

Supporting Information

Pb_{3.5}GeS₄Br₃: The first phase-matching thiogermanate halide IR nonlinear optical material

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Table S1. Atomic coordinates, equivalent isotropic displacement parameters ($\text{\AA}^2 \times 10^3$) of $\text{Pb}_3\text{GeS}_4\text{Br}_2$.

Atoms	x	y	z	U_{eq}	Wyckoff positions
Pb1	8013.3(4)	6928.8(5)	6484.4(4)	38.56(14)	4e
Pb2	8459.7(3)	2662.5(7)	4120.2(5)	45.47(15)	4e
Pb3	5460.9(3)	-944.2(4)	3366.2(4)	27.99(12)	4e
Ge1	6254.4(7)	2948.2(10)	5160.6(8)	15.87(18)	4e
S1	6672.5(17)	4938(3)	4097(2)	21.1(4)	4e
S2	7485.3(18)	915(3)	5463(2)	23.5(4)	4e
S3	4500.7(16)	1914(2)	3982.2(19)	16.0(4)	4e
S4	6511(2)	3843(3)	7074(2)	29.0(5)	4e
Br1	8735.7(10)	6875.4(15)	9343.5(10)	38.8(3)	4e
Br2	9674.3(8)	4356.4(13)	6993.3(10)	35.8(2)	4e

Table S2. Atomic coordinates, equivalent isotropic displacement parameters ($\text{\AA}^2 \times 10^3$) of $\text{Pb}_{3.5}\text{GeS}_4\text{Br}_3$.

Atoms	x	y	z	U_{eq}	Wyckoff positions
Pb1	1453.8(3)	4040.6(3)	8784.7(6)	24.32(13)	6c
Pb2	0	0	1517(2)	22.0(2)	2a
Ge1	3333.33	6666.67	4759(2)	13.0(3)	2b
S1	3333.33	6666.67	1140(5)	19.0(7)	2b
S2	1230.4(19)	6000(2)	6184(3)	15.4(4)	6c
Br1	786.3(7)	2606.3(7)	4002.8(15)	23.33(19)	2b

Table S3. Selected bond lengths of Pb₃GeS₄Br₂.

Atom	Atom	Length/Å	Atom	Atom	Length/Å
Pb1	S1	2.980(2)	Pb3	S3 ¹	3.120(2)
Pb1	Br14	3.1346(11)	Pb3	S1 ²	3.030(2)
Pb1	Br1	2.9899(11)	Pb3	S2	3.046(2)
Pb1	Br2	2.8432(10)	Pb3	S4 ³	2.939(2)
Pb2	S1	2.928(2)	Ge1	S1	2.218(2)
Pb2	S2	2.760(2)	Ge1	S2	2.194(2)
Pb2	S43	2.841(2)	Ge1	S3	2.216(2)
Pb3	S3	2.8430(19)	Ge1	S4	2.193(2)

¹1-X,-Y,1-Z; ²1-X,-1/2+Y,1/2-Z; ³+X,1/2-Y,-1/2+Z; ⁴+X,3/2-Y,-1/2+Z

Table S4. Selected bond lengths of $\text{Pb}_{3.5}\text{GeS}_4\text{Br}_3$.

Atom	Atom	Length/Å	Atom	Atom	Length/Å
Pb1	S1 ²	2.9490(16)	Pb2	Br1 ⁷	2.9613(10)
Pb1	S2 ¹	2.8960(19)	Pb2	Br1 ⁸	2.9613(10)
Pb1	S2	2.7797(19)	Pb2	Br1 ⁴	2.9702(11)
Pb1	Br1	3.2024(10)	Ge1	S1	2.191(3)
Pb2	Br1	2.9613(10)	Ge1	S2	2.2243(19)
Pb2	Br1 ⁵	2.9702(11)	Ge1	S2 ¹	2.2243(19)
Pb2	Br1 ⁶	2.9702(11)	Ge1	S2 ⁹	2.2243(19)

¹1-Y,1+X-Y,+Z; ²+X,+Y,1+Z; ³-X,-Y,1/2+Z; ⁴-X,-Y,-1/2+Z; ⁵+Y,-X+Y,-1/2+Z; ⁶-Y+X,+X,-1/2+Z; ⁷+Y-X,-X,+Z; ⁸-Y,+X-Y,+Z; ⁹+Y-X,1-X,+Z

Table S5. Selected angles (°) of Pb₃GeS₄Br₂.

Atom	Atom	Atom	Angle/°	Atom	Atom	Atom	Angle/°
S1	Pb1	Br1	140.79(5)	S1 ²	Pb3	S3 ¹	125.98(5)
S1	Pb1	Br1 ⁴	72.30(5)	S1 ²	Pb3	S2	136.75(6)
Br2	Pb1	Br1	85.53(3)	S2	Pb3	S3 ¹	73.25(6)
Br2	Pb1	Br1 ⁴	86.00(3)	S4 ³	Pb3	S3 ¹	145.30(6)
Br2	Pb1	S1	82.80(5)	S4 ³	Pb3	S1 ²	79.75(6)
Br1	Pb1	Br1 ⁴	143.89(4)	S4 ³	Pb3	S2	72.16(6)
S2	Pb2	S1	77.13(6)	S3	Ge1	S1	111.29(8)
S2	Pb2	S4 ³	78.02(7)	S2	Ge1	S3	106.52(8)
S4 ³	Pb2	S1	81.79(7)	S2	Ge1	S1	107.06(9)
S3	Pb3	S3 ¹	77.44(6)	S4	Ge1	S3	113.45(9)
S3	Pb3	S1 ²	74.27(6)	S4	Ge1	S1	110.33(10)
S3	Pb3	S2	73.68(5)	S4	Ge1	S2	107.86(9)
S3	Pb3	S4 ³	90.29(7)				

¹1-X,-Y,1-Z; ²1-X,-1/2+Y,1/2-Z; ³+X,1/2-Y,-1/2+Z; ⁴+X,3/2-Y,-1/2+Z; ⁵+X,3/2-Y,1/2+Z; ⁶1-X,1/2+Y,1/2-Z; ⁷+X,1/2-Y,1/2+Z

Table S6. Selected angles (°) of Pb_{3,5}GeS₄Br₃.

Atom	Atom	Atom	Angle/°	Atom	Atom	Atom	Angle/°
S2	Pb1	Br1	77.49(4)	Br1	Pb2	Br1 ⁸	83.721(9)
S2 ¹	Pb1	Br1	70.33(4)	Br1 ⁷	Pb2	Br1 ⁸	179.71(6)
S2	Pb1	S2 ¹	77.43(7)	Br1 ³	Pb2	Br1 ⁵	96.09(4)
S2	Pb1	S1 ²	78.67(6)	Br1 ⁶	Pb2	Br1 ³	83.722(9)
S2 ¹	Pb1	S1 ²	76.87(6)	Br1 ⁵	Pb2	Br1 ⁸	96.09(4)
S1 ²	Pb1	Br1	142.78(6)	Br1 ⁷	Pb2	Br1 ³	83.722(9)
Br1 ³	Pb2	Br1 ⁸	96.09(4)	Br1	Pb2	Br1 ⁵	83.721(9)
Br1	Pb2	Br1 ³	179.71(6)	S2	Ge1	S2 ¹	105.93(6)
Br1 ⁶	Pb2	Br1 ⁸	83.722(9)	S2 ⁹	Ge1	S2 ¹	105.93(6)
Br1 ⁶	Pb2	Br1 ⁷	96.47(4)	S2	Ge1	S2 ⁹	105.93(6)
Br1 ⁶	Pb2	Br1 ⁵	179.71(6)	S1	Ge1	S2 ¹	112.82(6)
Br1 ⁷	Pb2	Br1 ⁵	83.722(9)	S1	Ge1	S2 ⁹	112.82(6)
Br1 ⁶	Pb2	Br1	96.47(4)	S1	Ge1	S2	112.82(6)
Br1 ⁷	Pb2	Br1	96.47(4)				

¹1-Y,1+X-Y,+Z; ²+X,+Y,1+Z; ³-X,-Y,-1/2+Z; ⁴-X,-Y,1/2+Z; ⁵-Y+X,+X,-1/2+Z; ⁶+Y-X,-X,+Z; ⁷-Y,+X-Y,+Z; ⁸+Y,-X+Y,-1/2+Z; ⁹+Y-X,1-X,+Z; ¹⁰+Y-X,1-X,-1+Z; ¹¹+X,+Y,-1+Z; ¹²1-Y,1+X-Y,-1+Z

Table S7. Anisotropic displacement parameters ($\text{\AA}^2 \times 10^3$) for $\text{Pb}_3\text{GeS}_4\text{Br}_2$. The anisotropic displacement factor exponent takes the form: $-2\pi^2[h^2a^{*2}U_{11}+2hka^*b^*U_{12}+\dots]$.

Atom	U_{11}	U_{22}	U_{33}	U_{23}	U_{13}	U_{12}
Pb1	38.5(2)	48.7(3)	25.6(2)	-1.34(16)	11.60(17)	18.96(17)
Pb2	25.7(2)	74.7(3)	40.7(3)	-11.1(2)	18.88(18)	-10.34(18)
Pb3	34.3(2)	26.06(19)	27.5(2)	2.63(13)	17.18(16)	2.76(13)
Ge1	18.0(4)	18.3(4)	11.6(4)	0.2(3)	6.8(3)	0.2(3)
S1	21.1(9)	21.9(9)	16.8(10)	3.5(7)	5.3(7)	-2.0(7)
S2	20.2(9)	20.8(9)	26.7(11)	2.2(8)	7.7(8)	5.2(7)
S3	16.0(8)	18.8(9)	13.6(9)	-0.3(7)	6.9(7)	-0.1(6)
S4	30.1(11)	41.1(13)	11.7(10)	-4.4(8)	5.5(8)	15.7(9)
Br1	41.3(5)	59.5(7)	23.3(5)	-6.7(4)	21.2(4)	-14.9(5)
Br2	26.1(4)	36.5(5)	31.0(5)	-9.8(4)	0.0(4)	11.4(4)

Table S8. Anisotropic displacement parameters ($\text{\AA}^2 \times 10^3$) for $\text{Pb}_{3.5}\text{GeS}_4\text{Br}_3$. The anisotropic displacement factor exponent takes the form: $-2\pi^2[h^2a^2U_{11}+2hka^*b^*U_{12}+\dots]$.

Atom	U11	U22	U33	U23	U13	U12
Pb1	27.61(19)	21.53(18)	23.92(19)	4.86(17)	1.42(18)	12.36(13)
Pb2	17.6(3)	17.6(3)	30.9(6)	0	0	8.78(14)
Ge1	14.3(4)	14.3(4)	10.4(6)	0	0	7.1(2)
S1	23.3(11)	23.3(11)	10.5(17)	0	0	11.7(6)
S2	13.5(9)	16.6(10)	16.7(10)	-0.3(8)	0.4(7)	7.9(8)
Br1	22.3(4)	24.0(4)	21.5(4)	-2.1(4)	-4.3(4)	10.0(3)



Fig. S1 The optical image of $\text{Pb}_{3.5}\text{GeS}_4\text{Br}_3$ crystals.

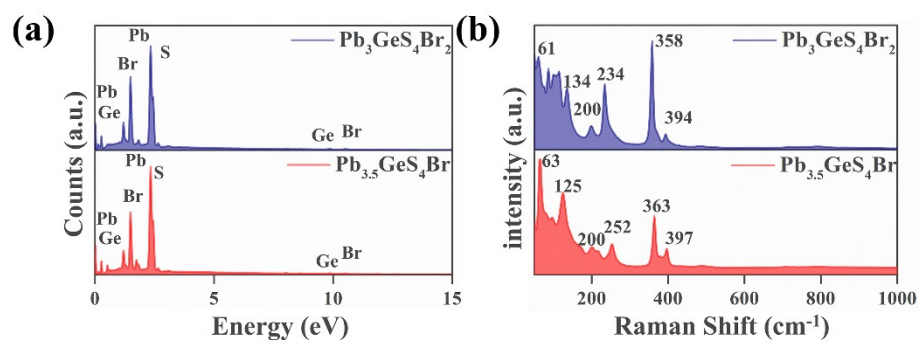


Fig. S2 The EDS (a) and Raman spectra (b) of $\text{Pb}_3\text{GeS}_4\text{Br}_2$ and $\text{Pb}_{3.5}\text{GeS}_4\text{Br}_3$.

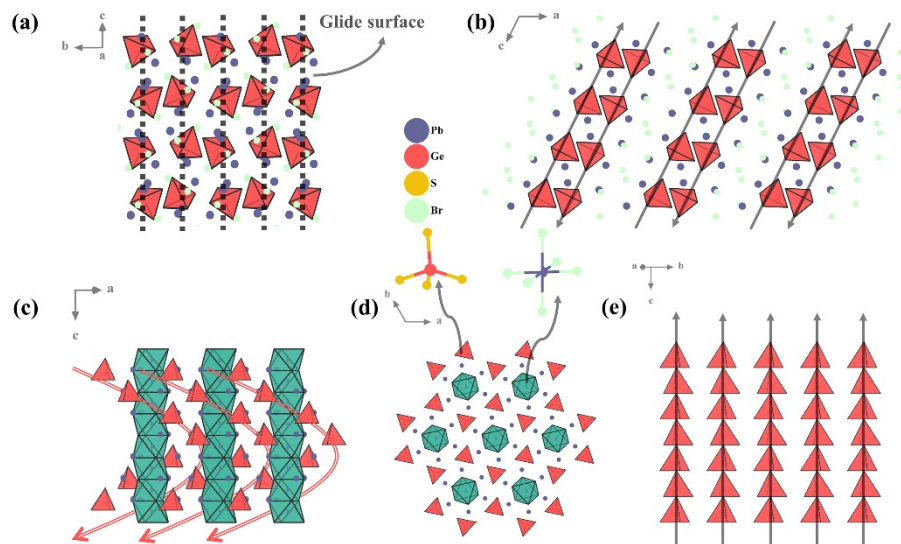


Fig. S3 The structures of $\text{Pb}_3\text{GeS}_4\text{Br}_2$ and $\text{Pb}_{3.5}\text{GeS}_4\text{Br}_3$. (a) The isolated $[\text{GeS}_4]$ pseudo-layer structure alignment along the glide surface in $\text{Pb}_3\text{GeS}_4\text{Br}_2$; (b) The opposite-arranged $[\text{GeS}_4]$ tetrahedra in $\text{Pb}_3\text{GeS}_4\text{Br}_2$; (c) The isolated $[\text{GeS}_4]$ tetrahedral arranged around the $[\text{PbS}_6]$ column configuration in $\text{Pb}_{3.5}\text{GeS}_4\text{Br}_3$; (d) The whole structure of $\text{Pb}_{3.5}\text{GeS}_4\text{Br}_3$; (e) The well-arranged $[\text{GeS}_4]$ tetrahedra in $\text{Pb}_{3.5}\text{GeS}_4\text{Br}_3$.

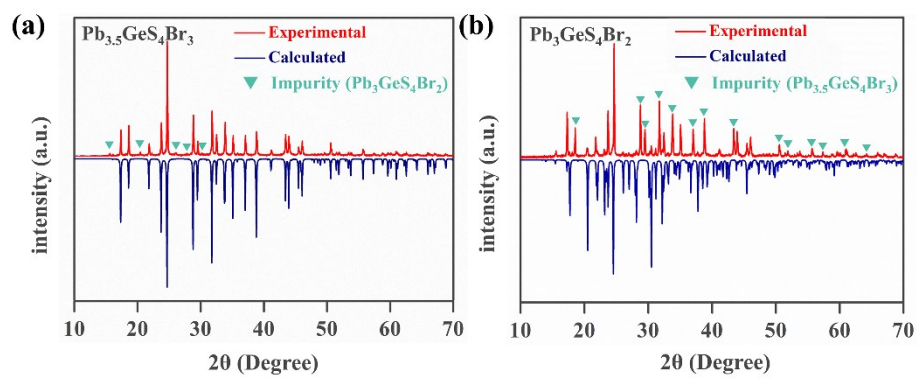


Fig. S4 The experimental and calculated XRD patterns of $\text{Pb}_{3.5}\text{GeS}_4\text{Br}_3$ (a) and $\text{Pb}_3\text{GeS}_4\text{Br}_2$ (b).

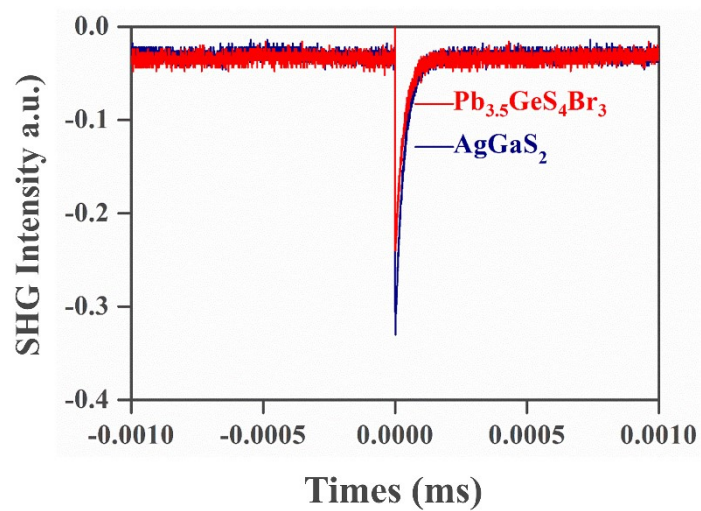


Fig. S5 Oscilloscope traces of SHG signals of $\text{Pb}_{3.5}\text{GeS}_4\text{Br}_3$ (red) with AgGaS_2 (blue) as a reference at a particle size of 180-212 μm .

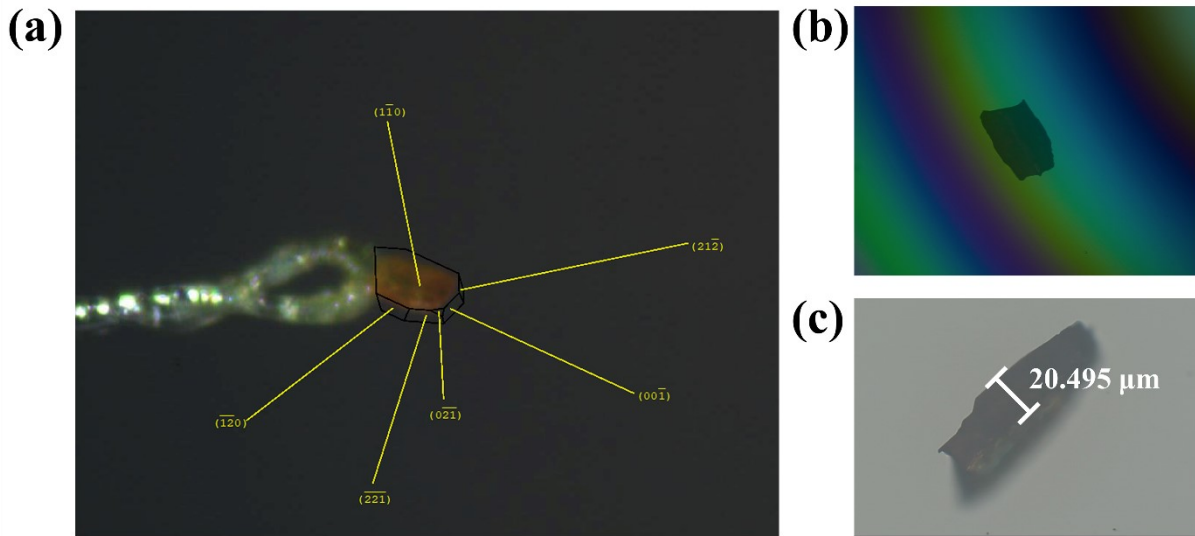


Fig. S6 The RID measurement of $\text{Pb}_{3.5}\text{GeS}_4\text{Br}_3$. (a) The plane indices determined by single crystal XRD. (b) The RID was measured to $0.05@546 \text{ nm}$ (c) The thickness of the single crystal is $20.495 \mu\text{m}$ measured by an optical microscope.

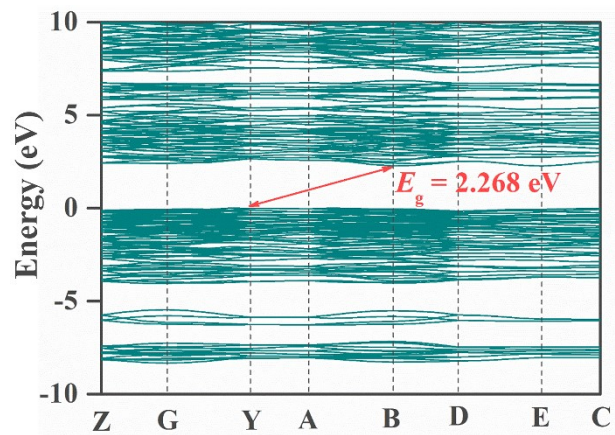


Fig. S7 The band structure of $\text{Pb}_3\text{GeS}_4\text{Br}_2$.