

Supporting Information

From $\text{BaAlBO}_3\text{F}_2$ to $\text{BaAlB}_3\text{O}_6\text{F}_2$ and $\text{BaAl}_2(\text{B}_3\text{O}_6)_2\text{F}_2$: the Enhancement of Birefringence and Band Gap by Extending the π -Conjugated System Combined with [Al-O/F] Functional Groups

Cheng Chen,^a Danyang Dou,^a Yunjie Bai,^a Bingbing Zhang,^{ab} Ying Wang^{ab*}

^a College of Chemistry and Materials Science, Hebei Research Center of the Basic Discipline of Synthetic Chemistry, Key Laboratory of Medicinal Chemistry and Molecular Diagnosis of the Ministry of Education, Key Laboratory of Chemical Biology of Hebei Province, Hebei University, Baoding 071002, China. Email: wangy@hbu.edu.cn

^bInstitute of Life Science and Green Development, Hebei University, Baoding 071002, China.

Table of Contents

Table S1. Crystal data and structure refinements for $\text{BaAlB}_3\text{O}_6\text{F}_2$ and $\text{BaAl}_2(\text{B}_3\text{O}_6)_2\text{F}_2$.

Table S2. Atomic coordinates and equivalent isotropic displacement parameters for $\text{BaAlB}_3\text{O}_6\text{F}_2$.

Table S3. Atomic coordinates and equivalent isotropic displacement parameters for $\text{BaAl}_2(\text{B}_3\text{O}_6)_2\text{F}_2$.

Table S4. Bond lengths [\AA] for $\text{BaAlB}_3\text{O}_6\text{F}_2$.

Table S5. Bond angles [deg] for $\text{BaAlB}_3\text{O}_6\text{F}_2$.

Table S6. Bond lengths [\AA] for $\text{BaAl}_2(\text{B}_3\text{O}_6)_2\text{F}_2$.

Table S7. Bond angles [deg] for $\text{BaAl}_2(\text{B}_3\text{O}_6)_2\text{F}_2$.

Table S8. Comparison of bandgap and birefringence for the known F-containing aluminoborates and the arrangement of the [Al-O/F] groups.

Figure. S1. Different arrangement of [Al-O/F] groups in (a) $\text{BaAlBO}_3\text{F}_2$, (b) $\text{BaAlB}_3\text{O}_6\text{F}_2$ and (c) $\text{BaAl}_2(\text{B}_3\text{O}_6)_2\text{F}_2$.

Figure. S2. The experimental and calculated sample XRD patterns of (a) $\text{BaAlB}_3\text{O}_6\text{F}_2$ and (b) $\text{BaAl}_2(\text{B}_3\text{O}_6)_2\text{F}_2$.

Figure. S3. TG/DSC curves of (a) $\text{BaAlB}_3\text{O}_6\text{F}_2$ and (b) $\text{BaAl}_2(\text{B}_3\text{O}_6)_2\text{F}_2$.

Figure. S4. IR Spectra of (a) $\text{BaAlB}_3\text{O}_6\text{F}_2$ and (b) $\text{BaAl}_2(\text{B}_3\text{O}_6)_2\text{F}_2$.

Figure. S5. The measurement of thickness of (a) $\text{BaAlB}_3\text{O}_6\text{F}_2$ and (b) $\text{BaAl}_2(\text{B}_3\text{O}_6)_2\text{F}_2$.

Figure. S6. The calculated band gaps (HSE06) of (a) $\text{BaAlB}_3\text{O}_6\text{F}_2$ and (b) $\text{BaAl}_2(\text{B}_3\text{O}_6)_2\text{F}_2$.

References

Table S1. Crystal data and structure refinements for BaAlB₃O₆F₂ and BaAl₂(B₃O₆)₂F₂.

Empirical formula	BaAlB ₃ O ₆ F ₂	BaAl ₂ (B ₃ O ₆) ₂ F ₂
Formula weight	330.75	486.16
Temperature [K]	273(2)	273(2)
Crystal system	monoclinic	trigonal
Space group (number)	<i>P</i> 2 ₁ / <i>c</i> (14)	<i>R</i> $\bar{3}$ <i>c</i> (167)
<i>a</i> [Å]	7.1245(6)	7.0654(18)
<i>b</i> [Å]	12.7080(10)	7.0654(18)
<i>c</i> [Å]	7.6246(7)	37.529(13)
α [°]	90	90
β [°]	112.189(3)	90
γ [°]	90	120
Volume [Å ³]	639.19(10)	1622.5(10)
<i>Z</i>	4	6
ρ_{calc} [g cm ⁻³]	3.437	2.958
μ [mm ⁻¹]	6.381	3.935
<i>F</i> (000)	600	1356
Radiation	MoK α ($\lambda=0.71073$ Å)	MoK α ($\lambda=0.71073$ Å)
2 θ range [°]	6.41 to 55.12	6.51 to 65.56
Index ranges	-9 $\leq h \leq$ 9 -16 $\leq k \leq$ 15 -9 $\leq l \leq$ 9	-10 $\leq h \leq$ 10 -10 $\leq k \leq$ 10 -55 $\leq l \leq$ 54
Reflections collected	15684	17663
Independent reflections	1457	644
	$R_{\text{int}} = 0.0250$	$R_{\text{int}} = 0.0250$
	$R_{\text{sigma}} = 0.0115$	$R_{\text{sigma}} = 0.0115$
Completeness	98.9 %	100.0 %
Data / Restraints / Parameters	1457/0/118	644/0/36
Goodness-of-fit on F^2	1.141	1.082
Final <i>R</i> indexes [$I \geq 2\sigma(I)$] ^a	$R_1 = 0.0110$, $wR_2 = 0.0277$	$R_1 = 0.0346$, $wR_2 = 0.0759$
Final <i>R</i> indexes [all data] ^a	$R_1 = 0.0113$, $wR_2 = 0.0278$	$R_1 = 0.0612$, $wR_2 = 0.0850$
Largest peak/hole [eÅ ⁻³]	0.32/-0.45	1.00/-1.52

^a $R_1 = F_o - F_c/F_o$ and $wR_2 = [w(F_o^2 - F_c^2)^2/wF_o^4]^{1/2}$ for $F_o^2 > 2(F_c^2)$.

Table S2. Atomic coordinates and equivalent isotropic displacement parameters for $\text{BaAlB}_3\text{O}_6\text{F}_2$. $U(\text{eq})$ is defined as one-third of the trace of the orthogonalized U_{ij} tensor.

Atom	x	y	z	U_{eq}	BVS
Ba1	-0.15914(2)	0.14249(2)	0.87733(2)	0.00965(4)	2.3
Al1	-0.04628(8)	0.09632(4)	0.38295(7)	0.00789(10)	3.1
B1	0.2955(3)	0.23551(16)	0.5266(3)	0.0105(4)	3.0
B2	0.5292(3)	0.39297(15)	0.6556(3)	0.0094(4)	3.0
B3	0.6407(3)	0.56044(16)	0.8284(3)	0.0109(4)	3.0
O1	0.11738(19)	0.21076(10)	0.39411(19)	0.0116(3)	2.1
O2	0.3522(2)	0.34022(10)	0.5523(2)	0.0136(3)	1.9
O3	0.7143(2)	0.35447(10)	0.69269(19)	0.0111(3)	2.0
O4	0.49269(19)	0.49536(10)	0.7083(2)	0.0140(3)	2.1
O5	0.83160(19)	0.52964(10)	0.91797(19)	0.0114(3)	2.2
O6	0.5740(2)	0.66074(10)	0.8511(2)	0.0144(3)	2.1
F1	0.02187(17)	0.03584(9)	0.20052(15)	0.0142(2)	1.1
F2	0.13429(18)	0.16314(9)	0.54769(16)	0.0157(2)	1.0

Table S3. Atomic coordinates and equivalent isotropic displacement parameters for $\text{BaAl}_2(\text{B}_3\text{O}_6)_2\text{F}_2$. $U(\text{eq})$ is defined as one-third of the trace of the orthogonalized U_{ij} tensor.

Atom	x	y	z	U_{eq}	BVS
Ba1	0.666667	0.333333	0.583333	0.02168(17)	1.8
Al1	0.666667	0.333333	0.69801(4)	0.0146(3)	3.1
B1	0.4966(6)	0.6087(6)	0.71292(9)	0.0187(6)	3.0
F1	0.666667	0.333333	0.65367(10)	0.0286(8)	1.0
O1	0.5505(4)	0.8269(4)	0.71260(7)	0.0238(5)	1.9
O2	0.6542(3)	0.5590(3)	0.71370(6)	0.0213(5)	2.0

Table S4. Bond lengths [\AA] for $\text{BaAlB}_3\text{O}_6\text{F}_2$.

Atom-Atom	lengths	Atom-Atom	lengths
Ba1–F2	2.5987(12)	Al1–O1	1.8458(14)
Ba1–F1 ^{#1}	2.6234(11)	Al1–O3 ^{#7}	1.8806(14)
Ba1–F1 ^{#2}	2.6780(11)	Al1–O5 ^{#7}	1.8883(14)
Ba1–O1 ^{#3}	2.6805(13)	Al1–O5 ^{#8}	1.8995(14)
Ba1–F2 ^{#3}	2.7652(12)	Al1–Al1 ^{#1}	2.9538(10)
Ba1–O6 ^{#4}	2.8166(13)	B1–O1	1.327(2)
Ba1–O3 ^{#5}	2.8697(14)	B1–O2	1.383(2)
Ba1–O4 ^{#4}	2.8979(13)	B1–O6 ^{#8}	1.408(2)
Ba1–O3 ^{#6}	3.0155(13)	B2–O3	1.333(2)
Ba1–B3 ^{#4}	3.355(2)	B2–O2	1.382(2)
Ba1–B1 ^{#3}	3.377(2)	B2–O4	1.415(2)
Ba1–Al1 ^{#3}	3.4117(6)	B3–O5	1.329(2)
Al1–F1	1.8088(12)	B3–O4	1.381(2)
Al1–F2	1.8130(13)	B3–O6	1.394(2)

Symmetry transformations used to generate equivalent atoms:

#1: -X, -Y, 1-Z; #2: +X, +Y, 1+Z; #3: +X, 0.5-Y, 0.5+Z; #4: -X, -0.5+Y, 1.5-Z; #5: -1+X, 0.5-Y, 0.5+Z; #6: -1+X, +Y, +Z; #7: -1+X, 0.5-Y, -0.5+Z; #8: 1-X, -0.5+Y, 1.5-Z; #9: +X, 0.5-Y, -0.5+Z; #10: +X, +Y, -1+Z; #11: -X, 0.5+Y, 1.5-Z; #12: 1+X, 0.5-Y, 0.5+Z; #13: 1+X, 0.5-Y, -0.5+Z; #14: 1+X, +Y, +Z; #15: 1-X, 0.5+Y, 1.5-Z;

Table S5. Bond angles [deg] for BaAlB₃O₆F₂.

Atom–Atom–Atom	Angle [°]	Atom–Atom–Atom	Angle [°]
F2–Ba1–F1	72.61(3)	F1–Ba1–B3	91.64(4)
F2–Ba1–F1	139.11(3)	F1–Ba1–B3	108.97(4)
F1–Ba1–F1	71.33(4)	O1–Ba1–B3	147.35(4)
F2–Ba1–O1	70.04(4)	F2–Ba1–B3	111.72(4)
F1–Ba1–O1	106.36(4)	O6–Ba1–B3	24.14(4)
F1–Ba1–O1	102.61(4)	O3–Ba1–B3	78.84(4)
F2–Ba1–F2	110.39(2)	O4–Ba1–B3	24.12(4)
F1–Ba1–F2	156.16(4)	O3–Ba1–B3	89.23(4)
F1–Ba1–F2	95.55(3)	F2–Ba1–B1	82.68(5)
O1–Ba1–F2	55.98(4)	F1–Ba1–B1	94.63(4)
F2–Ba1–O6	80.36(4)	F1–Ba1–B1	81.66(4)
F1–Ba1–O6	108.96(4)	O1–Ba1–B1	21.64(4)
F1–Ba1–O6	129.70(4)	F2–Ba1–B1	63.16(4)
O1–Ba1–O6	123.56(4)	O6–Ba1–B1	145.02(4)
F2–Ba1–O6	94.76(4)	O3–Ba1–B1	106.05(4)
F2–Ba1–O3	165.20(4)	O4–Ba1–B1	166.56(4)
F1–Ba1–O3	117.59(3)	O3–Ba1–B1	80.03(4)
F1–Ba1–O3	55.27(3)	B3–Ba1–B1	168.99(5)
O1–Ba1–O3	114.11(4)	F2–Ba1–Al1	79.17(3)
F2–Ba1–O3	65.10(3)	F1–Ba1–Al1	137.48(3)
O6–Ba1–O3	85.90(4)	F1–Ba1–Al1	116.84(3)
F2–Ba1–O4	101.35(4)	O1–Ba1–Al1	32.55(3)
F1–Ba1–O4	74.68(4)	F2–Ba1–Al1	32.01(3)
F1–Ba1–O4	87.12(4)	O6–Ba1–Al1	96.60(3)
O1–Ba1–O4	170.08(4)	O3–Ba1–Al1	97.09(3)
F2–Ba1–O4	125.72(4)	O4–Ba1–Al1	143.12(3)
O6–Ba1–O4	48.25(4)	O3–Ba1–Al1	33.31(3)
O3–Ba1–O4	72.96(4)	B3–Ba1–Al1	120.19(4)
F2–Ba1–O3	64.90(4)	B1–Ba1–Al1	50.03(4)
F1–Ba1–O3	137.51(4)	F1–Al1–F2	174.49(6)
F1–Ba1–O3	146.81(4)	F1–Al1–O1	91.25(6)
O1–Ba1–O3	59.04(4)	F2–Al1–O1	88.67(6)
F2–Ba1–O3	51.40(4)	F1–Al1–O3	88.68(6)
O6–Ba1–O3	65.09(4)	F2–Al1–O3	85.89(6)
O3–Ba1–O3	104.23(3)	O1–Al1–O3	98.44(6)
O4–Ba1–O3	113.33(4)	F1–Al1–O5	91.17(6)
F2–Ba1–B3	90.59(5)	F2–Al1–O5	90.04(6)

Symmetry transformations used to generate equivalent atoms:

#1: -X, -Y, 1-Z; #2: +X, +Y, 1+Z; #3: +X, 0.5-Y, 0.5+Z; #4: -X, -0.5+Y, 1.5-Z; #5: -1+X, 0.5-

Y, 0.5+Z; #6: -1+X, +Y, +Z; #7: -1+X, 0.5-Y, -0.5+Z; #8: 1-X, -0.5+Y, 1.5-Z; #9: +X, 0.5-Y, -0.5+Z; #10: +X, +Y, -1+Z; #11: -X, 0.5+Y, 1.5-Z; #12: 1+X, 0.5-Y, 0.5+Z; #13: 1+X, 0.5-Y, -0.5+Z; #14: 1+X, +Y, +Z; #15: 1-X, 0.5+Y, 1.5-Z;

Table S6. Bond lengths [\AA] for $\text{BaAl}_2(\text{B}_3\text{O}_6)_2\text{F}_2$.

Atom-Atom	lengths	Atom-Atom	lengths
Ba1-F1#1	2.640(4)	Ba1-O2#3	3.150(2)
Ba1-F1	2.640(4)	Ba1-O2#6	3.150(2)
Ba1-O1#2	3.109(2)	Al1-F1	1.664(4)
Ba1-O1#3	3.109(3)	Al1-O2#8	1.743(2)
Ba1-O1#4	3.109(3)	Al1-O2	1.743(2)
Ba1-O1#5	3.109(3)	Al1-O2#9	1.743(2)
Ba1-O1#6	3.109(3)	B1-O2	1.325(4)
Ba1-O1#7	3.109(2)	B1-O1	1.390(4)
Ba1-O2#2	3.150(2)	B1-O1#10	1.392(4)
Ba1-O2#4	3.150(2)		

Symmetry transformations used to generate equivalent atoms:

#1: $-3.66667+X-Y, 1.66667-Y, 1.16667-Z$; #2: $0.66667-X+Y, -0.66667+Y, -0.16667+Z$; #3: $-0.33333+X, 0.33333+X-Y, -0.16667+Z$; #4: $1.66667-Y, 1.33333-X, -0.16667+Z$; #5: $1.66667-X, 1.33333-Y, 1.33333-Z$; #6: $0.66667+X-Y, -0.66667+X, 1.33333-Z$; #7: $-0.33333+Y, 0.33333-X+Y, 1.33333-Z$; #8: $1-X+Y, 1-X, +Z$; #9: $1-Y, +X-Y, +Z$; #10: $-X+Y, 1-X, +Z$; #11: $1-Y, 1+X-Y, +Z$;

Table S7. Bond angles [deg] for BaAl₂(B₃O₆)₂F₂.

Atom–Atom–Atom	Angle [°]	Atom–Atom–Atom	Angle [°]
F1–Ba1–F1	180.0	O1–Ba1–O2	58.03(6)
F1–Ba1–O1	63.16(5)	O1–Ba1–O2	149.32(6)
F1–Ba1–O1	116.83(5)	O1–Ba1–O2	104.79(6)
F1–Ba1–O1	63.17(5)	O2–Ba1–O2	102.67(5)
F1–Ba1–O1	116.83(5)	F1–Ba1–O2	64.37(4)
O1–Ba1–O1	101.21(6)	F1–Ba1–O2	115.63(4)
F1–Ba1–O1	63.17(5)	O1–Ba1–O2	126.55(6)
F1–Ba1–O1	116.83(5)	O1–Ba1–O2	44.03(6)
O1–Ba1–O1	101.21(6)	O1–Ba1–O2	62.47(6)
O1–Ba1–O1	101.21(6)	O1–Ba1–O2	149.32(6)
F1–Ba1–O1	116.84(5)	O1–Ba1–O2	104.79(6)
F1–Ba1–O1	63.16(5)	O1–Ba1–O2	58.03(6)
O1–Ba1–O1	68.88(9)	O2–Ba1–O2	102.67(5)
O1–Ba1–O1	166.53(9)	O2–Ba1–O2	102.67(5)
O1–Ba1–O1	89.95(9)	F1–Ba1–O2	115.63(4)
F1–Ba1–O1	116.84(5)	F1–Ba1–O2	64.37(4)
F1–Ba1–O1	63.16(5)	O1–Ba1–O2	58.03(6)
O1–Ba1–O1	89.95(9)	O1–Ba1–O2	104.79(6)
O1–Ba1–O1	68.88(9)	O1–Ba1–O2	149.32(6)
O1–Ba1–O1	166.53(9)	O1–Ba1–O2	62.46(6)
O1–Ba1–O1	101.20(6)	O1–Ba1–O2	44.03(6)
F1–Ba1–O1	116.84(5)	O1–Ba1–O2	126.54(6)
F1–Ba1–O1	63.16(5)	O2–Ba1–O2	56.12(8)
O1–Ba1–O1	166.53(9)	O2–Ba1–O2	106.07(8)
O1–Ba1–O1	89.95(9)	O2–Ba1–O2	147.34(8)
O1–Ba1–O1	68.88(9)	F1–Al1–O2	109.75(9)
O1–Ba1–O1	101.20(6)	F1–Al1–O2	109.75(9)
O1–Ba1–O1	101.20(6)	O2–Al1–O2	109.19(9)
F1–Ba1–O2	64.37(4)	F1–Al1–O2	109.75(9)
F1–Ba1–O2	115.63(4)	O2–Al1–O2	109.19(9)
O1–Ba1–O2	44.03(6)	O2–Al1–O2	109.19(9)
O1–Ba1–O2	62.47(6)	O2–B1–O1	119.5(3)
O1–Ba1–O2	126.55(6)	O2–B1–O1	122.3(3)
O1–Ba1–O2	104.79(6)	O1–B1–O1	118.2(3)
O1–Ba1–O2	58.03(6)	Al1–F1–Ba1	180.0
O1–Ba1–O2	149.32(6)	B1–O1–B1	121.8(3)
F1–Ba1–O2	64.37(4)	B1–O1–Ba1	95.29(19)
F1–Ba1–O2	115.63(4)	B1–O1–Ba1	134.4(2)

O1–Ba1–O2	62.47(6)	B1–O2–A11	132.0(2)
O1–Ba1–O2	126.55(6)	B1–O2–Ba1	95.0(2)
O1–Ba1–O2	44.03(6)	A11–O2–Ba1	133.00(10)

Symmetry transformations used to generate equivalent atoms:

#1: $-3.66667+X-Y, 1.66667-Y, 1.16667-Z$; #2: $0.66667-X+Y, -0.66667+Y, -0.16667+Z$; #3: $-0.33333+X, 0.33333+X-Y, -0.16667+Z$; #4: $1.66667-Y, 1.33333-X, -0.16667+Z$; #5: $1.66667-X, 1.33333-Y, 1.33333-Z$; #6: $0.66667+X-Y, -0.66667+X, 1.33333-Z$; #7: $-0.33333+Y, 0.33333-X+Y, 1.33333-Z$; #8: $1-X+Y, 1-X, +Z$; #9: $1-Y, +X-Y, +Z$; #10: $-X+Y, 1-X, +Z$; #11: $1-Y, 1+X-Y, +Z$;

Table S8. Comparison of bandgap and birefringence for the known F-containing aluminoborates and the arrangement of the [Al-O/F] groups.

	Compound	Band gap / eV	Cut-off edge / nm	birefringence	[Al-O/F]
Aluminoborate fluorides	$K_3Ba_3Li_2Al_4B_6O_{20}F^1$	> 6.2	< 190	0.063	[AlO ₄]
	$K_3Sr_3Li_2Al_4B_6O_{20}F^2$	> 6.2	190	0.062	[AlO ₄]
	$Rb_3Ba_3Li_2Al_4B_6O_{20}F^3$	> 6.2	198	0.061	[AlO ₄]
Fluoroaluminoborates	$BaAlBO_3F_2^4$	> 6.2	165	0.0418	[AlO ₃ F ₂]
	$Rb_3Al_3B_3O_{10}F^5$	6.58*	< 200	/	[AlO ₃ F]
	$CsAlB_3O_6F^6$	7.49*	< 190	0.091	[AlO ₃ F]
	$RbAlB_3O_6F^7$	7.15*	< 190	0.0946	[AlO ₃ F]
	$Cs_{0.5}Rb_{0.5}AlB_3O_6F^7$	> 6.2	< 200	/	[AlO ₃ F]
	$Li_{0.5}Na_{0.5}AlB_2O_4F_2^8$	7.55*	< 200	0.108	[AlO ₃ F ₃]
	$SrAlB_3O_6F_2^9$	7.65*	< 200	0.075	[AlO ₄ F ₂]
	$Sr_2Al_{2.18}B_{5.82}O_{13}F_2^{10}$	7.28*	< 200	0.058	[AlO ₄ F ₂]
	$SnAl_2(BO_3)_2F_2^{11}$	4.08	240	0.024	[AlO ₄ F ₂]
	$Al_8(BO_3)_4(B_2O_5)F_8^{12}$	7.32*	< 200	/	[AlO ₄ F ₂]
	$Pb_2Al_2B_3O_8F_3^{13}$	5.26	213	0.0458	[AlO ₄ F ₂]
	$Pb_6AlB_2O_7F_7^{14}$	3.63	< 300	/	[AlF ₆]
	$Al_6B_5O_{15}F_3^{15}$	/	/	/	[AlO ₅ F]
	BaAlB₃O₆F₂ (this work)	7.53*	< 200	0.087	[AlO ₄ F ₂]
	BaAl₂(B₃O₆)₂F₂ (this work)	7.87*	< 200	0.105	[AlO ₃ F]

* DFT calculated results

Figure S1. Different arrangement of [Al-O/F] groups in (a) $\text{BaAlBO}_3\text{F}_2$, (b) $\text{BaAlB}_3\text{O}_6\text{F}_2$, and (c) $\text{BaAl}_2(\text{B}_3\text{O}_6)_2\text{F}_2$.

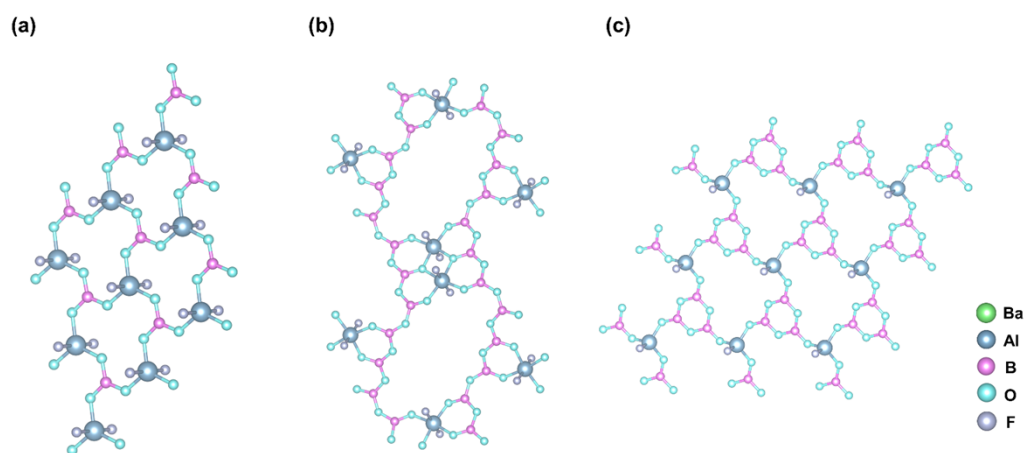


Figure S2. The experimental and calculated sample XRD patterns of (a) $\text{BaAlB}_3\text{O}_6\text{F}_2$ and (b) $\text{BaAl}_2(\text{B}_3\text{O}_6)_2\text{F}_2$.

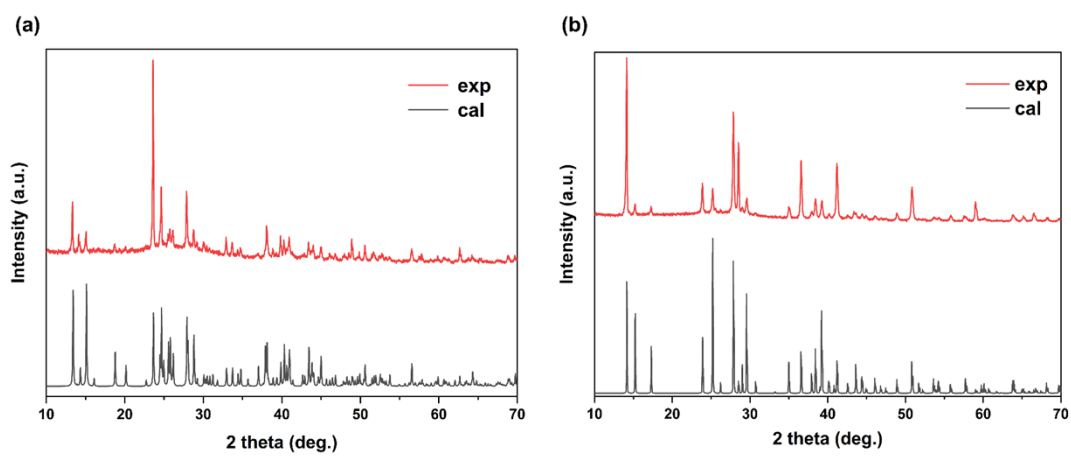


Figure S3. TG/DSC curves of (a) $\text{BaAlB}_3\text{O}_6\text{F}_2$ and (b) $\text{BaAl}_2(\text{B}_3\text{O}_6)_2\text{F}_2$.

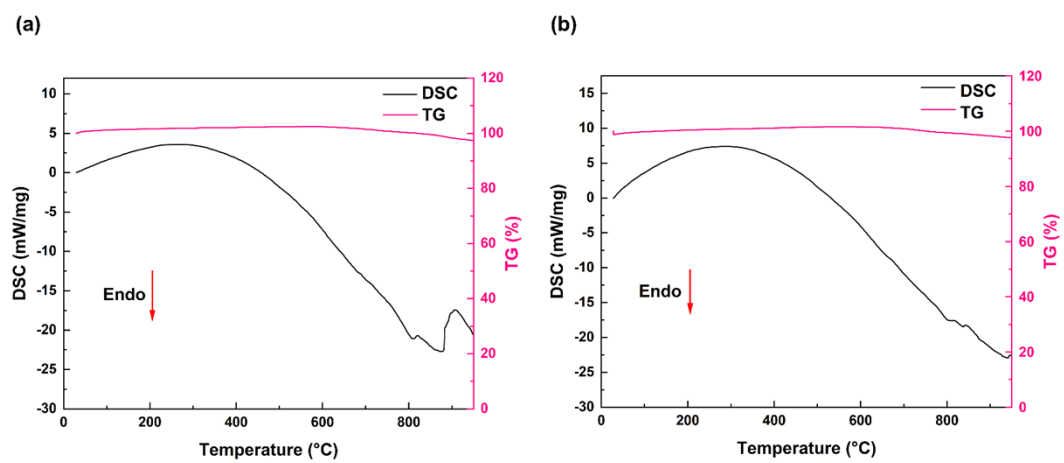


Figure S4. IR Spectra of (a) $\text{BaAlB}_3\text{O}_6\text{F}_2$ and (b) $\text{BaAl}_2(\text{B}_3\text{O}_6)_2\text{F}_2$.

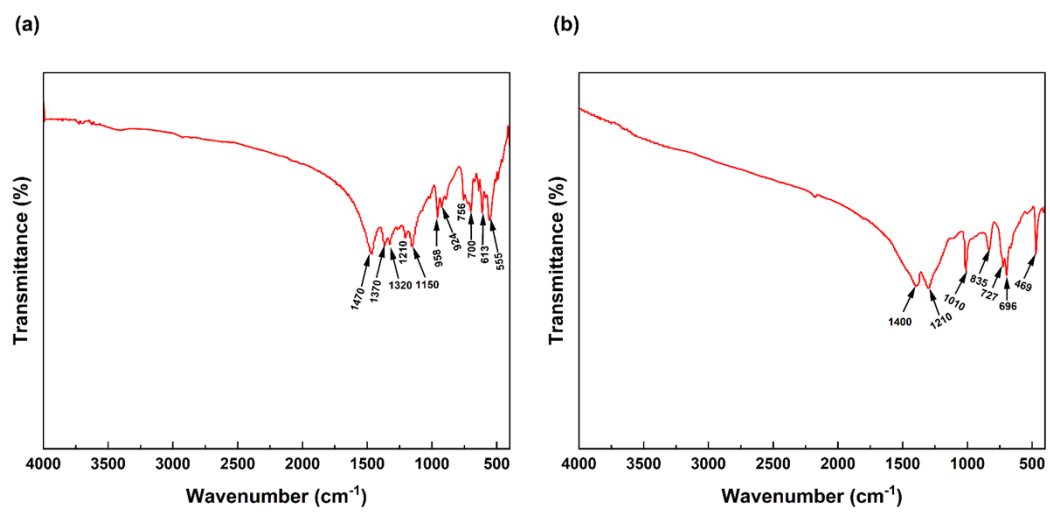


Figure S5. The measurement of thickness of (a) $\text{BaAlB}_3\text{O}_6\text{F}_2$ and (b) $\text{BaAl}_2(\text{B}_3\text{O}_6)_2\text{F}_2$.

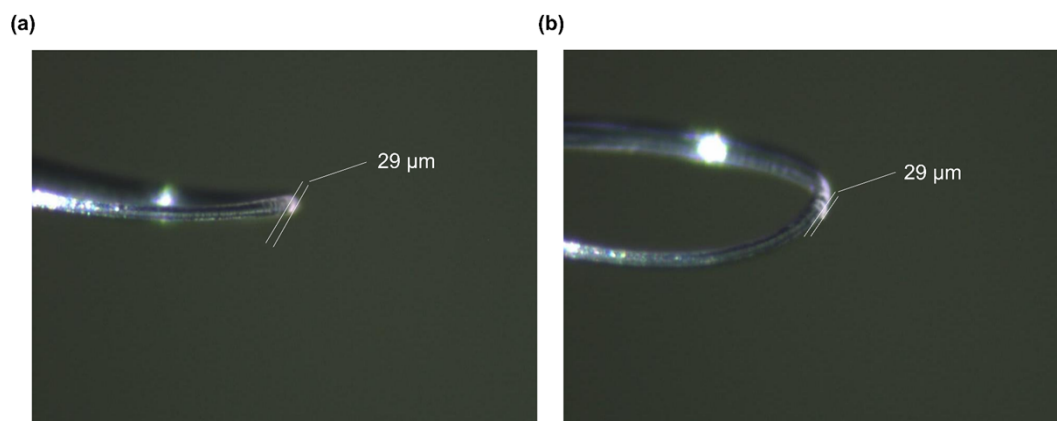
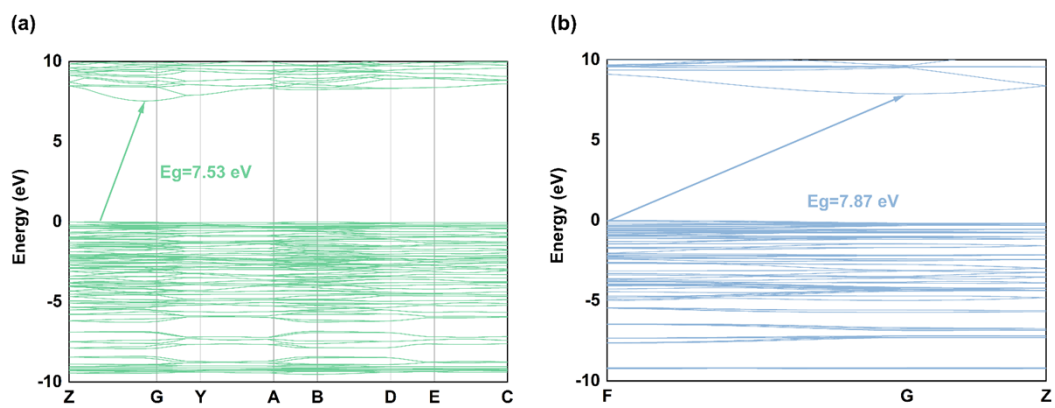


Figure S6. The calculated band gaps (HSE06) of (a) $\text{BaAlB}_3\text{O}_6\text{F}_2$ and (b) $\text{BaAl}_2(\text{B}_3\text{O}_6)_2\text{F}_2$.



References

1. B.Q. Zhao, B.X. Li, S.G. Zhao, X.T. Liu, Z.Y. Wu, Y.G. Shen, X.F. Li, Q.R. Ding, C.M. Ji and J.H. Luo, Physical properties of a promising nonlinear optical crystal $K_3Ba_3Li_2Al_4B_6O_{20}F$, *Cryst. Growth Des.*, 2018, **18**, 7368-7372.
2. Y. Yang, S.Z. Huang and S.L. Pan, $K_3Sr_3Li_2Al_4B_6O_{20}F$: a competitive nonlinear optical crystal for generation of a 266 nm laser, *J. Mater. Chem. C.*, 2022, **10**, 11232-11238.
3. J.K. Wang, H.P. Wu, Z.G. Hu, J.Y. Wang, Y.C. Wu and H.W. Yu, A promising ultraviolet nonlinear optical crystal: $Rb_3Ba_3Li_2Al_4B_6O_{20}F$ —crystal growth, physical properties, and 266 nm laser generation, *J. Mater. Chem. C.*, 2023, **11**, 1320-1328.
4. Z.G. Hu, M. Yoshimura, K. Muramatsu, Y. Mori and T. Sasaki, A new nonlinear optical crystal-BaAlBO₃F₂(BABF), *Jpn. J. Appl. Phys.*, 2002, **41**, L1131-L1133.
5. S.G. Zhao, P.F. Gong, S.Y. Luo, S.J. Liu, L.N. Li, M.A. Asghar, T.K. Asghar, M.C. Hong, Z.S. Lin and J.H. Luo, Beryllium-free $Rb_3Al_3B_3O_{10}F$ with reinforced interlayer bonding as a deep-ultraviolet nonlinear optical crystal, *J. Am. Chem. Soc.*, 2015, **137**, 2207-2210.
6. H.K. Liu, Y. Wang, B.B. Zhang, Z.H. Yang and S.L. Pan, CsAlB₃O₆F: a beryllium-free deep-ultraviolet nonlinear optical material with enhanced thermal stability, *Chem. Sci.*, 2020, **11**, 694-698.
7. H.K. Liu, B.B. Zhang, L. Li and Y. Wang, Exploring deep-UV nonlinear optical materials with enhanced second harmonic generation response and birefringence in fluoroaluminoborate crystals, *ACS Appl. Mater. Interfaces.*, 2021, **13**, 30853-30860.
8. Z.T. Yan, D.D. Chu, M. Zhang, Z.H. Yang and S.L. Pan, $Li_{0.5}Na_{0.5}AlB_2O_4F_2$: fluoroaluminoborate with aligned $^{1\infty}[BO_2]$ chain induced by unprecedented $[AlO_3F_3]^{6-}$ species features enhanced birefringence, *Adv. Opt. Mater.*, 2022, **11**, 2202353.
9. S. Bai, X.D. Zhang, B.B. Zhang, L. Li and Y. Wang, $SrAlB_3O_6F_2$: A fluoroaluminoborate with $[Al_2B_6O_{14}F_4]$ units and large birefringence, *Inorg. Chem.*, 2021, **60**, 10006-10011.
10. J.H. Jiao, A. Tudi, Z.T. Yan and M. Zhang, Structural motif cosubstitution strategy for designing fluoroaluminoborate with the $Sr_2Be_2B_2O_7$ -type double-layered structure, *Inorg. Chem.*, 2023, **62**, 4399-4404.
11. Y. Wang, J. Han, J.B. Huang, Z.H. Yang, S.Z. Huang and S.L. Pan, From $BaAl_2(BO_3)_2O$ to $SnAl_2(BO_3)_2F_2$: structure transformation based on ion regulation, *New J. Chem.*, 2020, **44**, 9852-9857.
12. Y. Wang, J. Han, J.B. Huang, Z.H. Yang and S.L. Pan, $Al_8(BO_3)_4(B_2O_5)F_8$: A F-containing aluminum borate featuring two types of isolated B–O groups, *Inorg. Chem.*, 2019, **59**, 810-817.
13. B. Jiang, S. Shu, Z.H. Yang, F.F. Zhang, M. Zhang and S.L. Pan, $Pb_2Al_2B_3O_8F_3$: structure and properties of a new fluoroaluminoborate with non-traditional chain-like B_3O_8 groups, *Dalton Trans.*, 2022, **51**, 3964-3969.
14. L.Y. Dong, S.L. Pan, Z.H. Yang, W.W. Zhao, X.Y. Dong, Y. Wang and Y.N. Huang, Synthesis, crystal structure, and properties of a new lead aluminum fluoride borate, $Pb_6AlB_2O_7F_7$, *Z. Anorg. Allg. Chem.*, 2012, **638**, 2280-2285.
15. E.V. Sokolova, Y.K. Egorov Tismenko, S.V. Kargal'tsev, V.A. Klyakhin and V.S. Urusov, Refinement of the crystalline structure of synthetic fluoruous jeremejevite $Al_6[BO_3]_5F_3$, *Geol. Geofiz.*, 1987, **42**, 82-84.