

## Supporting Information For

# Computer-Aided Screening of Bismuth Molybdates Nonlinear Optical Crystals $\gamma$ -Bi<sub>2</sub>MoO<sub>6</sub>

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**Table S1.** The chemical formula, ICSD collection-code, space group, band gap ( $E_g$ ), birefringence ( $\Delta n$ ), second-order susceptibility ( $\chi^{(2)}$ ), and the maximum  $\chi^{(2)}$  tensor of 5 bismuth molybdates.

**Table S2.** Calculation of dipole moments of the Mo-O and Bi-O Polyhedra for  $\gamma$ -Bi<sub>2</sub>MoO<sub>6</sub>.

**Table S3.** Calculation of dipole moments of the Mo-O and Bi-O Polyhedra for Bi<sub>10</sub>Mo<sub>3</sub>O<sub>24</sub>.

**Figure S1.** The Mo respective coordination polyhedra of  $\gamma$ -Bi<sub>2</sub>MoO<sub>6</sub> (a) and Bi<sub>10</sub>Mo<sub>3</sub>O<sub>24</sub> (b).

**Figure S2.** The Bi respective coordination polyhedra of  $\gamma$ -Bi<sub>2</sub>MoO<sub>6</sub>, with purple arrows indicating the directions of the group's dipole moments.

**Figure S3.** The Bi respective coordination polyhedra of Bi<sub>10</sub>Mo<sub>3</sub>O<sub>24</sub>, with purple arrows indicating the directions of the group's dipole moments.

**Figure S4.** The [Bi<sub>10</sub>O<sub>12</sub>]<sub>n</sub> layer (a). The ten-membered ring channels (b). Projection of Bi<sub>10</sub>Mo<sub>3</sub>O<sub>24</sub> refined crystal structure on to (010) plane (c).

**Figure S5.** The dipole moment directions generated by the asymmetric Bi-O groups in  $\gamma$ -Bi<sub>2</sub>MoO<sub>6</sub> (a) and Bi<sub>10</sub>Mo<sub>3</sub>O<sub>24</sub> (b). ( $\gamma$ -Bi<sub>2</sub>MoO<sub>6</sub> is along the c-axis, Bi<sub>10</sub>Mo<sub>3</sub>O<sub>24</sub> is along the b-axis.)

**Figure S6.** The TG-DSC curves of  $\gamma$ -Bi<sub>2</sub>MoO<sub>6</sub> (a) and Bi<sub>10</sub>Mo<sub>3</sub>O<sub>24</sub> (c). The XRD patterns of the  $\gamma$ -Bi<sub>2</sub>MoO<sub>6</sub> (b) and Bi<sub>10</sub>Mo<sub>3</sub>O<sub>24</sub> (d) samples obtained at different calcination temperatures.

**Figure S7.** The infrared vibration mode of  $\gamma$ -Bi<sub>2</sub>MoO<sub>6</sub>.

**Figure S8.** The infrared vibration mode of Bi<sub>10</sub>Mo<sub>3</sub>O<sub>24</sub>.

**Figure S9.** The bandgap of  $\gamma$ -Bi<sub>2</sub>MoO<sub>6</sub> calculated using the HSE06 method.

**Figure S10.** Partial DOSs of Bi1-Bi5 atoms from Bi<sub>10</sub>Mo<sub>3</sub>O<sub>24</sub> (a). The ELF of Bi<sub>10</sub>Mo<sub>3</sub>O<sub>24</sub> (b). The ELF for five independent Bi atoms in Bi<sub>10</sub>Mo<sub>3</sub>O<sub>24</sub> (c).

**Figure S11.** SHG density maps of occupied orbitals of the largest SHG coefficient  $d_{24}$  of  $\gamma$ -Bi<sub>2</sub>MoO<sub>6</sub> in different density color scale.

**Figure S12.** SHG density maps of occupied and unoccupied orbitals of the largest SHG coefficient  $d_{22}$  for Bi<sub>10</sub>Mo<sub>3</sub>O<sub>24</sub>.

**Table S1.** The chemical formula, ICSD collection-code, space group, band gap (Eg), birefringence ( $\Delta n$ ), second-order susceptibility ( $\chi^{(2)}$ ), and the maximum  $\chi^{(2)}$  tensor of 5 bismuth molybdates.

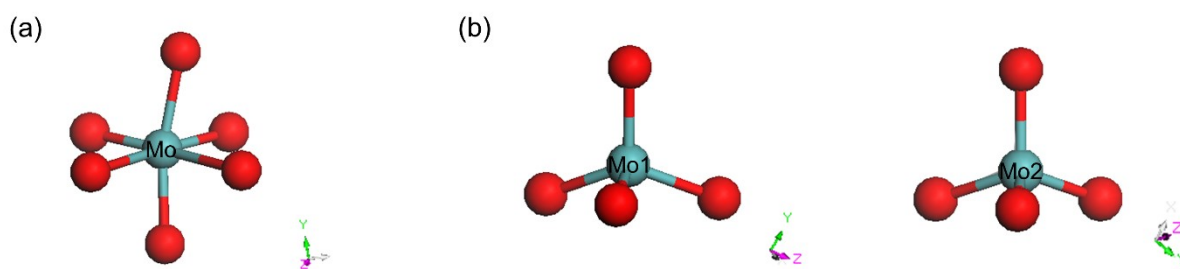
No.	Formula	ICSD	Space groups	Eg-GGA(eV)	$\Delta n$	$\chi^{(2)}$ (pm/V)	$ \chi^{(2)} _{\max}$ (pm/V)
1	Bi <sub>2</sub> MoO <sub>6</sub>	47139	Pca2 <sub>1</sub>	1.246	0.345	$\chi_{113}=-48.40$ ; $\chi_{223}=125.05$ ; $\chi_{333}=95.38$	125.05
2	Bi <sub>2</sub> MoO <sub>6</sub>	201685	Pca2 <sub>1</sub>	1.251	0.354	$\chi_{113}=-48.54$ ; $\chi_{223}=124.85$ ; $\chi_{333}=94.79$	124.85
3	Bi <sub>2</sub> MoO <sub>6</sub>	14266	Pca2 <sub>1</sub>	1.238	0.356	$\chi_{113}=-50.31$ ; $\chi_{223}=124.58$ ; $\chi_{333}=94.92$	124.58
4	Bi <sub>10</sub> Mo <sub>3</sub> O <sub>24</sub>	262963	C2	1.939	0.089	$\chi_{112}=-10.00$ ; $\chi_{123}=16.41$ ; $\chi_{222}=10.19$ ; $\chi_{233}=11.43$	16.41
5	Bi <sub>10</sub> Mo <sub>3</sub> O <sub>24</sub>	173837	C2	1.948	0.079	$\chi_{112}=-9.67$ ; $\chi_{123}=16.16$ ; $\chi_{222}=8.41$ ; $\chi_{233}=9.99$	16.16
6	Bi <sub>14</sub> Mo <sub>5</sub> O <sub>36</sub>	262964	C2	1.689	0.186	$\chi_{112}=0.06$ ; $\chi_{123}=-9.85$ ; $\chi_{222}=2.80$ ; $\chi_{233}=0.71$	9.85
7	Cs <sub>2</sub> NaBi(MoO <sub>4</sub> ) <sub>3</sub>	428061	R3c	2.475	0.042	$\chi_{113}=2.96$ ; $\chi_{122}=0.52$ ; $\chi_{222}=-$ $0.02$ ; $\chi_{223}=2.96$ ; $\chi_{333}=-3.50$ ;	3.50
8	Cs <sub>5</sub> Bi(MoO <sub>4</sub> ) <sub>4</sub>	20845	Cc	2.838	0.022	$\chi_{111}=0.45$ ; $\chi_{113}=0.50$ ; $\chi_{122}=-$ $0.41$ ; $\chi_{223}=-0.09$ ; $\chi_{333}=-1.54$	1.54

**Table S2.** Calculation of dipole moments of the Mo-O and Bi-O Polyhedra for  $\gamma$ -Bi<sub>2</sub>MoO<sub>6</sub>

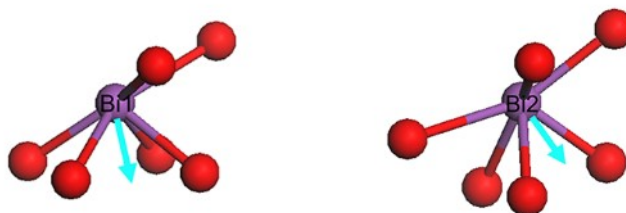
	Species	Symmetry code of cations	dipole moment					
			<i>x (a)</i>	<i>y (b)</i>	<i>z (c)</i>	magnitude		
						debye	$\times 10^{-18}$ esu·cm/Å <sup>3</sup>	
$\gamma$ -Bi <sub>2</sub> MoO <sub>6</sub>	Mo(1)O <sub>6</sub>	1+x, y, 1+z	0.053	-2.657	7.505	7.962	0.016	
		1/2-x, y, 1/2+z	-0.054	-2.658	7.506	7.963	0.016	
		1-x, 1-y, 1/2+z	-0.054	2.659	7.504	7.961	0.016	
		1/2+x, 1-y, 1+z	0.056	2.663	7.508	7.967	0.016	
		$\Sigma$ Mo(1)O <sub>6</sub>	0.001	0.007	30.024	30.036	0.061	
	Bi(1)O <sub>6</sub>	3/2-x, y, -1/2+z	-8.930	13.602	-6.180	17.405	0.036	
		x,y,z	8.931	13.600	-6.177	17.404	0.036	
		1-x, 1-y, -1/2+z	-8.932	-13.601	-6.179	17.405	0.036	
		-1/2+x, 1-y, z	8.934	-13.600	-6.180	17.406	0.036	
		$\Sigma$ Bi(1)O <sub>6</sub>	0.003	0.001	-24.717	24.710	0.050	
	Bi(2)O <sub>6</sub>	x,y,z	-4.588	-12.895	-6.288	15.062	0.031	
		1/2-x, y, -1/2+z	4.590	-12.894	-6.286	15.061	0.031	
		1/2+x, 1-y, z	-4.585	12.895	-6.287	15.061	0.031	
		1-x, 1-y, -1/2+z	4.588	12.895	-6.287	15.062	0.031	
		$\Sigma$ Bi(2)O <sub>6</sub>	0.004	0.001	-25.149	25.140	0.051	
		$\Sigma$ Bi-O	/	0.008	0.003	-49.866	49.850	0.102
		Unit cell		0.009	0.009	-19.842	19.813	0.040

**Table S3.** Calculation of dipole moments of the Mo-O and Bi-O Polyhedra for Bi<sub>10</sub>Mo<sub>3</sub>O<sub>24</sub>

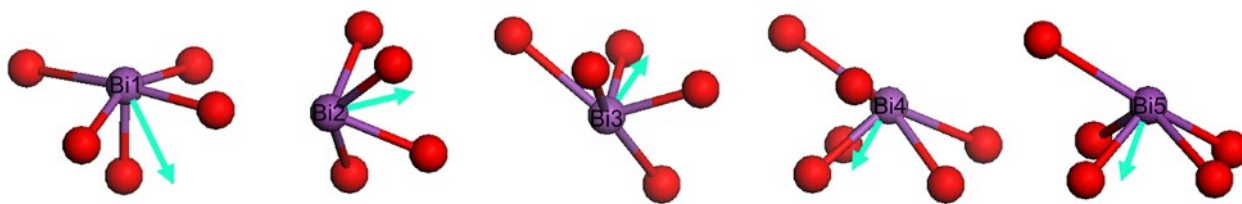
	Species	Symmetry code of cations	dipole moment					
			<i>x (a)</i>	<i>y (b)</i>	<i>z (c)</i>	magnitude		
						debye	$\times 10^{-18}$ esu·cm/Å <sup>3</sup>	
Bi <sub>10</sub> Mo <sub>3</sub> O <sub>24</sub>	Mo(1)O <sub>4</sub>	1-x, y, 1-z	5.082	-1.940	-1.972	5.961	0.005	
		x, y, z	-5.085	-1.937	1.970	5.962	0.005	
		1/2+x, 1/2+y, z	-5.083	-1.938	1.973	5.962	0.005	
		1/2-x, 1/2+y, 1-z	5.082	-1.941	-1.972	5.961	0.005	
		$\Sigma$ Mo(1)O <sub>4</sub>	-0.004	-7.757	-0.001	7.766	0.007	
	Mo(2)O <sub>4</sub>	1+x, y, 1+z	-0.002	-1.716	-0.001	1.716	0.001	
		1/2+x, 1/2+y, 1+z	-0.001	-1.714	0.000	1.714	0.001	
		$\Sigma$ Mo(2)O <sub>4</sub>	-0.004	-3.430	-0.001	3.438	0.003	
		$\Sigma$ Mo-O	/	-0.008	-11.187	-0.003	11.204	0.010
	Bi(1)O <sub>5</sub>	1-x, y, 1-z	9.329	-1.501	18.527	19.929	0.017	
		x, y, z	-9.318	-1.502	-18.517	19.916	0.017	
		1/2+x, 1/2+y, z	-9.323	-1.503	-18.523	19.923	0.017	
		1/2-x, 1/2+y, 1-z	9.322	-1.503	18.522	19.922	0.017	
		$\Sigma$ Bi(1)O <sub>5</sub>	0.011	-6.009	0.010	5.977	0.005	
	Bi(2)O <sub>4</sub>	1-x, -1+y, 1-z	0.915	18.293	-4.364	18.850	0.016	
		x, -1+y, z	-0.915	18.293	4.364	18.850	0.016	
		1/2+x, -1/2+y, z	-0.915	18.293	4.364	18.850	0.016	
		1/2-x, -1/2+y, 1-z	0.915	18.293	-4.364	18.850	0.016	
		$\Sigma$ Bi(2)O <sub>4</sub>	0.000	73.173	0.000	73.173	0.063	
	Bi(3)O <sub>5</sub>	1-x, y, 1-z	-3.893	8.212	-12.164	14.862	0.013	
		x, y, z	3.891	8.210	12.165	14.861	0.013	
		1/2+x, 1/2+y, z	3.891	8.210	12.165	14.861	0.013	
		1/2-x, 1/2+y, 1-z	-3.894	8.210	-12.165	14.862	0.013	
		$\Sigma$ Bi(3)O <sub>5</sub>	-0.004	32.842	0.001	32.837	0.028	
	Bi(4)O <sub>6</sub>	1-x, -1+y, 1-z	-0.758	-7.215	13.370	15.280	0.013	
		x, -1+y, z	0.758	-7.213	-13.370	15.279	0.013	
		1/2+x, -1/2+y, z	0.761	-7.214	-13.368	15.278	0.013	
		1/2-x, -1/2+y, 1-z	-0.756	-7.216	13.372	15.282	0.013	
		$\Sigma$ Bi(4)O <sub>6</sub>	0.004	-28.859	0.003	28.847	0.025	
	Bi(5)O <sub>5</sub>	1-x, y, 1-z	3.271	-6.099	15.107	16.310	0.014	
x, y, z		-3.271	-6.095	-15.108	16.310	0.014		
1/2+x, 1/2+y, z		-3.272	-6.097	-15.107	16.309	0.014		
1/2-x, 1/2+y, 1-z		3.271	-6.097	15.109	16.311	0.014		
	$\Sigma$ Bi(5)O <sub>5</sub>	-0.001	-24.388	0.001	24.388	0.021		
	$\Sigma$ Bi-O	/	0.009	46.759	0.015	46.797	0.040	
	Unit cell		0.001	35.572	0.013	35.594	0.031	



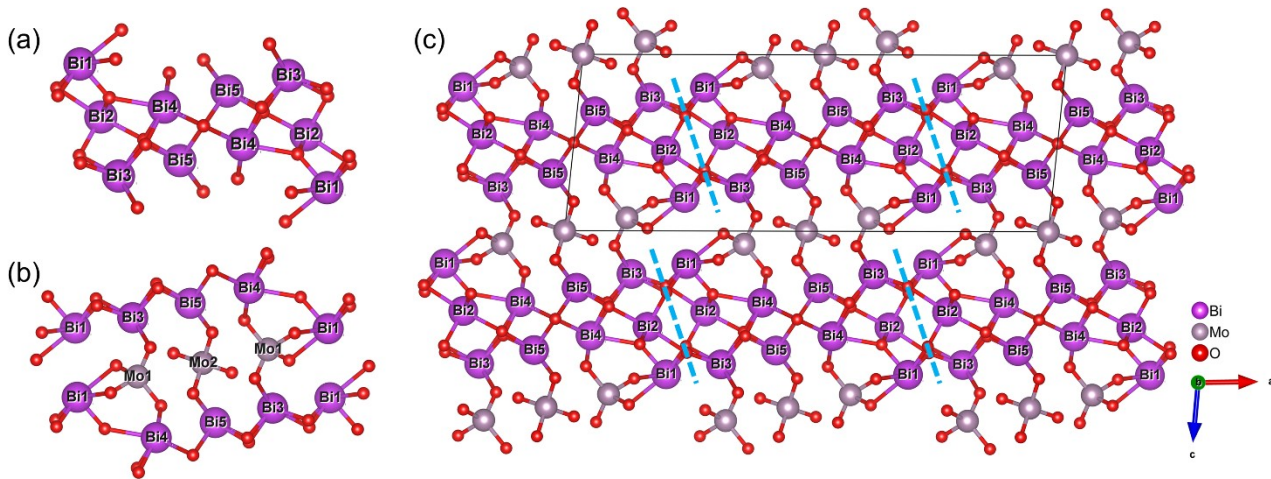
**Figure S1.** The Mo respective coordination polyhedra of  $\gamma\text{-Bi}_2\text{MoO}_6$  (a) and  $\text{Bi}_{10}\text{Mo}_3\text{O}_{24}$  (b).



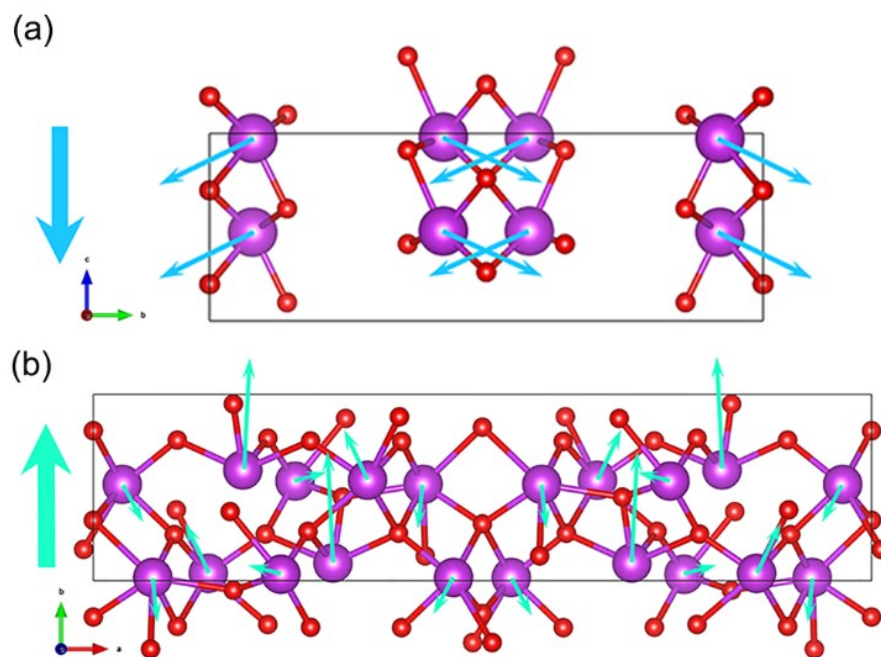
**Figure S2.** The Bi respective coordination polyhedra of  $\gamma\text{-Bi}_2\text{MoO}_6$ , with purple arrows indicating the directions of the group's dipole moments.



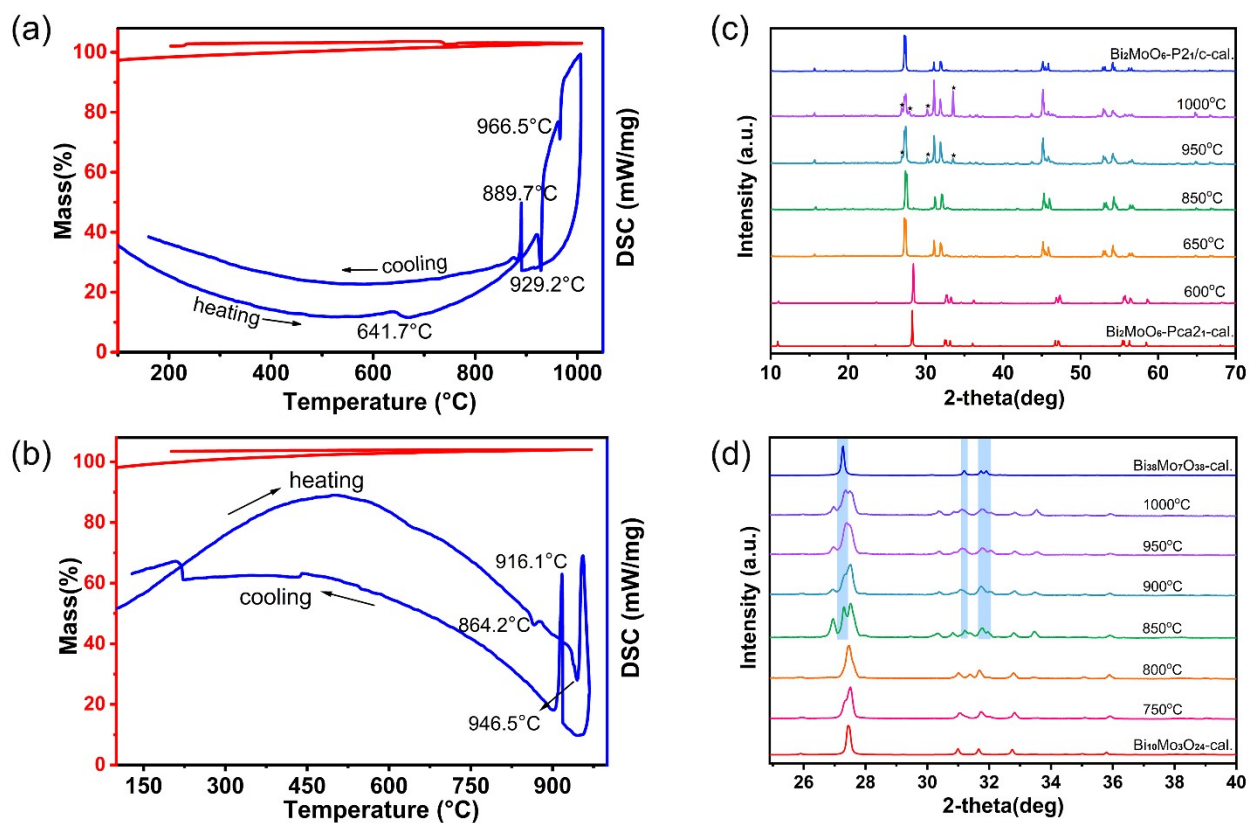
**Figure S3.** The Bi respective coordination polyhedra of  $\text{Bi}_{10}\text{Mo}_3\text{O}_{24}$ , with purple arrows indicating the directions of the group's dipole moments.



**Figure S4.** The  $[\text{Bi}_{10}\text{O}_{12}]_n$  layer (a). The ten-membered ring channels (b). Projection of  $\text{Bi}_{10}\text{Mo}_3\text{O}_{24}$  crystal structure on to (010) plane (c).

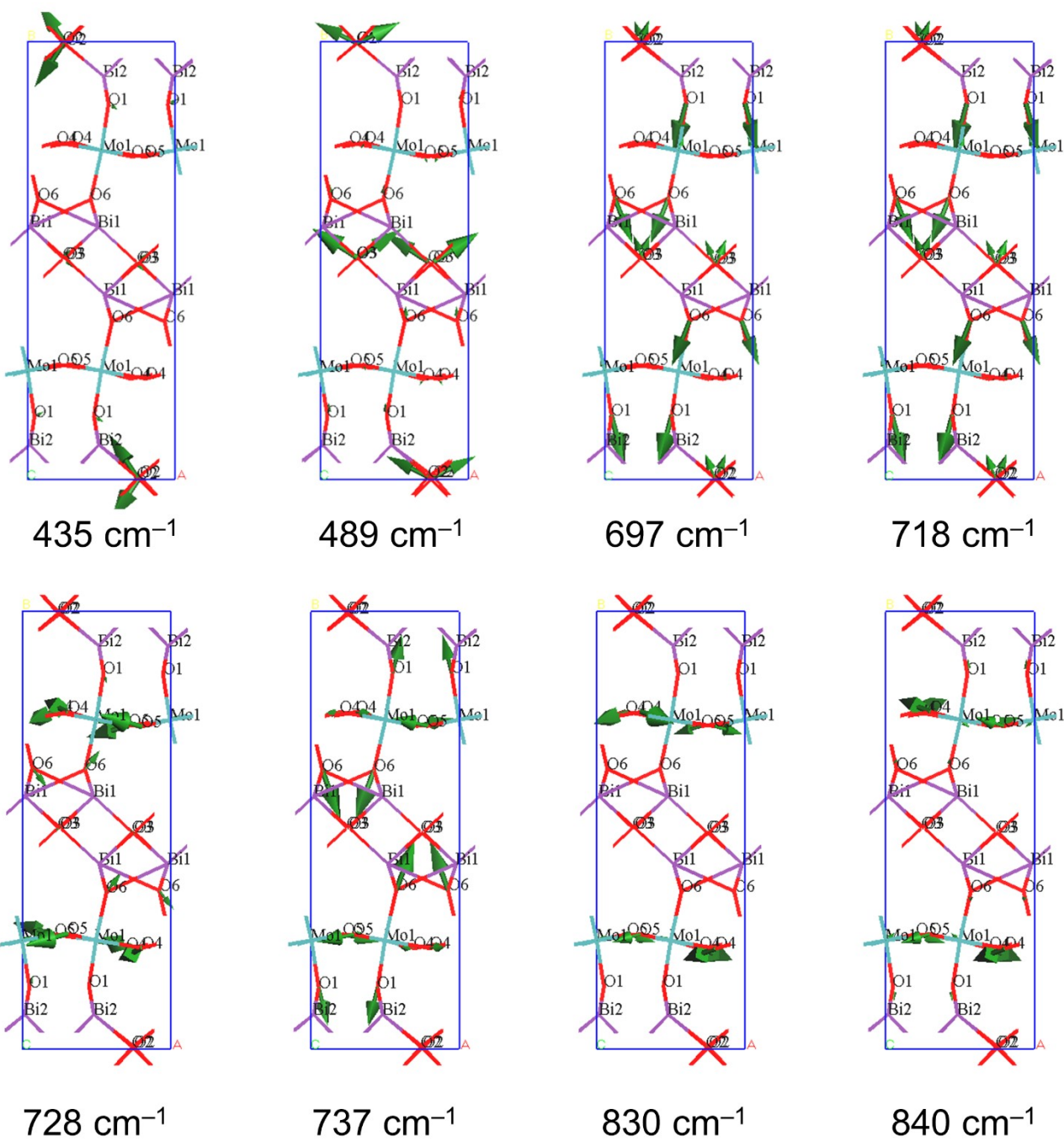


**Figure S5.** The dipole moment directions generated by the asymmetric Bi-O groups in  $\gamma\text{-Bi}_2\text{MoO}_6$  (a) and  $\text{Bi}_{10}\text{Mo}_3\text{O}_{24}$  (b). ( $\gamma\text{-Bi}_2\text{MoO}_6$  is along the c-axis,  $\text{Bi}_{10}\text{Mo}_3\text{O}_{24}$  is along the b-axis.)

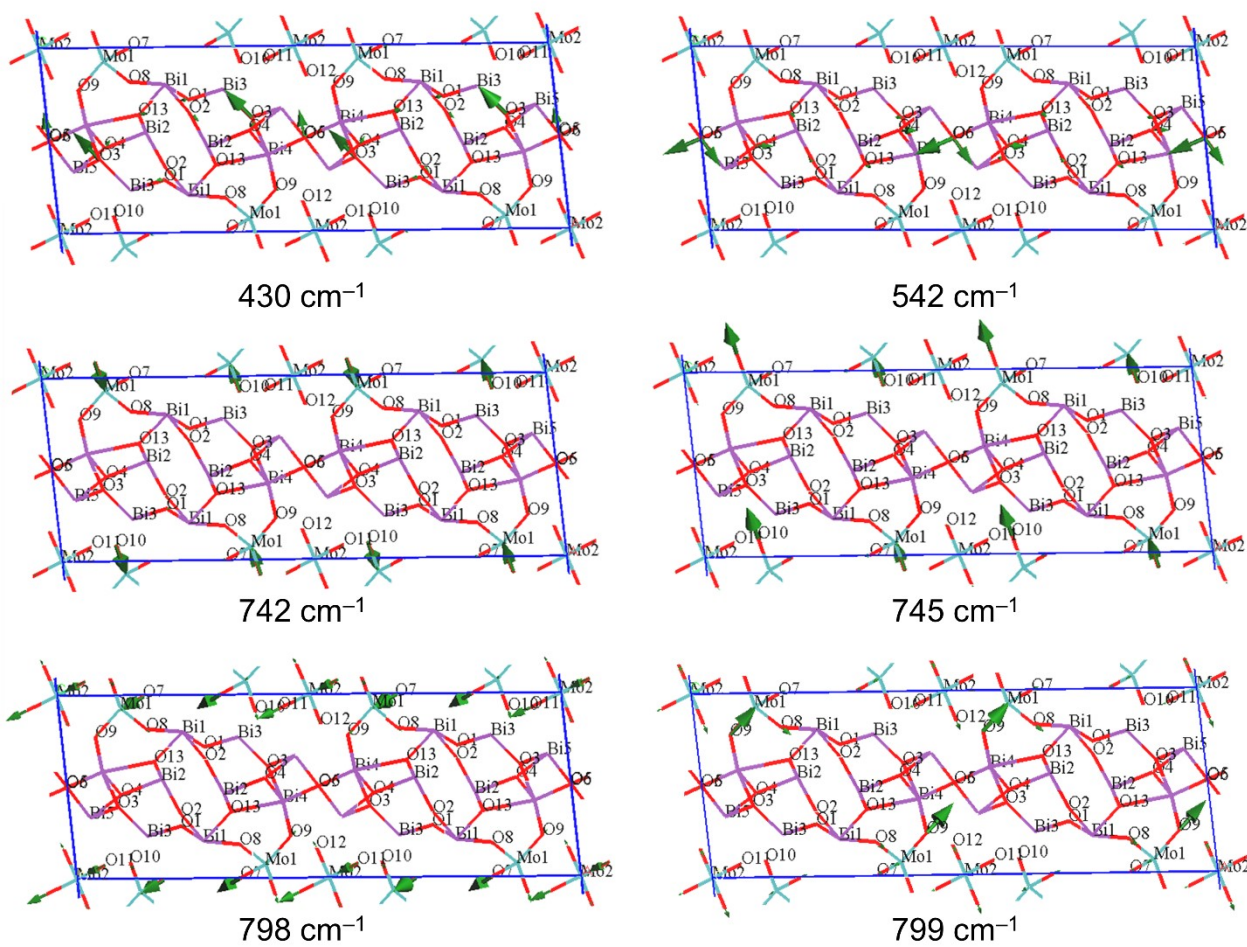


**Figure S6.** The TG-DSC curves of  $\gamma$ - $\text{Bi}_2\text{MoO}_6$  (a) and  $\text{Bi}_{10}\text{Mo}_3\text{O}_{24}$  (c). The XRD patterns of the  $\gamma$ - $\text{Bi}_2\text{MoO}_6$  (b) and  $\text{Bi}_{10}\text{Mo}_3\text{O}_{24}$  (d) samples obtained at different calcination temperatures.





**Figure S7.** The infrared vibration mode of  $\gamma\text{-Bi}_2\text{MoO}_6$ .



**Figure S8.** The infrared vibration mode of  $\text{Bi}_{10}\text{Mo}_3\text{O}_{24}$ .

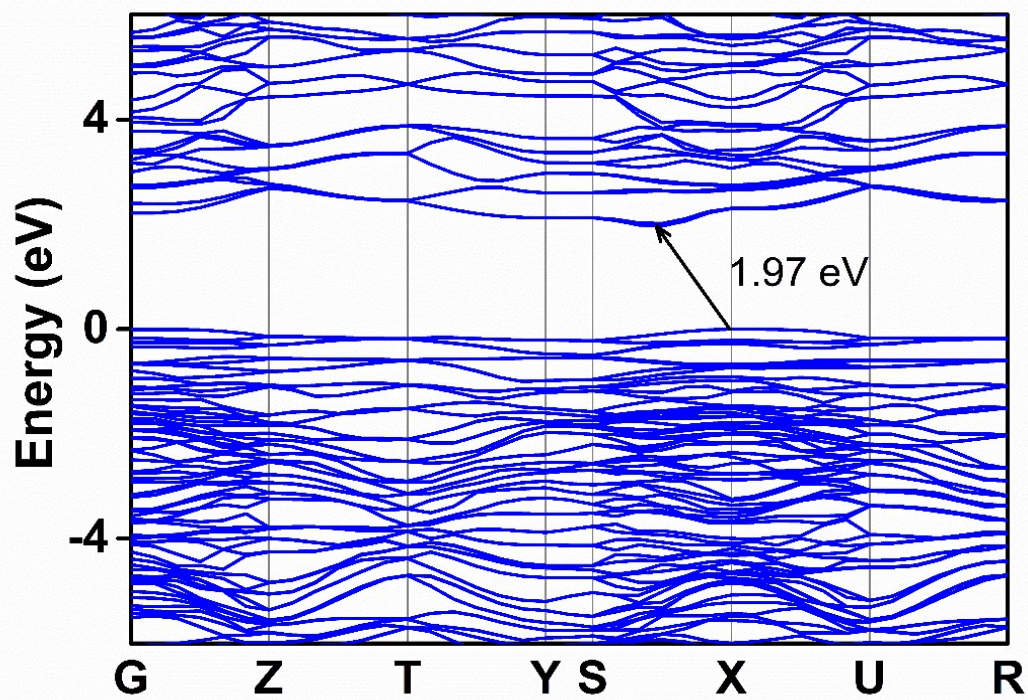
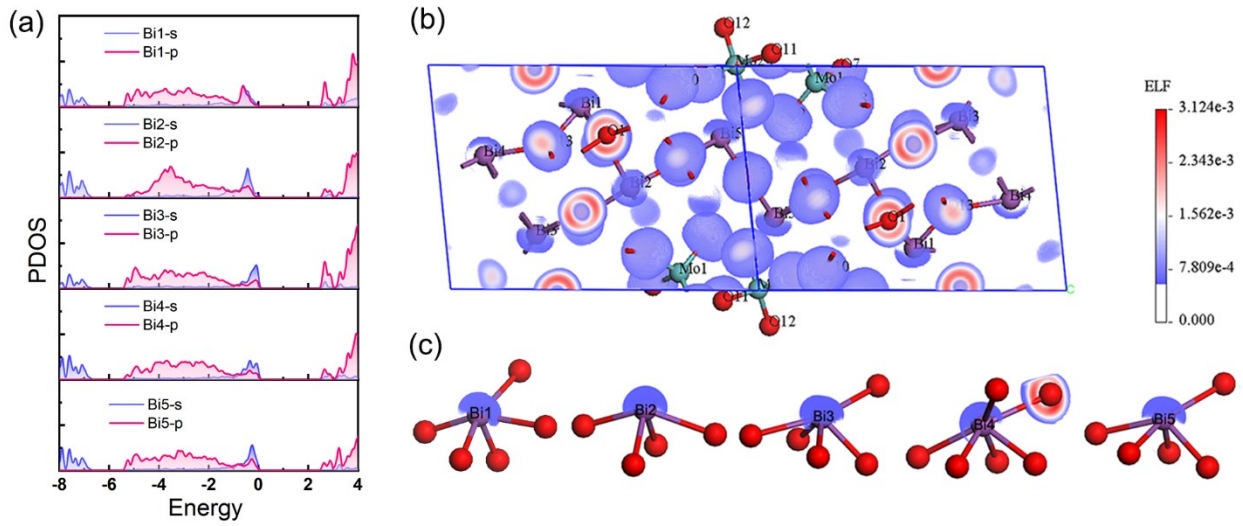
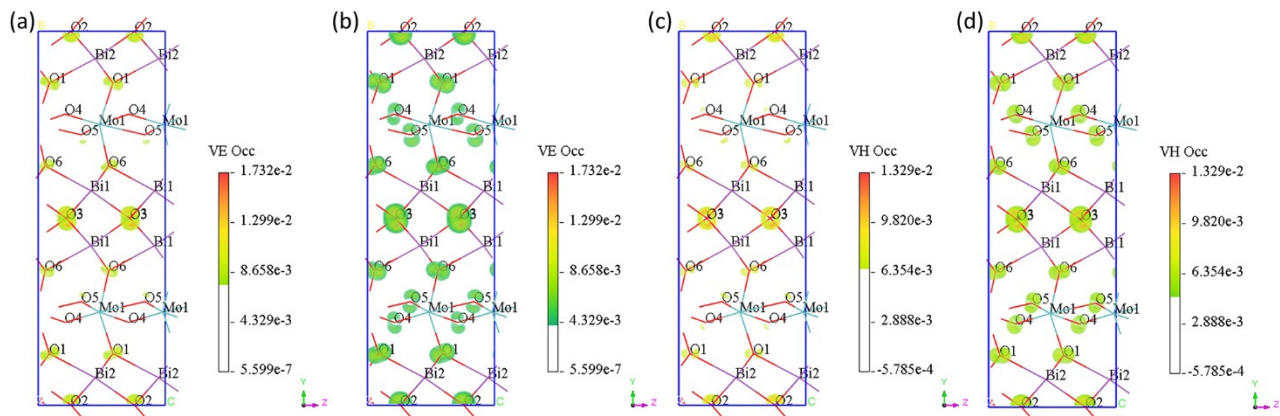


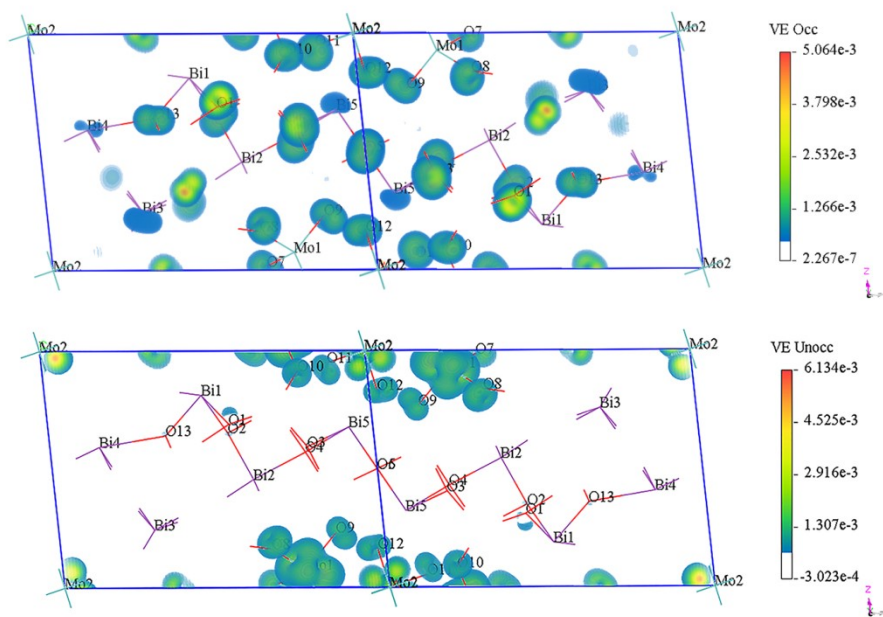
Figure S9. The bandgap of  $\gamma$ - $\text{Bi}_2\text{MoO}_6$  calculated using the HSE06 method.



**Figure S10.** Partial DOSs of Bi1-Bi5 atoms from  $\text{Bi}_{10}\text{Mo}_3\text{O}_{24}$  (a). The ELF of  $\text{Bi}_{10}\text{Mo}_3\text{O}_{24}$  (b). The ELF for five independent Bi atoms in  $\text{Bi}_{10}\text{Mo}_3\text{O}_{24}$  (c).



**Figure S11.** SHG density maps of occupied orbitals of the largest SHG coefficient  $d_{24}$  of  $\gamma$ - $\text{Bi}_2\text{MoO}_6$  in different density color scale.



**Figure S12.** SHG density maps of occupied and unoccupied orbitals of the largest SHG coefficient  $d_{22}$  for  $\text{Bi}_{10}\text{Mo}_3\text{O}_{24}$ .