

## Supplementary Information

### Stacking induced symmetry broken and gap opening in Dirac half-metal $\text{MnF}_3$

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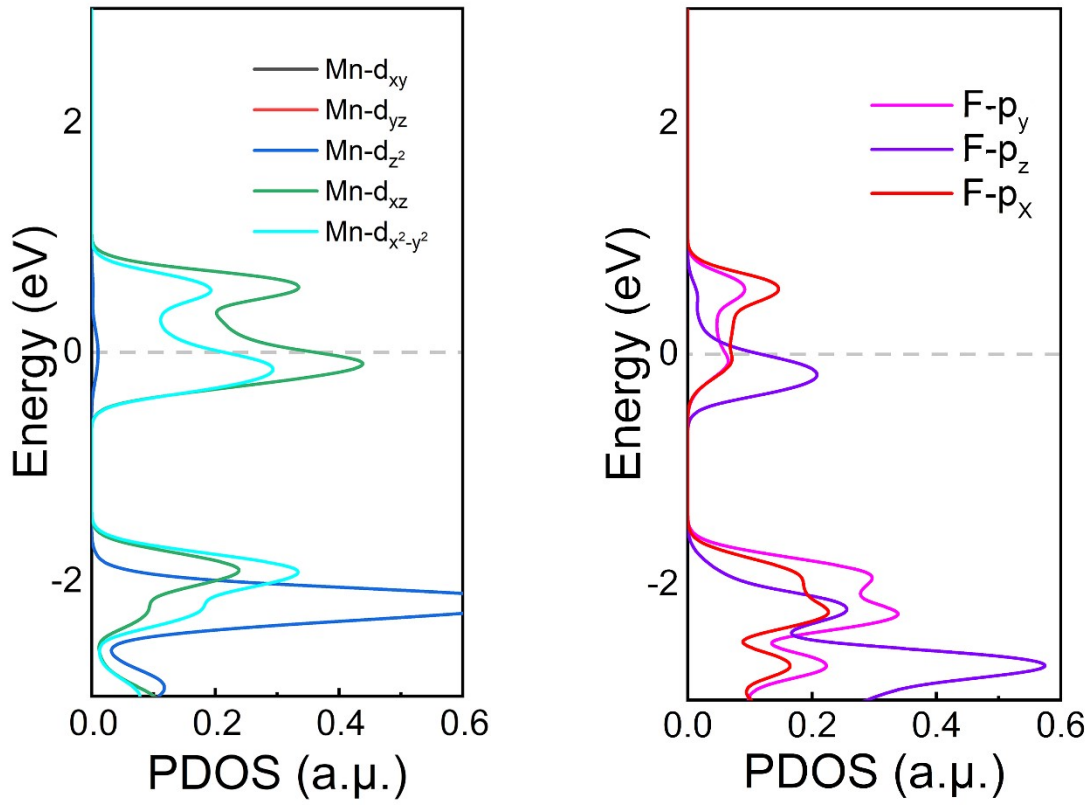
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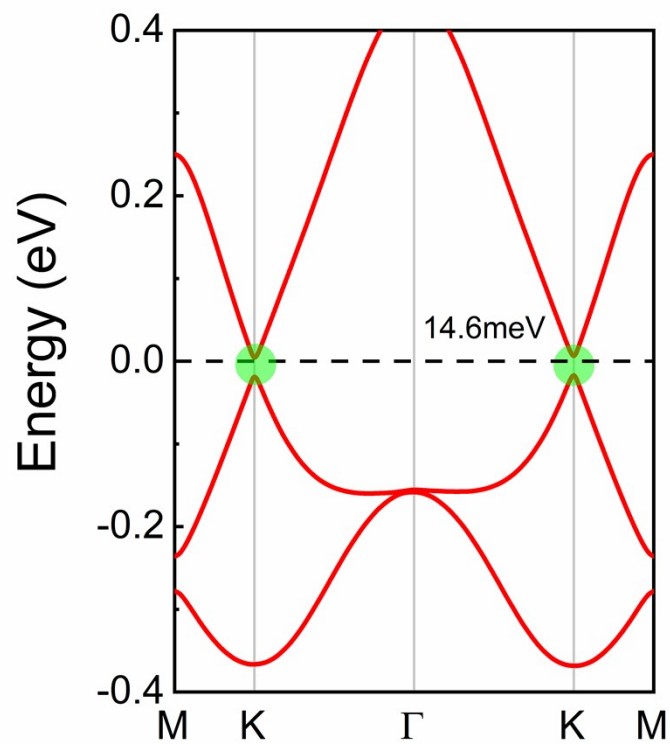
**Table. S1** Calculated formation energies of  $\text{MnF}_3$ ,  $\text{MnF}_4$  and  $\text{Mn}_2\text{F}_5$  along with this work and QOMD data.

<b>System</b>	<b>This work (<math>E_f</math>)</b>	<b>QOMD data<sup>1</sup></b>
<b><math>\text{MnF}_3</math></b>	-1.93 eV	-2.74 eV
<b><math>\text{MnF}_4</math></b>	-1.78 eV	-2.49 eV
<b><math>\text{Mn}_2\text{F}_5</math></b>	-2.13 eV	-2.69 eV

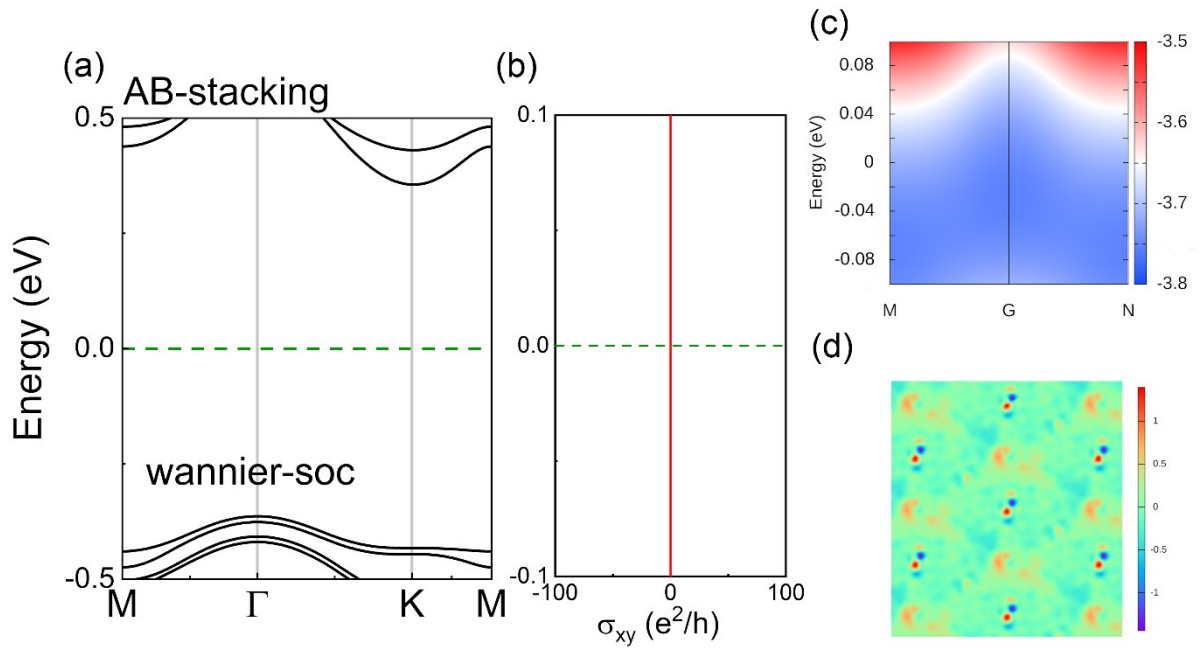
- 1 S. Kirklin, J. E Saal, B. Meredig, A. Thompson, J. W Doak, M. Aykol, S. Rühl and C. Wolverton, *npj Computational Materials*, 2015, 1, 15010.



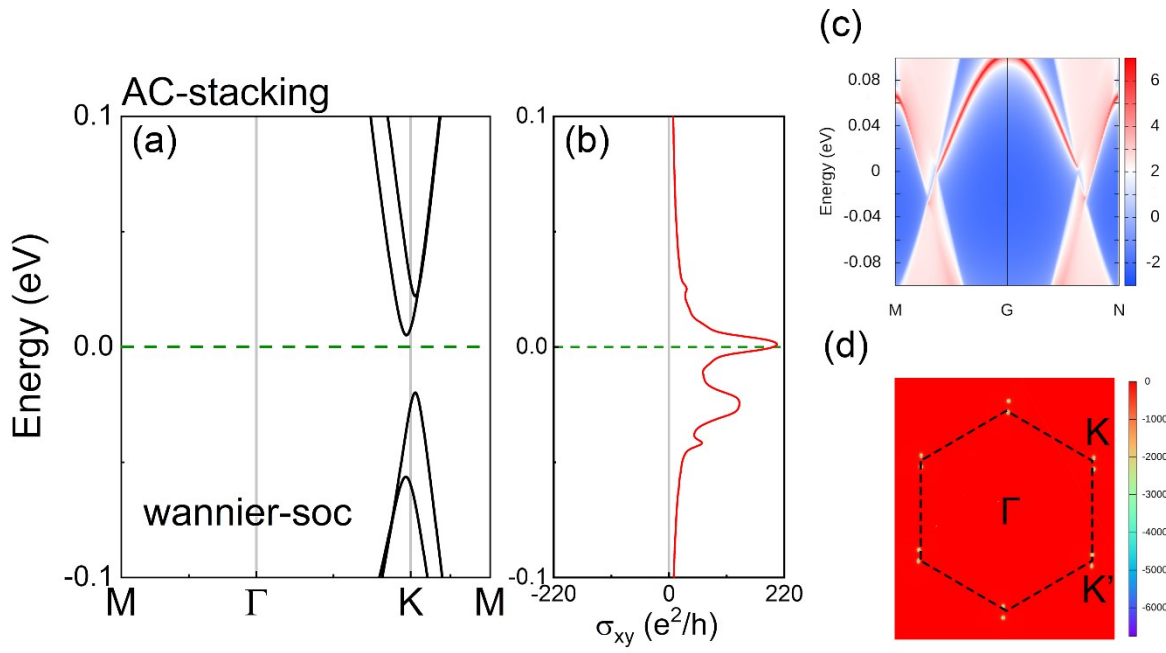
**Fig. S1.** PDOS of the spin-up channel in monolayer MnF<sub>3</sub>.



**Fig. S2** Band structure of the spin-up channel in monolayer MnF<sub>3</sub> with considering SOC.



**Fig. S3** (a) Band structure of AB-stacking MnF<sub>3</sub> bilayer calculated using the MLWFs method with SOC. (b) The corresponding anomalous Hall conductivity ( $\sigma_{xy}$ ), (c) edge state of a semi-infinite sheet, and (d) the Berry curvature with SOC.



**Fig. S4** (a) Band structure of AC-stacking MnF<sub>3</sub> bilayer calculated using the MLWFs method with SOC. (b) The corresponding anomalous Hall conductivity ( $\sigma_{xy}$ ), (c) edge state of a semi-infinite sheet, and (d) the Berry curvature with SOC.