## Suplementary information for "Transition metal atoms embedded in monolayer $C_{13}N_3$ as OER/ORR bifunctional electrocatalysts"

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TABLE S1.	The total ene	ergy of TM-C <sub>13</sub> N <sub>5</sub>	$(E_{TM-C_{13}N_3}), t$	total energy	of $C_{13}N_3$	with metal	vacancies( $E_{C_{13}N_3}$ ),	total energy of
the isolated <b>r</b>	metal atoms	$(E_{TM-single})$ , and	binding energy	$(E_{\text{bind}})$ . Al	l values ai	re in eV.		

	$E_{\rm TM-C_{13}N_3}$	$\mathrm{E}_{\mathrm{C}_{13}\mathrm{N}_3}$	$\mathrm{E}_{\mathrm{TM-single}}$	$\mathrm{E}_{\mathrm{bind}}$
$\operatorname{Cr}$	-295.05	-284.95	-5.45	-4.65
Mn	-294.71	-284.95	-5.15	-4.61
Fe	-292.93	-284.95	-3.30	-4.68
$\mathrm{Co}$	-291.37	-284.95	-1.73	-4.705
Ni	-290.32	-284.95	-0.29	-5.08
Cu	-288.82	-284.95	-0.25	-3.63
Ru	-292.52	-284.95	-2.00	-5.57
Rh	-291.46	-284.95	-1.26	-5.25
Pd	-289.94	-284.95	-1.48	-3.51
Ag	-288.29	-284.95	-0.20	-3.14
Os	-293.06	-284.95	-2.90	-5.21
Ir	-291.91	-284.95	-1.50	-5.46
$\operatorname{Pt}$	-289.79	-284.95	-0.50	-4.34
Au	-287.56	-284.95	0.19	-2.42

	$\Delta G_{*_{OH}}$	$\Delta G_{*_O}$	$\Delta G_{*_{OOH}}$
$\operatorname{Cr}$	0.20	1.43	3.49
Mn	0.00	2.19	3.37
Fe	0.03	1.43	3.29
Со	0.07	2.37	3.35
Ni	0.44	2.51	3.84
Cu	0.89	3.17	4.19
Ru	0.44	0.99	3.43
Rh	0.50	1.67	3.47
Pd	1.30	3.55	4.76
Ag	2.36	4.52	5.11
Os	-0.14	0.03	2.95
Ir	0.35	1.31	3.48
Pt	0.83	2.27	3.77
Au	1.59	3.52	4.76

TABLE S2. The adsorption energies (in eV) of \*OH, \*O and \*OOH ( $\Delta G_{*_{OH}}, \Delta G_{*_{O}}$  and  $\Delta G_{*_{OOH}}$ ).

	$\Delta G_1(eV)$	$\Delta G_2(eV)$	$\Delta G_3(eV)$	$\Delta G_4(eV)$	$\eta_{\rm OER}({\rm V})$	$\eta_{\rm ORR}({\rm V})$
$\operatorname{Cr}$	0.20	1.23	2.06	1.43	0.83	1.03
Mn	0.00	2.19	1.18	1.55	0.96	1.23
Fe	0.03	1.40	1.86	1.63	0.63	1.20
Co	0.07	2.30	0.98	1.57	1.07	1.16
Ni	0.44	2.06	1.34	1.08	0.74	0.79
Cu	0.89	2.29	1.01	0.73	1.06	0.50
Ru	0.44	0.55	2.44	1.49	1.21	0.79
$\operatorname{Rh}$	0.50	1.16	1.80	1.45	0.57	0.73
Pd	1.30	2.25	1.21	0.16	1.02	1.07
Ag	2.36	2.16	0.59	-0.19	1.13	1.42
Os	-0.14	0.17	2.92	1.97	1.69	1.37
Ir	0.35	0.96	2.17	1.44	0.94	0.88
Pt	0.83	1.44	1.50	1.15	0.27	0.39
Au	1.59	1.93	1.24	0.16	0.70	1.07

TABLE S3. The free energy changes of each elementary step ( $\Delta G_1$ ,  $\Delta G_2$ ,  $\Delta G_3$  and  $\Delta G_4$ ) and the overpotential of OER and ORR ( $\eta_{OER}$  and  $\eta_{ORR}$ ).



## **Supported TM**

FIG. S1.  $\mathrm{E}_{\mathrm{cluster}}$  energy calculated on TM-C\_{13}N\_3 system.



FIG. S2. Reaction pathways for O2 dissociation on C13N3 surfaces anchored by Pt atoms. IS, TS, FS represent the initial, transition, and final state along the reaction path.



FIG. S3. -COHP of Cr,Mn,Fe,Co,Ni,Cu,Ru,Rh,Pd,Ag,Ir and Au-C<sub>13</sub>N<sub>3</sub> with the reaction intermediate  $^{*}OH$ , where the Fermi level is set to zero.