

Supporting Information

Fluorite-Structured $\text{HfO}_2/\text{ZrO}_2/\text{HfO}_2$ Superlattice Based Self-Rectifying Ferroelectric Tunnel Junction Synapse

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Fig. S2 (a) Pulse scheme to measure polarization and resistance modulation hysteresis. (b) Polarization – voltage curve measured after each pulse of (a). (c) Resistance - voltage curve measured after each pulse of (a). The corresponding resistance modulation depending on the polarization states shows that the device is controlled by ferroelectric polarization.

Fig. S3 Multilevel J-V curve of the device with HZH with voltage amplitude from 3.2 to 3.7 V.

Fig. S4 (a-c) The measured J-V curves at 5 different points for each device with HfO₂, HZO, and HZH, respectively, show device-to-device variation (DTDV). The cycle-to-cycle variation (CTCV) was assessed with 5 cycles of DC voltage for devices with (d) HfO₂ and (e) HZO. For a precise assessment of the best-performing device, 50 cycles were conducted for the device with HZH, as shown in (f). (g) The quantitative evaluation of DTDV and CTCV by calculating the ratio of the standard deviation (σ) to the mean (μ) of the currents at -2 V.

Fig. S5 (a-c) The measured J-V curves at 5 different points for each device without HZH, TiO₂, and Al₂O₃ layers, respectively. The cycle-to-cycle variation (CTCV) was assessed with 5 cycles of DC voltage for devices without (d) HZH and (e) TiO₂. In the case of the device of TiN/TiO₂(17nm)/HZH/Pt, before the end of the 5 cycles, the resistance switching mechanism was changed from ferroelectric-based to defect-based. (g) The quantitative evaluation of DTDV and CTCV by calculating σ/μ of the currents at -2 V.

Fig. S6 (a) Endurance test conducted under ± 4 V, 10 kHz square pulse stress. (b) retention test conducted at 80 °C. The retention loss in the case of the FTJs is caused by the depolarization field, which is proportional to the P_r . The retention loss in FTJs is caused by the depolarization field, which is proportional to P_r . As P_r depolarizes, the depolarization field decreases, causing significant initial loss but eventual stabilization. Domain wall speed is exponentially proportional to the field, following Merz's law. Exponential decay fitting was used for extrapolation, demonstrating that the on/off ratio can be ~ 8 after 10 years.

Fig. S7 Oxygen quantification using STEM-EELS. (a, b) The EELS spectrum image, the quantified map showing the volumetric density of oxygen, and the line-scan profile of quantified oxygen intensities, were obtained from the sample (a) with and (b) without the Al₂O₃ layer. STEM-EELS quantification was conducted using Gatan Microscopy Suite software (GMS 3), based on the method inspired by the work of Verbeeck and Van Aert.¹ Oxygen K-edge signals from 532 eV to 674 eV were used and the plural scattering effect was corrected for the quantification.

Fig. S8 (a, b) Set and Reset switching speed measurement pulse scheme and results. (c, d) Power consumption of the set and reset process measured in (a, b).

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Fig. S9 (a) the $\ln(J/T^2)$ vs. $1000/T$ plot measured in the temperature range of 294-333K, where the slope means effective workfunction (Φ_{eff}) shown in the inset. (b) the plot of the Φ_{eff} vs. $E^{1/2}$, where the intercept means barrier height of the TiN/TiO₂ interface.

Fig. S10 (a) The resistance modulation depending on the applied number of optimized pulses in Fig. 6(b). The measurement was conducted 5 times in a single cell. (b) The resistance modulation in 5 different devices with the optimized pulses.

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Fig. S12 (a) Upper panel shows measured resistance at each state and voltage. Except for the $R@V_{\text{HRS}}$, the resistances are measured in LRS. The bottom panel shows the assumed value of pull-up resistance (R_{pull}) and linear device resistance. The $R@linearV_r/2$ and $R@linearV_r/3$ are calculated resistance by dividing $R@V_{\text{LRS}}$ with 2 and 3, respectively. The values are compatible with an array consisting of 100 μm^2 -sized cells. (b, c) The comparison of the N x N array scalability of the device in this study and assumed linear device with parameters in (a) in which (b) shows the case with the $V_r/2$ scheme and (c) for the $V_r/3$ scheme.

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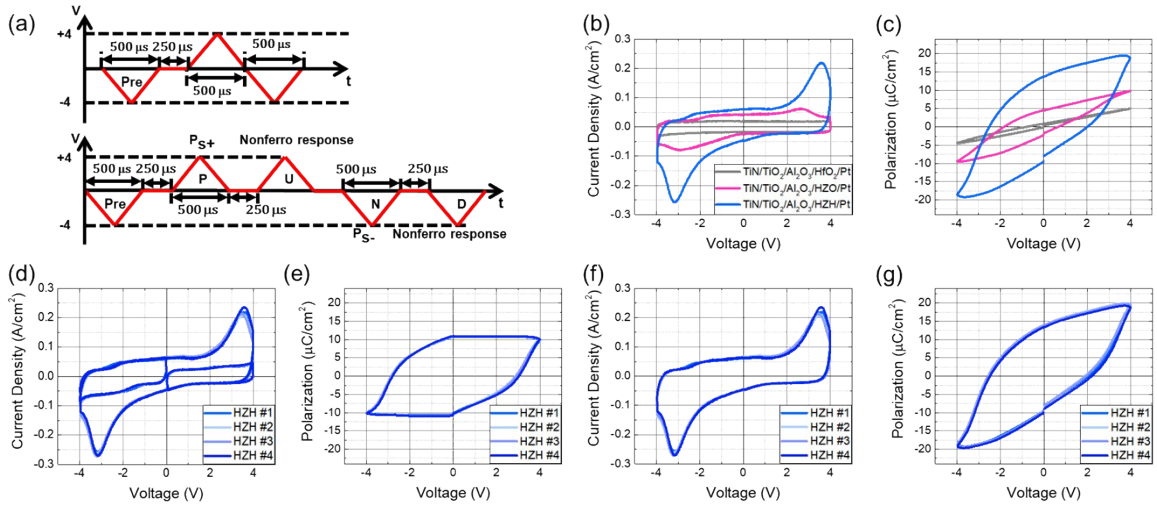


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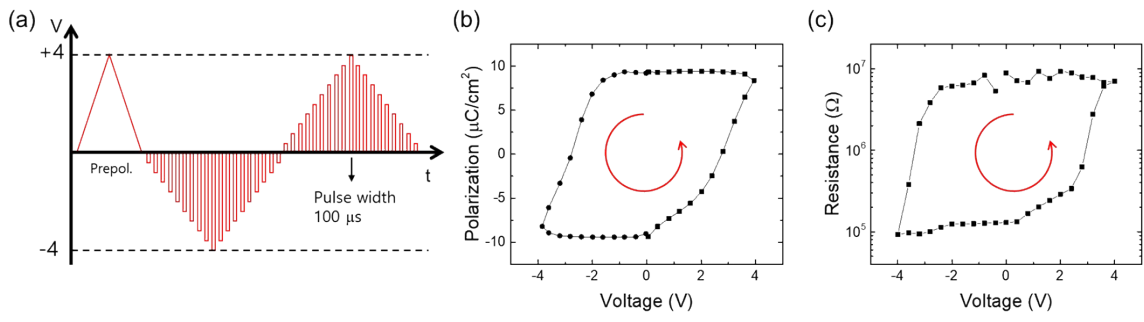


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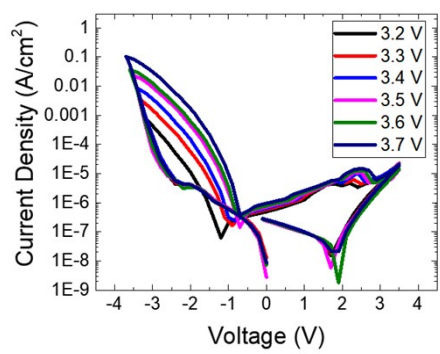
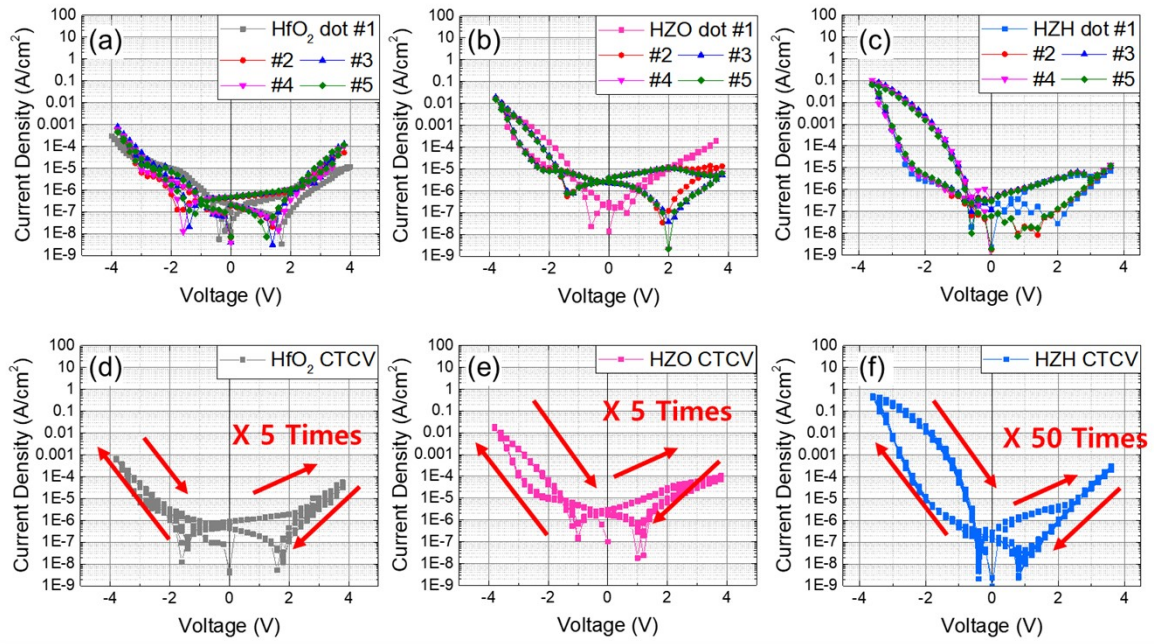


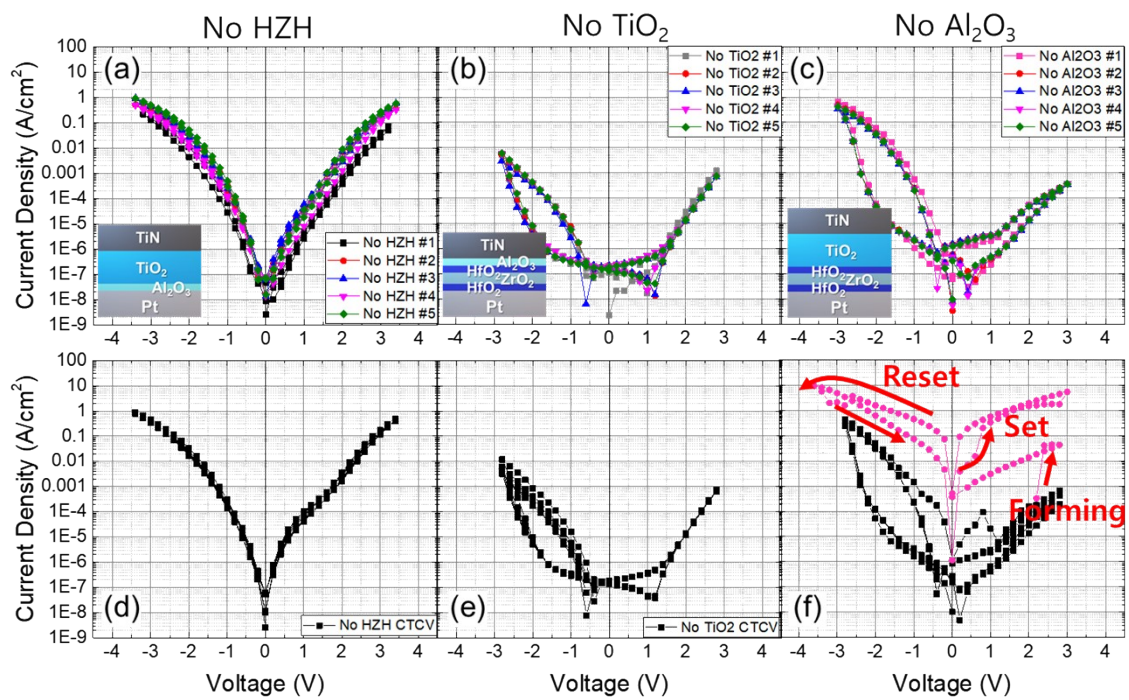
Fig. S3 Multilevel J-V curve of the device with HZH with voltage amplitude from 3.2 to 3.7 V.



(g) $\sigma/\mu*100$ (%)	HfO ₂	HZO	HZH
DTDV	55.2	50.3	16.0*
CTCV	28.9	15.1	11.6

* This value is calculated using data from a 9X9 crossbar array

Fig. S4 (a-c) The measured J-V curves at 5 different points for each device with HfO₂, HZO, and HZH, respectively, show device-to-device variation (DTDV). The cycle-to-cycle variation (CTCV) was assessed with 5 cycles of DC voltage for devices with (d) HfO₂ and (e) HZO. For a precise assessment of the best-performing device, 50 cycles were conducted for the device with HZH, as shown in (f). (g) The quantitative evaluation of DTDV and CTCV by calculating the ratio of the standard deviation (σ) to the mean (μ) of the currents at -2 V.



(g) $\sigma/\mu \cdot 100$ (%)	No HZH	No TiO ₂	No Al ₂ O ₃
DTDV	42.1	25.7	21.3
CTCV	10.3	30.5	-

Fig. S5 (a-c) The measured J-V curves at 5 different points for each device without HZH, TiO₂, and Al₂O₃ layers, respectively. The cycle-to-cycle variation (CTCV) was assessed with 5 cycles of DC voltage for devices without (d) HZH and (e) TiO₂. In the case of the device of TiN/TiO₂(17nm)/HZH/Pt, before the end of the 5 cycles, the resistance switching mechanism was changed from ferroelectric-based to defect-based. (g) The quantitative evaluation of DTDV and CTCV by calculating σ/μ of the currents at -2 V.

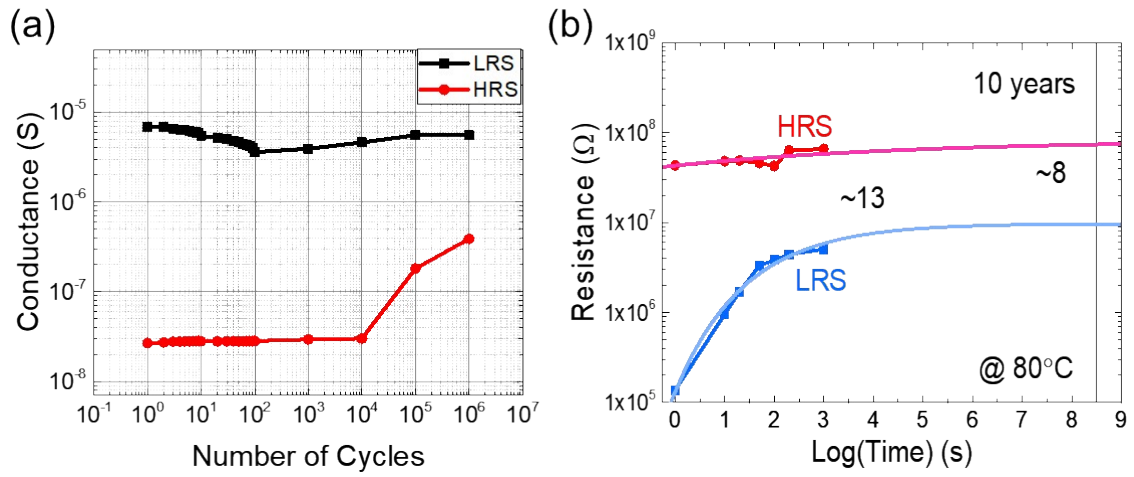


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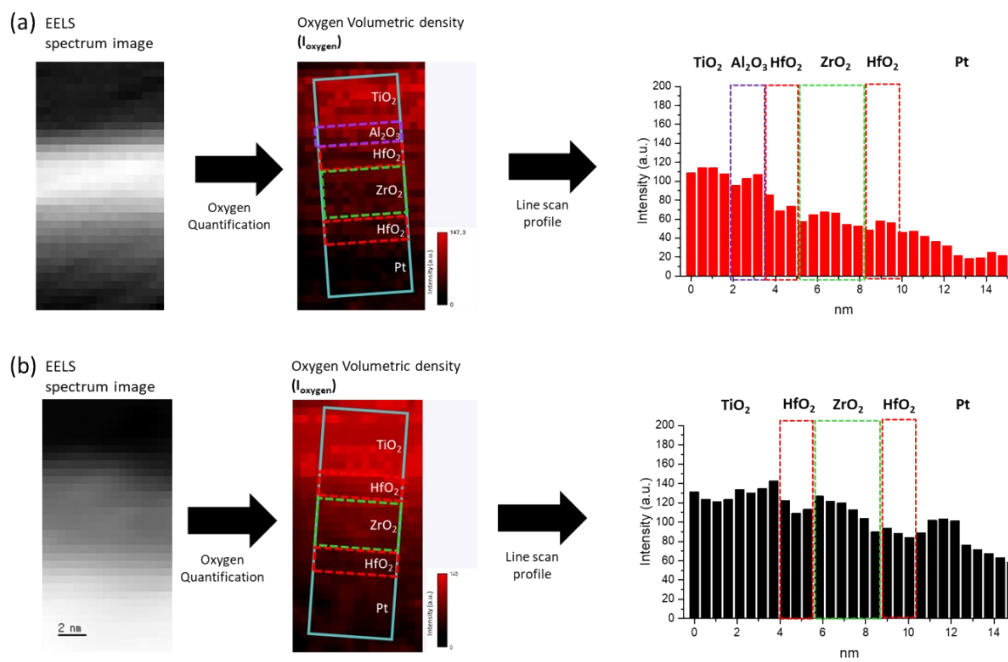


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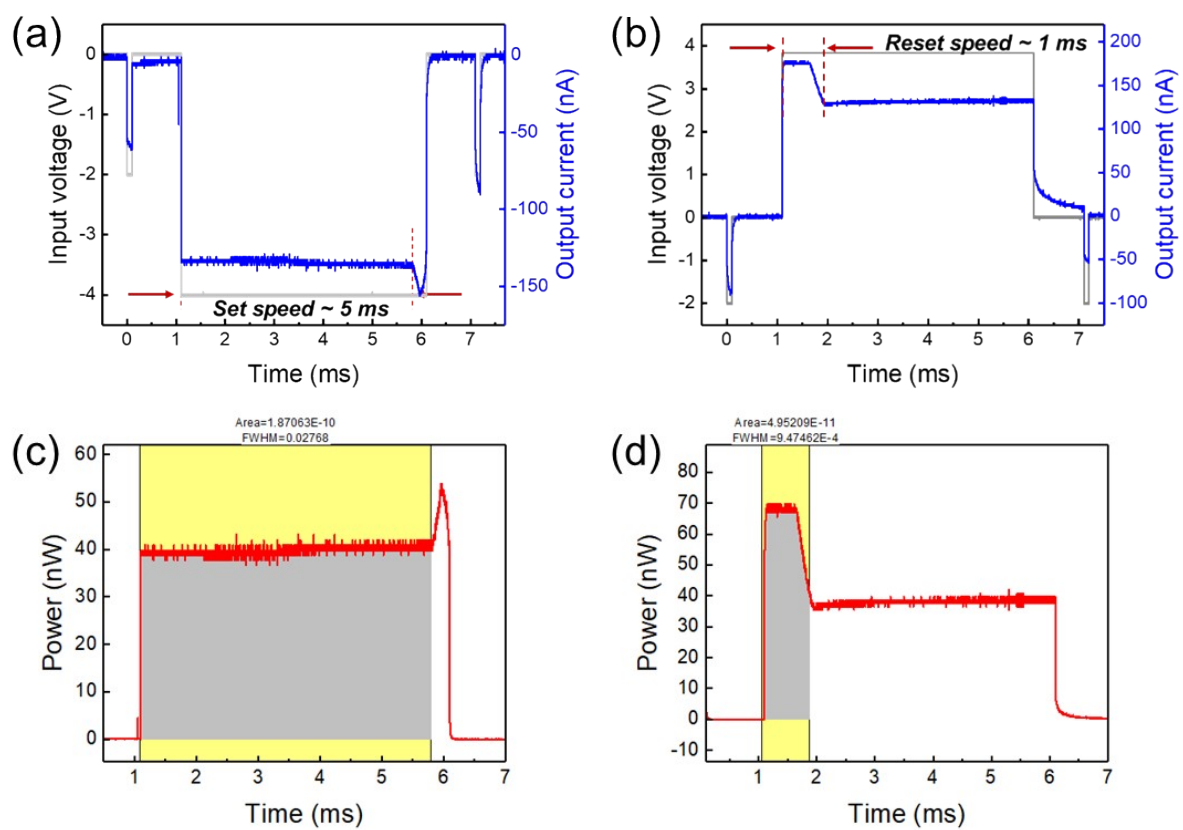


Fig. S8 (a, b) Set and Reset switching speed measurement pulse scheme and results. (c, d) Power consumption of the set and reset process measured in (a, b).

Device structure	Operation voltage	On-current	Switching speed	Rectifying ratio	Non-linearity	Ref
Ti/TiO ₂ /HfO ₂ /Si	-6 ~ 10 V	~100 μ A	-	~ 100	~ 100	2
Pt/TaO _y / TaO _x NP/Ta	-8 ~ 8 V	~1 μ A	-	~100	~100	3
Pt/Ta ₂ O ₅ /Nb ₂ O _{5-x} /Al ₂ O _{3-y} /Ti	-10 ~ 10 V	~1 μ A	10 ms	~ 1000	~100	4
ITO/NiO _x /WO _x /Pt	-6 ~ 8.5 V	~1 mA	10 ms	~ 86.9	~10	5
Au/Ti/TiO _{2-x} /Au/SiO ₂ /Si	-5 ~ 5 V	~10 mA	10 ms	~ 400	~ 100	6
TiN/TiO ₂ /Al ₂ O ₃ /HZH(6nm)/Pt	-3.8 ~ 4 V	~1 μ A	5 ms	1549	94	This work

Table S1 Comparison of switching characteristics with reported self-rectifying devices.

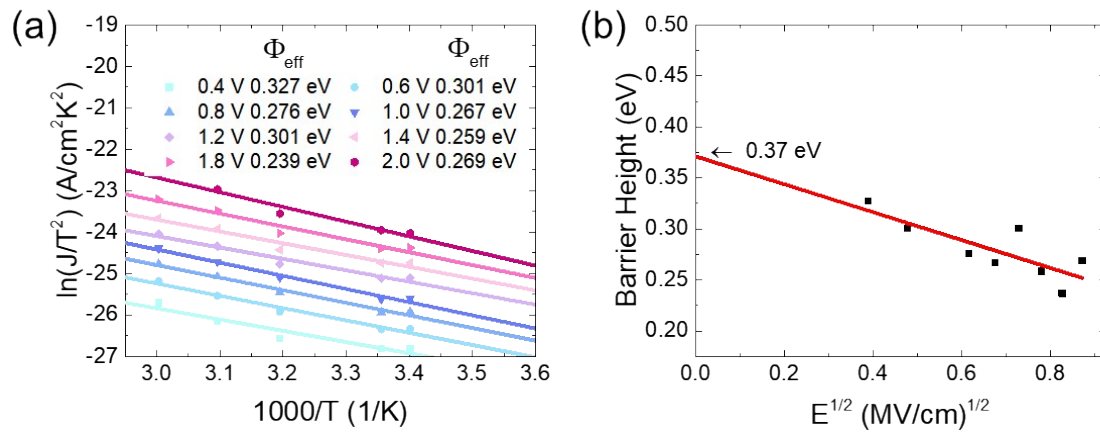


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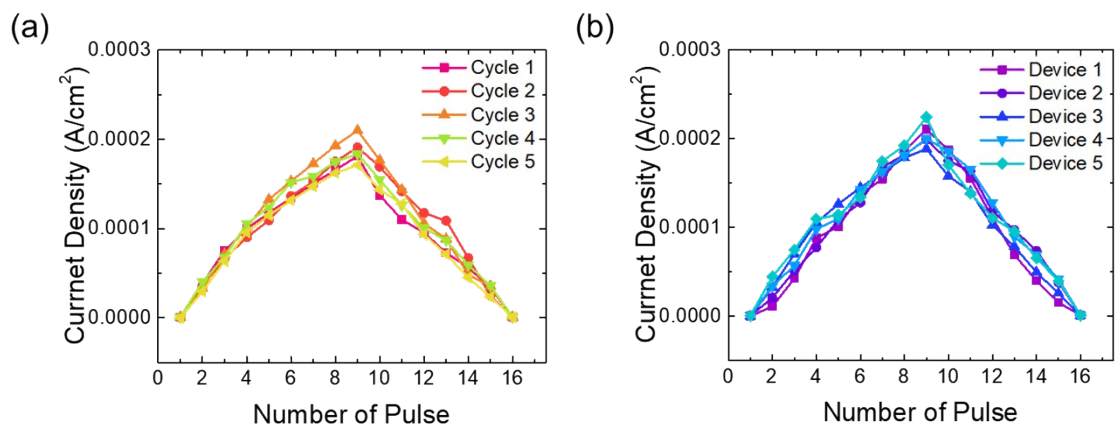


Fig. S10 (a) The resistance modulation depending on the applied number of optimized pulses in Fig. 6(b). The measurement was conducted 5 times in a single cell. (b) The resistance modulation in 5 different devices with the optimized pulses.

1 string

$$(M-1)R_{s1} + R_{s2} + (N-1)R_{s3}$$

Total # of R string

$$(M-1)(N-1)$$

Total parallel R

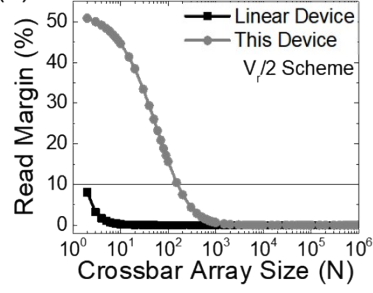
$$\frac{R_{s1}}{N-1} + \frac{R_{s2}}{(N-1)(M-1)} + \frac{R_{s3}}{M-1}$$

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(a)

This Device	Ohm ($G\Omega$)
$R@V_r_HRS$	710.085
$R@V_r_LRS$	0.558
$R@V_r/2$	52.213
$R@V_r/3$	914.627
$R@-V_r/3$	701.145
Assumption	Ohm ($G\Omega$)
R_{pull}	0.6
$R@linearV_r/2$	0.279
$R@linearV_r/3$	0.186

(b)



(c)

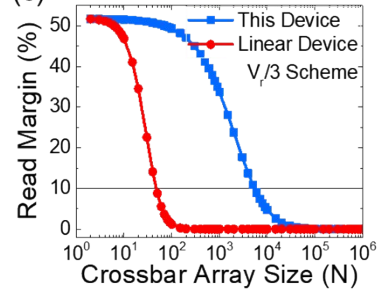


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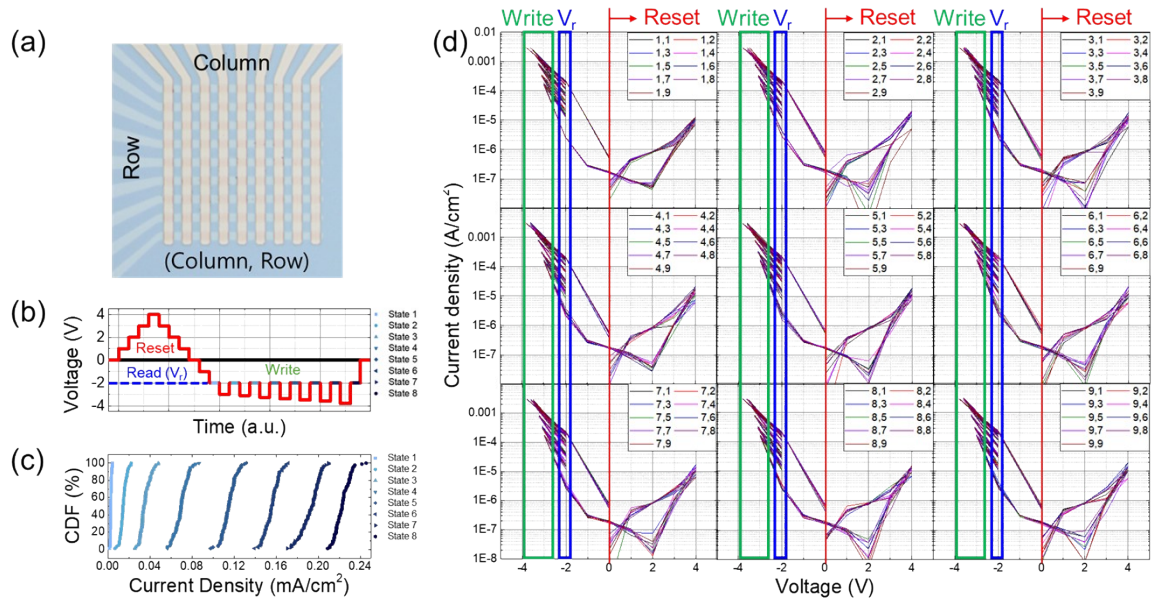


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