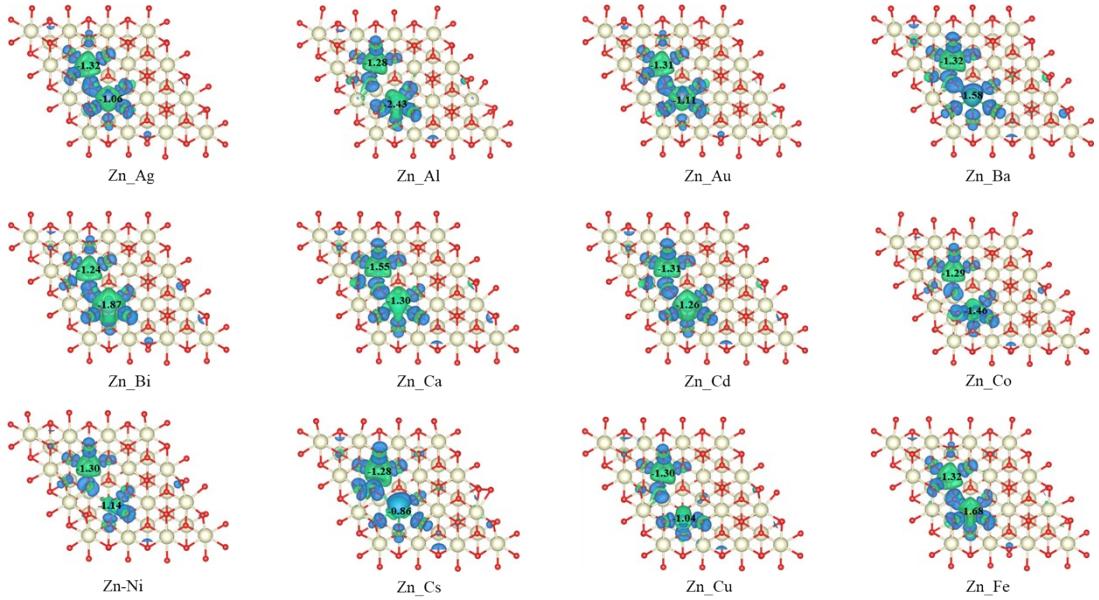


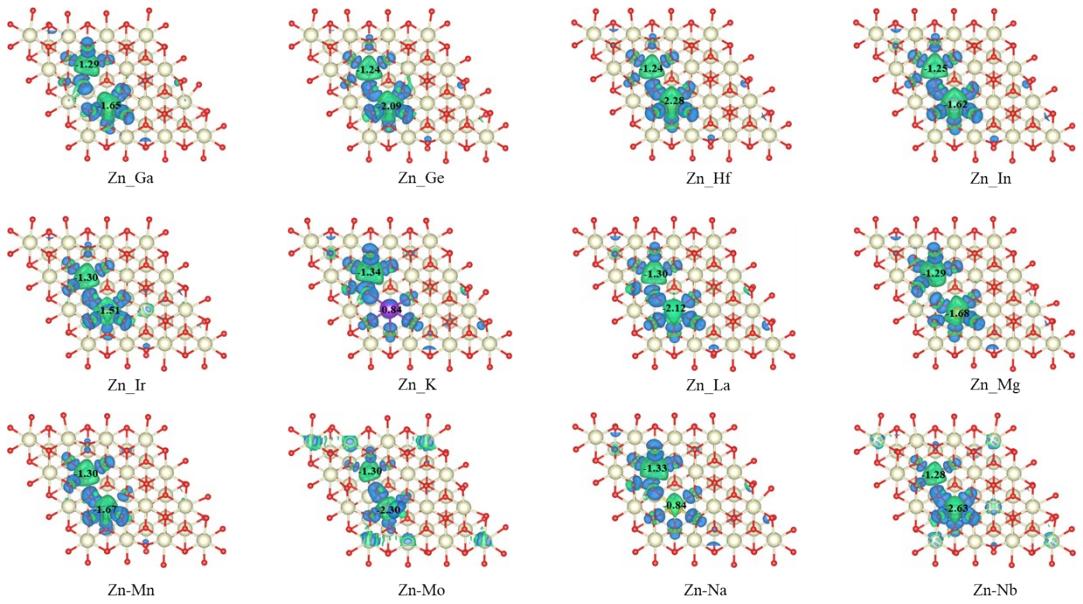
**Table S1.** Effective bader charge of substituted metal atoms with oxygen atoms near oxygen vacancies when Zn and other metal atoms are co-substituted on the CeO<sub>2</sub> (111) surface.

Co-substituted metal	Zn	M	O <sub>1</sub>	O <sub>2</sub>	O <sub>3</sub>
Zn-Rb	-1.29	-0.85	0.55	1.15	1.19
Zn-Nd	-1.23	-2.04	1.21	1.22	1.21
Zn-In	-1.25	-1.62	1.12	1.16	1.21
Zn-K	-1.34	-0.84	0.85	1.13	1.15
Zn-Pb	-1.24	-1.70	1.09	1.13	1.23
Zn-Na	-1.33	-0.84	0.81	1.15	1.15
Zn-Cd	-1.31	-1.26	0.86	1.17	1.16
Zn-Ag	-1.32	-1.06	0.97	1.05	1.20
Zn-Ca	-1.55	-1.30	0.92	1.22	1.16
Zn-Sc	-1.32	-2.10	1.17	1.25	1.20
Zn-Sr	-1.34	-1.59	0.98	1.21	1.16
Zn-Ba	-1.32	-1.58	0.97	1.19	1.16
Zn-Mn	-1.30	-1.67	1.09	1.15	1.22
Zn-Zr	-1.24	-2.31	1.23	1.23	1.21
Zn-Mg	-1.29	-1.68	0.84	1.26	1.19
Zn-Tl	-1.28	-1.19	1.01	1.08	1.19
Zn-Ti	-1.30	-1.99	1.17	1.19	1.21
Zn-Y	-1.24	-2.21	1.25	1.26	1.20
Zn-Hf	-1.24	-2.28	1.23	1.23	1.20
Zn-La	-1.30	-2.12	1.14	1.23	1.21
Zn-Ga	-1.29	-1.65	0.90	1.19	1.18
Zn-Fe	-1.32	-1.68	1.04	1.14	1.21
Zn-Al	-1.28	-2.43	0.89	1.37	1.17
Zn-Sn	-1.24	-2.17	1.18	1.19	1.19
Zn-Au	-1.31	-1.11	0.97	1.05	1.19
Zn-Pr	-1.22	-2.23	1.22	1.22	1.22
Zn-Rh	-1.30	-1.41	1.04	1.08	1.21

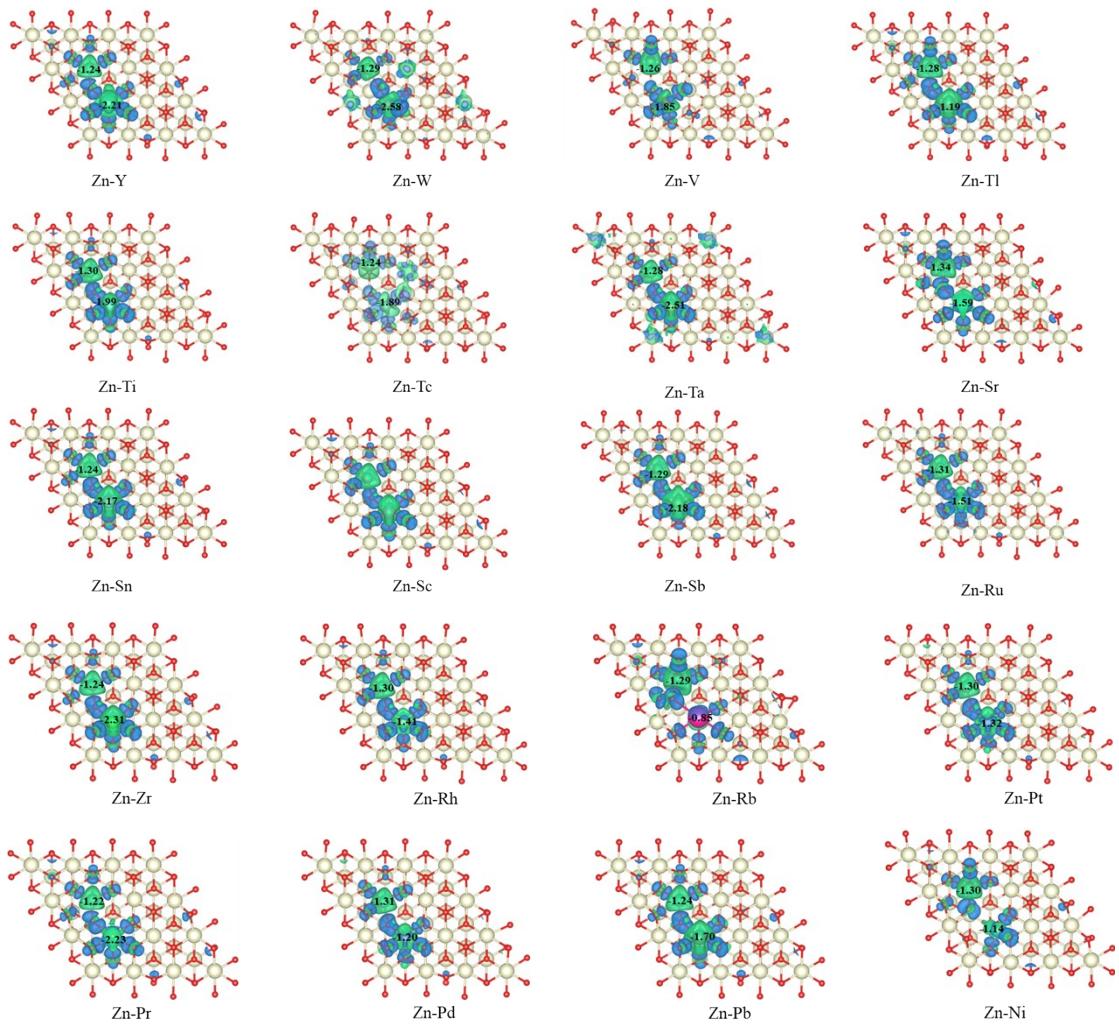
Zn-Bi	-1.24	-1.87	1.14	1.15	1.21
Zn-Ge	-1.24	-2.09	1.17	1.17	1.20
Zn-Cu	-1.30	-1.04	0.86	1.11	1.18
Zn-Pd	-1.31	-1.20	1.00	1.19	1.21
Zn-Cs	-1.28	-0.86	0.53	1.14	1.20
Zn-Cr	-1.27	-1.76	1.02	1.15	1.20
Zn-Nb	-1.28	-2.63	1.21	1.23	1.21
Zn-Ta	-1.28	-2.51	1.19	1.21	1.19
Zn-Pt	-1.30	-1.32	1.02	1.07	1.20
Zn-Co	-1.29	-1.46	0.90	1.18	1.19
Zn-Ru	-1.31	-1.51	1.09	1.11	1.21
Zn-Sb	-1.29	-2.18	1.17	1.19	1.20
Zn-V	-1.26	-1.85	1.03	1.18	1.21
Zn-Ni	-1.30	-1.14	0.90	1.11	1.18
Zn-W	-1.29	-2.58	1.07	1.21	1.23
Zn-Mo	-1.30	-2.30	0.99	1.21	1.21
Zn-Ir	-1.30	-1.51	1.05	1.10	1.19
Zn-Os	-1.30	-1.78	1.09	1.12	1.19



**Fig. S1** DFT calculated the charge-density difference of Zn and other metal atoms co-substituted CeO<sub>2</sub>(111). (Other metal ions are Ag, Al, Au, Ba, Bi, Ca, Cd, Co, Ni, Cs, Cu and Fe.)



**Fig. S2** DFT calculated the charge-density difference of Zn and other metal atoms co-substituted  $\text{CeO}_2$ (111). (Other metal ions are Ga, Ge, Hf, In, Ir, K, La, Mg, Mn, Mo, Na and Nb.)



**Fig. S3** DFT calculated the charge-density difference of Zn and other metal atoms co-substituted CeO<sub>2</sub>(111). (Other metal ions are Y, W, V, Tl, Ti, Tc, Ta, Sr, Sn, Sc, Sb, Ru, Zr, Rh, Rb, Pt, Pr, Pd, Pb and Ni.)

**Table S2.** Adsorption sites and adsorption energies ( $E_{\text{ads}}$ ) of  $\text{CH}_4$  in chemical looping dry reforming of methane on the surface of pristine  $\text{CeO}_2$  (111) as well as on the surface of Zn and Nd co-substituted  $\text{CeO}_2$  (111).

pristine $\text{CeO}_2$ (111)							
Adsorption sites	Ce-Top <sub>1</sub>	Ce-Top <sub>2</sub>	O-Top	Oxygen Vacancy	O-O-Bridge	Ce-O-Bridge	Hollow
$E_{\text{ads}}/\text{eV}$	-0.71	-0.53	-0.20	-0.83	-0.14	-0.15	-0.19
Zn and Nd co-substituted $\text{CeO}_2$ (111)							
Adsorption sites	Ce-Top	Zn-Top	Nd-Top	O-Top <sub>1</sub>	O-Top <sub>2</sub>	O-Top <sub>3</sub>	O-Top <sub>4</sub>
$E_{\text{ads}}/\text{eV}$	-0.28	-0.27	0.65	0.82	-0.16	0.98	0.77
Adsorption sites	Oxygen Vacancy	O-O-Bridge <sub>1</sub>	O-O-Bridge <sub>2</sub>	Ce-O-Bridge <sub>1</sub>	Ce-O-Bridge <sub>2</sub>	Hollow <sub>1</sub>	Hollow <sub>2</sub>
$E_{\text{ads}}/\text{eV}$	0.44	-0.20	0.95	-0.21	-0.18	-0.39	-0.29

**Table S3.** Adsorption sites and adsorption energies ( $E_{\text{ads}}$ ) of  $\text{CH}_3$  in chemical looping dry reforming of methane on the surface of pristine  $\text{CeO}_2$  (111) as well as on the surface of Zn and Nd co-substituted  $\text{CeO}_2$  (111).

pristine $\text{CeO}_2$ (111)							
Adsorption sites	Ce-Top <sub>1</sub>	Ce-Top <sub>2</sub>	O-Top	Oxygen Vacancy	O-O-Bridge	Ce-O-Bridge	Hollow
$E_{\text{ads}}/\text{eV}$	-1.88	-1.88	-2.59	-1.63	-0.59	-0.79	-1.88

Zn and Nd co-substituted $\text{CeO}_2$ (111)							
Adsorption sites	Ce-Top	Zn-Top	Nd-Top	O-Top <sub>1</sub>	O-Top <sub>2</sub>	O-Top <sub>3</sub>	O-Top <sub>4</sub>
$E_{\text{ads}}/\text{eV}$	-0.42	-4.22	0.48	-3.60	-3.69	-3.75	-4.26

Adsorption sites	Oxygen Vacancy	O-O-Bridge <sub>1</sub>	O-O-Bridge <sub>2</sub>	Ce-O-Bridge <sub>1</sub>	Ce-O-Bridge <sub>2</sub>	Hollow <sub>1</sub>	Hollow <sub>2</sub>
$E_{\text{ads}}/\text{eV}$	0.35	-3.71	-4.31	-2.61	-3.71	0.57	-0.56

**Table S4.** Adsorption sites and adsorption energies ( $E_{\text{ads}}$ ) of  $\text{CH}_2$  in chemical looping dry reforming of methane on the surface of pristine  $\text{CeO}_2$  (111) as well as on the surface of Zn and Nd co-substituted  $\text{CeO}_2$  (111).

pristine $\text{CeO}_2$ (111)							
Adsorption sites	Ce-Top <sub>1</sub>	Ce-Top <sub>2</sub>	O-Top	Oxygen Vacancy	O-O-Bridge	Ce-O-Bridge	Hollow
$E_{\text{ads}}/\text{eV}$	-2.54	-2.54	-3.81	-2.51	-2.54	-3.90	-2.54

Zn and Nd co-substituted $\text{CeO}_2$ (111)							
Adsorption sites	Ce-Top	Zn-Top	Nd-Top	O-Top <sub>1</sub>	O-Top <sub>2</sub>	O-Top <sub>3</sub>	O-Top <sub>4</sub>
$E_{\text{ads}}/\text{eV}$	-3.76	-4.81	-4.73	-3.62	-3.82	-3.64	-5.65

Adsorption sites	Oxygen Vacancy	O-O-Bridge <sub>1</sub>	O-O-Bridge <sub>2</sub>	Ce-O-Bridge <sub>1</sub>	Ce-O-Bridge <sub>2</sub>	Hollow <sub>1</sub>	Hollow <sub>2</sub>
$E_{\text{ads}}/\text{eV}$	-3.73	-4.82	-4.79	-3.76	-3.75	-3.77	-4.79

**Table S5.** Adsorption sites and adsorption energies ( $E_{\text{ads}}$ ) of CH in chemical looping dry reforming of methane on the surface of pristine CeO<sub>2</sub> (111) as well as on the surface of Zn and Nd co-substituted CeO<sub>2</sub> (111).

pristine CeO <sub>2</sub> (111)							
Adsorption sites	Ce-Top <sub>1</sub>	Ce-Top <sub>2</sub>	O-Top	Oxygen Vacancy	O-O-Bridge	Ce-O-Bridge	Hollow
$E_{\text{ads}}/\text{eV}$	-3.34	-3.34	-5.16	-3.34	-3.34	-5.13	-3.34

Zn and Nd co-substituted CeO <sub>2</sub> (111)							
Adsorption sites	Ce-Top	Zn-Top	Nd-Top	O-Top <sub>1</sub>	O-Top <sub>2</sub>	O-Top <sub>3</sub>	O-Top <sub>4</sub>
$E_{\text{ads}}/\text{eV}$	-5.21	-7.21	-5.11	-5.04	-5.93	-5.97	-6.21
Adsorption sites	Oxygen Vacancy	O-O-Bridge <sub>1</sub>	O-O-Bridge <sub>2</sub>	Ce-O-Bridge <sub>1</sub>	Ce-O-Bridge <sub>2</sub>	Hollow <sub>1</sub>	Hollow <sub>2</sub>
$E_{\text{ads}}/\text{eV}$	-6.04	-5.20	-6.77	-5.04	-5.22	-5.99	-5.22

**Table S6.** Adsorption sites and adsorption energies ( $E_{\text{ads}}$ ) of C in chemical looping dry reforming of methane on the surface of pristine CeO<sub>2</sub> (111) as well as on the surface of Zn and Nd co-substituted CeO<sub>2</sub> (111).

pristine CeO <sub>2</sub> (111)							
Adsorption sites	Ce-Top <sub>1</sub>	Ce-Top <sub>2</sub>	O-Top	Oxygen Vacancy	O-O-Bridge	Ce-O-Bridge	Hollow
$E_{\text{ads}}/\text{eV}$	-2.92	-2.92	-6.50	-2.92	-6.50	-6.58	-2.91

Zn and Nd co-substituted CeO <sub>2</sub> (111)							
Adsorption sites	Ce-Top	Zn-Top	Nd-Top	O-Top <sub>1</sub>	O-Top <sub>2</sub>	O-Top <sub>3</sub>	O-Top <sub>4</sub>
$E_{\text{ads}}/\text{eV}$	-4.90	-8.24	-6.68	-7.01	-7.47	-7.29	-8.48
Adsorption sites	Oxygen Vacancy	O-O-Bridge <sub>1</sub>	O-O-Bridge <sub>2</sub>	Ce-O-Bridge <sub>1</sub>	Ce-O-Bridge <sub>2</sub>	Hollow <sub>1</sub>	Hollow <sub>2</sub>
$E_{\text{ads}}/\text{eV}$	-7.28	-7.46	-8.48	-7.35	-7.46	-8.24	-3.97

**Table S7.** Adsorption sites and adsorption energies ( $E_{\text{ads}}$ ) of H in chemical looping dry reforming of methane on the surface of pristine CeO<sub>2</sub> (111) as well as on the surface of Zn and Nd co-substituted CeO<sub>2</sub> (111).

pristine CeO <sub>2</sub> (111)							
Adsorption sites	Ce-Top <sub>1</sub>	Ce-Top <sub>2</sub>	O-Top	Oxygen Vacancy	O-O-Bridge	Ce-O-Bridge	Hollow
$E_{\text{ads}}/\text{eV}$	-2.32	-2.32	-3.44	-2.13	-0.52	-3.75	-2.30

Zn and Nd co-substituted CeO <sub>2</sub> (111)							
Adsorption sites	Ce-Top	Zn-Top	Nd-Top	O-Top <sub>1</sub>	O-Top <sub>2</sub>	O-Top <sub>3</sub>	O-Top <sub>4</sub>
$E_{\text{ads}}/\text{eV}$	0.84	-5.13	-0.17	-4.58	-4.72	-4.76	-5.12

Adsorption sites	Oxygen Vacancy	O-O-Bridge <sub>1</sub>	O-O-Bridge <sub>2</sub>	Ce-O-Bridge <sub>1</sub>	Ce-O-Bridge <sub>2</sub>	Hollow <sub>1</sub>	Hollow <sub>2</sub>
$E_{\text{ads}}/\text{eV}$	-4.25	0.79	-5.20	-4.58	-4.73	-3.39	0.29

**Table S8.** Adsorption sites and adsorption energies ( $E_{\text{ads}}$ ) of O in chemical looping dry reforming of methane on the surface of pristine CeO<sub>2</sub> (111) as well as on the surface of Zn and Nd co-substituted CeO<sub>2</sub> (111).

pristine CeO <sub>2</sub> (111)							
Adsorption sites	Ce-Top <sub>1</sub>	Ce-Top <sub>2</sub>	Oxygen Vacancy	Ce-O-Bridge	Hollow		
$E_{\text{ads}}/\text{eV}$	-6.26	-6.25	-6.26	-3.53	-6.26		
Zn and Nd co-substituted CeO <sub>2</sub> (111)							
Adsorption sites	Ce-Top	Zn-Top	Nd-Top	O-Top <sub>1</sub>	O-Top <sub>2</sub>	O-Top <sub>3</sub>	O-Top <sub>4</sub>
$E_{\text{ads}}/\text{eV}$	-2.67	-3.16	-1.35	-3.25	-2.62	-3.38	-3.30
Adsorption sites	Oxygen Vacancy	O-O-Bridge <sub>1</sub>	O-O-Bridge <sub>2</sub>	Ce-O-Bridge <sub>1</sub>	Ce-O-Bridge <sub>2</sub>	Hollow <sub>1</sub>	Hollow <sub>2</sub>
$E_{\text{ads}}/\text{eV}$	-1.29	-2.47	-0.46	-2.51	-3.62	-0.70	-1.47

**Table S9.** Adsorption sites and adsorption energies ( $E_{\text{ads}}$ ) of CO in chemical looping dry reforming of methane on the surface of pristine  $\text{CeO}_2$  (111) as well as on the surface of Zn and Nd co-substituted  $\text{CeO}_2$  (111).

pristine $\text{CeO}_2$ (111)							
Adsorption sites	Ce-Top <sub>1</sub>	Ce-Top <sub>2</sub>	O-Top	Oxygen Vacancy	O-O-Bridge	Ce-O-Bridge	Hollow
$E_{\text{ads}}/\text{eV}$	-0.81	-0.65	-0.45	-0.77	-0.30	-0.48	-0.31
Zn and Nd co-substituted $\text{CeO}_2$ (111)							
Adsorption sites	Ce-Top	Zn-Top	Nd-Top	O-Top <sub>1</sub>	O-Top <sub>2</sub>	O-Top <sub>3</sub>	O-Top <sub>4</sub>
$E_{\text{ads}}/\text{eV}$	0.53	-0.59	-0.38	0.43	-0.17	-0.17	-3.67
Adsorption sites	Oxygen Vacancy	O-O-Bridge <sub>1</sub>	O-O-Bridge <sub>2</sub>	Ce-O-Bridge <sub>1</sub>	Ce-O-Bridge <sub>2</sub>	Hollow <sub>1</sub>	Hollow <sub>2</sub>
$E_{\text{ads}}/\text{eV}$	-0.46	-0.39	-0.33	0.44	-0.41	-0.35	0.44

**Table S10.** Adsorption sites and adsorption energies ( $E_{\text{ads}}$ ) of CO<sub>2</sub> in chemical looping dry reforming of methane on the surface of pristine CeO<sub>2</sub> (111) as well as on the surface of Zn and Nd co-substituted CeO<sub>2</sub> (111).

pristine CeO <sub>2</sub> (111)							
Adsorption sites	Ce-Top <sub>1</sub>	Ce-Top <sub>2</sub>	O-Top	Oxygen Vacancy	O-O-Bridge	Ce-O-Bridge	Hollow
$E_{\text{ads}}/\text{eV}$	-0.86	-0.81	-0.68	-0.23	-0.79	-0.62	-0.91

Zn and Nd co-substituted CeO <sub>2</sub> (111)							
Adsorption sites	Ce-Top	Zn-Top	Nd-Top	O-Top <sub>1</sub>	O-Top <sub>2</sub>	O-Top <sub>3</sub>	O-Top <sub>4</sub>
$E_{\text{ads}}/\text{eV}$	0.60	0.44	-0.43	0.69	-0.44	-0.28	-0.26

Adsorption sites	Oxygen Vacancy	O-O-Bridge <sub>1</sub>	O-O-Bridge <sub>2</sub>	Ce-O-Bridge <sub>1</sub>	Ce-O-Bridge <sub>2</sub>	Hollow <sub>1</sub>	Hollow <sub>2</sub>
$E_{\text{ads}}/\text{eV}$	0.38	0.71	-0.59	0.51	0.40	0.35	0.41

**Table S11.** Adsorption sites and adsorption energies ( $E_{\text{ads}}$ ) of H<sub>2</sub> in chemical looping dry reforming of methane on the surface of pristine CeO<sub>2</sub> (111) as well as on the surface of Zn and Nd co-substituted CeO<sub>2</sub> (111).

pristine CeO <sub>2</sub> (111)							
Adsorption sites	Ce-Top <sub>1</sub>	Ce-Top <sub>2</sub>	O-Top	Oxygen Vacancy	O-O-Bridge	Ce-O-Bridge	Hollow
$E_{\text{ads}}/\text{eV}$	-0.51	-0.58	-0.04	-0.04	-0.50	-0.54	-0.14

Zn and Nd co-substituted CeO <sub>2</sub> (111)							
Adsorption sites	Ce-Top	Zn-Top	Nd-Top	O-Top <sub>1</sub>	O-Top <sub>2</sub>	O-Top <sub>3</sub>	O-Top <sub>4</sub>
$E_{\text{ads}}/\text{eV}$	-0.20	-0.15	0.72	0.87	0.80	0.80	0.76

Adsorption sites	Oxygen Vacancy	O-O-Bridge <sub>1</sub>	O-O-Bridge <sub>2</sub>	Ce-O-Bridge <sub>1</sub>	Ce-O-Bridge <sub>2</sub>	Hollow <sub>1</sub>	Hollow <sub>2</sub>
$E_{\text{ads}}/\text{eV}$	0.68	0.78	0.74	0.78	0.77	0.71	0.77

**Table S12.** Adsorption sites and adsorption energies ( $E_{\text{ads}}$ ) of  $\text{CH}_3\text{O}$  in chemical looping dry reforming of methane on the surface of pristine  $\text{CeO}_2$  (111) as well as on the surface of Zn and Nd co-substituted  $\text{CeO}_2$  (111).

pristine $\text{CeO}_2$ (111)							
Adsorption sites	Ce-Top <sub>1</sub>	Ce-Top <sub>2</sub>	O-Top	Oxygen Vacancy	O-O-Bridge	Ce-O-Bridge	Hollow
$E_{\text{ads}}/\text{eV}$	-4.04	-4.05	-4.04	-4.06	-4.06	-4.06	-4.05

Zn and Nd co-substituted $\text{CeO}_2$ (111)							
Adsorption sites	Ce-Top	Zn-Top	Nd-Top	O-Top <sub>1</sub>	O-Top <sub>2</sub>	O-Top <sub>3</sub>	O-Top <sub>4</sub>
$E_{\text{ads}}/\text{eV}$	-1.97	-1.02	-1.91	-0.89	-0.66	-1.98	-1.44

Adsorption sites	Oxygen Vacancy	O-O-Bridge <sub>1</sub>	O-O-Bridge <sub>2</sub>	Ce-O-Bridge <sub>1</sub>	Ce-O-Bridge <sub>2</sub>	Hollow <sub>1</sub>	Hollow <sub>2</sub>
$E_{\text{ads}}/\text{eV}$	-1.03	0.95	-1.37	-0.61	-1.97	-1.96	-1.83

**Table S13.** Adsorption sites and adsorption energies ( $E_{\text{ads}}$ ) of  $\text{CH}_2\text{O}$  in chemical looping dry reforming of methane on the surface of pristine  $\text{CeO}_2$  (111) as well as on the surface of Zn and Nd co-substituted  $\text{CeO}_2$  (111).

pristine $\text{CeO}_2$ (111)							
Adsorption sites	Ce-Top <sub>1</sub>	Ce-Top <sub>2</sub>	O-Top	Oxygen Vacancy	O-O-Bridge	Ce-O-Bridge	Hollow
$E_{\text{ads}}/\text{eV}$	-1.34	-1.34	-1.87	-1.37	-1.34	-2.03	-2.02

Zn and Nd co-substituted $\text{CeO}_2$ (111)							
Adsorption sites	Ce-Top	Zn-Top	Nd-Top	O-Top <sub>1</sub>	O-Top <sub>2</sub>	O-Top <sub>3</sub>	O-Top <sub>4</sub>
$E_{\text{ads}}/\text{eV}$	-0.01	-0.22	-1.17	0.01	-0.02	-0.28	-5.15

Adsorption sites	Oxygen Vacancy	O-O-Bridge <sub>1</sub>	O-O-Bridge <sub>2</sub>	Ce-O-Bridge <sub>1</sub>	Ce-O-Bridge <sub>2</sub>	Hollow <sub>1</sub>	Hollow <sub>2</sub>
$E_{\text{ads}}/\text{eV}$	0.20	-0.19	-1.11	-0.29	-0.11	-0.20	-0.05

**Table S14.** Adsorption sites and adsorption energies ( $E_{\text{ads}}$ ) of CHO in chemical looping dry reforming of methane on the surface of pristine CeO<sub>2</sub> (111) as well as on the surface of Zn and Nd co-substituted CeO<sub>2</sub> (111).

pristine CeO <sub>2</sub> (111)							
Adsorption sites	Ce-Top <sub>1</sub>	Ce-Top <sub>2</sub>	O-Top	Oxygen Vacancy	O-O-Bridge	Ce-O-Bridge	Hollow
$E_{\text{ads}}/\text{eV}$	-1.72	-0.90	-4.10	-1.71	-0.95	-3.99	-1.70

Zn and Nd co-substituted CeO <sub>2</sub> (111)							
Adsorption sites	Ce-Top	Zn-Top	Nd-Top	O-Top <sub>1</sub>	O-Top <sub>2</sub>	O-Top <sub>3</sub>	O-Top <sub>4</sub>
$E_{\text{ads}}/\text{eV}$	-4.75	-4.62	-2.94	-3.81	-4.92	-3.91	-4.62

Adsorption sites	Oxygen Vacancy	O-O-Bridge <sub>1</sub>	O-O-Bridge <sub>2</sub>	Ce-O-Bridge <sub>1</sub>	Ce-O-Bridge <sub>2</sub>	Hollow <sub>1</sub>	Hollow <sub>2</sub>
$E_{\text{ads}}/\text{eV}$	5.99	-4.97	-5.57	-3.80	-4.00	-4.23	-2.84

**Table S15.** The zero-point energies (ZPE), the product of the vibrational entropy and temperature (TS), the optimized structural energies ( $E_{SCF}$ ), the Gibbs free energy correction values ( $G_{\text{correction}}$ ), the Gibbs free energies (G) for gas-phase molecules have been obtained from the frequency calculations at 1073.15K.

intermediates	Gas molecule				
	ZPE	TS	$E_{SCF}$	$G_{\text{correction}}$	G
CH <sub>4</sub>	1.19, 1.19 <sup>1</sup>	2.81	-24.03, -24.03 <sup>1</sup>	-1.07	-25.10
CO	0.13, 0.13 <sup>1</sup>	2.70	-14.79, -14.79 <sup>1</sup>	-2.23	-17.02
O <sub>2</sub>	0.10, 0.10 <sup>1</sup>	2.78	-9.86, -9.86 <sup>1</sup>	-2.34	-12.19
H <sub>2</sub>	0.27, 0.27 <sup>1</sup>	1.86	-6.76, -6.76 <sup>1</sup>	-1.27	-8.03
CO <sub>2</sub>	0.31, 0.31 <sup>1</sup>	3.20	-22.99, -22.99 <sup>1</sup>	-2.40	-25.40

1. ACS Catalysis, 2023, 13, 1381-1399

**Table S16.** The zero-point energies (ZPE), the product of the vibrational entropy and temperature (TS), the optimized structural energies ( $E_{SCF}$ ), the Gibbs free energy correction values ( $G_{\text{correction}}$ ), the Gibbs free energies (G) for gas-phase molecules adsorbed on the surface of pristine CeO<sub>2</sub> (111) have been obtained from the frequency calculations at 1073.15K.

intermediates	pristine CeO <sub>2</sub> (111)				
	ZPE	TS	$E_{SCF}$	$G_{\text{correction}}$	G
CH <sub>4</sub>	1.23	1.83	-677.57	0.09	-677.48
CH <sub>3</sub>	1.00	1.04	-673.49	0.39	-673.11
CH <sub>2</sub>	0.67	0.97	-668.71	0.13	-668.58
CH	0.38	0.43	-663.97	0.17	-663.81
C	0.11	0.55	-660.61	-0.24	-660.84
H	0.29	0.27	-657.58	0.15	-657.42
O	0.06	0.51	-660.56	-0.23	-660.79
CO	0.16	1.07	-668.32	-0.55	-668.87
CO <sub>2</sub>	0.32	1.50	-676.60	-0.66	-677.26
H <sub>2</sub>	0.33	1.16	-660.05	-0.43	-660.48
CH <sub>3</sub> O	1.07	1.95	-681.24	-0.14	-681.38
CH <sub>2</sub> O	0.83	1.25	-676.88	0.15	-676.73
CHO	0.55	1.11	-673.90	-0.10	-674.00

**Table S17.** The zero-point energies (ZPE), the product of the vibrational entropy and temperature (TS), the optimized structural energies ( $E_{SCF}$ ), the Gibbs free energy correction values ( $G_{\text{correction}}$ ), the Gibbs free energies (G) for gas-phase molecules adsorbed on the surface of Zn and Nd co-substituted  $\text{CeO}_2$  (111) have been obtained from the frequency calculations at 1073.15K.

intermediates	Zn and Nd co-substituted $\text{CeO}_2$ (111)				
	ZPE	TS	$E_{SCF}$	$G_{\text{correction}}$	G
$\text{CH}_4$	1.21	1.34	-667.58	0.40	-667.18
$\text{CH}_3$	1.01	1.25	-665.66	0.27	-665.39
$\text{CH}_2$	0.69	1.07	-660.92	0.04	-660.88
CH	0.38	0.70	-656.04	-0.01	-656.06
C	0.10	0.36	-652.96	-0.15	-653.11
H	0.28	0.32	-649.40	0.10	-649.30
O	0.03	0.42	-647.92	-0.23	-648.15
CO	0.26	0.34	-661.33	0.11	-661.22
$\text{CO}_2$	0.33	1.79	-666.74	-0.86	-667.60
$\text{H}_2$	0.33	1.16	-650.12	-0.43	-650.55
$\text{CH}_3\text{O}$	1.11	1.44	-669.62	0.29	-669.33
$\text{CH}_2\text{O}$	0.75	1.49	-666.48	-0.17	-666.65
CHO	0.55	1.03	-665.83	-0.01	-665.84