the Barnase-Barstar protein complex (left) and its corresponding $\Delta E_{\rm int}$ surface generated with Li⁺ probe within the xTB-iFF framework (right).

2. Variable probes and their usages

A variety of probes designed to investigate distinct interaction types within molecular systems are incorporated into our Python package (Figure S2). For example, metal (M^+) and halogen (X⁻) probes can be employed for studying cation- π and an ion- π interactions, respectively. For electrophilic interactions, the CH_3^+ probe is ideal as it maps interaction with electron-rich areas of π electron density. In contrast, the CH₃⁻ probe is best suited for probing electron-deficient regions of a molecule. SH⁻, being a softer nucleophile than CH_3^- can also serve as a nucleophilic probe. The acetylene (C_2H_2) and ethylene (C_2H_4) probes can be used for examining ligand interactions in transition metal complexes. The benzene probe is ideal for investigating π -stacking, polar- π , cation- π , anion- π , and lone pair- π interactions. Additionally, the carbon monoxide (CO) probe can be used to assess bonding and back-bonding interactions in transition metal complexes. Finally, BH_3 and BF_3 can be used as Lewis acid probes. Additional probes can readily be included. Each probe is oriented perpendicular to the tangential plane of the surface being investigated. This orientation is illustrated in **Figure S2** by blue arrows. The placement of these arrows about the molecular structure indicates the point used to align and orient the probe. Once positioned, each molecular probe undergoes a semi-empirical (xTB) rigid rotor scan about the normal vector to obtain a minimum energy probe orientation.



Figure S2. Probes and their geometries. Blue arrows indicate the alignment/orientation of probes toward the surface.

3. Spherical grid generation

The visualization of probes around a benzene molecule, as depicted in **Figure S3**, uses the Fibonacci sphere algorithm. The placement of probes around each atom follows the Fibonacci sphere distribution, with radii based on the atomic van der Waals radii. The number of probes can be fine-tuned, and those intersecting with neighboring atoms are removed to avoid overlap.



Figure S3. Spherical grid generated around benzene using the Fibonacci sphere algorithm.

4. Overview of IMIP map generation

An overview of the method used for surface generation is given in **Figure S4**. Benzene is used as an example using a CH_3^+ probe for surface generation. Initially, a sparse cubic grid is generated around the molecule (**Figure S4** (\mathbf{a}, \mathbf{b})). For each grid point, the electron density is computed using Multiwfn, and the results are exported from wave function files and stored in the Molden format. An isodensity range is then set to filter off points (**Figure**) S4 (c)). Subsequently, a volume element is created for each remaining grid point, and within this volume, a finer grid is constructed and filtered. This refined grid captures grid points with a narrow electron density range (Figure S4 (d, e, f)). After grid generation and filtration, probes are positioned at each grid point. Single-atom probes are positioned without ambiguity. If molecular probes are used, their alignment would be determined by vectors normal to the tangential plane of each grid point on the molecular surface (Figure S4 (g)). This definition is intended to account for the orbital directionality of molecular probes. The normal vectors are computed using the Open3D Python library. Open3D estimates the normal vectors on the surface by statistical analysis of neighboring grid points. By combining this approach with a rigid rotor scan using GFN2-xTB (Figure S4 (g)), the lowest energy orientation of the probe can be determined in a reasonable time frame. At this point, EDA computations are conducted on the grid points, and their corresponding energy values are stored as extended xyz files and used to construct the surfaces using Ovito Pro software (Figure S4 (h, i)).



Figure S4. Overview of methodology for IMIP map generation (a) structure optimization (b) grid generation (c) preliminary isodensity selection (d) volume element construction (e) volume element search (f) final filtration (g) probe positioning and orientation (h) EDA calculation (i) surface generation (units: kcal/mol).

5. Dependence of IMIP surfaces on basis sets and functionals

It can be shown that IMIP surfaces using different sized basis sets or functionals are qualitatively similar. (Figure S5). Comparison of the surfaces for $r^2SCAN/def2$ -SVP to $r^2SCAN/def2$ -TZVP shows little difference between the surfaces. While the absolute values between different functionals differ slightly (cf. r^2SCAN to B3LYP), the qualitative trends hold.



Figure S5. ΔE_{int} , ΔE_{elec} , and ΔE_{orb} surfaces of aniline generated at the r²SCAN/def2-SVP, r²SCAN/def2-TZVP, and B3LYP/def2-SVP level of theory, within the LMO-EDA framework.

6. Comparing IMIP surfaces generated from probe orientations via xTB and DFT scans

When molecular probes were employed, the lowest energy orientation of the probe was identified through a rigid rotor scan using the GFN2-xTB method. The comparison between molecular probe-based surfaces generated using GFN2-xTB and r²SCAN/def2-SVP rotor scans shows qualitative consistency (**Figure S6**), suggesting that the faster semi-empirical xTB scans can replace the more costly DFT scans for determining probe orientations.



Figure S6. ΔE_{int} , ΔE_{elec} , and ΔE_{orb} surfaces of aniline (first and second rows) with CH₃⁺ probe, and benzene (third and fourth rows) with stacked C₆H₆ probe. xTB scans (first and third rows), DFT scans (second and fourth rows).

7. $\Delta E_{\text{int}}, \Delta E_{\text{elec}}, \Delta E_{\text{orb}}$, and σ^+ values for EAS Hammett plots

Table S1 lists ΔE_{int} , ΔE_{elec} , ΔE_{orb} , and σ^+ values used to generate Hammett plots shown in Figure 6 (EAS section) in the main manuscript. ΔE_{int} and ΔE_{orb} show a stronger correlation with relative reactivity patterns observed in the literature than ΔE_{elec} . ΔE_{int} , ΔE_{elec} , and ΔE_{orb} values were collected at the most favorable ΔE_{int} sites within the para regions of the π systems.

Groups	$\Delta E_{\rm int}$ ΔE_{elec}		ΔE_{orb}	σ^+	
$N(CH_3)_2$	-77.4595	-14.86750	-61.8911	-1.70	
$\rm NH_2$	-70.2927	-14.34040	-56.1900	-1.30	
$\rm NHC(O)CH_3$	-63.7592	-10.53960	-53.7226	-0.60	
OCH_3	-63.3863	-11.18530	-52.6538	-0.78	
OH	-60.0525	-10.15930	-52.3355	-0.92	
tBu	-59.5491	-11.15340	-48.5984	-0.26	
iPr	-58.7684	-11.94530	-47.2946	-0.28	
Propyl	-58.7562	-11.35270	-47.7845	-0.29	
Ethyl	-57.9687	-11.15960	-47.3228	-0.30	
CH_3	-57.7466	-11.15460	-46.8313	-0.31	
$OC(O)CH_3$	-57.1349	-9.40318	-48.2091	-0.19	
Br	-53.0551	-5.93261	-47.0005	0.15	
Η	-52.5277	-1.04272	-42.9562	0.00	
Cl	-52.2368	-6.97245	-45.6446	0.11	
\mathbf{F}	-51.9715	-6.84082	-45.5959	-0.07	
CHO	-45.4417	-4.64978	-42.0392	0.73	
COOH	-43.6908	-1.84148	-42.7697	0.42	
CF_3	-43.5836	-3.91859	-40.9728	0.61	
$_{\rm CN}$	-43.3605	-1.24201	-43.3159	0.66	
NO_2	-39.7259	-0.74441	-40.1554	0.79	

Table S1. ΔE_{int} , ΔE_{elec} , and ΔE_{orb} (kcal/mol) and σ^+ values of variable mono-substituted benzene derivatives (and benzene). Energies were obtained at the para-positions of the π systems.

8. Cation- π IMIP surfaces of benzene, naphthalene, anthracene, phenanthrene, and anthracene

Figures S7-S14 depict surfaces for benzene, naphthalene, anthracene, phenanthrene, and tetracene generated using Li⁺, Na⁺, K⁺, Be²⁺, Mg²⁺, Ca²⁺, Ag⁺, and Zn²⁺. The focus is on how these metal ions, varying in size and charge, interact within the π systems. The isodensity values used in each metal-PAH system are derived from those optimized isodensities between benzene and each respective probe (Table S2). This allows for comparing energy values between different molecules using the same probe. These figures include all energy components.

Table S2. Isodensities of various cation probes based on optimized interactions with benzene.

Probe	Li^+	Na^+	K^+	Be^{2+}	Ca^{2+}	Ag^{2+}	Zn^+
Isodensity	7.52×10^{-4}	9.15×10^{-6}	8.21×10^{-5}	3.15×10^{-3}	1.32×10^{-4}	1.93×10^{-4}	5.49×10^{-4}



Figure S7. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of benzene, naphthalene, anthracene, phenanthrene, and tetracene; Ag⁺ probe.



Figure S8. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of benzene, naphthalene, anthracene, phenanthrene, and tetracene; Be²⁺ probe.



Figure S9. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of benzene, naphthalene, anthracene, phenanthrene, and tetracene; Ca²⁺ probe.



Figure S10. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of benzene, naphthalene, anthracene, phenanthrene, and tetracene; K⁺ probe.



Figure S11. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of benzene, naphthalene, anthracene, phenanthrene, and tetracene; Li⁺ probe.



Figure S12. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of benzene, naphthalene, anthracene, phenanthrene, and tetracene; Mg²⁺ probe.



Figure S13. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of benzene, naphthalene, anthracene, phenanthrene, and tetracene; Na⁺ probe.



Figure S14. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of benzene, naphthalene, anthracene, phenanthrene, and tetracene; Zn^{2+} probe.

9. IMIP surfaces between benzene derivatives and cation probes

Figures S15-S50 depict surfaces for benzene and several of its derivatives (R-Ph). This list includes: Iodo-benzene, bromo-benzene, chloro-benzene, fluoro-benzene, toluene, benzaldehyde, cyano-benzene, ethylbenzene, cumene, benzamide, aniline, nitrobenzene, anisole, acetoxy benzene, phenol, propyl benzene, thiophenol, benzenesulfonic acid and tert-butyl-benzene, and benzotrifluoride. The isodensities used to generate each surface were based on the optimized values between benzene and the metal cation probe, as detailed in Table S2.



Figure S15. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of bromobenzene with Li^+ , Na^+ , K^+ , Be^{2+} probes.



Figure S16. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of bromobenzene with Mg²⁺, Ca²⁺, Ag⁺, Zn²⁺ probes.



Figure S17. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of trifluorotoluene with $\text{Li}^+, \text{Na}^+, \text{K}^+, \text{Be}^{2+}$ probes.



Figure S18. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of trifluorotoluene with Mg²⁺, Ca²⁺, Ag⁺, Zn²⁺ probes.



Figure S19. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of toluene with $\text{Li}^+, \text{Na}^+, \text{K}^+, \text{Be}^{2+}$ probes.



Figure S20. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of toluene with $Mg^{2+}, Ca^{2+}, Ag^+, Zn^{2+}$ probes.



Figure S21. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of chlorobenzene with $\text{Li}^+, \text{Na}^+, \text{K}^+, \text{Be}^{2+}$ probes.



Figure S22. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of chlorobenzene with Mg^{2+} , Ca^{2+} , Ag^+ , Zn^{2+} probes.



Figure S23. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of benzaldehyde with $\text{Li}^+, \text{Na}^+, \text{K}^+, \text{Be}^{2+}$ probes.


Figure S24. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of benzaldehyde with Mg^{2+} , Ca^{2+} , Ag^+ , Zn^{2+} probes.



Figure S25. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of benzonitrile with $\text{Li}^+, \text{Na}^+, \text{K}^+, \text{Be}^{2+}$ probes.



Figure S26. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of benzonitrile with Mg^{2+} , Ca^{2+} , Ag^+ , Zn^{2+} probes.



Figure S27. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of ethylbenzene with $\text{Li}^+, \text{Na}^+, \text{K}^+, \text{Be}^{2+}$ probes.



Figure S28. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of ethylbenzene with Mg^{2+} , Ca^{2+} , Ag^+ , Zn^{2+} probes.



Figure S29. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of fluorobenzene with Li^+ , Na^+ , K^+ , Be^{2+} probes.



Figure S30. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of fluorobenzene with Mg^{2+} , Ca^{2+} , Ag^+ , Zn^{2+} probes.



Figure S31. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of cumene with $\text{Li}^+, \text{Na}^+, \text{K}^+, \text{Be}^{2+}$ probes.



Figure S32. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of cumene with $Mg^{2+}, Ca^{2+}, Ag^+, Zn^{2+}$ probes.



Figure S33. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of acetanilide with $\text{Li}^+, \text{Na}^+, \text{K}^+, \text{Be}^{2+}$ probes.



Figure S34. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of acetanilide with $Mg^{2+}, Ca^{2+}, Ag^+, Zn^{2+}$ probes.



Figure S35. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of aniline with $\text{Li}^+, \text{Na}^+, \text{K}^+, \text{Be}^{2+}$ probes.



Figure S36. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of aniline with $Mg^{2+}, Ca^{2+}, Ag^+, Zn^{2+}$ probes.



Figure S37. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of nitrobenzene with $\text{Li}^+, \text{Na}^+, \text{K}^+, \text{Be}^{2+}$ probes.



Figure S38. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of nitrobenzene with Mg^{2+} , Ca^{2+} , Ag^+ , Zn^{2+} probes.



Figure S39. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of anisole with $\text{Li}^+, \text{Na}^+, \text{K}^+, \text{Be}^{2+}$ probes.



Figure S40. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of anisole with $Mg^{2+}, Ca^{2+}, Ag^+, Zn^{2+}$ probes.



Figure S41. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of phenyl-acetate with Li^+ , Na^+ , K^+ , Be^{2+} probes.



Figure S42. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of phenyl-acetate with Mg²⁺, Ca²⁺, Ag⁺, Zn²⁺ probes.



Figure S43. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of phenol with $\text{Li}^+, \text{Na}^+, \text{K}^+, \text{Be}^{2+}$ probes.



Figure S44. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of phenol with $Mg^{2+}, Ca^{2+}, Ag^+, Zn^{2+}$ probes.



Figure S45. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of n-propylbenzene with Li^+ , Na^+ , K^+ , Be^{2+} probes.



Figure S46. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of n-propylbenzene with Mg^{2+} , Ca^{2+} , Ag^+ , Zn^{2+} probes.



Figure S47. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of benzenesulfonic acid with Li⁺, Na⁺, K⁺, Be²⁺ probes.



Figure S48. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of benzenesulfonic acid with Mg²⁺, Ca²⁺, Ag⁺, Zn²⁺ probes.



Figure S49. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of tert-butylbenzene with Li⁺, Na⁺, K⁺, Be²⁺ probes.



Figure S50. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of tert-butylbenzene with Mg²⁺, Ca²⁺, Ag⁺, Zn²⁺ probes.

The surfaces of mono-substituted benzene derivatives (S51) with a Na⁺ probe reveal that the interaction is strongest with donating groups (NH2) and weakest with withdrawing groups (CN). The variation in ΔE_{int} tracks with ΔE_{elec} , indicating the influence is primarily electrostatic.



Figure S51. ΔE_{int} , ΔE_{elec} , and ΔE_{orb} surfaces of variable benzene derivatives with Na⁺ probes. A constant scale is used to demonstrate substituent effects on energetics.

Furthermore, Hammett plots of ΔE_{int} and ΔE_{elec} vs. σ_{total} show strong correlation coefficients of 0.929 and 0.947 (**Figure. S52**), for benzene derivatives with Na⁺, respectively. ΔE_{int} was collected from the surface region of the surface corresponding to the most favorable interaction energy within the arene π -system. ΔE_{elec} is the electrostatic component of ΔE_{int} . ΔE_{orb} did not correlate well. These results suggest that the strength of cation- π binding is strongly correlated with electrostatic effects brought on by introducing substituents and that orbital effects have minimal impact on binding strength trends.

	$-\mathrm{NH}_2$	-OH	$-\mathrm{OCH}_3$	-tBu	-Pr	-iPr	-Et	Bz
σ_{para}	-0.16	0.12	0.12	-0.1	-0.07	-0.07	-0.07	0
σ_{meta}	-0.66	-0.37	-0.27	-0.2	-0.13	-0.15	-0.15	0
σ_{total}	-0.82	-0.25	-0.15	-0.3	-0.2	-0.22	-0.22	0
	-CN	-COOH	-F	-Cl	-Br	-I	-CHO	
σ_{para}	0.56	0.38	0.34	0.37	0.39	0.35	0.35	
σ_{meta}	0.66	0.5	0.06	0.23	0.23	0.18	0.42	
σ_{total}	1.22	0.88	0.4	0.6	0.62	0.53	0.77	

Table S3. σ_{para} , σ_{meta} , and σ_{total} values for various benzene derivatives



Figure S52. Hammett plots of benzene derivatives illustrating the relationships between different energy terms and σ_{total} : (1) ΔE_{elec} vs. σ_{total} and (2) ΔE_{int} vs. σ_{total} .

10. IMIP surfaces generated with halide probes

Figures S53-S57 depict surfaces representing interactions between various halogens (F^- , Cl^- , Br^- , and I^-) and molecules known for their anion- π interactions. These molecules include hexafluorobenzene, triazine, trifluorotriazine, trinitrobenzene, and 1,2,4,5-tetracyanobenzene. Isodensities for these surfaces were established at the center of the trinitrobenzene molecule, following a restricted optimization for each halogen probe. The isodensities are listed in Table S4.

Table S4. Isodensities of various anion probes based on optimized interactions with benzene.

Probe	F^-	Cl^-	Br^-	I^-
Isodensity	5.62×10^{-5}	1.22×10^{-6}	2×10^{7}	3.15×1^{-8}



Figure S53. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of hexflourobenzene with F^- , Cl^- , Br^- , I^- probes.



Figure S54. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of 1,2,4,5-tetracyanobenzene with F⁻, Cl⁻, Br⁻, I⁻ probes.



Figure S55. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of 1,3,5-trinitrobenzene with F^- , Cl^- , Br^- , I^- probes.



Figure S56. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of triazine with F^- , Cl^- , Br^- , I^- probes.



Figure S57. ΔE_{int} , ΔE_{elec} , ΔE_{orb} , $\Delta E_{\text{ex-rep}}$, and $\Delta E_{\text{disp-corr}}$ surfaces of trifluoroazine with F^- , Cl^- , Br^- , I^- probes.
11. Pd-allyl complexes



Figure S58. Most favorable interaction energies mapped onto each atom within the allyl portion of the Pd-allyl transition metal complexes, selecting and mapping the most favorable interaction within the region of each atom for: (a) unsubstituted, (b) methoxy-substituted, (c) methyl-substituted, and (d) 1-methoxy-3-methyl configurations.