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Supplementary Information

Density functional theory and microkinetics of ethylene chain growth and termination on silica grafted group 4 metal hydrides

Neha Mehra and William F. Schneider*

Department of Chemical and Biomolecular Engineering, University of Notre Dame, Notre Dame, Indiana 46556, United States

*E-mail: wschneider@nd.edu

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Multi-product reaction cycle and assumptions

Scheme S1: Schematic summary of reactions relevant to ethylene (C₂H₄) oligomerization on MH (M=metal ion) sites, color coded by reaction type. Surface sites are enclosed in bubbles. Solid circular bubble on bottom left: insertion of ethylene into M-H (1) forms MC₂H₅ that proceeds to form linear chained MC₄H₉ by ethylene insertion into M-C bond (2), leading to chain growth by C-C bond formation. β -H elimination to M (3) or to an ethylene monomer (5), or β -alkyl transfer to metal (4), all lead to olefin. σ -bond metathesis with ethylene (6) or with H₂ (7) yields saturated products and either generates M-vinyl that can undergo ethylene insertion to form alkylidene chains (not shown here) or restores the M-H site.

Secondary reactions of olefins begin by reinsertion at an internal olefinic carbon. Repeated terminationinsertion steps result in chain-walking, and through β -alkyl transfer (table shows possibilities for MC₄H₉), to odd-numbered C chains or their surface sites (dashed bubbles).

Microkinetic models assume that rate constants for the 7 distinct reaction types are independent of the chain length. Further, we neglect the contributions of reinsertion reactions, thus assuming that transport from active sites is more rapid than reinsertion reactions.

Raw gas molecule energies

Table S1: PBE computed (E^{DFT}) and zero-point (E^{ZPE}) energies in eV for gas molecules enclosed in 15Å x 15Å x 15Å cell

	EDFT	EZPE
Ethene (C_2H_4)	-31.971	1.359
1-Butene $(1-C_4H_8)$	-65.179	2.884
Ethane (C_2H_6)	-40.494	1.989
Methane (CH ₄)	-24.031	1.188
Hydrogen (H ₂)	-6.760	0.272
Water (H ₂ O)	-14.222	0.573
Si(OH) ₄	-52.020	1.531
Ti(CH ₃) ₄	-86.542	3.605
Zr(CH ₃) ₄	-87.462	3.584
Hf(CH ₃) ₄	-89.322	3.592

Silica surfaces representations



Fig. S1: a) Bulk β -cristobalite¹ unit cell **b)** (111) silica surface having 4 OH groups on top surface **c)** (001) silica surface with geminal silanols (two OH groups on a Si). Atoms are colored as H in green (•), O in red (•), Si in blue (•).



Fig. S2: a) 3-4mr (\equiv SiO)₃MH on (111) silica **b)** 3-3mr (\equiv SiO)₃MH on reconstructed (111) silica **c)** 1-3mr (\equiv SiO)₂MH₂ on dehydroxylated (001) surface. Linkages separating the M-O-Si bonds are marked in light blue shade.

Grafting and hydrogenolysis of M(CH₃)₄ to 3-4mr site

Grafting is performed with the precursor $M(CH_3)_4$ on silanols of silica surface. The sequential reactions leading to formation of M(IV) hydrides are presented in reaction (s1) and reaction (s2) where n=1,2 or 3 for silica (111). The goal is to compare the relative stabilities of these species and not to reproduce the actual grafting process where breaking of strained siloxane (\equiv Si-O-Si \equiv) bridges and generation of silicon hydrides Si-H_x accompany the formation of M(IV)-hydrides.

$$\begin{split} n(\equiv Si-OH) + (CH_3)_4 M &\to (\equiv SiO)_n M(CH_3)_{4-n} + nCH_4 \\ (\equiv SiO)_n M(CH_3)_{4-n} + (4-n)H_2 &\to (\equiv SiO)_n M(H)_{4-n} + (4-n)CH_4 \end{split}$$

Structures of $(\equiv SiO)_n M(CH_3)_{4-n}$, obtained from reaction (s1) are in Fig. S3 and their energies in Table S2. Thermodynamics associated with the sequential loss of methyl ligand as the metal ion anchors to single silanols of silica (111) is shown for Zr^{4+} ion in Fig. S4(a). A parity plot comparing heats of grafting (listed in Table S3) for $(\equiv SiO)_n M(CH_3)_{4-n}$ complexes over (111) surface for the three metal ions against Zr's is shown in Fig. S4(b). The heats of grafting are in the order of Hf < Zr < Ti and are exothermic. This is in line with M-O and M-C bond energies reported in literature² (Table S4).

Hydrogenolysis of $(\equiv SiO)_n Zr(CH_3)_{4-n}$ complexes to their corresponding hydrides $(\equiv SiO)_n Zr(H)_{4-n}$ (structures in Fig. S5) as per reaction (s2) is exothermic (Table S3). Hydrogenolysis energy varies non-periodically across metal ions as Ti > Zr < Hf. The H-bonding between the M-hydride and H⁺ of \equiv SiOH in the vicinity, enhances the stability of $(\equiv SiO)M(H)_3$ and $(\equiv SiO)_2M(H)_2$, while such an interaction is not there in $(\equiv SiO)_3M(H)$ (Fig. S5). Overall, this indicates that supported organic complexes of Group-4 metals when pre-treated with hydrogen will convert to hydrides that have higher coordination to support as reported by experimental characterizations.

Table S2: PBE computed E^{DFT} (*without ZPE correction*) energies in eV for structures in grafting and hydrogenolysis reactions on (111) silica of Fig. S1b

Species	Ti	Zr	Hf
$(\equiv SiO)M(CH_3)_3$	-501.691	-502.706	-504.678
$(\equiv SiO)_2M(CH_3)_2$	-479.322	-480.612	-482.615
$(\equiv SiO)_3M(CH_3)$	-456.819	-458.182	-460.223
$(\equiv SiO)M(H)_3$	-450.350	-451.514	-453.406
$(\equiv SiO)_2M(H)_2$	-445.390	-446.626	-448.612
(≡SiO) ₃ M(H)	-439.705	-441.116	-443.153
Clean Silica slab		-437.004	

Table S3: DFT computed heats of grafting $(CH_3)_4M$ in eV on silica (111) surface using energies from Table S2

	Grafting I	M(CH ₃) ₄ on si	lica (111)	Hydrogenolysis	of grafted (≡SiO) _n M(CH ₃) _{4-n}		
Μ	Calcula	ated by reaction	on (s1)	Calcul	(s2)		
	n=1	n=2	n=3	n=1	n=2	n=3	
Ti	-2.18	-3.84	-5.37	-0.47	-0.61	-0.16	
Zr	-2.27	-4.21	-5.81	-0.62	-0.56	-0.21	
Hf	-2.38	-4.35	-5.99	-0.54	-0.54	-0.20	

Table S4: M-C and M-O bond energy trends for Ti, Zr and Hf compounds from literature.² Energies in kcal/mol

Bond	Compounds from reference	Bond Energies ²	Average Energy of M-O, M-C bonds	(M-O)-(M-C)		
	Ti(CH ₂ CMe ₃) ₄	44				
Ti-C	Ti(CH ₂ SiMe ₃) ₄	64	57	55		
	Ti(CH ₂ Ph) ₄	63				
Ti-O	Ti(OPr ⁱ) ₄	112	112			
	$Zr(CH_2CMe_3)_4$	54				
Zr-C	Zr(CH ₂ SiMe ₃) ₄	75	68	68		
	Zr(CH ₂ Ph) ₄	74		00		
Zr-O	Zr(OPr ⁱ) ₄	136	136			
Hf-C	$Hf(CH_2CMe_3)_4$	58	58	79		
Hf-O	Hf(OPr ⁱ) ₄	137	137	1)		



Fig. S3: Structures of $(\equiv$ SiO)_nM(CH₃)_{4-n} on silica(111). Top row for M= Ti, second row for M= Zr, and third row for M= Hf with n = 1, 2, 3 (from left to right). Atoms are colored as H: green, C: brown, O: red, Si: blue, Ti: black (•), Zr: yellow (•), Hf: cyan (light blue, •). All distances in Å. CONTCARs in Zenodo.¹¹



Fig. S4 a) Heats of formation of $(\equiv SiO)_n Zr(CH_3)_{4-n}$ (R= CH₃) and $(\equiv SiO)_n Zr(H)_{4-n}$ on silica (111) [n= 1,2,3] **b**) Parity plot comparing heats of formation of $(\equiv SiO)_n M(CH_3)_{4-n}$ for Ti, Zr and Hf on silica (111) against $(\equiv SiO)_n Zr(CH_3)_{4-n}$.

"	Fable S5: Comparison of wavenumbers	m ⁻¹) of M-H bone	d stretching for 3-4mr	monohydride,
(\equiv SiO) ₃ M(H) sites to the experimentall	ported values		

	TiH	ZrH	HfH
DFT	1756	1689	1725
Experimental	1706, 1692, 1679, and 1647, ⁹	1633 ^{4,5}	1701 ⁶
	$1600-1725^3$		



Fig. S5: Structures of $(\equiv SiO)_n M(H)_{4-n}$ on (111) silica. Top row for M=Ti, second row for M=Zr, and third row for M=Hf with n = 1, 2, 3 (from left to right). Atoms are colored as H: green, O: red, Si: blue, Ti : black (\bullet), Zr : yellow (\circ), Hf : cyan (light blue, \bullet). All distances in Å. CONTCARs in Zenodo.¹¹



3-4mr oligomerization intermediates and reactions

Fig. S6: Geometries of species formed along pathways shown in Fig. 2 on 3-4mr (\equiv SiO)₃MH site on periodic (111) silica surface. Top two rows show species for (\equiv SiO)₃TiH, followed by two rows of (\equiv SiO)₃ZrH species and the last two rows for (\equiv SiO)₃HfH species. Bond distances in Å and angles in degrees (°). CONTCARs in Zenodo.¹¹

		M-O (Å)	$\overline{M-O}$	M-H or	4	-O-M-O	(°)	ZOMO	∠Dihedral
Species	M-01	M-O2	M-O3	(Å)	M-C(Å)	O1-M- O2	O2-M- O3	O3-M- O1	(°)	(°)
Ti-H	1.84	1.85	1.85	1.85	1.7	112.4	112.8	112.5	112.6	
Zr-H	1.99	1.99	1.99	1.99	1.87	109.5	110.3	109.8	109.9	
Hf-H	1.95	1.95	1.96	1.95	1.85	110	110.9	110.4	110.4	
C ₂ H ₄ -TiH	1.84	1.86	1.85	1.85	1.69	111.7	113.2	112.2	112.4	
C ₂ H ₄ -ZrH	2	2	2.01	2.00	1.88	104.8	105.5	113.7	108.0	
C ₂ H ₄ -HfH	1.97	1.96	1.98	1.97	1.85	105.1	105.8	113.3	108.1	
TS1_Ti	1.87	1.87	1.88	1.87	1.72	105.4	105.4	118.4	109.7	4.7 (Ti-C-C-H)
TS1_Zr	2	2.01	2.01	2.01	1.9	103.7	104.1	114	107.3	4.1 (7r-C-C-H)
TS1_Hf	1.97	1.97	1.99	1.98	1.89	103.7	103.8	114	107.2	3.9 (Hf-C-C-H)
TiC ₂ H ₅	1.85	1.86	1.87	1.86	2.07*	112.3	113.3	112.9	112.8	
ZrC ₂ H ₅	1.99	2	2.01	2.00	2.23*	110.9	111.6	110.5	111.0	
HfC ₂ H ₅	1.96	1.97	1.97	1.97	2.21*	111.5	110.7	110.3	110.8	
C ₂ H ₄ -TiC ₂ H ₅	1.86	1.87	1.86	1.86	2.07	113.0	112.2	113.4	112.9	
C ₂ H ₄ -ZrC ₂ H ₅	2.01	1.99	2.0	2.0	2.23	110.9	109.7	110.7	110.4	
C ₂ H ₄ -HfC ₂ H ₅	1.97	1.96	1.97	1.97	2.21	111.2	110.7	110.0	110.6	
TS2_Ti	1.88	1.88	1.91	1.89	2.24 **	116.3	100.6	100.4	105.8	24.3 (Ti-C-C-C)
TS2_Zr	2.03	2.02	2.04	2.03	2.35 **	118.8	98.2	97.2	104.7	18.5 (Zr-C-C-C)
TS2_Hf	1.99	1.99	2	1.99	2.32 **	115.9	98.3	99.2	104.5	24.7 (Hf-C-C-C)
TiC ₄ H ₉	1.86	1.86	1.86	1.86	2.07 *	112.5	113.1	112.8	112.8	
ZrC ₄ H ₉	2	2	2	2.00	2.23*	110.5	110.6	110	110.4	
HfC ₄ H ₉	1.96	1.96	1.97	1.96	2.21*	110.7	111.2	110.5	110.8	
TS3a_Ti	1.87	1.91	1.87	1.88	1.75	103.3	105	119.1	109.1	11.8 (Ті-С-С-Н)
TS3a_Zr	2	2	2.05	2.02	1.94	101.4	103.4	115.1	106.6	12.5 (Zr-C-C-H)
TS3a_Hf	1.96	1.97	2.01	1.98	1.91	102.6	104.0	113.7	106.8	9.5 (Hf-C-C-H)
C ₄ H ₈ -TiH	1.85	1.84	1.86	1.85	1.69	111.9	113.6	111.1	112.1	
C ₄ H ₈ -ZrH	1.98	2	2.0	1.99	1.87	105.8	113.9	105.9	108.5	
C ₄ H ₈ -HfH	1.95	1.97	1.97	1.96	1.85	104.6	105.7	114.5	108.3	
C ₂ H ₄ -TiC ₄ H ₉	1.86	1.87	1.87	1.87	2.06	113.5	112.6	112.4	112.8	
C ₂ H ₄ -ZrC ₄ H ₉	2.0	2.02	2.01	2.01	2.25	105.3	114.2	105.7	108.4	
C ₂ H ₄ -HfC ₄ H ₉	1.97	1.97	1.96	1.97	2.20	110.1	111.0	110.8	110.6	
TS3c Ti	1.89	1.91	1.84	1.88	2.27	112.7	112	99.9	108.2	

Table S6: M-O bond distances and O-M-O bond angles of intermediates formed along the $2C_2H_4 \rightarrow C_4H_8$ pathway on **3-4mr** (\equiv SiO)₃MH site. $\overline{M - O}$ and $\overline{\angle OMO}$ are average distances and angles, respectively. Dihedral angle for transition state is between the atoms in which bond is formed or broken

					(C of C ₄ H ₈)					
TS3c_Zr	2.04	1.98	2.02	2.01	2.42	108.4	110.7	100.5	106.5	
TS3c_Hf	2.01	1.95	1.99	1.98	2.39	108.8	110.6	99.8	106.4	
C ₄ H ₈ -TiC ₂ H ₅	1.86	1.86	1.86	1.86	2.06 *	113.6	112.8	112.7	113.0	
C ₄ H ₈ -ZrC ₂ H ₅	2.0	2.01	2.0	2.0	2.24 *	109.4	111.4	108.7	109.8	
C ₄ H ₈ -HfC ₂ H ₅	1.96	1.97	1.96	1.96	2.21 *	110.3	110.9	110.0	110.4	
H ₂ -TiC ₂ H ₅	1.87	1.86	1.86	1.86	2.07 *	113.0	113.3	112.3	112.9	
H ₂ -ZrC ₂ H ₅	2.01	2.0	2.0	2.0	2.23 *	110.7	111.2	109.5	110.5	
H ₂ -HfC ₂ H ₅	1.95	1.98	1.96	1.96	2.21 *	111.4	110.0	110.7	110.7	
TS4_Ti	1.86	1.85	1.91	1.87	$1.8^{\#}$	116.8	107.0	104.7	109.5	6.9 (Ti-C-H-H)
TS4_Zr	1.99	1.99	2.04	2.01	1.96#	113.5	104.4	103.3	107.1	21.6 (Zr-H-C-C)
TS4_Hf	1.96	1.95	2.0	1.97	1.93#	112.6	105.0	103.3	107.0	0.5 (Hf-C-H-H)
C ₂ H ₆ -TiH	1.84	1.85	1.84	1.84	1.69	113.2	112.7	112.8	112.9	
C ₂ H ₆ -ZrH	1.98	2.0	1.99	1.99	1.87	109.2	111.5	108.2	109.6	
C ₂ H ₆ -HfH	1.95	1.96	1.96	1.96	1.84	110.0	111.6	109.0	110.2	

**: Bond distance is between M and carbon (C) of incoming ethylene that is nearest to M.
*: Bond distance is between M and C_α of alkyl chain attached to M.
#: Bond distance is between M and H being transferred to ethyl chain

Table S7: PBE computed (E^{DFT}) and zero-point (E^{ZPE}) energies in eV of intermediates on 3-4mr $(\equiv SiO)_3MH$ site.

	(SiO) ₃ TiH	(SiO)	₃ ZrH	(SiO) ₃ HfH		
	E^{DFT}	E^{ZPE}	E^{DFT}	E^{ZPE}	E^{DFT}	E^{ZPE}	
(SiO) ₃ MH (clean)	-439.705	0.248	-441.12	0.484	-443.153	0.209	
C_2H_4 MH(SiO) ₃	-471.708	1.628	-473.279	1.897	-475.253	1.621	
TS(1)	-471.630	1.668	-473.165	1.898	-475.054	1.620	
(SiO) ₃ MC ₂ H ₅	-473.277	1.763	-474.574	2.008	-476.579	1.727	
C_2H_4 $MC_2H_5(SiO)_3$	-505.310	3.138	-506.576	3.380	-508.576	3.109	
TS(2) or TS(3b)	-503.827	3.212	-505.744	3.454	-507.525	3.176	
(SiO) ₃ MC ₄ H ₉	-506.334	3.276	-507.652	3.514	-509.658	3.235	
TS(3a)	-504.683	3.150	-506.222	3.385	-508.161	3.112	
1-C ₄ H ₈ MH(SiO) ₃	-504.922	3.133	-506.456	3.396	-508.418	3.123	
C ₂ H ₄ MC ₄ H ₉ (SiO) ₃	-538.369	4.658	-539.663	4.898	-541.676	4.611	
TS(3c)	-536.717	4.581	-538.413	4.824	-540.436	4.552	
$1-C_{4}H_{8}-MC_{2}H_{5}(SiO)_{3}$	-538.531	4.652	-539.756	4.900	-541.781	4.629	
H_2 MC_2H_5	-480.058	2.080	-481.359	2.321	-483.314	2.035	
TS(4)	-479.044	2.173	-480.538	2.399	-482.501	2.118	
MHC ₂ H ₆	-480.210	2.242	-481.655	2.484	-483.686	2.210	

Name	Reactions]	Гі	2	Zr	Hf	
		Ea	dE	Ea	dE	Ea	dE
1*	$C_2H_4(g) + MH \rightarrow C_2H_4MH$	0	-0.01	0	-0.14	0	-0.08
1	$C_2H_4MH \rightarrow MC_2H_5$	0.12	-1.43	0.12	-1.18	0.20	-1.22
2*	$C_2H_4(g) + MC_2H_5 \rightarrow C_2H_4 - MC_2H_5$	0	-0.05	0	-0.02	0	-0.004
2	$C_2H_4-MC_2H_5 \rightarrow MC_4H_9$	1.56	-0.89	0.91	-0.94	1.12	-0.96
3 a	$MC_4H_9 \rightarrow C_4H_8MH$	1.52	1.27	1.30	1.08	1.37	1.13
3a*	$C_4H_8MH \rightarrow 1-C_4H_8(g) + MH$	0	0.04	0	0.13	0	0.06
3c*	$C_2H_4(g) + MC_4H_9 \rightarrow C_2H_4MC_4H_9$	0	-0.04	0	-0.02	0	-0.03
3c	$C_2H_4MC_4H_9 \rightarrow MC_2H_5+1-C_4H_8(g)$	1.57	-0.10	1.18	-0.10	1.18	-0.09
4*	$\mathbf{H}_{2}(\mathbf{g}) + \mathbf{M}\mathbf{C}_{2}\mathbf{H}_{5} \rightarrow \mathbf{H}_{2} - \mathbf{M}\mathbf{C}_{2}\mathbf{H}_{5}$	0	0.03	0	0.02	0	0.06
4	H_2 $MC_2H_5 \rightarrow HM + C_2H_6(g)$	1.11	0.02	0.9	-0.1	0.90	-0.17

Table S8: ZPE corrected reactions (**dE**) and activation (E_a) energies in eV for ethylene dimerization on 3-4mr (\equiv SiO)₃M(H). Non-activated adsorption steps are denoted by "*".

a)

Reaction Coordinate

Fig. S7: Transition state search results on 3-4mr (SiO)3MH sites. (a), (b), (c) CI-NEB results for TS(1), TS(2), TS(3a), respectively, on $(\equiv$ SiO)₃HfH (d) CI-NEB and dimer results for TS(3c) on $(\equiv$ SiO)₃ZrH. (e) CI-NEB and dimer results for TS(4) on $(\equiv$ SiO)₃TiH.

3-4mr transition state distortions

Induced strain is measured by the average stretch, $\langle a \rangle$ generated in M-O-Si angle during transition from initial state (not to be a physiosorbed state) to TS where the most rearrangement occurs in the metal's coordination sphere and is calculated as

$$\langle a \rangle = \frac{\sum_{l=1}^{3} (a_l^{\dagger} - a_l)}{3}$$

 a_l and a_l^{\dagger} are M-O-Si angles in initial state (IS) and the leading TS. For instance, IS and TS pairs are $(\equiv SiO)_3MH$ and TS(1), $(\equiv SiO)_3MC_2H_5$ and TS(2), $(\equiv SiO)_3MC_4H_9$ and TS(3a), respectively. From Table S9, $\langle a \rangle$ is largest in TS(2) than in TS(3a) and TS(1). It is not precisely correlated to changes in activation barrier across Ti, Zr and Hf, but provides a summary about geometric distortion in TS relative to IS.

Species on 3-	4	∠Si-O-M (°)	∠ <i>Si</i> 0M	ced Strain, <a>(°)	
4mr silica(111)	Si1-O1-M	Si2-O2-M	Si3-O3-M	(°)	$IS \rightarrow TS$	<a>(°)
Ti-H	142.4	141.7	139.9	141.3		
Zr-H	141.8	141	139.1	140.6		
Hf-H	142.1	141.6	139.5	141.1		
TS1_Ti	148.1	143.9	140.1	144	TiH→TS1	144 -141.3 = 2.7
TS1_Zr	144.8	144.2	140.7	143.2	ZrH→TS1	143.2 - 140.6 = 2.6
TS1_Hf	145.8	144.9	142.3	144.3	HfH→TS1	144.3 - 141.1 = 3.2
$TC_2H_5(2)$	143.3	137.1	140.4	140.3		
$\operatorname{ZrC}_{2}\operatorname{H}_{5}(2)$	138.8	134.8	142.6	138.7		
$HfC_2H_5(2)$	143.8	140.0	136.0	139.3		
TS2_Ti	171.2	139.4	139.7	150.1	Ti: 2→TS2	150.1 - 140.3 = 9.8
TS2_Zr	163.6	138.6	138.3	146.8	Zr: 2→TS2	146.8 - 138.7 = 8.1
TS2_Hf	165.1	140.2	139.9	148.4	Hf: 2→TS2	148.4 - 139.3 = 9.1
TiC4H9 (4)	141.3	140.2	138.9	140.1		
$\operatorname{ZrC_4H_9}(4)$	140.2	138.1	140.0	139.4		
$\mathbf{HfC_{4}H_{9}(4)}$	141.4	140.7	138.0	140.0		
TS3a_Ti	147.0	144.0	141.3	144.1	Ti: 4→TS3a	144.1 - 140.1 = 4.0
TS3a_Zr	147.3	141.4	141.2	143.3	Zr: 4→TS3a	143.3 - 139.4 = 3.9
TS3a_Hf	149.1	141.7	142.6	144.5	<mark>Hf:</mark> 4→TS3a	144.5 - 140.0 = 4.5

Table S9: M-O-Si bond angles (\angle) and (a) in degrees (°) for 3-4mr (\equiv SiO)₃MH site (M=Ti, Zr, Hf)

Entropy models

ASE's¹⁰ IdealGasThermo and HarmonicThermo functions are used to calculate ideal gas entropy and entropy of surface species plus transition state species, respectively in the harmonic limit with rigid rotor approximation.

$$S_{total} = S_{trans}^{o} + S_{vibrational} + S_{rotational} + S_{electronic}$$
(S.3)

Translation entropy (S_{trans}) of ideal gas of molecular mass, m at standard pressure, P^o and temperature, T from Sackur-Tetrode Equation⁸

$$S_{trans}^{o} = k_{B} \left[ln \left[\left(\frac{2\pi m k_{B} T}{h^{2}} \right)^{\frac{3}{2}} \frac{k_{B} T}{P^{o}} \right] + \frac{5}{2} \right]$$
(S.4)

Where k_B is Boltzmann constant and h is Plank's constant. At 298 K and 475 K, $T.S^o_{trans,C2H4}$ is 0.464 eV and 0.784 eV, respectively, while $T.S^o_{trans,C4H8}$ is 0.491 eV and 0.826 eV, respectively.

 $S_{electronic} = 0$ as no spin degenerate ground states exist for any species

$$S_{vibrational} = k_B \sum_i \frac{hv_i}{k_B T} \left(\frac{1}{\frac{hv_i}{e^{\overline{k_B T}} - 1}} \right) - k_B \sum_i \ln\left(1 - e^{-\frac{hv_i}{k_B T}}\right)$$
(S.5)

Being non-linear, they have 3N-6 real vibrational modes (v_i), where N is the number of atoms in the gas molecule. Both ethylene and 1-butene are non-linear molecules with symmetry numbers of 4 and 1, respectively. For surface species with some atoms frozen, there should be 3N real modes and 3N-1 real modes of vibration for a transition state.

Additionally, for non-linear gas molecules,

$$S_{rotational} = k_B \left[\ln \left[\left(\frac{8\pi^2 k_B T}{h^2} \right)^{\frac{3}{2}} \frac{\sqrt{I_A I_B I_C}}{\sigma} \right] + 1 \right]$$
(S.6a)

Where $I_A I_B I_C$ is the product of inertia of a molecule, summed over all atoms of the molecule, σ denotes the "rotational symmetry number" for the molecule.

While for linear gas molecules like hydrogen,

$$S_{rotational} = k_B \left[\ln \left(\frac{8\pi^2 l k_B T}{\sigma h^2} \right) + 1 \right]$$
(S.6b)

3-4mr free energy surfaces

Fig. S8: Energy profiles of $2C_2H_4 \rightarrow 1-C_4H_8$ on 3-4mr (\equiv SiO)₃M(H) sites of **a**) **Ti**, **b**) **Zr** and **c**) **Hf**. ZPE corrected electronic energy profile (dashed lines): Ti (black), Zr (yellow) and Hf (blue). Red (dot dashed) and green (solid) curves are the free energies at T = 473 K, P = 1 bar with either **1**) complete loss of translational entropy (S_{trans}) of gas molecule on reacting with surface, while retaining rotational and vibrational entropy (red curve) 2) from harmonic vibrational modes of surface species combined with rigid rotor approximation (S_{total}) (green curve). Physiosorbed states are excluded from this comparison.

Fig. S9: PES of termination routes at T = 298 K and T = 473 K, P = 1 bar on the 3-4mr (\equiv SiO)₃MC₄H₉ sites on silica (111). Termination routes are color coded as in Fig. 4: β -H to M (blue curve, via TS(3a)), β -alkyl transfer to M (green curve) and β -H transfer to ethylene (red curve). Dashed line is energy barrier associated with chain growth via TS(2).

3-4mr microkinetic models

Fig. S10: Steady state coverages for 3-4mr (\equiv SiO)₃MH site of **a**) Ti, **b**) Zr and **c**) Hf against temperature at P_{C2H4} =17 bar.

Fig. S11: Degree of rate control at $P_{C2H4} = 17$ bar on **a**) Ti **b**) Zr and **c**) Hf 3-4mr (\equiv SiO)₃MH site. Reactions are color coded as shown.

Degree of Polymerization $(\overline{P_n})$

Number average molecular weight M_n is calculated by equation (S.7a). M_i is the molecular weight of grown hydrocarbon chain composed of "*i*" monomer units. N_i is the number of chains having that molecular weight. M_o is the molecular weight of ethylene monomer.

We express the rate of production of N_i (eq. S.7a) as the rate of chain termination from surface species having identical monomer units or its coverage θ_i , where k_{term} is the termination rate constant.

$$M_{n} = \frac{\Sigma M_{i} N_{i}}{\Sigma N_{i}} = \frac{\Sigma (i M_{o}) N_{i}}{\Sigma N_{i}}$$
(S.7a)

$$M_{n} = \frac{M_{o} \sum_{i=1}^{\infty} i.(k_{term} \theta_{i})}{\Sigma k_{term} \theta_{i}}$$
(S.7b)

Assuming, C-C bond formation step by migratory insertion into M-C bond and termination to be irreversible and rate constants k_{cc} , k_{term} remaining same for oligomers of all chain lengths, coverage of every surface species is expressed in terms of its predecessor⁷ and a constant (α). α is probability of propagation in Cossee-Arlman mechanism.

For
$$i > 1$$
, $\theta_i = \alpha \theta_{i-1} = \alpha^{i-1} \cdot \theta_1$ (S.8)

Upon simplifying eq. S.7b by substituting eq. S.8, $\overline{P_n}$ can be calculated from eq S.9⁷

$$\overline{P_n} = \frac{M_n}{M_o} = \frac{1}{(1-\alpha)}$$
(S.9)

In $\overline{P_n}$ calculation, physisorption step is not considered and M-C insertion takes place as $MP_{i-1} + C_2H_4 \rightarrow MP_i$. MP_i is surface species composed of hydrocarbon chain of "*i*" monomer units bonded to metal site.

At steady state, by mole balance

$$MP_{i} = \frac{P_{C2H4.}k_{cc}}{(P_{C2H4.}k_{cc} + k_{term})} MP_{i-1}$$
(S.10)

$$\alpha = \frac{P_{C2H4.k_{cc}}}{(P_{C2H4.k_{cc}} + k_{term})}$$
(S.11)

With hydrogen present,

By steady state mole balance, MP_i = $\frac{P_{C2H4.}k_{cc}}{(P_{C2H4.}k_{cc} + k_{term} + P_{H2.}k_{hyd})}$ MP_{i-1}

$$\overline{P_n} = \frac{1}{(1 - \alpha_{H2})} = \frac{1}{(1 - \frac{P_{C2H4} \cdot k_{cc}}{P_{C2H4} \cdot k_{cc} + k_{term} + P_{H2} \cdot k_{hyd}})} = 1 + \frac{P_{C2H4} \cdot k_{cc}}{k_{term} + P_{H2} \cdot k_{hyd}}$$
(S.12)

Kinetic parameters, k_{cc} from 2 \rightarrow TS(2), k_{term} from 4 to TS(3a), k_{hyd} is hydrogenolysis rate constant.

Low pressure and temperature rates and $\overline{P_n}$ for Zr site models

Fig. S12: (a) Computed rates, r and (b) degree of polymerization on model ZrH sites at $P_{C2H4} = 0.02$ bar (colored points) and 0.27 bar (grayscale points)

Fig. S13: (top) Free energy profiles for competing M-alkyl (MR') reaction on Ti, Zr, and Hf 3-4mr sites at 298 K. (second row) $\overline{P_n}$ against H₂/C₂H₄ molar ratio at 298 K. Third and fourth rows, same results at 473 K. Reactions shown are: 1) M-C insertion via TS(2), 2) hydrogenolysis to alkane (R'H) via TS(4) and 3) termination by β -H to M via TS(3a) to olefin ($R^{"}_{=}$).

Grafting and hydrogenolysis of Zr(CH₃)₄ to 3-3mr site

Fig. S14: Generation of reconstructed silica (in b) from functionalization of silica (111) facet (in a).

Grafting of precursor $Zr(CH_3)_4$ on silanols of reconstructed silica surface (Fig. S14b) is performed as per reaction (s1) to form (\equiv SiO)_n $Zr(CH_3)_{4-n}$ species on surface, where n=1, 2 or 3. The transformation of these grafted Zr-alkyls to corresponding hydrides occurs as per reactions (s2). Structures of (\equiv SiO)_n $Zr(CH_3)_{4-n}$, and (\equiv SiO)_n $Zr(H)_{4-n}$ are in Fig. S16, in top row and bottom row, respectively with their energies in Table S10. Thermodynamics of sequential grafted complexes and their hydrogenation is shown in Fig. S15a with reaction energies in Table S11. Fig. S15b is a parity plot comparing heats of grafting (ΔE_{rxn}^{DFT}) of $Zr(CH_3)_4$ on reconstructed silica against the original silica(111) model.

Table S10: PBE computed energies (E^{DFT})	in eV of grafting and hydrogenolysis structures on
reconstructed silica.	

Species	n	E^{DFT} (eV)
(≡SiO)M(CH ₃) ₃	1	-573.702
$(\equiv SiO)_2M(CH_3)_2$	2	-551.044
$(\equiv SiO)_3M(CH_3)$	3	-527.632
$(\equiv SiO)M(H)_3$	1	-522.341
$(\equiv SiO)_2M(H)_2$	2	-516.885
$(\equiv SiO)_3M(H)$	3	-510.564
Clean Silica slab		-508.103

	Gra	fting Zr(C	^C H ₃) ₄	Hydrogenolysis of grafted (SiO) _n Zr(CH ₃) _{4-n}			
Μ	Calcula	ted by read	ction (s1)	Calculated by reaction (s2)			
	n=1	n=2	n=3	n=1	n=2	n=3	
Zr on reconstructed	-2.17	-3.54	-4.16	-0.45	-0.38	-0.20	
Zr on silica (111)	-2.27	-4.21	-5.81	-0.62	-0.56	-0.21	
(from Table S3)	,						

Table S11: PBE-computed heats of grafting (CH₃)₄Zr in eV on reconstructed silica surface

Fig. S15: a) Grafting and hydrogenolysis of $Zr(CH_3)_4$ on reconstructed silica(111) **b)** Parity plot of $Zr(CH_3)_4$ grafting energies on reconstructed silica vs parent/as-cleaved silica (111). Parity line shown in yellow.

Fig. S16: Grafting and hydrogenolysis intermediates on reconstructed silica. H: green, C: brown, O: red, Si: blue, Zr: yellow (). Distances in Å. CONTCARs in Zenodo.¹¹

3-3mr oligomerization intermediates and reactions

Fig. S17: Oligomerization intermediates on 3-3mr (≡SiO)₃**Zr**H site. Distances in Å. CONTCARs in Zenodo.¹¹

Table S12: Structural parameters of species formed along pathways in Fig. 2 for $2C_2H_4 \rightarrow C_4H_8$ and C_2H_4 + H₂ \rightarrow C₂H₆ on 3-3mr (\equiv SiO)₃ZrH site. **M-O** (Å) is bond distance between M and nearest O atoms. $\overline{M-O}$ is the average M-O bond distance and is calculated by: $\overline{M-O} = \frac{(M-O1)+(M-O2)+(M-O3)}{3}$. Similarly, $\overline{\angle OMO}$ is the average O-M-O angle (\angle) in degrees (°). Dihedral angle is between atoms in

	M-O (Å)		Smallest		۷	O-M-O	(°)			
c •	M-	M-	M-	<u>м</u> – О (Å)	M-H or	01-M-	02-	03-M-	∠0M0 (°)	∠Dihedral (°)
Species	01	02	03		MI-C(A)	02	M-03	01		
Zr-H	2.01	2.01	2.01	2.01	1.89	100.3	100.4	100.7	100.5	
C ₂ H ₄ -ZrH	2.02	2.02	2.01	2.02	1.89	103.3	97.0	96.6	99.0	
TS1_Zr	2.02	2.01	2.04	2.02	1.93	103.9	95.8	95.7	98.5	9.8
ZrC ₂ H ₅	2.03	2.02	2.02	2.02	2.23	100.3	102.0	100.2	100.8	
C_2H_4 - ZrC_2H_5	2.02	2.02	2.04	2.03	2.26	97.2	96.4	105.6	99.7	
TS2 or TS3b	2.11	2.01	2.01	2.04	2.35	102.2	93.2	93.2	96.2	10.2
ZrC ₄ H ₉	2.02	2.02	2.02	2.02	2.23	100.8	101.9	100.5	101.1	
TS3a_Zr	2.06	2.02	2.01	2.03	1.95	105.5	94.5	94.1	98.0	12.4
C ₄ H ₈ -ZrH	2.02	2.03	2.01	2.02	1.89	104.2	95.7	96.4	98.8	
C ₂ H ₄ -ZrC ₄ H ₉	2.03	2.01	2.05	2.03	2.26	105.5	97.6	96.2	99.8	
TS3c_Zr	2.07	2.00	2.02	2.03	2.42 (C of C ₄ H ₈)	101.3	96.6	95.4	97.8	
C_4H_8 - ZrC_2H_5	2.03	2.01	2.04	2.03	2.25	98.6	98.1	103.2	100.0	
H ₂ -ZrC ₂ H ₅	2.02	2.03	2.02	2.02	2.25	99.6	102.3	99.6	100.5	
TS4_Zr	2.05	2.02	2.01	2.03	1.99 (H of H ₂)	100.5	94.3	98.1	97.6	21.7 (Zr-H-H-C)
C ₂ H ₆ -ZrH	2.01	2.0	2.0	2.0	1.88	100.7	100.2	99.9	100.3	

which bond is formed or broken during transition state

M = Zr	3-3mr (SiO) ₃ ZrH				
	$E^{DFT}(eV)$	$E^{ZPE}(eV)$			
(SiO) ₃ MH (clean)	-510.525	0.484			
C_2H_4 MH(SiO) ₃	-542.872	1.892			
TS(1)	-542.730	1.887			
(SiO) ₃ MC ₂ H ₅	-544.006	1.993			
C_2H_4 $MC_2H_5(SiO)_3$	-576.151	3.399			
TS(2) or $TS(3b)$	-575.539	3.444			
(SiO) ₃ MC ₄ H ₉	-577.098	3.512			
TS(3a)	-575.800	3.385			
C ₄ H ₈ MH(SiO) ₃	-576.008	3.393			
C_2H_4 MC ₄ H ₉ (SiO) ₃	-609.258	4.917			
TS(3c)	-608.057	4.825			
$C_4H_8-MC_2H_5(SiO)_3$	-609.290	4.898			
H_2 MC_2H_5	-550.821	2.348			
TS(4)	-550.112	2.383			
MHC ₂ H ₆	-551.061	2.478			
Bim-TS(3a)	-607.976	4.788			
TS(3d)	-608.101	4.819			
ZrC ₂ H ₃	-535.719	1.401			

Table S13: PBE computed (E^{DFT}) and zero-point (E^{ZPE}) energies of 3-3mr (\equiv SiO)₃ZrH intermediates.

Table S14: ZPE corrected reactions energies (**d**E) and activation energies (**E**_a) in eV for ethylene dimerization on 3-3mr (\equiv SiO)₃Zr(H) site on reconstructed silica. Physisorption denoted by "*". For non-activated adsorption, barriers are assumed to be 0

No.	Reactions	2	<u>L</u> r
		Ea	dE
1*	$C_2H_4 + MH \rightarrow C_2H_4$ MH	0	-0.33
1	$C_2H_4MH \rightarrow MC_2H_5$	0.14	-1.03
2*	$C_2H_4 + MC_2H_5 \rightarrow C_2H_4 - MC_2H_5$	0	-0.13
2	$C_2H_4-MC_2H_5 \rightarrow MC_4H_9$	0.66	-0.83
3a	$MC_4H_9 \rightarrow C_4H_8MH$	1.17	0.97
3a*	$C_4H_8MH \rightarrow 1-C_4H_8 + MH$	0	0.27
3c*	$C_2H_4 + MC_4H_9 \rightarrow C_2H_4 - MC_4H_9$	0	-0.14
3c	$C_2H_4MC_4H_9 \rightarrow MC_2H_5+1-C_4H_8$	1.11	-0.05
3d	$C_2H_4-MC_4H_9 \rightarrow MC_2H_3+C_4H_{10}$	1.06	-0.01
4	$H_2 + MC_2H_5 \rightarrow HM + C_2H_6$	0.77	-0.06

3-3mr transition state distortions

We compared the C-C bond formation from M-C insertion and β -H termination barriers for the 3-4mr and 3-3mr (\equiv SiO)₃ZrH sites in Fig. 8b. Barriers are lower on the latter site, and the effect is more significant for the C-C bond formation via M-C insertion reaction. Greater H-M-O angles at the more strained 3-3mr site are consistent with more ready access of ethylene. Similar, smaller average distortion (a) at the transition state is consistent with lower barriers.

Table S15: Structural parameters of species formed on 3-4mr and 3-3mr (≡SiO) ₃ ZrH site on as-cleaved	
and reconstructed silica (111), respectively. Bond distances in angstroms (Å) and angles (\angle) in degrees (°)

		3-4mr				3-3mr			
	1	∠Si-O-M (°))	∠ <i>Si</i> OM	∠Si-O-M (°)			∠ <i>Si</i> OM	
Species	Si1-O1-M	Si2-O2-M	Si3-O3-M	(°)	Si1-O1-M	Si2-O2-M	Si3-O3-M	(°)	
Zr-H	141.8	141	139.1	140.6	113.2	113.3	113.2	113.2	
TS1_Zr	144.8	144.2	140.7	143.2	116.7	114.1	113.8	114.9	
$\operatorname{ZrC}_{2}\operatorname{H}_{5}(2)$	138.8	134.8	142.6	138.7	112.0	111.9	112.9	112.3	
TS2_Zr	163.6	138.6	138.3	146.8	117.5	116.9	116.2	116.9	
ZrC ₄ H ₉ (4)	140.2	138.1	140.0	139.4	111.8	111.9	112.7	112.1	
TS3a_Zr	147.3	141.4	141.2	143.9	113.8	117.4	114.3	115.2	
			Averag	e Induced	d Strain, <a< th=""><th>a> (°)</th><th></th><th></th></a<>	a> (°)			
Zr: ZrH→TS1		143.2-140).6 = 2.6			114.9 -113	.2 = 1.7		
Zr: 2→TS2		146.8 - 139	€.2 = 8.1			112.3 - 116	9 = 4.6		
Zr: 4→TS3a		143.9 - 139	-4.5		115.2 - 112.1 = 3.1				

3-3mr microkinetic model

Fig. S18: (a,b) Termination vs oligomerization free energy surfaces at 3-3mr (SiO)₃ZrH site at 298 and 473 K and 1 bar ethylene. Termination routes color coded as in Fig. 4: (c) Steady state coverages vs temperature at P_{C2H4} =17 bar d) Degree of rate control at P_{C2H4} =17 bar. Reactions color-coded as in Fig. S11.

Table S16: (top) Activation energies for chain growth via TS(2) and termination via TS(3a), bim-TS(3a), TS(3b), TS(3c) and TS(3d) for 3-3mr (SiO)₃ZrH site at T = 0 K, 298 K and 473 K. (bottom) Consequences of various termination routes on computed $\overline{P_n}$ at low and high ethylene pressure (P_{C2H4}).

Reactions	ΔE^{\neq} (eV)	$\Delta G^{\neq,298K}$ (eV)		$\Delta G^{\neq,473K}$ (eV)	
$C_2H_4 + MC_2H_5 \rightarrow TS(2)$	0.53	0.994		1.3	14
$MC_4H_9 \rightarrow TS(3a)$	1.172	1.1	72	1.1	72
$C_2H_4 + MC_4H_9 \rightarrow \text{bim-TS}(3a)$	1.01	1.4	74	1.7	94
$C_2H_4 + MC_4H_9 \rightarrow TS(3c)$	0.966	1.4	-3	1.7	75
$MC_4H_9 \rightarrow TS(3b)$	1.492	1.4	92	1.492	
$C_2H_4 + MC_4H_9 \rightarrow TS(3d)$	0.915	1.379		1.70	
		$\overline{P_n}$		$\overline{P_n}$	
$\overline{P_n}$ Expressions		<i>P_{C2H4}</i> = 0.27 bar	$P_{C2H4} = 17$ bar	<i>P_{C2H4}=</i> 0.27 bar	$P_{C2H4} = 17$ bar
$\overline{P_n} = 1 + \frac{k_{CC}}{k_{term}} P_{C2H4}$ Where $k_{term} = k_{TS(3a)}$	-	277	1.74 x10 ⁴	1.01	1.52
$\overline{P_n} = 1 + \frac{k_{CC}}{k_{term}} P_{C2H4}$ where $k_{term} = k_{TS(3a)} + k_{TS(3b)} + P_{C2H4} \cdot k_{TS(3c)} + P_{C2H4} k_{bim-TS(3a)} + P_{C2H4} k_{TS(3d)}$	-	277	1.73 x10 ⁴	1.01	1.52

 $k_{TS(3a)}, k_{TS(3b)}, k_{TS(3c)}, k_{TS(3d)}, k_{bim-TS(3a)}$ are rate constant for different chain termination processes. k_{CC} is chain growth rate constant. ΔE^{\neq} is ZPE corrected DFT energy barrier and ΔG^{\neq} is free energy barriers at a given temperature

Fig. S19: Free energy profiles for the 3-3mr Zr-alkyl (MR') surface site along and corresponding $\overline{P_n}$ changes with P_{H2}/P_{C2H4} from 0 to 1 at **a**) T = 298 K **b**) T = 473 K for **1**) M-C insertion upon ethylene coordination via TS(2), **2**) hydrogenolysis upon hydrogen addition via TS(4), **3**) termination by β -H transfer to M via (TS3a) to olefin (R''=).

Fig. S20: a) (001) silica surface with geminal silanols and two Si-OHs that are condensed are circled **b)** Dehydroxylated (001) silica surface having the new Si-O-Si bond between the two silanols left on top.

Grafting and hydrogenolysis of M(CH₃)₄ to 1-3mr site

Grafting of M(CH₃)₄ on silanols of dehydroxylated (001) silica surface (Fig. S20b) is performed as per reaction (s1) to form (\equiv SiO)_nM(CH₃)_{4-n} species on surface, where n=1, 2 and their further transformation to hydrides occurs as per reactions (s2). Thermodynamics of sequential grafted complexes of Zr(CH₃)₄ and their hydrogenation is shown in Fig. S21a, while Fig. S21b compares heats of grafting (ΔE_{rxn}^{DFT}) of M(CH₃)_{4-n} on the (001) silica against (\equiv SiO)_nZr(CH₃)_{4-n} on (111) silica. Grafting is exothermic for all species. Structural energies are in Table S17 and reaction energies in Table S18. Structures of (\equiv SiO)_nM(CH₃)_{4-n}, and (\equiv SiO)_nM(H)_{4-n} are in Fig. S22 in the top row and bottom row, respectively.

A non-periodic trend is visible in hydrogenolysis energies on (001) facet (Table S18), alike that on silica (111) surface (Table S3).

Table S17: PBE computed energies E^{DFT} (*without ZPE correction*) in eV for structures in grafting and hydrogenolysis process on dehydroxylated (001) silica shown in Fig. S20b

		$E^{DFT}(eV)$				
Species	n	Ti	Zr	Hf		
$(\equiv SiO)M(CH_3)_3$	1	-250.038	-251.087	-252.992		
$(\equiv SiO)_2M(CH_3)_2$	2	-227.693	-228.708	-230.717		
$(\equiv SiO)M(H)_3$	1	-198.590	-200.019	-201.891		
$(\equiv SiO)_2M(H)_2$	2	-193.448	-194.584	-196.561		
Clean dehydroxylated (001) silica	-		-185.500			

Table S18: DFT computed heats of grafting $M(CH_3)_4$ on dehydroxylated silica (001) surface using energies (in eV) from Table S17

	Grafting M(CH	[₃) ₄ on silica (001)	Hydrogenolysis of grafted (SiO) _n M(CH ₃) _{4-n}			
Μ	A Calculated by reaction (s1)		Calculated by reaction (s2)			
	n=1	n=2	n=1	n=2		
Ti	-2.03	-3.71	-0.37	-0.30		
Zr	-2.16	-3.81	-0.74	-0.42		
Hf	-2.20	-3.96	-0.71	-0.39		

Fig. S21: a) Heats of formation of $(\equiv SiO)_n Zr(CH_3)_{4-n}$ (R= CH₃) and hydrogenolysis to $(\equiv SiO)_n Zr(H)_{4-n}$ [n=1,2] on dehydroxylated (001) silica **b)** Parity plot comparing heats of formation of $(\equiv SiO)_n M(CH_3)_{4-n}$ for Ti, Zr and Hf [n=1, 2] on dehydroxylated silica (001) against $(\equiv SiO)_n Zr(CH_3)_{4-n}$ on as-cleaved silica (111) [n = 1,2,3]. Energies of $(\equiv SiO)_n Zr(CH_3)_{4-n}$ on reconstructed silica also shown.

Fig. S22: Structures of $(\equiv SiO)_n M(CH_3)_{4-n}$ in top row and $(\equiv SiO)_n M(H)_{4-n}$ in bottom for Ti, Zr and Hf from left to right on dehydroxylated silica (001). H: green, C: brown, Si: blue, O: red. Distances in Å.

1-3mr oligomerization intermediates and reactions

Table S19: PBE computed energies (\mathbf{E}^{DFT} , *without ZPE correction*) and zero-point energy (\mathbf{E}^{ZPE}) correction in eV for different species on (\equiv SiO)₂MH₂ on silica (001)

	(≡Si0	$D)_2$ Ti H_2	(≡SiO	$)_2$ Zr H ₂	$(\equiv SiO)_2 HfH_2$	
	EDFT	EZPE	EDFT	EZPE	EDFT	EZPE
(SiO) ₂ MH ₂ (clean)	-193.438	0.387	-194.549	0.353	-196.528	0.357
C_2H_4 (SiO) ₂ MH ₂	-225.732	1.812	-227.079	1.791	-228.991	1.800
$(SiO)_2MH(C_2H_5)$	-227.156	1.911	-228.210	1.876	-230.123	1.873
C_2H_4 MH(C_2H_5)(SiO) ₂	-259.271	3.327	-260.495	3.285	-262.402	3.285
TS(1')	-259.186	3.340	-260.406	3.291	-262.249	3.293
$(SiO)_2M(C_2H_5)_2$	-260.548	3.418	-261.494	3.396	-263.443	3.387
$C_2H_4M(C_2H_5)_2(SiO)_2$	-292.592	4.805	-293.527	4.829	-295.467	4.771
TS(2')	-291.916	4.916	-293.219	4.868	-295.031	4.860
$(SiO)_2M(C_2H_5)(C_4H_9)$	-293.743	4.949	-294.707	4.909	-296.656	4.914
TS(3'a)	-292.322	4.829	-293.547	4.788	-295.402	4.787
$(1-C_4H_8)M(C_2H_5)(SiO)_2$	-292.448	4.836	-293.669	4.803	-295.550	4.798

Fig. S23: Geometries of species along the catalytic cycle on $(\equiv SiO)_2MH_2$ site [M= Ti, Zr, Hf] on dehydroxylated (001) silica. Top row shows $(\equiv SiO)_2MH_2$ site, followed by species for $(\equiv SiO)_2TiH_2$, then by $(\equiv SiO)_2ZrH_2$ and last row for $(\equiv SiO)_2HfH_2$. Bond distances in Å. Angles in degrees (°). CONTCARs in Zenodo.¹¹

Table S20: ZPE corrected heats of reactions (dE) in eV for ethylene dimerization on (\equiv SiO)₂M(H)₂. The barrier (Ea) is the energy differences between transition state and initial state at infinite separation. If a value is negative, we treat it as barrierless. For non-activated adsorption, the barriers are assumed to be 0

No.	Reactions	Ti		Zr		Hf	
		Ea	dE	Ea	dE	Ea	dE
1*	$C_2H_4 + MH_2 \rightarrow C_2H_4 - M(H)_2$	0.0	-0.26	0.0	-0.48	0.0	-0.41
2	$C_2H_4M(H)_2 \rightarrow MH(C_2H_5)$	0.0	-1.33	0.0	-1.05	0.0	-1.06
3*	$C_2H_4 + MH(C_2H_5) \rightarrow C_2H_4 - MH(C_2H_5)$	0.0	-0.09	0.0	-0.27	0.0	-0.26
4	$C_2H_4MH(C_2H_5) \rightarrow M(C_2H_5)_2$	0.13	-1.19	0.10	-0.89	0.16	-0.94
5*	$C_2H_4 + M(C_2H_5)_2 \rightarrow C_2H_4 - M(C_2H_5)_2$	0.0	-0.05	0.0	0.01	0.0	-0.03
6	$C_2H_4M(C_2H_5)_2 \rightarrow M(C_2H_5)(C_4H_9)$	0.79	-1.01	0.35	-1.10	0.52	-1.05
7	$M(C_{2}H_{5})(C_{4}H_{9}) \rightarrow C_{4}H_{8}MH(C_{2}H_{5})$	1.30	1.18	1.04	0.93	1.13	0.99
8*	$C_4H_8MH(C_2H_5) \rightarrow 1-C_4H_8 + MH(C_2H_5)$	0.0	0.07	0.0	0.24	0.0	0.21

Fig. S24: PES for ethylene dimerization mechanism on $(\equiv SiO)_2M(H)_2$ grafted on dehydroxylated silica (001), M = **Ti (black)**, **Zr (yellow)** and **Hf (blue)**. Energies are referenced to 1-3mr($\equiv SiO)_2M(H)_2$ site and $3C_2H_4$ gas molecules. Species numbers correspond to catalytic cycle shown in Fig. 11b.

The PES (Fig. S24) is referenced to the dihydride site, $(\equiv SiO)_2MH_2$ and ethylene molecules. Ethylene forms a stronger π -complex with $(\equiv SiO)_2MH_2$ than with $(\equiv SiO)_3MH$. The first ethylene insertion into M-H bond is exothermic and barrierless as no transition state is located when ethylene approaches the metal vertically downward rather than sideways (CI-NEB for Zr is similar to Hf in Fig. S26, Fig. S27 for Ti). It is further exogenic for ethylene to insert into the second M-H bond of $(\equiv SiO)_2MH(C_2H_5)$ (**2'a**) and occurs via a four-centered transition state TS(1') (Fig. S23). TS(1') has a tiny barrier as compared to the next step of chain growth on $(\equiv SiO)_2M(C_2H_5)_2$ (**2'b**) to produce $(\equiv SiO)_2M(C_2H_5)(C_4H_9)$ (**4'**) by M-C insertion of ethylene. The four-centered TS(2') (Fig. S23) shows ethylene conjoining M-ethyl to form the C-C bond approaches much closer to Ti than to Zr and Hf while the non-participating ethyl chain is aligned nonagostically. 1-butene is released from **4'** by endothermic β -H transfer to M via TS(3'a) leaving behind $(\equiv SiO)_2MH(C_2H_5)$, **2'a**. The order in energy barriers is $E_{a,term} > E_{a,C-C} > E_{a,M-H}$ for M(Et)H (Et = ethyl, C_2H_5) for M= Ti, Zr and Hf, same as that on 3-4mr ($\equiv SiO)_3MH$ sites.

Fig. S25: TS(1') and TS(3'a) structures on left and right, respectively, with (top row) and without (bottom) agostic interaction of the side alkyl chain on $(\equiv SiO)_2MH_2$ site (M= Ti (black), Zr (yellow), Hf (blue)). E^{DFT} energies are lower for non-agostic structures.

Fig. S26: CI-NEB trajectories for insertion of ethylene into Hf-H bond of $(\equiv SiO)_2$ HfH₂. Similar trajectories found for this insertion into Zr-H bond of $(\equiv SiO)_2$ ZrH₂. Top row shows ethylene coming sideways with energy graph on the left of bottom row. Middle row shows ethylene coming to M ion vertically downward and is zero barrier path from energy plot (right in bottom row). Distances in Å.

Fig. S27: CI-NEB images and energy graph for a) insertion of ethylene approaching vertically downward into Ti-H bond of $(\equiv SiO)_2 TiH_2$ site. No transition state is located for this reaction step. b) ethylene insertion on one of the Ti-C bonds of $(\equiv SiO)_2 Ti(Et)_2$ c) Termination by β -H transfer to M yielding 1-butene and $(\equiv SiO)_2 Ti(H)(Et)$. Similar trajectories have been used to locate corresponding TSs on Zr and Hf sites. Distances in Å.

1-3mr microkinetic models

Fig. S28: a) Parity plot of activation energies of M-C insertion ($E_{a,C-C}$) and β -H termination to M ($E_{a,term}$) on 1-3mr (\equiv SiO)₂MH₂ (triangles) and 3-3mr (\equiv SiO)₃MH (square) against those on 3-4mr (\equiv SiO)₃ZrH (circle) sites **b**) $\overline{P_n}$ on log scale vs temperature at P_{C2H4}=17 bar for 1-3mr Ti (black), Zr (orange), Hf (blue) sites.

References

- 1) Wyckoff, R. W. G. Crystal Structures, 2nd ed., John Wiley & Sons, **1963**, vol. 1, chapter 4, 239.
- 2) Davidson, P. J.; Lappert, M. F.; Pearce, R., Chem. Rev., 1976, 76, 2, 219-242.
- Larabi, C.; Merle, N.; Norsic, S.; Taoufik, M.; Baudouin, A.; Lucas, C.; Cazat, J. T.; Mallmann, A.; Basset, J. M., Organometallics, 2009, 28, 5647–5655.
- 4) Thieuleux, C.; Quadrelli, E. A.; Basset, J. M.; Döbler, J.; Sauerb, J., *Chem. Commun.*, **2004**, 1729-1731.
- 5) Corker, J.; Lefebvre, F.; Lecuyer, C.; Dufaud, V.; Quignard, F.; Choplin, A.; Evans, J.; Basset, J.M., *J.-M. Science*, **1996**, 271 (5251), 966-969.
- 6) Tosin, G.; Santini, C. C.; Baudouin, A.; Mallman, A. d; Fiddy, S.; Dablemont, C.; and Basset, J.-M., *Organometallics*, **2007**, 26, 17, 4118-4127.
- 7) Lo, D. P.; Ray, W. H., Ind. Eng. Chem. Res., 2005, 44, 5932-5949.
- 8) Campbell, C. T.; Sellers, J. R.V., J. Am. Chem. Soc., 2012, 134, 18109–18115.
- 9) Rosier, C.; Niccolai, G. P.; Basset, J.-M., J. Am. Chem. Soc. 1997, 119, 12408-12409.
- 10) Larsen, A. H. et al. J. Phys.: Condens. Matter, 2017, 29, 273002.
- 11) Mehra, N.; Schneider, W. F. https://doi.org/10.5281/zenodo.11251373, 2024