## **Supporting Information**

# Controlling the symmetry of hexamonodentate 3d-transition metal complexes through symmetry propagation from highsymmetry Ti–Mo and Zr–Mo clusters via hydrogen-bonding interactions

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**Figure S7**. Dc field dependence of (a) the  $\chi_M$ ' vs. frequency plots and (b)  $\chi_M$ '' vs. frequency plots for **CoTi** at 1.9 K with ac frequency of 1–1488 Hz. The lines are guide for the eye.

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Table S11. Cole-Cole fit values for CoZr at 1.9–4.5 K with an applied dc field of 0.8 kOe.

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# 1. <sup>1</sup>H NMR spectrum



**Figure S1**. <sup>1</sup>H NMR spectra of **ZnZr** in dmso-d<sub>6</sub>. Two sets of resonance peaks for N–H atoms were observed at 7.07 and 5.23 ppm in 1:2 integration ratio.

2 6 1		
	FeTi	FeZr
Formula	$C_{36}H_{102}Cl_{6}FeMo_{6}N_{18}O_{48}Ti$	C <sub>36</sub> H <sub>102</sub> Cl <sub>6</sub> FeMo <sub>6</sub> N <sub>18</sub> O <sub>48</sub> Zr
Formula weight	2447.44	2490.76
Crystal system	Trigonal	Trigonal
Size / mm	0.14×0.12×0.09	0.10×0.06×0.04
Space group	R3	R3
a / Å	21.6648(4)	21.8319(4)
<i>c</i> / Å	14.6787(4)	14.7616(3)
V / Å <sup>3</sup>	5966.6(3)	6093.2(3)
Ζ	3	3
T/K	104(2)	102(2)
Density / g cm <sup>-3</sup>	2.043	2.036
$\mu / \mathrm{mm}^{-1}$	1.499	1.498
F(000)	3690	3744
$2\theta_{\rm max}/\circ$	55	55
No. of reflections	10783	10009
measured		
No. of independent	4493 ( $R_{int} = 0.0210$ )	5470 ( $R_{\rm int} = 0.0279$ )
reflections		
Data/restraints/parameters	4493/148/399	5470/152/399
$R_1 [I > 2.00\sigma(I)]$	0.0317	0.0308
$wR_2$ (all reflections)	0.0877	0.0790
Goodness of fit	0.822	1.075
Highest peak, deepest	1.602, -1.700	0.745, -1.606
hole / $e Å^{-3}$	,	· · · · ·
Flack	0.44(5)	0.019(18)
CCCDC Deposition #	2372554	2372558

**2. X-Ray crystallography Table S1**. Crystallographic information of **FeTi** and **FeZr**.

## Table S2. Crystallographic information of CoTi and CoZr.

	СоТі	CoZr
Formula	C <sub>36</sub> H <sub>102</sub> Cl <sub>6</sub> CoMo <sub>6</sub> N <sub>18</sub> O <sub>48</sub> Ti	$C_{36}H_{102}Cl_6CoMo_6N_{18}O_{48}Zr$
Formula weight	2450.52	2493.84
Crystal system	Trigonal	Trigonal
Size / mm	0.14×0.09×0.05	0.08×0.06×0.04
Space group	R3	R3
a / Å	21.5929(7)	21.7971(4)
<i>c</i> / Å	14.6575(5)	14.7552(3)
$V/ Å^3$	5918.5(4)	6071.2(3)
Ζ	3	3
T / K	104(2)	102(2)
Density / g cm <sup>-3</sup>	2.063	2.046
$\mu / \text{mm}^{-1}$	1.537	1.529
<i>F</i> (000)	3693	3747
$2\theta_{\rm max}/\circ$	55	57
No. of reflections	9959	17067
measured		
No. of independent reflections	4799 ( $R_{\rm int} = 0.0339$ )	$6463 \ (R_{\rm int} = 0.0296)$
Data/restraints/parameters	4799/164/399	6463/252/411
$R_1 [I > 2.00\sigma(I)]$	0.0410	0.0354
$wR_2$ (all reflections)	0.01091	0.0902
Goodness of fit	1.040	1.074
Highest peak, deepest	1.022, -1.449	0.628, -1.739
hole / e Å <sup>-3</sup>		
Flack	0.44(5)	0.004(15)
CCCDC Deposition #	2372555	2372559

	NiTi	NiZr
Formula	C <sub>36</sub> H <sub>102</sub> Cl <sub>6</sub> Mo <sub>6</sub> N <sub>18</sub> NiO <sub>48</sub> Ti	C <sub>36</sub> H <sub>102</sub> Cl <sub>6</sub> Mo <sub>6</sub> N <sub>18</sub> NiO <sub>48</sub> Zr
Formula weight	2450.30	2493.62
Crystal system	Trigonal	Trigonal
Size / mm	0.16×0.12×0.06	0.08×0.07×0.04
Space group	R3	R3
a / Å	21.6510(8)	21.7869(4)
<i>c</i> / Å	14.6425(4)	14.6803(3)
V / Å <sup>3</sup>	5944.3(5)	6034.7(3)
Ζ	3	3
T/K	100(2)	102(2)
Density / $g \text{ cm}^{-3}$	2.053	2.058
$\mu / \mathrm{mm}^{-1}$	1.559	1.566
F(000)	3696	3750
$2\theta_{\rm max}/\circ$	55	55
No. of reflections	10374	8842
measured		
No. of independent	$4240 \ (R_{\rm int} = 0.0346)$	5351 ( $R_{\rm int} = 0.0194$ )
reflections	. , ,	
Data/restraints/parameters	4240/148/399	6351/202/401
$R_1 [I > 2.00\sigma(I)]$	0.0428	0.0337
$wR_2$ (all reflections)	0.01174	0.0902
Goodness of fit	0.984	1.074
Highest peak, deepest	2.483, -1.447	0.759, -2.051
hole / e Å <sup>-3</sup>		-
Flack	0.06(4)	0.00(4)
CCCDC Deposition #	2372556	2372560

Table S3. Crystallographic information of NiTi and NiZr.

Table S4. Crystallographic information of ZnTi and ZnZr.

	ZnTi	ZnZr
Formula	$C_{36}H_{102}Cl_6Mo_6N_{18}O_{48}TiZn$	C <sub>36</sub> H <sub>102</sub> Cl <sub>6</sub> Mo <sub>6</sub> N <sub>18</sub> O <sub>48</sub> ZnZr
Formula weight	2456.96	2500.28
Crystal system	Trigonal	Trigonal
Size / mm	0.22×0.16×0.12	0.16×0.11×0.06
Space group	R3	R3
a / Å	21.6448(3)	21.7780(3)
<i>c</i> / Å	14.6822(3)	14.7532(2)
$V / Å^3$	5957.0(3)	6059.72(19)
Ζ	3	3
T / K	104(2)	102(2)
Density / $g \text{ cm}^{-3}$	2.055	2.055
$\mu/\mathrm{mm}^{-1}$	1.621	1.623
F(000)	3702	3756
$2\theta_{\rm max}/\circ$	55	55
No. of reflections	10464	10949
measured		
No. of independent	$4770 (R_{int} = 0.0123)$	$5055 (R_{int} = 0.0183)$
reflections		× ,
Data/restraints/parameters	4799/170/399	5055/169/400
$R_1 [I > 2.00\sigma(I)]$	0.0292	0.0238
$wR_2$ (all reflections)	0.00826	0.0640
Goodness of fit	1.040	1.083
Highest peak, deepest	0.826, -2.077	0.533, -1.556
hole / e Å <sup>-3</sup>	,	,
Flack	0.39(3)	0.15(2)
CCCDC Deposition #	2372557	2372561



**Figure S2**. Crystal structures of the cationic part of **MTi** along the *a*-axis. (a) **FeTi**, (b) **CoTi**, (c) **NiTi** and (d) **ZnTi**. The perchlorate anions were removed for clarity. White and light blue balls are Ti and Mo, respectively.



Figure S3. Crystal structures of MZr along the *a*-axis. (a) FeZr, (b) CoZr, (c) NiZr and (d) ZnZr. The perchlorate anions were removed for clarity. Yellow and light blue balls are Zr and Mo, respectively.

Table S5. Selected distances and angles in MTi.

	FeTi	СоТі	NiTi	ZnTi
Ti–O1 / Å	1.936(5)	1.937(6)	1.941(6)	1.937(4)
Ti–O4 / Å	1.936(4)	1.938(6)	1.935(6)	1.937(4)
O1-O1 <sup><i>i</i></sup> -O1 <sup><i>ii</i></sup> ··· O4-O4 <sup><i>i</i></sup> -O4 <sup><i>ii</i></sup> / Å	2.232(7)	2.224(8)	2.228(8)	2.233(6)
Mo1…Mo2 / Å	4.601(1)	4.600(1)	4.612(1)	4.608(1)
$Mo1 \cdots Mo1^i / Å$	4.620(1)	4.619(1)	4.630(1)	4.625(1)
$Mo2\cdots Mo2^i$ / Å	4.726(1)	4.717(1)	4.714(1)	4.723(3)
Mo1-Mo1 <sup><i>i</i></sup> -Mo1 <sup><i>ii</i></sup> ··· Mo2-Mo2 <sup><i>i</i></sup> -Mo2 <sup><i>ii</i></sup> / Å	4.554(1)	4.552(1)	4.562(1)	4.560(1)
Short Ti…M / Å	7.270(3)	7.243(4)	7.222(4)	7.257(3)
Long Ti…M / Å	7.408(3)	7.415(4)	7.421(4)	7.425(3)

Symmetry code: (i = '-x+y, 1-x, z', ii = '1-y, x-y+1, z').

Tal	ble	<b>S6</b> .	Selected	bonding	parameters	in <b>MZr</b> .
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	FeZr	CoZr	NiZr	ZnZr	
Zr–O1 / Å	2.072(4)	2.066(5)	2.066(5)	2.070(4)	
Zr–O4 / Å	2.075(4)	2.078(5)	2.077(5)	2.068(4)	
O1-O1 <sup><i>i</i></sup> -O1 <sup><i>ii</i></sup> ··· O4-O4 <sup><i>i</i></sup> -O4 <sup><i>ii</i></sup> / Å	2.395(7)	2.401(6)	2.394(7)	2.594(5)	
Mo1…Mo2 / Å	4.700(1)	4.702(1)	4.703(1)	4.702(1)	
$Mo1 \cdots Mo1^i / Å$	4.795(1)	4.798(1)	4.795(1)	4.793(1)	
$Mo2\cdots Mo2^i$ / Å	4.908(1)	4.904(1)	4.892(1)	4.890(3)	
Mo1-Mo1 <sup><i>i</i></sup> -Mo1 <sup><i>ii</i></sup> Mo2-Mo2 <sup><i>i</i></sup> -Mo2 <sup><i>ii</i></sup> / Å	4.657(1)	4.658(1)	4.658(1)	4.656(1)	
Short Zr⋯M / Å	7.307(3)	7.283(3)	7.226(3)	7.278(2)	
Long Zr…M / Å	7.455(3)	7.472(3)	7.454(3)	7.475(2)	
Summature and as $(i = i + 1) + 1 + 2$ , $i = i + 1 + 2$	$\frac{1}{2}$				

Symmetry code: (i = '-x+y, 1-x, z', ii = '1-y, x-y+1, z').

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	FeTi	FeZr	СоТі	CoZr	NiTi	NiZr	ZnTi	ZnZr
M-07	2.103(6)	2.114(6)	2.086(7)	2.082(6)	2.046(8)	2.037(7)	2.082(6)	2.084(4)
M08	2.089(6)	2.090(6)	2.062(8)	2.060(6)	2.017(8)	2.030(7)	2.044(6)	2.058(4)
$O7 \cdots O7^i$	2.974(10)	2.989(11)	2.913(14)	2.922(11)	2.875(14)	2.881(12)	2.915(11)	2.922(8)
O8⋯O8 <sup><i>i</i></sup>	3.037(12)	3.029(11)	2.967(16)	2.955(12)	2.918(15)	2.927(13)	2.952(12)	2.964(9)
S	3.01	3.01	2.94	2.94	2.90	2.90	2.93	2.94
(average)								
h	2.351(10)	2.365(9)	2.383(11)	2.376(9)	2.305(10)	2.301(10)	2.353(9)	2.367(7)
s/h	1.28	1.27	1.23	1.24	1.26	1.26	1.25	1.24
$\varphi$	48.8(3)	48.8(4)	49.5(5)	49.7(4)	52.9(4)	52.8(5)	49.8(4)	49.7(3)

**Table S7.** Selected bonding parameters around  $[M(H_2O)_6]^{2+}$  cations (M = Fe, Co, Ni, and Zn; Å, °).

Symmetry code: (i = -x+y, 1-x, +z').

### **3. EPR Measurements**



**Figure S4**. X-band powder EPR spectrum of **CoZr** at 4 K. The fitted parameter:  $g_x$ ,  $g_y = 1.940$ ,  $g_z = 8.450$ , Ax, Ay = 637 MHz, Az = 850 MHz.

### 4. Magnetic Measurements



Figure S5. Magnetization curves for (a) FeTi, (b) CoTi and, (c) NiTi at 2, 4, 6, and 8 K. The black solid lines represent fits of the Hamiltonians.



Figure S6. Magnetization curves for (a) FeZr, (b) CoZr and, (c) NiZr at 2, 4, 6, and 8 K. The black solid lines represent fits of the Hamiltonians.



**Figure S7**. Dc field dependence of (a) the  $\chi_M$ ' vs. frequency plots and (b)  $\chi_M$ '' vs. frequency plots for **CoTi** at 1.9 K with ac frequency of 1–1488 Hz. The lines are guide for the eye.



**Figure S8**. (a) Cole–Cole plot for **CoTi** at 1.9 K under variable field. The solid lines represent the fit to a generalized Debye model. (b) The field dependence of the relaxation time derived from the fit.

H/kOe	$\chi_S/cm_3 mol^{-1}$	$\chi_T/cm_3 mol^{-1}$	au / s	α
0.2	$6.274 \times 10^{-1}$	9.968 ×10 <sup>-1</sup>	4.722 ×10 <sup>-4</sup>	2.459 ×10 <sup>-2</sup>
0.4	$3.088 \times 10^{-1}$	9.965 ×10 <sup>-1</sup>	$5.655 \times 10^{-4}$	4.559 ×10 <sup>-2</sup>
0.6	$1.528 \times 10^{-1}$	$9.934 \times 10^{-1}$	$6.094 \times 10^{-4}$	6.043 ×10 <sup>-2</sup>
1.0	$5.484 \times 10^{-2}$	$9.794 \times 10^{-1}$	$6.280 \times 10^{-4}$	7.068 ×10 <sup>-2</sup>
1.5	$1.949 \times 10^{-2}$	9.526 ×10 <sup>-1</sup>	5.725 ×10 <sup>-4</sup>	9.316 ×10 <sup>-2</sup>
2.0	$1.034 \times 10^{-14}$	$9.174 \times 10^{-1}$	5.093 ×10 <sup>-4</sup>	1.233 ×10 <sup>-1</sup>
2.5	$1.374 \times 10^{-14}$	$8.755 \times 10^{-1}$	$4.649 \times 10^{-4}$	1.477 ×10 <sup>-1</sup>
3.0	2.118 ×10 <sup>-15</sup>	$8.038 \times 10^{-1}$	$4.004 \times 10^{-4}$	$1.485 \times 10^{-1}$
3.5	2.667 ×10 <sup>-15</sup>	$7.478 \times 10^{-1}$	$3.574 \times 10^{-4}$	$1.685 \times 10^{-1}$
4.0	3.824 ×10 <sup>-15</sup>	$6.937 \times 10^{-1}$	3.167 ×10 <sup>-4</sup>	$1.982 \times 10^{-1}$

Table S8. Cole-Cole fit values for CoTi at 1.9 K with an applied dc field of 0.2-4 kOe.



**Figure S9**. Temperature dependence of (a) the in-phase  $\chi_M$ ' vs. frequency plots and (b) out-of-phase  $\chi_M$ '' vs. frequency plots for **CoTi** in the presence of 1 kOe with ac frequency of 1–1488 Hz. The lines are guide for the eye.



**Figure S10**. Cole–Cole plot for **CoTi** in the presence of 1 kOe dc field at variable temperature. The solid lines represent the fit to a generalized Debye model.

T/K	$\chi_S/cm_3 mol^{-1}$	$\chi_T/cm_3 mol^{-1}$	$\tau / s$	α
1.9	$4.828 \times 10^{-2}$	$9.438 \times 10^{-1}$	6.900 ×10 <sup>-4</sup>	6.342 ×10 <sup>-2</sup>
2.0	$4.459 \times 10^{-2}$	8.971 ×10 <sup>-1</sup>	5.873 ×10 <sup>-4</sup>	6.193 ×10 <sup>-2</sup>
2.1	$4.056 \times 10^{-2}$	$8.550 \times 10^{-1}$	$5.009 \times 10^{-4}$	6.048 ×10 <sup>-2</sup>
2.2	$3.983 \times 10^{-2}$	$8.250 \times 10^{-1}$	4.496 ×10 <sup>-4</sup>	5.715 ×10 <sup>-2</sup>
2.3	$3.717 \times 10^{-2}$	$7.881 \times 10^{-1}$	$3.879 \times 10^{-4}$	5.520 ×10 <sup>-2</sup>
2.4	$4.246 \times 10^{-2}$	$7.559 \times 10^{-1}$	$3.432 \times 10^{-4}$	4.959 ×10 <sup>-2</sup>
2.6	2.766 ×10 <sup>-2</sup>	6.997 ×10 <sup>-1</sup>	2.653 ×10 <sup>-4</sup>	5.100 ×10 <sup>-2</sup>
2.8	$3.454 \times 10^{-2}$	$6.509 \times 10^{-1}$	2.183 ×10 <sup>-4</sup>	4.012 ×10 <sup>-2</sup>
3.0	$3.431 \times 10^{-2}$	$6.089 \times 10^{-1}$	$1.804 \times 10^{-4}$	$4.049 \times 10^{-2}$
3.2	$4.249 \times 10^{-2}$	5.721 ×10 <sup>-1</sup>	$1.546 \times 10^{-4}$	3.328 ×10 <sup>-2</sup>
3.4	$2.518 \times 10^{-2}$	$5.395 \times 10^{-1}$	$1.256 \times 10^{-4}$	4.201 ×10 <sup>-2</sup>
3.6	$3.337 \times 10^{-2}$	$5.103 \times 10^{-1}$	$1.124 \times 10^{-4}$	2.255 ×10 <sup>-2</sup>
4.0	$2.478 \times 10^{-2}$	$4.618 \times 10^{-1}$	8.194 ×10 <sup>-5</sup>	4.197 ×10 <sup>-2</sup>
4.5	$5.065 \times 10^{-3}$	$4.112 \times 10^{-1}$	5.605 ×10 <sup>-5</sup>	$3.674 \times 10^{-2}$

Table S9. Cole-Cole fit values for CoTi at 1.9–4.5 K with an applied dc field of 1 kOe.



**Figure S11**. Dc field dependence of (a) the in-phase  $\chi_M$ ' vs. frequency plots and (b) out-of-phase  $\chi_M$ '' vs. frequency plots for **CoZr** at 1.9 K with ac frequency of 1–1488 Hz. The lines are guide for the eye.



**Figure S12**. (a) Cole–Cole plot for **CoZr** at 1.9 K under variable field. The solid lines represent the fit to a generalized Debye model. (b) The field dependence of the relaxation time derived from the fit.

H/kOe	$\chi_S/cm_3 mol^{-1}$	$\chi_T/cm_3 mol^{-1}$	$\tau / s$	α
0.2	5.756 ×10 <sup>-1</sup>	9.205 ×10 <sup>-1</sup>	3.634 ×10 <sup>-4</sup>	7.601 ×10 <sup>-2</sup>
0.4	2.568 ×10 <sup>-1</sup>	9.206 ×10 <sup>-1</sup>	4.461 ×10 <sup>-4</sup>	1.020 ×10 <sup>-1</sup>
0.6	$1.126 \times 10^{-1}$	9.155 ×10 <sup>-1</sup>	5.130 ×10 <sup>-4</sup>	$1.070 \times 10^{-1}$
0.8	5.894 ×10 <sup>-2</sup>	$9.074 \times 10^{-1}$	$5.448 \times 10^{-4}$	$1.110 \times 10^{-1}$
1.0	$3.265 \times 10^{-2}$	$8.968 \times 10^{-1}$	$5.410 \times 10^{-4}$	$1.209 \times 10^{-1}$
1.2	$1.735 \times 10^{-2}$	$8.829 \times 10^{-1}$	5.171 ×10 <sup>-4</sup>	$1.307 \times 10^{-1}$
1.4	6.783 ×10 <sup>-3</sup>	$8.675 \times 10^{-1}$	$4.856 \times 10^{-4}$	$1.402 \times 10^{-1}$
1.6	$7.289 \times 10^{-8}$	$8.505 \times 10^{-1}$	4.556 ×10 <sup>-4</sup>	$1.480 \times 10^{-1}$
1.8	$1.066 \times 10^{-7}$	$8.320 \times 10^{-1}$	4.283 ×10 <sup>-4</sup>	1.553 ×10 <sup>-1</sup>
2.0	$1.465 \times 10^{-7}$	$8.117 \times 10^{-1}$	$4.025 \times 10^{-4}$	1.621 ×10 <sup>-1</sup>
2.5	$2.226 \times 10^{-7}$	$7.598 \times 10^{-1}$	$3.450 \times 10^{-4}$	$1.880 \times 10^{-1}$
3.0	$3.137 \times 10^{-7}$	$7.050 \times 10^{-1}$	$2.975 \times 10^{-4}$	2.164 ×10 <sup>-1</sup>
3.5	$3.506 \times 10^{-7}$	$6.516 \times 10^{-1}$	$2.539 \times 10^{-4}$	$2.542 \times 10^{-1}$
4.0	$4.876 \times 10^{-7}$	$5.992 \times 10^{-1}$	$2.203 \times 10^{-4}$	$2.933 \times 10^{-1}$
4.5	4.839 ×10 <sup>-7</sup>	5.523 ×10 <sup>-1</sup>	1.942 ×10 <sup>-4</sup>	$3.422 \times 10^{-1}$
5.0	5.542 ×10 <sup>-7</sup>	$5.083 \times 10^{-1}$	1.736 ×10 <sup>-4</sup>	$3.881 \times 10^{-1}$

Table S10. Cole-Cole fit values for CoZr at 1.9 K with an applied dc field of 0.2–5 kOe.



**Figure S13**. Temperature dependence of (a) the in-phase  $\chi_M$ ' vs. frequency plots and (b) out-of-phase  $\chi_M$ '' vs. frequency plots for **CoZr** in the presence of 0.8 kOe with ac frequency of 1–1488 Hz. The lines are guide for the eye.



**Figure S14**. Cole–Cole plot for **CoZr** in the presence of 1 kOe dc field at variable temperature. The solid lines represent the fit to a generalized Debye model.

T/K	$\chi_S/cm_3 mol^{-1}$	$\chi_T/cm_3 mol^{-1}$	$\tau / s$	α
1.9	5.894 ×10 <sup>-2</sup>	9.074 ×10 <sup>-1</sup>	5.448 ×10 <sup>-4</sup>	$1.110 \times 10^{-1}$
2.0	5.322 ×10 <sup>-2</sup>	$8.627 \times 10^{-1}$	$4.742 \times 10^{-4}$	1.101 ×10 <sup>-1</sup>
2.1	5.087 ×10 <sup>-2</sup>	$8.215 \times 10^{-1}$	4.162 ×10 <sup>-4</sup>	$1.083 \times 10^{-1}$
2.2	4.690 ×10 <sup>-2</sup>	$7.931 \times 10^{-1}$	3.778 ×10 <sup>-4</sup>	$1.079 \times 10^{-1}$
2.3	$4.744 \times 10^{-2}$	$7.555 \times 10^{-1}$	3.355 ×10 <sup>-4</sup>	$1.032 \times 10^{-1}$
2.4	4.718 ×10 <sup>-2</sup>	$7.246 \times 10^{-1}$	3.006 ×10 <sup>-4</sup>	$1.024 \times 10^{-1}$
2.5	$4.027 \times 10^{-2}$	6.964 ×10 <sup>-1</sup>	2.670 ×10 <sup>-4</sup>	$1.062 \times 10^{-1}$
2.6	4.256 ×10 <sup>-2</sup>	$6.698 \times 10^{-1}$	2.439 ×10 <sup>-4</sup>	$1.017 \times 10^{-1}$
2.7	4.031 ×10 <sup>-2</sup>	$6.440 \times 10^{-1}$	2.211 ×10 <sup>-4</sup>	9.659 ×10 <sup>-2</sup>
2.8	4.436 ×10 <sup>-2</sup>	$6.229 \times 10^{-1}$	2.064 ×10 <sup>-4</sup>	9.403 ×10 <sup>-2</sup>
2.9	$4.078 \times 10^{-2}$	$6.024 \times 10^{-1}$	$1.874 \times 10^{-4}$	9.853 ×10 <sup>-2</sup>
3.0	4.229 ×10 <sup>-2</sup>	$5.830 \times 10^{-1}$	1.730 ×10 <sup>-4</sup>	9.504 ×10 <sup>-2</sup>
3.2	4.652 ×10 <sup>-2</sup>	$5.469 \times 10^{-1}$	$1.505 \times 10^{-4}$	$8.741 \times 10^{-2}$
3.4	$3.741 \times 10^{-2}$	$5.155 \times 10^{-1}$	$1.270 \times 10^{-4}$	$8.761 \times 10^{-2}$
3.6	$3.808 \times 10^{-2}$	$4.877 \times 10^{-1}$	$1.106 \times 10^{-4}$	$8.300 \times 10^{-2}$
3.8	$4.584 \times 10^{-2}$	$4.626 \times 10^{-1}$	9.926 ×10 <sup>-5</sup>	$7.598 \times 10^{-2}$
4.0	4.561 ×10 <sup>-2</sup>	$4.408 \times 10^{-1}$	8.670 ×10 <sup>-5</sup>	6.919 ×10 <sup>-2</sup>

Table S11. Cole-Cole fit values for CoZr at 1.9–4.5 K with an applied dc field of 0.8 kOe.

## 4. DFT Calculation



**Figure S15**. The energy levels of *d*-orbital-related molecular orbitals for  $[Ni(H_2O)_6]^{2+}$  complex cation in **NiTi** on the basis of the DFT computation (LC-BOP/6-31G).

## 4. AOM Calculation



**Figure S16**. The energy level diagrams for six-coordinate d<sup>6</sup> ion. (a) Bailar twisting distortion from. (b) Trigonal elongation/compression. Racah and AOM parameters:  $B = 1050 \text{ cm}^{-1}$ ,  $C = 4500 \text{ cm}^{-1}$ ,  $e_{\sigma} = 4000 \text{ cm}^{-1}$ .