

Table.S1. Nonlinear equations of kinetic, classic isotherm, and advanced isotherm models

Kinetic models		
Model	Equation	Parameters
Pseudo-first-order	$Q_t = Q_e (1 - e^{-k_1 t})$	Q_t (mg/g) is the adsorbed ions at time (t), and K_1 is the rate constant of the first-order adsorption (1/min)
Pseudo-second-order	$Q_t = \frac{Q_e^2 k_2 t}{1 + Q_e k_2 t}$	Q_e is the quantity of adsorbed ions after equilibration (mg/g), and K_2 is the model rate constant (g/mg min).
Classic Isotherm models		
Model	Equation	Parameters
Langmuir	$Q_e = \frac{Q_{max} b C_e}{(1 + b C_e)}$	C_e is the rest ions concentrations (mg/L), Q_{max} is the theoretical maximum adsorption capacity (mg/g), and b is the Langmuir constant (L/mg)
Freundlich	$Q_e = K_f C_e^{1/n}$	K_f (mg/g) is the constant of Freundlich model related to the adsorption capacity and n is the constant of Freundlich model related to the adsorption intensities
Dubinin–Radushkevich	$Q_e = Q_m e^{-\beta \epsilon^2}$	β (mol ² /KJ ²) is the D-R constant, ϵ (KJ ² /mol ²) is the polanyi potential, and Q_m is the adsorption capacity (mg/g)
Advanced isotherm models		
Model	Equation	Parameters
Monolayer model with one energy site (Model 1)	$Q = n N_o = \frac{n N_M}{1 + (\frac{C1/2}{C})^n} = \frac{Q_o}{1 + (\frac{C1/2}{C})^n}$	Q is the adsorbed quantities in mg/g n is the number of adsorbed ion per site N_m is the density of the effective receptor sites (mg/g)
Monolayer model with two energy sites (Model 2)	$Q = \frac{n_1 N_{1M}}{1 + (\frac{C_1}{C})^{n_1}} + \frac{n_2 N_{2M}}{1 + (\frac{C_2}{C})^{n_2}}$	Q_o is the adsorption capacity at the saturation state in mg/g $C1/2$ is the concentration of the ions at half saturation stage in mg/L
Double layer model with one energy site (Model 3)	$Q = Q_o \frac{(\frac{C}{C1/2})^n + 2(\frac{C}{C1/2})^{2n}}{1 + (\frac{C}{C1/2})^n + (\frac{C}{C1/2})^{2n}}$	$C1$ and $C2$ are the concentrations of the ions at the half saturation stage for the first active sites and the second active sites, respectively $n1$ and $n2$ are the adsorbed ions per site for the first active sites and the second active sites, respectively
Double layer model with two energy sites (Model 3)	$Q = Q_o \frac{(\frac{C}{C1})^n + 2(\frac{C}{C2})^{2n}}{1 + (\frac{C}{C1})^n + (\frac{C}{C2})^{2n}}$	

Table.S2. Comparison study between the developed Mth/EXG as adsorbent and other adsorbents in literature

Adsorbent	q_{\max} (mg/g)	References
SFR		
Ppy NF/Zn-Fe LDH	63.4	Mohamed et al., (2018)
Glass-MCM-48	62.5	Abukhadra et al., (2019)
MCM-41	68.8	Kaur et al., (2015)
MgO-FLG-FE	201.1	Reddy et al., (2018)
CuO-NP	189.5	Vidovix et al., (2021)
N/porous graphite	20.66	Shaban et al., (2017)
Sepiolite	233.81	Barhdadi et al., (2024)
Ferruginous kaolinite	59.3	Debnath et al., (2017)
HM24	211.4	This study
PO₄³⁻		
Lanthanum hydroxides	107.5	Xie et al., (2014)
La doping magnetic graphene	116.28	Nodeh et al., (2017)
Biochar	133	Yao et al., (2011)
Red mud-chitosan microspheres	23.54	Tandekar et al., (2021)
Mg(OH) ₂ /ZrO ₂	87.2	Lin et al., (2019)
Zirconia/graphite oxide	149.3	Zong et al., (2013)
ZrO ₂ nanoparticles	99	Su et al., (2013)
La ₁₀₀ SBA-15	45.6	Yang et al., (2011)
Hydrous zirconium oxide	51.8	Lin et al., (2017)
Calcined Mg-Al-LDHs	40.78	Das et al., (2006)
Kaolintic clay	38.46	Hamdi and Srasra, 2012
HM24	148	This study