Electronic Supplementary Information

Vibrational frequencies utilized for the assessment of exchangecorrelation functionals in the description of metal-adsorbate systems: C_2H_2 and C_2H_4 on transition-metal surfaces

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S1. Geometry analysis of C_2H_2 and C_2H_4

Geometry optimizations for the molecules in the gas phase are performed. The obtained geometrical parameters are listed in Table S1 along with the corresponding experimental values.

Table S1: Calculated and experimental geometrical parameters (bond lengths d and angles ∠ in Å and degree, respectively) for the C_2H_2 and C_2H_4 molecules in the gas phase.

C_2H_2	mBEEF	RPBE	Exp ¹
$d_{\mathrm{CH}}(\mathrm{A})$	1.059	1.070	1.061
$d_{\rm CC}(\rm A)$	1.194	1.210	1.203
C_2H_4	mBEEF	RPBE	Exp ²
$d_{\rm CC}$ (A)	1.322	1.337	1.337 ± 0.003
$d_{\text{CH}}(\text{Å})$	1.081	1.092	1.086 ± 0.003
\angle (HCC)	121.78	121.75	121.35 ± 1
\angle (HCH)	116.4	116.5	
\angle ((CH ₂)-C)	179.97	179.94	180.00

S2. Bulk lattice constants

Table S2: Bulk lattice constant *a* (in Å) of each material in its stable crystal phase (FCC structure with space group *Fm*¯3*m*) obtained by mBEEF and RPBE XC functionals. A k-point mesh of 20×20×20 was used for each calculation. The values in parentheses next to the mBEEF and RPBE values indicate the deviation from experimental results. Last row shows the mean absolute percentage error (MAPE) of each functional. mBEEF(QHA) and RPBE(QHA) are the results incorporating thermal effects via the quasi-harmonic approximation (QHA) at the experimental temperature at which the lattice constants were measured. The QHA was evaluated using the phonon analysis as implemented in Phonopy.²⁸

S3. Vibrational modes

Figure S1 illustrates different vibrational modes of acetylene and ethylene in gas phase. Arrows in orange are showing the movement direction. Dot and cross marks inside the orange circles are used to show the movement direction. Here, we briefly describe the movements of atoms in each type of the vibrational modes. As shown in the figure, "twisting" modes are related to a change in the angle between planes containing groups of atoms. "Rocking" modes represent a change in the angle between the group of H-C-H atoms (shown in pink) and the rest of the molecule. A change in the angle between the plane of a group of H-C-H atoms (shown in pink) and a plane through the rest of the molecule refers to "wagging" modes. Rocking is distinguished from wagging by the fact that the atoms in the group stay in the same plane as the rest of the ethylene molecule. The inplane and out-of-plane bending modes are denoted by *δ* and *γ*, respectively. In a rocking, wagging or twisting coordinate the bond lengths within the atomic groups involved slightly change. So the dominant movements are in the angles.

Figure S1: Vibrational modes of acetylene and ethylene in gas phase. *ν*, *δ* and *γ* denote stretch mode, in-plane bending mode and out-of-plane bending mode, respectively. "a" and "s" represent asymmetric and symmetric stretches, respectively. Dot and cross marks inside the orange circles denote the out-of-plane movement direction of an atom or group of atoms.

S4. Vibrational frequencies of C_2H_2 and C_2H_4 in the gas phase

The calculated vibrational frequencies of C_2H_2 and C_2H_4 in the gas phase and the corresponding experimental values are summarized in Table S3 (detailed description of each vibrational mode is provided in the previous section and shown in FIG. $S1$). C_2H_2 is a symmetric linear molecule with 3*N* − 5 = 7 normal modes. However, only five modes are reported in the table because the bending modes come in degenerate pairs, i.e., there are two equivalent modes with the same frequency. According to the calculated data shown in the table, the vibrational frequencies obtained by the mBEEF functional are overestimated while the RPBE functional underestimates them: the mean percentage error (MPE = $\frac{100}{16} \sum_{i=1}^{16} \frac{DF A_i - Exp_i}{Exp_i}$ $\frac{16}{i=1} \frac{D \cdot R_1 - E \cdot D_1}{E \cdot R}$ of all the considered vibrational modessummarized in Table S3 obtained by mBEEF and RPBE are 3*.*04% and −0*.*13%, respectively.

To simplify the comparison, the frequency differences of each vibrational mode of the C_2H_2 and C_2H_4 molecules (in gas phase) with respect to the experimental values are shown in the FIG. S2. Our analysis shows that the root mean square error (RMSE) of the vibrational frequencies obtained with RPBE is smaller than for mBEEF by 79 cm⁻¹ for C₂H₂ and 58 cm⁻¹ for C₂H₄.

Another notable result in the FIG. S2 is the larger deviation of the mBEEF results for the stretching modes while the bending modes (rocking, wagging, and scissoring) display smaller deviations. From comparison of calculated vibrational frequencies of stretching modes with experiment it can be inferred that mBEEF overestimates the strength of the bonds. However, the electrostatic interactions and orbital hybridization determining the bending force constants are less affected by the approximations in the XC functional, which results in smaller frequency deviations for bending-type vibrational modes.

Figure S2: Deviations of calculated vibrational frequencies of C_2H_2 and C_2H_4 molecules in gas phase from experimental values. The blue squares and pink triangles indicate the deviations for mBEEF and RPBE functionals, respectively. (See Table S3 for the values of vibrational frequencies and experimental references.) RMSE and MPE denote root mean squared error and mean percentage error, respectively.

Table S3: The vibrational frequencies (in cm−1) of the C2H2 and C2H4 molecules in the gas phase. *ν*, *δ* and *γ* denote stretch mode, in-plane bending mode and out-of-plane bending mode, respectively. "a" and "s" denote asymmetric and symmetric modes, respectively. RMSE and MPE denote the values of root mean squared error and mean percentage error, respectively.

C_2H_2	mBEEF	RPBE	Exp. ⁴
δ^s CH	555	578	612
$\delta^a{}_{\rm CH}$	782	730	729
$v_{\rm CC}$	2082	2001	1974
${\rm v}^{\rm s}{}_{\rm CH}$	3446	3342	3295
$\rm v^a{}_{\rm CH}$	3551	3439	3373
$RMSE$ (cm ⁻¹)	120	41	
MPE $(\%)$	2.658	-0.133	
C_2H_4	mBEEF	RPBE	Exp. ⁵
$\delta^\text{rock}{}_\text{CH2}$	839	804	826
$\gamma^{\rm wag}{}_{\rm CH2}$	950	929	940
γ ^{wag} CH ₂	973	941	949
γ^{twist} CH2	1080	1032	
$\delta^\text{rock}{}_\text{CH2}$	1250	1203	1222
$\delta^{\rm scissor}$ CH2	1390	1340	1342
$\delta^{\rm scissor}$ CH2	1477	1430	1444
$v_{\rm CC}$	1697	1631	1623
v^s CH	3140	3052	2989
v^s CH	3159	3065	3026
v^a CH	3216	3121	3103
v^a CH	3242	3150	3105
$RMSE$ (cm ⁻¹)	87	29	
MPE $(\%)$	3.216	-0.130	

S5. Vibrational frequencies of adsorbed C_2H_2 and C_2H_4

Table S4 summarizes the chamber exposures and the reported coverage for the adsorbed species. The vibrational frequencies of adsorbed C_2H_2 and C_2H_4 on FCC(111) surfaces of Pt, Pd, Rh, and Cu are summarized in Table S5.

system	P	H
$C_2H_2/Pd(111)^6$	3	1/3
$C_2H_2/Pd(111)^7$	1.5	1/3
$C_2H_2/Rh(111)^8$	0.5	1/4
$C_2H_2/Cu(111)^9$	2.3	
$C_2H_2/Pt(111)^{10}$	\mathcal{P}	
$C_2H_4/Cu(111)^{11}$	100	1/3
$C_2H_4/Pd(111)^{12}$	30	

Table S4: Experimental/theoretical data on the coverage (*θ* in ML) and gas exposure (*P* in L, 1L= 1 langmuir = 1×10[−]6 Torr-second) for the adsorbed systems.

Table S5: Calculated and experimental vibrational frequencies (in cm⁻¹) for C₂H₂ and C₂H₄ adsorbed on different TMSs at the coverage of 1*/*9 ML and 1*/*4 ML. The values for 1*/*4 ML are shown in parentheses. Stretch modes are labeled by *ν*, while *δ* and *γ* denote in-plane and out-ofplane bending modes, respectively.

mode	method	Pt(111)	Pd(111)	Rh(111)	Cu(111)
C_2H_2		(fcc-par)	(fcc-par)	(fcc-par)	$(b-per)$
$\nu_{\text{CH},\text{s}}$	Exp.	3010^{10}	2990, ⁶ 2992 ⁷	2960^{8}	$2920, 92913$ ¹³
	mBEEF	3164(3146)	3145(3132)	3121(3190)	3090(3069)
	RPBE	3078(3065)	3064(3057)	3043(3036)	3003(2992)
$\nu_{\rm CC}$	Exp.	1310^{10}	1400, 61402 ⁷	12608	$1307, 91294$ ¹³
	mBEEF	1324(1335)	1353(1365)	1295(1298)	1325(1352)
	RPBE	1262(1273)	1303(1316)	1238(1241)	1261(1291)
$\delta_{\rm CH, a}$	Exp.	985^{10}	1034 $\overline{2}$	11208	$920, \frac{9}{9}920$ ¹³
	mBEEF	1170(1170)	1090(1087)	1132(1127)	1152(1144)
	RPBE	1119(1119)	1033(1030)	1078(1073)	1105(1100)
$\delta_{\mathrm{CH},\mathrm{s}}$	Exp.		$872~^{\square}$	950^{8}	
	mBEEF	1017(1024)	929(946)	967(985)	964(973)
	RPBE	976 (985)	885(900)	924(941)	925(935)
$\gamma_{\rm CH, a}$	Exp.		880 ⁶		

Continued on next page

		Pt(111)	Pd(111)		
C_2H_4		$(b-par)$	$(b-par)$		
	mBEEF	872(869)	795(792)	833(825)	914(915)
	RPBE	837(831)	766(761)	802(793)	882(887)
γ CH,s	Exp.	770^{10}	660, 6673 ⁷	720^{8}	680^{9}
	mBEEF	796(794)	710(706)	733(726)	690(671)
	RPBE	759(752)	678(672)	704(695)	659(644)
$\nu_{\rm MC,s}$	Exp.	570^{10}	500 \overline{z}		420^9
	mBEEF	579(593)	532(539)	562(558)	428(435)
	RPBE	546(557)	482(489)	515(513)	394(401)
$\nu^{\bf a}_{\rm CH2}$	Exp.	3000 14			
	mBEEF	3133(3111)	3129(3112)		
	RPBE	3051(3041)	3060(3052)		
$\nu^{\rm s}_{\rm CH}$	Exp.	2940 ¹⁰	$2900,\frac{12}{2}928$ ^{II}		
	mBEEF	3077(3062)	3066(3055)		
	RPBE	2992(2989)	2993(2989)		
$\nu^{\rm s} _{\rm CH2}$	Exp.	2920 14			
	mBEEF	3065(3048)	3054(3040)		
	RPBE	2985(2977)	2985(2978)		
$\delta^{\rm scissor,s}_{\rm CH2}$	Exp.	1430 14	1428 11		
	mBEEF	1470(1471)	1478(1478)		
	RPBE	1422(1423)	1433(1433)		
$\nu_{\rm CC}$	Exp.	1050 14	$1103,121097$ ^{II}		
	mBEEF	1023(1022)	1102(1095)		
	RPBE	980(983)	1087(1081)		

Table S5 $\emph{Continued from previous page}$

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		Pt(111)	Pd(111)	
C_2H_4		$(b-par)$	$(b-par)$	
$\gamma^{\rm{wag,s}}_{\rm{CH2}}$	Exp.	980^{14}	871 11	
	mBEEF	976(980)	910(913)	
	RPBE	932(937)	862(869)	
$\gamma_{\text{CH2}}^{\text{twist,s}}$	Exp.	790^{14}		
	mBEEF	819(811)	796(782)	
	RPBE	790(781)	786(770)	
$\delta^{\rm rock,s}_{\rm CH2}$	Exp.	660^{14}		
	mBEEF	683(678)	603(594)	
	RPBE	649(644)	552(545)	
$\nu^{\rm a}_{\rm MC}$	Exp.	560^{14}		
	mBEEF	587(591)	512(515)	
	RPBE	546(549)	447(453)	
$\nu^{\rm s}_{\rm MC}$	Exp.	$470^{10,14}$		
	mBEEF	493(499)	437(443)	
	RPBE	450(454)	359(370)	

Table $S5$ – *Continued from previous page*

 ^{E} T=130 K, 3L C₂H₂,($\sqrt{3}$ x $\sqrt{3}$)R30, ^e T=130 K, 3L C₂H₂,($\sqrt{3}$ x $\sqrt{3}$)R30,

 $^{\boxtimes}$ 77K,
0.5L C2H2,
0.25ML, $^{\text{I\hspace{-.1em}I\hspace{-.1em}I}}$ C2H₂/Pt(111) at 150-300 K and C₂H₄/Pt
(111) at 140-260 K,

 $\overline{2}$ T=150 K,1.5L C₂H₂, ($\sqrt{3} \times \sqrt{3}$)R30, ^o 110-120 K,

 $\overline{13}$ 250 K, $\overline{14}$ pressure $<10^{-9}$ Pa, T=92K,

 $\overline{\text{ }^{12}}$ 80K, $\overline{\text{ }^{11}}<10^{-10}$ mbar,100K

S6. Adsorption energies of C_2H_2 and C_2H_4 on Pd(111)

The adsorption energies of C_2H_2 and C_2H_4 on Pd(111) are summarised in Table S6.

Table S6: The comparison of our calculated (mBEEF and RPBE) E*ads* (in eV) with available experimental and theoretical data reported in the literature. (θ is the coverage in ML)

S7. Comparison with other XC functionals and effect of van-der-Waals (vdW) corrections

To demonstrate further applications of our approach and the influence of vdW corrections, we calculated vibrational frequencies and adsorption enthalpy of C_2H_4 on the Pt(111) surface with TPSS²², PBEsol²³, and RPBE with the Tkatchenko-Scheffler vdW correction²⁴ (RPBE+TS). TPSS is reported as the reliable functional for the bulk and surface properties of metals²⁵, and PBEsol is also widely used functional for solid systems. As shown in Figure S3a and Table S7, PBEsol gives the lowest RMSE for the vibrational frequency. TPSS shows a moderate performance among the adopted XC functionals, and there is not significant effect of the vdW correction on the accuracy of the vibrational frequency in RPBE+TS. On the other hand, as shown in Figure S3b, RPBE+TS overestimates the adsorption enthalpy compared to RPBE by 0.42 eV. Additionally, PBEsol shows the worst error among the considered functionals while the performance of TPSS is moderate.

We also investigated reaction enthalpy of the semi-hydrogenation of C_2H_2 to C_2H_4 in the gas phase. The calculated reaction enthalpy $H_r(DFA)$ is the difference of the enthalpy of each molecule in the gas phase.

$$
H_r(DFA) = H_{C_2H_4} - (H_{C_2H_2} + H_{H_2})
$$

 $H_r(DFA)$ was compared with experimental reaction enthalpy $H_r(EXp)$ derived from the standard enthalpy of formation.²⁶

$$
H_r(Exp.) = \Delta_f H_{C_2 H_4}^0 - \Delta_f H_{C_2 H_2}^0
$$

As shown in Figure S3c, RPBE showed the best performance. TPSS also showed a good performance, but mBEEF and PBEsol are not so accurate. This trend is also fit to the accuracy trend on the adsorption enthalpy.

By considering the result shown in Figure S3, RPBE is the most reliable functional for the target system because of its high accuracy for the investigated properties. On the other hand, PBEsol showed a good accuracy for the vibrational frequency, but its accuracy for the adsorption and reaction enthalpy is lower than the other functionals. These results suggest that, ideally, the assessment of the XC functionals should be based on multiple aspects. However, in practice, we are bound to use limited available measured quantities, such as vibrational frequencies, for benchmarking the calculation methods to describe metal-adsorbate systems.

Figure S3: Investigation with other XC functionals and vdW correction. Accuracy for (a) vibrational frequencies and (b) adsorption enthalpy of the $C_2H_4/Pt(111)$ system. Note that only vibrations of the adsorbate and its nearest-neighbor Pt atoms are considered for calculating the vibrational frequencies in these investigations. (c) Assessment for the reaction enthalpy of the semihydrogenation of C_2H_2 to C_2H_4 in the gas phase.

Table S7: Summary of the vibrational frequencies of the $C_2H_4/Pt(111)$ system with other XC functionals. Note that only vibrations of the adsorbate and its nearest-neighbor Pt atoms are considered for calculating the vibrational frequencies in this investigation.

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