

Electronic Supplementary Information for

Shooting short-wavelength nonlinear optical materials with targeted balance performances in hydroxyborates through first-principles high-throughput screening

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Figure S1 (a) Band structures by the HSE06 functional. (b) Total and partial density of states (PDOS) and band-resolved NLO coefficients. (c) SHG-weighted density of occupied and unoccupied states in virtual-electron (VE) progress of $\text{KCa}_4(\text{B}_{22}\text{O}_{32}(\text{OH})_{10}\text{Cl})\cdot 4\text{H}_2\text{O}$. Here, $\chi_{122} = 2d_{12}$.

Notes and references

Table S1 The ICSD code, crystal system, space group, and chemical formula of 222 hydroxyborates crystals with non-centrosymmetric (NCS) structures collected from ICSD.

ICSD code	Crystal system	Space group	Formula
39637	Triclinic	$P1$	$\text{KCa}_4(\text{B}_{22}\text{O}_{32})(\text{OH})_{10}\text{Cl}\cdot 4\text{H}_2\text{O}$
187776	Triclinic	$P1$	$\text{KCa}_4(\text{B}_{22}\text{O}_{32}(\text{OH})_{10}\text{Cl})\cdot 4\text{H}_2\text{O}$
172480	Triclinic	$P1$	$\text{Bi}(\text{B}_4\text{O}_6(\text{OH})_2)(\text{OH})$
76888	Triclinic	$P1$	$\text{Ca}_9\text{B}_{26}\text{O}_{34}(\text{OH})_{24}\text{Cl}_4\cdot 13\text{H}_2\text{O}$
172482	Triclinic	$P1$	$\text{Bi}_3(\text{B}_6\text{O}_{13}(\text{OH}))$
174161	Triclinic	$P1$	$\text{Ba}_3\text{Na}(\text{OH})(\text{B}_9\text{O}_{16})(\text{B}(\text{OH})_4)$
182942	Triclinic	$P1$	$\text{Tl}((\text{UO}_2)(\text{B}_5\text{O}_8)(\text{OH})\text{F})$
261299	Triclinic	$P1$	$(\text{NH}_4)_8(\text{Co}_2\text{B}_4\text{P}_8\text{O}_{30}(\text{OH})_4)$
409327	Triclinic	$P1$	$\text{Mg}_2(\text{BP}_2\text{O}_7(\text{OH})_3)$
420549	Triclinic	$P1$	$\text{Ca}_2(\text{B}_5\text{O}_8(\text{OH}))_2\text{B}(\text{OH})_3\cdot \text{H}_2\text{O}$
134988	Triclinic	$P1$	$\text{Ca}_2(\text{B}_5\text{O}_8(\text{OH}))_2(\text{B}(\text{OH})_3)\cdot \text{H}_2\text{O}$
137621	Triclinic	$P1$	$\text{Na}_{0.711}(\text{Al}_{1.315}\text{Fe}_{1.685})\text{Al}_6(\text{BO}_3)_3\text{Si}_6\text{O}_{18}\text{O}(\text{OH})_3$
137622	Triclinic	$P1$	$\text{Na}_{0.889}(\text{Al}_{2.078}\text{Fe}_{0.922})\text{Al}_6(\text{BO}_3)_3\text{Si}_6\text{O}_{18}\text{O}(\text{OH})_3$
42570	Triclinic	$P1$	$\text{Ba}_2\text{B}_{13}\text{O}_{19}(\text{OH})_5\cdot 5\text{H}_2\text{O}$
91539	Monoclinic	$P2$	$\text{Ba}_5(\text{B}_{20}\text{O}_{33}(\text{OH})_4)\cdot \text{H}_2\text{O}$
28426	Monoclinic	$P2_1$	$\text{CaB}_3\text{O}_4(\text{OH})_3\cdot \text{H}_2\text{O}$
28427	Monoclinic	$P2_1$	$\text{Ca}(\text{B}_3\text{O}_4(\text{OH})_3)\cdot \text{H}_2\text{O}$
171019	Monoclinic	$P2_1$	$\text{CaB}_8\text{O}_{11}(\text{OH})_4$
250323	Monoclinic	$P2_1$	$\text{Ca}(\text{B}_8\text{O}_{11}(\text{OH})_4)$
256908	Monoclinic	$P2_1$	$\text{Ba}_3(\text{B}_6\text{O}_{10}(\text{OH})_2)(\text{CO}_3)$
262502	Monoclinic	$P2_1$	$\text{Ba}_2(\text{B}_6\text{O}_9(\text{OH})_4)$
263504	Monoclinic	$P2_1$	$\text{CaB}_3\text{O}_4(\text{OH})_3\cdot \text{H}_2\text{O}$
263505	Monoclinic	$P2_1$	$\text{CaB}_3\text{O}_4(\text{OH})_3\cdot \text{H}_2\text{O}$
263506	Monoclinic	$P2_1$	$\text{CaB}_3\text{O}_4(\text{OH})_3\cdot \text{H}_2\text{O}$
263507	Monoclinic	$P2_1$	$\text{CaB}_3\text{O}_4(\text{OH})_3\cdot \text{H}_2\text{O}$
263508	Monoclinic	$P2_1$	$\text{CaB}_3\text{O}_4(\text{OH})_3\cdot \text{H}_2\text{O}$
263509	Monoclinic	$P2_1$	$\text{CaB}_3\text{O}_4(\text{OH})_3\cdot \text{H}_2\text{O}$
263510	Monoclinic	$P2_1$	$\text{CaB}_3\text{O}_4(\text{OH})_3\cdot \text{H}_2\text{O}$
415082	Monoclinic	$P2_1$	$\text{Ca}(\text{B}_8\text{O}_{11}(\text{OH})_4)$
432814	Monoclinic	$P2_1$	$\text{Ca}_2(\text{B}_5\text{O}_8(\text{OH}))_2(\text{B}(\text{OH})_3)\cdot \text{H}_2\text{O}$
4228	Monoclinic	$P2_1$	$\text{Sr}(\text{B}_8\text{O}_{11}(\text{OH})_4)$
20074	Monoclinic	$P2_1$	$\text{Sr}_2(\text{B}_5\text{O}_8(\text{OH}))_2(\text{B}(\text{OH})_3)\cdot \text{H}_2\text{O}$
20963	Monoclinic	$P2_1$	$\text{LiNd}(\text{BO}_3(\text{OH}))$
22336	Monoclinic	$P2_1$	$\text{Na}(\text{B}(\text{OH})_2\text{Si}_2\text{O}_5)$
28014	Monoclinic	$P2_1$	$\text{Sr}_2(\text{B}_5\text{O}_8(\text{OH}))_2(\text{B}(\text{OH})_3)\cdot \text{H}_2\text{O}$
100400	Monoclinic	$P2_1$	$(\text{NH}_4)_2(\text{B}_4\text{O}_5(\text{OH})_4)\cdot 2\text{H}_2\text{O}$
237586	Monoclinic	$P2_1$	$\text{Eu}(\text{B}_8\text{O}_{11}(\text{OH})_4)$
248128	Monoclinic	$P2_1$	$(\text{UO}_2)_2(\text{B}_9\text{O}_{14}(\text{OH})_4)$
254204	Monoclinic	$P2_1$	$\text{K}_5(\text{UO}_2)_2(\text{B}_2\text{P}_3\text{O}_{12}(\text{OH}))_2(\text{OH})\cdot 2\text{H}_2\text{O}$
49364	Monoclinic	$P2_1$	$(\text{NH}_4)_2\text{B}_4\text{O}_5(\text{OH})_4(\text{H}_2\text{O})_2$
49365	Monoclinic	$P2_1$	$(\text{NH}_4)_2\text{B}_4\text{O}_5(\text{OH})_4(\text{H}_2\text{O})_2$
17641	Monoclinic	$P2_1$	$\text{La}_3\text{B}_6\text{O}_{13}(\text{OH})$
19922	Monoclinic	$P2_1$	$\text{Ba}_2(\text{B}_5\text{O}_8(\text{OH}))_2(\text{B}(\text{OH})_3)\cdot \text{H}_2\text{O}$

ICSD code	Crystal system	Space group	Formula
141235	Monoclinic	$P2_1$	$\text{NaRb}_3\text{B}_6\text{O}_9(\text{OH})_3(\text{HCO}_3)$
145071	Monoclinic	$P2_1$	$\text{Zn}(\text{NH}_2\text{CH}_2\text{CH}_2\text{NH}_2)_2\text{Al}(\text{B}_5\text{O}_9(\text{OH}))(\text{BO}(\text{OH})_2)$
95447	Monoclinic	$C2$	$\text{Na}_2\text{Ba}_2(\text{B}_{10}\text{O}_{17}(\text{OH})_2)$
403149	Monoclinic	$C2$	$\text{Ba}_3(\text{B}_{10}\text{O}_{17}(\text{OH})_2)$
92819	Monoclinic	$C2$	$\text{Sr}_2(\text{B}_5\text{O}_9(\text{OH}))\cdot\text{H}_2\text{O}$
182000	Monoclinic	$C2$	$(\text{NH}_4)_6(\text{Mn}_3\text{B}_6\text{P}_9\text{O}_{36}(\text{OH})_3)\cdot 4\text{H}_2\text{O}$
250334	Monoclinic	$C2$	$\text{Pb}_2(\text{B}_4\text{O}_5(\text{OH})_6)\cdot\text{H}_2\text{O}$
261799	Monoclinic	$C2$	$\text{Pb}_2(\text{B}_4\text{O}_5(\text{OH})_4)(\text{OH})_2\cdot\text{H}_2\text{O}$
131283	Monoclinic	$C2$	$\text{B}_5\text{DyH}_2\text{O}_{10}$
11600	Monoclinic	Pm	$\text{Mn}_5(\text{BO}_3)_3(\text{OH})$
76661	Monoclinic	Pc	$\text{Ca}_3(\text{B}_5\text{O}_6(\text{OH})_6)(\text{OH})\text{Cl}_2\cdot 8\text{H}_2\text{O}$
89259	Monoclinic	Pc	$\text{Ca}_3(\text{B}_5\text{O}_6(\text{OH})_6)(\text{OH})\text{Cl}_2\cdot 8\text{H}_2\text{O}$
262542	Monoclinic	Pc	$\text{Ba}_3\text{B}_6\text{O}_{11}(\text{OH})_2$
154523	Monoclinic	Pc	$\text{Na}_4(\text{B}_{10}\text{O}_{16}(\text{OH})_2)\cdot 4\text{H}_2\text{O}$
26380	Monoclinic	Pc	$\text{NH}_4(\text{B}_5\text{O}_6(\text{OH})_4)\cdot 2\text{H}_2\text{O}$
110994	Monoclinic	Cm	$(\text{Cu}(\text{NH}_3)_4(\text{H}_2\text{O})_2)(\text{B}_4\text{O}_5(\text{OH})_4)\cdot 2\text{H}_2\text{O}$
124825	Monoclinic	Cm	$\text{Pr}_3\text{Mo}_4\text{B}_6\text{O}_{24}(\text{OH})_3$
2942	Monoclinic	Cc	$\text{Sr}_2(\text{B}_5\text{O}_8(\text{OH}))_2(\text{B}(\text{OH})_3)\cdot\text{H}_2\text{O}$
16921	Monoclinic	Cc	$\text{Sr}_2(\text{B}_5\text{O}_8(\text{OH}))_2(\text{B}(\text{OH})_3)\cdot\text{H}_2\text{O}$
251872	Monoclinic	Cc	$\text{La}_2(\text{CH}_3\text{CO}_2)_2(\text{B}_5\text{O}_9(\text{OH}))\cdot\text{H}_2\text{O}$
251873	Monoclinic	Cc	$\text{Ce}_2(\text{CH}_3\text{CO}_2)_2(\text{B}_5\text{O}_9(\text{OH}))\cdot\text{H}_2\text{O}$
251874	Monoclinic	Cc	$\text{Pr}_2(\text{CH}_3\text{CO}_2)_2(\text{B}_5\text{O}_9(\text{OH}))\cdot\text{H}_2\text{O}$
251875	Monoclinic	Cc	$\text{La}_2(\text{CH}_3\text{CO}_2)_2(\text{B}_5\text{O}_9(\text{OH}))$
251876	Monoclinic	Cc	$\text{Ce}_2(\text{CH}_3\text{CO}_2)_2(\text{B}_5\text{O}_9(\text{OH}))$
251877	Monoclinic	Cc	$\text{Pr}_2(\text{CH}_3\text{CO}_2)_2(\text{B}_5\text{O}_9(\text{OH}))$
260879	Monoclinic	Cc	$\text{Na}_3(\text{B}_3\text{O}_4(\text{OH})_4)$
262373	Monoclinic	Cc	$\text{Ce}(\text{B}_4\text{O}_6(\text{OH})_2)\text{Cl}$
425058	Monoclinic	Cc	$\text{Cu}_3(\text{B}_2(\text{PO}_4)_3(\text{OH})_3)$
426915	Monoclinic	Cc	$\text{Ca}_2(\text{B}_5\text{O}_9)(\text{OH})\cdot\text{H}_2\text{O}$
760166	Monoclinic	Cc	$\text{LaB}_4\text{O}_6(\text{OH})_2\text{Cl}$
760167	Monoclinic	Cc	$\text{CeB}_4\text{O}_6(\text{OH})_2\text{Cl}$
95909	Monoclinic	Cc	$\text{Pr}(\text{B}_4\text{O}_6(\text{OH})_2)\text{Cl}$
95910	Monoclinic	Cc	$\text{Nd}(\text{B}_4\text{O}_6(\text{OH})_2)\text{Cl}$
151307	Monoclinic	Cc	$(\text{Ru}_2((\text{CH}_3)\text{COO})_4(\text{H}_2\text{O})_2)(\text{BF}_4)$
182938	Monoclinic	Cc	$\text{Na}(\text{UO}_2)(\text{B}_5\text{O}_8)(\text{OH})\text{F}\cdot\text{H}_2\text{O}$
182941	Monoclinic	Cc	$\text{Rb}((\text{UO}_2)(\text{B}_5\text{O}_8)(\text{OH})\text{F})$
182943	Monoclinic	Cc	$\text{Na}((\text{NpO}_2)(\text{B}_5\text{O}_8)(\text{OH})\text{F})\cdot\text{H}_2\text{O}$
253445	Monoclinic	Cc	$\text{Co}_3(\text{BPO}_4)_2(\text{PO}_4)(\text{OH})_3$
261402	Monoclinic	Cc	$\text{Ba}_3(\text{Ge}_2\text{B}_7\text{O}_{16}(\text{OH})_2)(\text{OH})\cdot\text{H}_2\text{O}$
261422	Monoclinic	Cc	$(\text{UO}_2)(\text{B}_8\text{O}_{11}(\text{OH})_4)$
261423	Monoclinic	Cc	$(\text{NpO}_2)(\text{B}_8\text{O}_{11}(\text{OH})_4)$
261424	Monoclinic	Cc	$(\text{PuO}_2)(\text{B}_8\text{O}_{11}(\text{OH})_4)$
262913	Monoclinic	Cc	$\text{La}(\text{B}_4\text{O}_6(\text{OH})_2)\text{Cl}$
262914	Monoclinic	Cc	$\text{Ce}(\text{B}_4\text{O}_6(\text{OH})_2)\text{Cl}$
262918	Monoclinic	Cc	$\text{Pu}(\text{B}_4\text{O}_6(\text{OH})_2)\text{Cl}$

ICSD code	Crystal system	Space group	Formula
420984	Monoclinic	<i>Cc</i>	Na(UO ₂)(B ₆ O ₁₀ (OH))·2H ₂ O
420987	Monoclinic	<i>Cc</i>	PuO ₂ (B ₈ O ₁₁ (OH) ₄)
423058	Monoclinic	<i>Cc</i>	Pu(B ₄ O ₆ (OH) ₂ Cl)
124040	Monoclinic	<i>Cc</i>	Ba ₂ B ₁₀ O ₁₆ (OH) ₂ (H ₃ BO ₃)·H ₂ O
34648	Orthorhombic	<i>P2₁2₁2₁</i>	K ₂ (B ₄ O ₅ (OH) ₄)·2H ₂ O
59278	Orthorhombic	<i>P2₁2₁2₁</i>	(NH ₄) ₂ Ca(B ₄ O ₅ (OH) ₄) ₂ ·8H ₂ O
81193	Orthorhombic	<i>P2₁2₁2₁</i>	(B(C ₂ H ₆ N ₅))(OH) ₂ ·H ₂ O
155932	Orthorhombic	<i>P2₁2₁2₁</i>	(Mg ₂ (H ₂ O))(BP ₃ O ₉ (OH) ₄)
425065	Orthorhombic	<i>P2₁2₁2₁</i>	LiCu ₂ (BP ₂ O ₈ (OH) ₂)
4229	Orthorhombic	<i>P2₁2₁2₁</i>	Rb ₂ Sr(B ₄ O ₅ (OH) ₄) ₂ ·8H ₂ O
35090	Orthorhombic	<i>P2₁2₁2₁</i>	CaK ₂ (B ₄ O ₅ (OH) ₄) ₂ ·8H ₂ O
80648	Orthorhombic	<i>P2₁2₁2₁</i>	(NH ₄) ₂ Ca(B ₄ O ₅ (OH) ₄) ₂ ·8H ₂ O
93005	Orthorhombic	<i>P2₁2₁2₁</i>	K ₂ Ca(B ₄ O ₅ (OH) ₄) ₂ ·8H ₂ O
98351	Orthorhombic	<i>P2₁2₁2₁</i>	Rb ₂ Ca(B ₄ O ₅ (OH) ₄) ₂ ·8H ₂ O
99219	Orthorhombic	<i>P2₁2₁2₁</i>	Cs ₂ Ca(B ₄ O ₅ (OH) ₄) ₂ ·8H ₂ O
100670	Orthorhombic	<i>P2₁2₁2₁</i>	Tl ₂ (B ₄ O ₆ (OH) ₂)·2H ₂ O
192187	Orthorhombic	<i>P2₁2₁2₁</i>	K ₂ Ca(B ₄ O ₅ (OH) ₄) ₂ ·8H ₂ O
200950	Orthorhombic	<i>P2₁2₁2₁</i>	K ₂ Ca(B ₄ O ₅ (OH) ₄) ₂ ·8H ₂ O
263926	Orthorhombic	<i>P2₁2₁2₁</i>	RbSe ₃ B ₂ O ₉ (OH)
263927	Orthorhombic	<i>P2₁2₁2₁</i>	CsSe ₃ B ₂ O ₉ (OH)
57297	Orthorhombic	<i>P2₁2₁2₁</i>	Ba(BO ₂ (OH))
13423	Orthorhombic	<i>C222</i>	Li ₂ CsB ₇ O ₁₀ ·4H ₂ O
431106	Orthorhombic	<i>Pca2₁</i>	Na(B ₅ O ₇ (OH) ₂)·H ₂ O
250215	Orthorhombic	<i>Pnc2</i>	CaLi ₄ (B ₅ O ₈ (OH) ₂) ₂
36431	Orthorhombic	<i>Pnc2</i>	Li ₃ (B ₅ O ₈ (OH) ₂)
413627	Orthorhombic	<i>Pmn2₁</i>	K ₇ ((BO ₃)Mn(B ₁₂ O ₁₈ (OH) ₆))·H ₂ O
70514	Orthorhombic	<i>Pmn2₁</i>	K ₇ ((BO ₃)Co(B ₁₂ O ₁₈ (OH) ₆))·H ₂ O
145793	Orthorhombic	<i>Pmn2₁</i>	Tb ₃ B ₁₀ O ₁₇ (OH) ₅
22192	Orthorhombic	<i>Pna2₁</i>	CaB ₃ O ₅ (OH)
23880	Orthorhombic	<i>Pna2₁</i>	CaB ₃ O ₅ (OH)
1973	Orthorhombic	<i>Pna2₁</i>	(Na(H ₂ O)) ₂ (B ₅ O ₈ (OH))
34700	Orthorhombic	<i>Pna2₁</i>	K ₂ (B ₅ O ₈ (OH))·2H ₂ O
59277	Orthorhombic	<i>Pna2₁</i>	K ₂ Sr(B ₄ O ₅ (OH) ₄) ₂ ·10H ₂ O
249876	Orthorhombic	<i>Pna2₁</i>	Na ₂ B ₅ O ₈ (OH)·2H ₂ O
252381	Orthorhombic	<i>Pna2₁</i>	CaB ₃ O ₅ (OH)
426601	Orthorhombic	<i>Pna2₁</i>	Mg(B ₆ O ₉ (OH) ₂)·4H ₂ O
4220	Orthorhombic	<i>Pna2₁</i>	K ₃ (B ₃ O ₄ (OH) ₄)·2H ₂ O
4221	Orthorhombic	<i>Pna2₁</i>	Rb ₃ (B ₃ O ₄ (OH) ₄)·2H ₂ O
200266	Orthorhombic	<i>Pna2₁</i>	K ₃ (B ₃ O ₄ (OH) ₄)·2H ₂ O
408211	Orthorhombic	<i>Pna2₁</i>	Na ₂ (BP ₂ O ₇ (OH))
133088	Orthorhombic	<i>Pna2₁</i>	KHC ₂ O ₄ B(OH) ₃
117561	Orthorhombic	<i>Pna2₁</i>	La ₂ B ₃ O ₄ (OH) ₃ (SO ₄) ₂
253012	Orthorhombic	<i>Cmc2₁</i>	K ₃ B ₃ O ₄ (OH) ₄ ·2H ₂ O
138088	Orthorhombic	<i>Cmc2₁</i>	Na ₈ Li ₂ (B ₆ O ₁₀) ₄ (B(OH) ₃) ₂ (OH) ₂
113334	Orthorhombic	<i>Cmc2₁</i>	(NH ₄) ₂ (B ₄ O ₅ (OH) ₄)·2H ₂ O

ICSD code	Crystal system	Space group	Formula
63014	Orthorhombic	<i>Amm2</i>	Tl ₄ Cu(Cu ₂ B ₁₈ O ₂₈ (OH) ₈)·10H ₂ O
241953	Orthorhombic	<i>Ama2</i>	K((UO ₂)B ₆ O ₁₀ (OH))
6292	Orthorhombic	<i>Aba2</i>	K(B ₅ O ₆ (OH) ₄)·2H ₂ O
29406	Orthorhombic	<i>Aba2</i>	RbB ₅ O ₆ (OH) ₄ ·2H ₂ O
90001	Orthorhombic	<i>Aba2</i>	(NH ₄)(B ₅ O ₆ (OH) ₄)·2H ₂ O
410811	Orthorhombic	<i>Aba2</i>	(NH ₄)(B ₅ O ₆ (OH) ₄)·2H ₂ O
21332	Orthorhombic	<i>Aba2</i>	LiNaRbB ₅ O ₈ (OH) ₂
4481	Orthorhombic	<i>Fdd2</i>	K ₃ B ₅ O ₈ (OH) ₂
425727	Orthorhombic	<i>Fdd2</i>	Ba ₃ Al ₂ (B ₃ O ₆ (OH)) ₂ (B ₄ O ₇ (OH) ₂)
425867	Orthorhombic	<i>Fdd2</i>	Ba ₃ Ga ₂ (B ₃ O ₆ (OH)) ₂ (B ₄ O ₇ (OH) ₂)
264389	Orthorhombic	<i>Fdd2</i>	InB ₆ O ₉ (OH) ₃
20662	Tetragonal	<i>P4₂</i>	Mg(B ₂ O(OH) ₆)
24920	Tetragonal	<i>P4₂</i>	Mg(B ₂ O(OH) ₆)
4222	Tetragonal	<i>$\bar{4}$</i>	Cs(B(OH) ₄)·2H ₂ O
27527	Tetragonal	<i>$\bar{4}$</i>	Ca ₂ BAsO ₄ (OH) ₄
142127	Tetragonal	<i>$\bar{4}$</i>	H ₂ Na ₂ K ₂ (OCu ₄ B ₂₀ O ₃₂ (OH) ₈)·21H ₂ O
142128	Tetragonal	<i>$\bar{4}$</i>	H ₂ Rb _{1.6} K _{2.4} (OCu ₄ B ₂₀ O ₃₂ (OH) ₈)·15H ₂ O
20155	Tetragonal	<i>P4₁2₁2</i>	Li ₃ (B ₅ O ₈ (OH) ₂)
20173	Tetragonal	<i>P4₁2₁2</i>	Li ₃ (B ₅ O ₈ (OH) ₂)
418166	Tetragonal	<i>P4₃2₁2</i>	Li ₃ (B ₅ O ₈ (OH) ₂)
34580	Tetragonal	<i>P$\bar{4}$₂1c</i>	K ₆ Al ₄ Si ₆ BH ₄ O ₂₄ Cl
79472	Trigonal	<i>P3</i>	(Li(H ₂ O) ₄)(B(OH) ₄)·2H ₂ O
430533	Trigonal	<i>P3</i>	Li(H ₂ O) ₄ B(OH) ₄ ·2H ₂ O
431212	Trigonal	<i>P3₂</i>	Pb ₆ B ₁₂ O ₂₁ (OH) ₆
240324	Trigonal	<i>P3₁21</i>	Co(BPO ₄ (OH) ₂)
416089	Trigonal	<i>P3₁21</i>	Mg(BPO ₄ (OH) ₂)
416129	Trigonal	<i>P3₁21</i>	Ni(BPO ₄ (OH) ₂)
431536	Trigonal	<i>P3₁21</i>	Ba ₂ (B ₄ O ₇ (OH) ₂)
240322	Trigonal	<i>P3₂21</i>	Mn(BPO ₄ (OH) ₂)
240323	Trigonal	<i>P3₂21</i>	Fe(BPO ₄ (OH) ₂)
10266	Trigonal	<i>R32</i>	Na ₂ (B ₄ O ₅ (OH) ₄)·3H ₂ O
70998	Trigonal	<i>R32</i>	NaRb ₆ (B ₄ O ₅ (OH) ₄) ₃ (BO ₂)
70999	Trigonal	<i>R32</i>	NaRb ₆ (B ₄ O ₅ (OH) ₄) ₃ (BO ₂)
4493	Trigonal	<i>P31c</i>	Pb ₃ (OH)(B ₉ O ₁₆)(B(OH) ₃)
4494	Trigonal	<i>P31c</i>	Ba ₃ (OH)(B ₉ O ₁₆)(B(OH) ₃)
428677	Trigonal	<i>P31c</i>	LiBa ₃ (OH)(B ₉ O ₁₆)(B(OH) ₄)
94525	Trigonal	<i>P31c</i>	Pb ₃ (OH)(B ₉ O ₁₆)(B(OH) ₃)
261808	Trigonal	<i>P31c</i>	Pb ₃ (OH)(B ₉ O ₁₆)(B(OH) ₃)
42341	Trigonal	<i>R3m</i>	NaAl ₉ (BO ₃) ₃ (Si ₆ O ₂₁)(OH)
136829	Trigonal	<i>R3m</i>	(Na _{0.479} Li _{0.024})Al _{2.976} Al ₆ (Si _{5.676} B _{0.324} O ₁₈)(BO ₃) ₃ (OH) ₃ O
136830	Trigonal	<i>R3m</i>	(Na _{0.617} Li _{0.165})Al _{2.835} Al ₆ (Si _{5.718} B _{0.282} O ₁₈)(BO ₃) ₃ (OH) ₃ O
112290	Trigonal	<i>R3m</i>	(Na _{0.44} Ca _{0.56})(Mg _{1.56} Fe _{1.55} Al _{5.89})(Si ₆ O ₁₈)(BO ₃) ₃ (OH) ₃ O
112291	Trigonal	<i>R3m</i>	(Na _{0.095} Ca _{0.905})(Mg _{2.30} Fe _{0.83} Al _{5.86})(Si ₆ O ₁₈)(BO ₃) ₃ (OH) ₃ O
137133	Trigonal	<i>R3m</i>	Na _{0.768} (Mn _{1.032} Al _{1.878} Fe _{0.09})Al ₆ (Si ₆ O ₁₈)(BO ₃) ₃ (OH) ₃ O
127049	Trigonal	<i>R3m</i>	Na _{0.824} K _{0.176} Fe ₃ (Fe _{2.397} Mg _{0.681} Al _{2.922})(Si ₆ O ₁₈)(BO ₃) ₃ (OH) ₃ O

ICSD code	Crystal system	Space group	Formula
37833	Trigonal	<i>R3m</i>	$\text{Na}_{0.42}(\text{Mn}_{1.39}\text{Fe}_{0.16}\text{Mg}_{0.01}\text{Al}_{1.14}\text{Fe}_{0.01}\text{Li}_{0.28}\text{Ti}_{0.01})\text{Al}_6((\text{Si}_{5.99}\text{Al}_{0.01})\text{O}_{18})$ $(\text{BO}_3)_3(\text{OH})_3((\text{OH})_{0.65}\text{F}_{0.03}\text{O}_{0.32})$
37834	Trigonal	<i>R3m</i>	$\text{Na}_{0.49}\text{Mn}_{0.49}(\text{Mn}_{0.90}\text{Fe}_{0.50}\text{Al}_{1.36}\text{Fe}_{0.04}\text{Li}_{0.17}\text{Zn}_{0.04})(\text{Al}_{5.91}\text{Mn}_{0.09})$ $((\text{Si}_{5.75}\text{B}_{0.25})\text{O}_{18})(\text{BO}_3)_3(\text{OH})_3((\text{OH})_{0.35}\text{F}_{0.17}\text{O}_{0.48})$
138478	Trigonal	<i>R3m</i>	$\text{Ca}_{0.589}\text{Na}_{0.354}\text{Mg}_{1.196}\text{Fe}_{0.912}\text{Al}_{0.892}(\text{Al}_5\text{Mg})(\text{Si}_6\text{O}_{18})$ $(\text{BO}_3)_3(\text{OH})_3(\text{OH})_{0.945}\text{F}_{0.055}$
112348	Trigonal	<i>R3m</i>	$\text{Na}_{0.854}(\text{Al}_{1.124})_3(\text{Al}_{1.047})_6\text{Si}_6\text{B}_3\text{O}_{27}(\text{OH})_3(\text{F}_{0.58}(\text{OH})_{0.42})$
112349	Trigonal	<i>R3m</i>	$\text{Na}_{0.854}(\text{Al}_{1.173})_3(\text{Al}_{1.022})_6\text{Si}_6\text{B}_3\text{O}_{27}(\text{OH})_3(\text{F}_{0.58}(\text{OH})_{0.42})$
112350	Trigonal	<i>R3m</i>	$\text{Na}_{0.854}(\text{Al}_{1.169})_3(\text{Al}_{1.024})_6\text{Si}_6\text{B}_3\text{O}_{27}(\text{OH})_3(\text{F}_{0.58}(\text{OH})_{0.42})$
112351	Trigonal	<i>R3m</i>	$\text{Na}_{0.854}(\text{Al}_{1.175})_3(\text{Al}_{1.021})_6\text{Si}_6\text{B}_3\text{O}_{27}(\text{OH})_3(\text{F}_{0.58}(\text{OH})_{0.42})$
112352	Trigonal	<i>R3m</i>	$\text{Na}_{0.854}(\text{Al}_{1.176})_3(\text{Al}_{1.021})_6\text{Si}_6\text{B}_3\text{O}_{27}(\text{OH})_3(\text{F}_{0.58}(\text{OH})_{0.42})$
112353	Trigonal	<i>R3m</i>	$\text{Na}_{0.854}(\text{Al}_{1.181})_3(\text{Al}_{1.018})_6\text{Si}_6\text{B}_3\text{O}_{27}(\text{OH})_3(\text{F}_{0.58}(\text{OH})_{0.42})$
112354	Trigonal	<i>R3m</i>	$\text{Na}_{0.854}(\text{Al}_{1.184})_3(\text{Al}_{1.016})_6\text{Si}_6\text{B}_3\text{O}_{27}(\text{OH})_3(\text{F}_{0.58}(\text{OH})_{0.42})$
112355	Trigonal	<i>R3m</i>	$\text{Na}_{0.854}(\text{Al}_{1.185})_3(\text{Al}_{1.016})_6\text{Si}_6\text{B}_3\text{O}_{27}(\text{OH})_3(\text{F}_{0.58}(\text{OH})_{0.42})$
112356	Trigonal	<i>R3m</i>	$\text{Na}_{0.854}(\text{Al}_{1.180})_3(\text{Al}_{1.019})_6\text{Si}_6\text{B}_3\text{O}_{27}(\text{OH})_3(\text{F}_{0.58}(\text{OH})_{0.42})$
112357	Trigonal	<i>R3m</i>	$\text{Na}_{0.854}(\text{Al}_{1.186})_3(\text{Al}_{1.015})_6\text{Si}_6\text{B}_3\text{O}_{27}(\text{OH})_3(\text{F}_{0.58}(\text{OH})_{0.42})$
112358	Trigonal	<i>R3m</i>	$\text{Na}_{0.854}(\text{Al}_{1.183})_3(\text{Al}_{1.017})_6\text{Si}_6\text{B}_3\text{O}_{27}(\text{OH})_3(\text{F}_{0.58}(\text{OH})_{0.42})$
112359	Trigonal	<i>R3m</i>	$\text{Na}_{0.854}(\text{Al}_{1.183})_3(\text{Al}_{1.017})_6\text{Si}_6\text{B}_3\text{O}_{27}(\text{OH})_3(\text{F}_{0.58}(\text{OH})_{0.42})$
112360	Trigonal	<i>R3m</i>	$\text{Na}_{0.854}(\text{Al}_{1.176})_3(\text{Al}_{1.021})_6\text{Si}_6\text{B}_3\text{O}_{27}(\text{OH})_3(\text{F}_{0.58}(\text{OH})_{0.42})$
112361	Trigonal	<i>R3m</i>	$\text{Na}_{0.854}(\text{Al}_{1.175})_3(\text{Al}_{1.021})_6\text{Si}_6\text{B}_3\text{O}_{27}(\text{OH})_3(\text{F}_{0.58}(\text{OH})_{0.42})$
112362	Trigonal	<i>R3m</i>	$\text{Na}_{0.854}(\text{Al}_{1.169})_3(\text{Al}_{1.024})_6\text{Si}_6\text{B}_3\text{O}_{27}(\text{OH})_3(\text{F}_{0.58}(\text{OH})_{0.42})$
112363	Trigonal	<i>R3m</i>	$\text{Na}_{0.854}(\text{Al}_{1.127})_3(\text{Al}_{1.045})_6\text{Si}_6\text{B}_3\text{O}_{27}(\text{OH})_3(\text{F}_{0.58}(\text{OH})_{0.42})$
112364	Trigonal	<i>R3m</i>	$\text{Na}_{0.854}(\text{Al}_{1.109})_3(\text{Al}_{1.054})_6\text{Si}_6\text{B}_3\text{O}_{27}(\text{OH})_3(\text{F}_{0.58}(\text{OH})_{0.42})$
112365	Trigonal	<i>R3m</i>	$\text{Na}_{0.854}(\text{Al}_{1.109})_3(\text{Al}_{1.054})_6\text{Si}_6\text{B}_3\text{O}_{27}(\text{OH})_3(\text{F}_{0.58}(\text{OH})_{0.42})$
143071	Trigonal	<i>R3m</i>	$(\text{Na}_{0.40}\text{Ca}_{0.26})(\text{Al}_{2.04}\text{Li}_{0.78}\text{Mn}_{0.18})\text{Al}_6(\text{Si}_{5.5}\text{B}_{0.5})\text{O}_{18}$ $(\text{BO}_3)_3(\text{OH})_3((\text{OH})_{0.38}\text{F}_{0.13}\text{O}_{0.49})$
120219	Trigonal	<i>R3m</i>	$\text{Na}_{0.781}(\text{Fe}_{0.697}\text{Al}_{0.303})_3(\text{Al}_{0.912}\text{Fe}_{0.088})_6(\text{Si}_6\text{O}_{18})$ $(\text{BO}_3)_3(\text{OH})_3((\text{OH})_{0.591}\text{F}_{0.409})$
125271	Trigonal	<i>R3m</i>	$\text{Na}_{0.790}\text{Mg}_{1.329}\text{Fe}_{2.025}\text{Ca}_{0.210}\text{Al}_{5.646}(\text{Si}_6\text{O}_{18})(\text{BO}_3)_3(\text{OH})_3\text{O}$
125066	Trigonal	<i>R3m</i>	$(\text{Ca}_{0.56}\text{Na}_{0.44})(\text{Mg}_{1.515}\text{Fe}_{1.485})\text{Al}_6(\text{BO}_3)_3(\text{Si}_6\text{O}_{18})(\text{OH})_3(\text{O}_{0.79}\text{F}_{0.21})$
125067	Trigonal	<i>R3m</i>	$(\text{Na}_{0.95}\text{Ca}_{0.05})(\text{Mg}_{1.71}\text{Fe}_{1.29})\text{Al}_6(\text{Si}_6\text{O}_{18})(\text{BO}_3)_3(\text{OH})_3\text{O}$
127050	Trigonal	<i>R3m</i>	$\text{Na}_{0.767}\text{K}_{0.233}\text{Fe}_3(\text{Fe}_{3.786}\text{Mg}_{0.336}\text{Al}_{1.878})(\text{Si}_6\text{O}_{18})(\text{BO}_3)_3(\text{OH})_3\text{O}$
127051	Trigonal	<i>R3m</i>	$\text{Na}_{0.90}\text{K}_{0.10}\text{Fe}_3(\text{Fe}_{3.54}\text{Mg}_{0.402}\text{Al}_{2.058})(\text{Si}_6\text{O}_{18})(\text{BO}_3)_3(\text{OH})_3\text{O}$
127052	Trigonal	<i>R3m</i>	$\text{Na}_{0.85}\text{K}_{0.15}\text{Fe}_3(\text{Fe}_{3.41}\text{Mg}_{0.43}\text{Al}_{2.17})(\text{Si}_6\text{O}_{18})(\text{BO}_3)_3(\text{OH})_3\text{O}$
127053	Trigonal	<i>R3m</i>	$\text{Na}_{0.78}\text{K}_{0.22}\text{Fe}_3(\text{Fe}_{4.002}\text{Mg}_{0.276}\text{Al}_{1.722})(\text{Si}_6\text{O}_{18})(\text{BO}_3)_3(\text{OH})_3\text{O}$
421260	Trigonal	<i>R3c</i>	$\text{Y}(\text{B}_2\text{O}_3(\text{OH}))_3$
250161	Trigonal	<i>R3c</i>	$\text{Ho}(\text{B}_6\text{O}_9(\text{OH})_3)$
250162	Trigonal	<i>R3c</i>	$\text{Gd}(\text{B}_6\text{O}_9(\text{OH})_3)$
112337	Hexagonal	<i>P6₃</i>	$\text{Ca}_3(\text{Si}_{0.64}\text{Al}_{0.36})((\text{B}(\text{OH})_4)_{0.64}(\text{CO}_3)_{1.08}(\text{AsO}_3)_{0.28})(\text{OH})_6 \cdot 12\text{H}_2\text{O}$
50539	Hexagonal	<i>P6₃cm</i>	$\text{Pb}_5(\text{B}_3\text{O}_8(\text{OH})_3) \cdot \text{H}_2\text{O}$
238716	Hexagonal	<i>P6₂m</i>	$\text{KGd}(\text{B}_6\text{O}_{10}(\text{OH})_2)$
432932	Hexagonal	<i>P6₂m</i>	$\text{Ni}_3\text{B}_{18}\text{O}_{28}(\text{OH})_4 \cdot 4\text{H}_2\text{O}$
403324	Hexagonal	<i>P6₂c</i>	$\text{K}_9(\text{B}_4\text{O}_5(\text{OH})_4)_3(\text{CO}_3)\text{Br} \cdot 7\text{H}_2\text{O}$
403325	Hexagonal	<i>P6₂c</i>	$\text{K}_9(\text{B}_4\text{O}_5(\text{OH})_4)_3(\text{CO}_3)\text{Cl} \cdot 7\text{H}_2\text{O}$
425207	Hexagonal	<i>P6₂c</i>	$\text{Li}_3(\text{B}_8\text{O}_{12}(\text{OH})_3)$

ICSD code	Crystal system	Space group	Formula
429622	Hexagonal	$P\bar{6}2c$	$K_9(B_4O_5(OH)_4)_3(CO_3)(BH_4) \cdot 7H_2O$
14601	Hexagonal	$P\bar{6}2c$	$NaK_{15}(B_4O_5(OH)_4)_6(NO_2)_2(CO_3) \cdot 7H_2O$
56497	Cubic	$P\bar{4}3m$	$Na_8(Al_6Si_6O_{24})(B(OH)_4)_2$
428956	Cubic	$F\bar{4}3c$	$Na_4Ga_3B_4O_{12}(OH)$

Table S2 The basic information of hydroxyborates with 0D isolated anionic clusters.

No.	ICSD code	Compounds	(A+OH)/B ratio	Anionic units	FBB units	Anionic cluster
1	100400	$(\text{NH}_4)_2(\text{B}_4\text{O}_5(\text{OH})_4) \cdot 2\text{H}_2\text{O}$	1.5	$[\text{BO}_2(\text{OH})]$, $[\text{BO}_3(\text{OH})]$	$[\text{B}_4\text{O}_5(\text{OH})_4]$	$[\text{B}_4\text{O}_5(\text{OH})_4]$
2	49364	$(\text{NH}_4)_2\text{B}_4\text{O}_5(\text{OH})_4 \cdot 2\text{H}_2\text{O}$	1.5	$[\text{BO}_2(\text{OH})]$, $[\text{BO}_3(\text{OH})]$	$[\text{B}_4\text{O}_5(\text{OH})_4]$	$[\text{B}_4\text{O}_5(\text{OH})_4]$
3	49365	$(\text{NH}_4)_2\text{B}_4\text{O}_5(\text{OH})_4 \cdot 2\text{H}_2\text{O}$	1.5	$[\text{BO}_2(\text{OH})]$, $[\text{BO}_3(\text{OH})]$	$[\text{B}_4\text{O}_5(\text{OH})_4]$	$[\text{B}_4\text{O}_5(\text{OH})_4]$
4	26380	$\text{NH}_4(\text{B}_5\text{O}_6(\text{OH})_4) \cdot 2\text{H}_2\text{O}$	1	$[\text{BO}_2(\text{OH})]$, $[\text{BO}_4]$	$[\text{B}_5\text{O}_6(\text{OH})_4]$	$[\text{B}_5\text{O}_6(\text{OH})_4]$
5	260879	$\text{Na}_3(\text{B}_3\text{O}_4(\text{OH})_4)$	2.333	$[\text{BO}_3]$, $[\text{BO}_2(\text{OH})_2]$	$[\text{B}_3\text{O}_4(\text{OH})_4]$	$[\text{B}_3\text{O}_4(\text{OH})_4]$
6	34648	$\text{K}_2(\text{B}_4\text{O}_5(\text{OH})_4) \cdot 2\text{H}_2\text{O}$	1.5	$[\text{BO}_2(\text{OH})]$, $[\text{BO}_4]$, $[\text{BO}_3(\text{OH})]$	$[\text{B}_4\text{O}_5(\text{OH})_4]$	$[\text{B}_4\text{O}_5(\text{OH})_4]$
7	57297	$\text{Ba}(\text{BO}_2(\text{OH}))$	2	$[\text{BO}_2(\text{OH})]$	$[\text{BO}_2(\text{OH})]$	$[\text{BO}_2(\text{OH})]$
8	253012	$\text{K}_3\text{B}_3\text{O}_4(\text{OH})_4 \cdot 2\text{H}_2\text{O}$	2.333	$[\text{BO}_3]$, $[\text{BO}_2(\text{OH})_2]$	$[\text{B}_3\text{O}_4(\text{OH})_4]$	$[\text{B}_3\text{O}_4(\text{OH})_4]$
9	113334	$(\text{NH}_4)_2(\text{B}_4\text{O}_5(\text{OH})_4) \cdot 2\text{H}_2\text{O}$	1.5	$[\text{BO}_2(\text{OH})]$, $[\text{BO}_3(\text{OH})]$	$[\text{B}_4\text{O}_5(\text{OH})_4]$	$[\text{B}_4\text{O}_5(\text{OH})_4]$
10	6292	$\text{K}(\text{B}_5\text{O}_6(\text{OH})_4) \cdot 2\text{H}_2\text{O}$	1	$[\text{BO}_2(\text{OH})]$, $[\text{BO}_4]$	$[\text{B}_5\text{O}_6(\text{OH})_4]$	$[\text{B}_5\text{O}_6(\text{OH})_4]$
11	29406	$\text{RbB}_5\text{O}_6(\text{OH})_4 \cdot 2\text{H}_2\text{O}$	1	$[\text{BO}_2(\text{OH})]$, $[\text{BO}_4]$	$[\text{B}_5\text{O}_6(\text{OH})_4]$	$[\text{B}_5\text{O}_6(\text{OH})_4]$
12	90001	$(\text{NH}_4)(\text{B}_5\text{O}_6(\text{OH})_4) \cdot 2\text{H}_2\text{O}$	1	$[\text{BO}_2(\text{OH})]$, $[\text{BO}_4]$	$[\text{B}_5\text{O}_6(\text{OH})_4]$	$[\text{B}_5\text{O}_6(\text{OH})_4]$
13	410811	$(\text{NH}_4)(\text{B}_5\text{O}_6(\text{OH})_4) \cdot 2\text{H}_2\text{O}$	1	$[\text{BO}_2(\text{OH})]$, $[\text{BO}_4]$	$[\text{B}_5\text{O}_6(\text{OH})_4]$	$[\text{B}_5\text{O}_6(\text{OH})_4]$
14	4481	$\text{K}_3\text{B}_5\text{O}_8(\text{OH})_2$	1	$[\text{BO}_3]$, $[\text{BO}_2(\text{OH})]$, $[\text{BO}_4]$	$[\text{B}_5\text{O}_8(\text{OH})_2]$	$[\text{B}_5\text{O}_8(\text{OH})_2]$
15	20662	$\text{Mg}(\text{B}_2\text{O}(\text{OH})_6)$	3.5	$[\text{BO}(\text{OH})_3]$	$[\text{B}_2\text{O}(\text{OH})_6]$	$[\text{B}_2\text{O}(\text{OH})_6]$
16	24920	$\text{Mg}(\text{B}_2\text{O}(\text{OH})_6)$	3.5	$[\text{BO}(\text{OH})_3]$	$[\text{B}_2\text{O}(\text{OH})_6]$	$[\text{B}_2\text{O}(\text{OH})_6]$
17	10266	$\text{Na}_2(\text{B}_4\text{O}_5(\text{OH})_4) \cdot 3\text{H}_2\text{O}$	1.5	$[\text{BO}_2(\text{OH})]$, $[\text{BO}_3(\text{OH})]$	$[\text{B}_4\text{O}_5(\text{OH})_4]$	$[\text{B}_4\text{O}_5(\text{OH})_4]$
18	70998	$\text{NaRb}_6(\text{B}_4\text{O}_5(\text{OH})_4)_3 (\text{BO}_2)$	1.462	$[\text{BO}_2]$, $[\text{BO}_2(\text{OH})]$, $[\text{BO}_3(\text{OH})]$	$[\text{B}_4\text{O}_5(\text{OH})_4]$, $[\text{BO}_2]$	$[\text{B}_4\text{O}_5(\text{OH})_4]$, $[\text{BO}_2]$
19	70999	$\text{NaRb}_6(\text{B}_4\text{O}_5(\text{OH})_4)_3 (\text{BO}_2)$	1.462	$[\text{BO}_2]$, $[\text{BO}_2(\text{OH})]$, $[\text{BO}_3(\text{OH})]$	$[\text{B}_4\text{O}_5(\text{OH})_4]$, $[\text{BO}_2]$	$[\text{B}_4\text{O}_5(\text{OH})_4]$, $[\text{BO}_2]$

Table S3 The basic information of hydroxyborates with 1D infinite anionic chains.

No.	ICSD code	Compounds	(A+OH)/B ratio	Anionic units	FBB units	Anionic chain
1	172480	Bi(B ₄ O ₆ (OH) ₂)(OH)	0.75	[BO ₃], [BO ₂ (OH)], [BO ₄]	[B ₄ O ₇ (OH) ₂]	¹ [B ₄ O ₆ (OH) ₂] _∞
2	28426	CaB ₃ O ₄ (OH) ₃ ·H ₂ O	1.333	[BO ₃], [BO ₃ (OH)], [BO ₂ (OH) ₂]	[B ₃ O ₅ (OH) ₃]	¹ [B ₃ O ₄ (OH) ₃] _∞
3	28427	CaB ₃ O ₄ (OH) ₃ ·H ₂ O	1.333	[BO ₃], [BO ₃ (OH)], [BO ₂ (OH) ₂]	[B ₃ O ₅ (OH) ₃]	¹ [B ₃ O ₄ (OH) ₃] _∞
4	141235	NaRb ₃ B ₆ O ₉ (OH) ₃ (HCO ₃)	1.167	[BO ₂ (OH)], [BO ₄]	[B ₆ O ₁₁ (OH) ₃]	¹ [B ₆ O ₉ (OH) ₃] _∞
5	262542	Ba ₃ B ₆ O ₁₁ (OH) ₂	0.833	[BO ₃], [BO ₄], [BO ₂ (OH) ₂]	[B ₆ O ₁₃ (OH) ₂]	¹ [B ₆ O ₁₁ (OH) ₂] _∞
6	431106	Na(B ₅ O ₇ (OH) ₂)·H ₂ O	0.6	[BO ₃], [BO ₂ (OH)], [BO ₄]	[B ₅ O ₈ (OH) ₂]	¹ [B ₅ O ₇ (OH) ₂] _∞
7	431536	Ba ₂ (B ₄ O ₇ (OH) ₂)	1	[BO ₃], [BO ₄], [BO ₂ (OH) ₂]	[B ₄ O ₉ (OH) ₂]	¹ [B ₄ O ₇ (OH) ₂] _∞

Table S4 The basic information of hydroxyborates with 2D anionic layered configurations.

No.	ICSD code	Compounds	(A+OH)/B ratio	Anionic units	FBB units	Anionic layered configuration
1	39637	KCa ₄ (B ₂₂ O ₃₂)(OH) ₁₀ Cl ·4H ₂ O	0.682	[BO ₃], [BO ₂ (OH)], [B(OH) ₃], [BO ₄]	[B(OH) ₃], [B ₅ O ₁₀ (OH)]	[B(OH) ₃], ² [B ₅ O ₈ (OH)] _∞
2	187776	KCa ₄ (B ₂₂ O ₃₂ (OH) ₁₀ Cl) ·4H ₂ O	0.682	[BO ₃], [BO ₂ (OH)], [B(OH) ₃], [BO ₄]	[B(OH) ₃], [B ₅ O ₁₀ (OH)]	[B(OH) ₃], ² [B ₅ O ₈ (OH)] _∞
3	420549	Ca ₂ (B ₅ O ₈ (OH)) ₂ B(OH) ₃ ·H ₂ O	0.636	[BO ₃], [BO ₂ (OH)], [B(OH) ₃], [BO ₄]	[B(OH) ₃], [B ₅ O ₁₀ (OH)]	[B(OH) ₃], ² [B ₅ O ₈ (OH)] _∞
4	134988	Ca ₂ (B ₅ O ₈ (OH)) ₂ (B(OH) ₃)·H ₂ O	0.636	[BO ₃], [BO ₂ (OH)], [B(OH) ₃], [BO ₄]	[B(OH) ₃], [B ₁₀ O ₂₀ (OH) ₂]	[B(OH) ₃], ² [B ₅ O ₈ (OH)] _∞
5	42570	Ba ₂ B ₁₃ O ₁₉ (OH) ₅ ·5H ₂ O	0.539	[BO ₃], [BO ₂ (OH)], [BO(OH) ₂], [BO ₄], [BO ₃ (OH)]	[B ₁₃ O ₂₅ (OH) ₅]	² [B ₁₃ O ₁₉ (OH) ₅] _∞
6	171019	CaB ₈ O ₁₁ (OH) ₄	0.625	[BO ₃], [BO ₂ (OH)], [BO(OH) ₂], [BO ₄]	[B ₈ O ₁₃ (OH) ₄]	² [B ₈ O ₁₁ (OH) ₄] _∞
7	250323	CaB ₈ O ₁₁ (OH) ₄	0.625	[BO ₃], [BO ₂ (OH)], [BO(OH) ₂], [BO ₄]	[B ₈ O ₁₃ (OH) ₄]	² [B ₈ O ₁₁ (OH) ₄] _∞
8	262502	Ba ₂ (B ₆ O ₉ (OH) ₄)	1	[BO ₃], [BO ₄], [BO ₃ (OH)] , [BO ₂ (OH) ₂]	[B ₆ O ₁₃ (OH) ₄]	² [B ₆ O ₉ (OH) ₄] _∞
9	415082	Ca(B ₈ O ₁₁ (OH) ₄)	0.625	[BO ₃], [BO ₂ (OH)], [BO(OH) ₂], [BO ₄]	[B ₈ O ₁₃ (OH) ₄]	² [B ₈ O ₁₁ (OH) ₄] _∞
10	432814	Ca ₂ (B ₅ O ₈ (OH)) ₂ (B(OH) ₃)·H ₂ O	0.636	[BO ₃], [BO ₂ (OH)], [B(OH) ₃], [BO ₄]	[B(OH) ₃], [B ₅ O ₁₀ (OH)]	[B(OH) ₃], ² [B ₅ O ₈ (OH)] _∞
11	4228	Sr(B ₈ O ₁₁ (OH) ₄)	0.625	[BO ₃], [BO ₂ (OH)], [BO(OH) ₂], [BO ₄]	[B ₈ O ₁₃ (OH) ₄]	² [B ₈ O ₁₁ (OH) ₄] _∞
12	20074	Sr ₂ (B ₅ O ₈ (OH)) ₂ (B(OH) ₃)(H ₂ O)	0.636	[BO ₃],[BO ₂ (OH)], [B(OH) ₃], [BO ₄]	[B(OH) ₃], [B ₅ O ₁₀ (OH)]	[B(OH) ₃], ² [B ₅ O ₈ (OH)] _∞
13	28014	Sr ₂ (B ₅ O ₈ (OH)) ₂ (B(OH) ₃)·H ₂ O	0.636	[BO ₃],[BO ₂ (OH)], [B(OH) ₃], [BO ₄]	[B(OH) ₃], B ₅ O ₁₀ (OH)]	[B(OH) ₃], ² [B ₅ O ₈ (OH)] _∞
14	19922	Ba ₂ (B ₅ O ₈ (OH)) ₂ (B(OH) ₃)·H ₂ O	0.636	[BO ₃], [BO ₂ (OH)], [B(OH) ₃], [BO ₄]	[B(OH) ₃], [B ₅ O ₁₀ (OH)]	[B(OH) ₃], ² [B ₅ O ₈ (OH)] _∞
15	95447	Na ₂ Ba ₂ (B ₁₀ O ₁₇ (OH) ₂)	0.6	[BO ₃], [BO ₂ (OH)], [BO ₄]	[B ₁₀ O ₂₁ (OH) ₂]	² [B ₁₀ O ₁₇ (OH) ₂] _∞
16	403149	Ba ₃ (B ₁₀ O ₁₇ (OH) ₂)	0.5	[BO ₃], [BO ₂ (OH)], [BO ₄]	[B ₁₀ O ₂₃ (OH) ₂]	² [B ₁₀ O ₁₇ (OH) ₂] _∞
17	154523	Na ₄ (B ₁₀ O ₁₆ (OH) ₂)·4H ₂ O	0.6	[BO ₃], [BO ₂ (OH)], [BO ₄]	[B ₅ O ₁₀ (OH)]	² [B ₅ O ₈ (OH)] _∞
18	2942	Sr ₂ (B ₅ O ₈ (OH)) ₂ (B(OH) ₃)·H ₂ O	0.636	[BO ₃], [BO ₂ (OH)], [B(OH) ₃], [BO ₄]	[B(OH) ₃], [B ₅ O ₁₀ (OH)]	[B(OH) ₃], ² [B ₅ O ₈ (OH)] _∞
19	262913	La(B ₄ O ₆ (OH) ₂ Cl)	0.75	[BO ₃], [BO ₃ (OH)]	[B ₄ O ₁₀ (OH) ₂]	² [B ₄ O ₆ (OH) ₂] _∞
20	124040	Ba ₂ B ₁₀ O ₁₆ (OH) ₂ (H ₃ BO ₃) ·H ₂ O	0.636	[BO ₃], [BO ₂ (OH)], [B(OH) ₃], [BO ₄]	[B(OH) ₃], [B ₅ O ₁₀ (OH)]	[B(OH) ₃], ² [B ₅ O ₈ (OH)] _∞

No.	ICSD code	Compounds	(A+OH)/B ratio	Anionic units	FBB units	Anionic layered configuration
21	13423	Li ₂ CsB ₇ O ₁₀ (OH) ₄	1	[BO ₃], [BO ₄], [BO ₂ (OH) ₂]	[B ₇ O ₁₂ (OH) ₄]	² [B ₇ O ₁₀ (OH) ₄] _∞
22	250215	CaLi ₄ (B ₅ O ₈ (OH) ₂) ₂	0.9	[BO ₃], [BO ₄], [BO ₃ (OH)]	[B ₅ O ₁₀ (OH) ₂]	² [B ₅ O ₈ (OH) ₂] _∞
23	36431	Li ₃ (B ₅ O ₈ (OH) ₂)	1	[BO ₃], [BO ₄], [BO ₃ (OH)]	[B ₅ O ₁₀ (OH) ₂]	² [B ₅ O ₈ (OH) ₂] _∞
24	22192	CaB ₃ O ₅ (OH)	0.667	[BO ₃], [BO ₄], [BO ₃ (OH)]	[B ₃ O ₇ (OH)]	² [B ₃ O ₅ (OH)] _∞
25	23880	CaB ₃ O ₅ (OH)	0.667	[BO ₃], [BO ₄], [BO ₃ (OH)]	[B ₃ O ₇ (OH)]	² [B ₃ O ₅ (OH)] _∞
26	1973	(Na(H ₂ O)) ₂ (B ₅ O ₈ (OH))	0.6	[BO ₃], [BO ₂ (OH)], [BO ₄]	[B ₅ O ₁₀ (OH)]	² [B ₅ O ₈ (OH)] _∞
27	249876	Na ₂ B ₅ O ₈ (OH)·2H ₂ O	0.6	[BO ₃], [BO ₂ (OH)], [BO ₄]	[B ₅ O ₁₀ (OH)]	² [B ₅ O ₈ (OH)] _∞
28	252381	CaB ₃ O ₅ (OH)	0.667	[BO ₃], [BO ₄], [BO ₃ (OH)]	[B ₃ O ₉ (OH)]	² [B ₃ O ₅ (OH)] _∞
29	425207	Li ₃ (B ₈ O ₁₂ (OH) ₃)	0.75	[BO ₂ (OH)], [BO ₄]	[B ₈ O ₁₈ (OH) ₃]	² [B ₈ O ₁₂ (OH) ₃] _∞

Table S5 The basic information of hydroxyborates with 3D anionic frameworks.

No.	ICSD code	Compounds	(A+OH)/B ratio	Anionic units	FBB units	Anionic framework
1	76888	$\text{Ca}_9\text{B}_{26}\text{O}_{34}(\text{OH})_{24}\text{Cl}_4$ $\cdot 13\text{H}_2\text{O}$	1.269	$[\text{BO}_3]$, $[\text{BO}_2(\text{OH})]$, $[\text{BO}_4]$, $[\text{BO}_2(\text{OH})_2]$, $[\text{BO}_3(\text{OH})]$	$[\text{B}_{26}\text{O}_{47}(\text{OH})_2]$	$^3[\text{B}_{26}\text{O}_{34}(\text{OH})_{24}]$ ∞
2	20155	$\text{Li}_3(\text{B}_5\text{O}_8(\text{OH})_2)$	1	$[\text{BO}_3]$, $[\text{BO}_4]$, $[\text{BO}_3(\text{OH})]$	$[\text{B}_5\text{O}_{10}(\text{OH})_2]$	$^3[\text{B}_5\text{O}_8(\text{OH})_2]_\infty$
3	20173	$\text{Li}_3(\text{B}_5\text{O}_8(\text{OH})_2)$	1	$[\text{BO}_3]$, $[\text{BO}_4]$, $[\text{BO}_3(\text{OH})]$	$[\text{B}_5\text{O}_{10}(\text{OH})_2]$	$^3[\text{B}_5\text{O}_8(\text{OH})_2]_\infty$
4	418166	$\text{Li}_3(\text{B}_5\text{O}_8(\text{OH})_2)$	1	$[\text{BO}_3]$, $[\text{BO}_4]$, $[\text{BO}_3(\text{OH})]$	$[\text{B}_5\text{O}_{10}(\text{OH})_2]$	$^3[\text{B}_5\text{O}_8(\text{OH})_2]_\infty$
5	421260	$\text{Y}(\text{B}_2\text{O}_3(\text{OH}))_3$	0.667	$[\text{BO}_3]$, $[\text{BO}_3(\text{OH})]$	$[\text{B}_2\text{O}_5(\text{OH})]$	$^3[\text{B}_2\text{O}_3(\text{OH})]_\infty$

Table S6 The ICSD collection numbers, chemical formula, space group, GGA and HSE06 band gaps, second harmonic generation (SHG) coefficients, and birefringence Δn at 1064 nm of 60 screening hydroxyborates crystals. Note that SHG coefficients, and birefringence Δn have been corrected with scissors operators.

No.	ICSD code	Compounds	Space group	Band gap (eV)		SHG coefficients (pm/V)	Δn at 1064 nm
				GGA	HSE06		
1	39637	$\text{KCa}_4(\text{B}_{22}\text{O}_{32})(\text{OH})_{10}\text{Cl}\cdot 4\text{H}_2\text{O}$	$P1$	5.49	7.02	$d_{11} = 0.54, d_{12} = -0.57$ $d_{16} = 0.48, d_{22} = -0.56$	0.064
2	187776	$\text{KCa}_4(\text{B}_{22}\text{O}_{32})(\text{OH})_{10}\text{Cl}\cdot 4\text{H}_2\text{O}$	$P1$	5.48	7.08	$d_{11} = -0.55, d_{12} = 0.59$ $d_{16} = 0.50, d_{22} = -0.55$	0.065
3	172480	$\text{Bi}(\text{B}_4\text{O}_6(\text{OH})_2)(\text{OH})$	$P1$	4.69	5.59	0	0.110
4	76888	$\text{Ca}_9\text{B}_{26}\text{O}_{34}(\text{OH})_{24}\text{Cl}_4\cdot 13\text{H}_2\text{O}$	$P1$	5.36	6.65	$d_{23} = 0.12, d_{24} = -0.41, d_{33}$ $= 0.09$ $d_{11} = -0.59, d_{12} = 0.67,$	0.031
5	420549	$\text{Ca}_2(\text{B}_5\text{O}_8(\text{OH}))_2\text{B}(\text{OH})_3\cdot \text{H}_2\text{O}$	$P1$	5.52	7.08	$d_{13} = 0.12, d_{14} = -0.14,$ $d_{16} = -0.56, d_{22} = 0.51,$ $d_{24} = -0.17, d_{33} = 0.10$	0.060
6	134988	$\text{Ca}_2(\text{B}_5\text{O}_8(\text{OH}))_2\text{B}(\text{OH})_3\cdot \text{H}_2\text{O}$	$P1$	5.90	7.38	$d_{11} = 0.66, d_{12} = -0.67,$ $d_{16} = 0.60, d_{22} = -0.55$	0.071
7	42570	$\text{Ba}_2\text{B}_{13}\text{O}_{19}(\text{OH})_5\cdot 5\text{H}_2\text{O}$	$P1$	5.15	6.58	$d_{16} = -0.29, d_{22} = -0.49,$ $d_{23} = 0.65$	0.035
8	28426	$\text{CaB}_3\text{O}_4(\text{OH})_3\cdot \text{H}_2\text{O}$	$P2_1$	5.59	7.28	$d_{11} = 0.13$	0.011
9	28427	$\text{Ca}(\text{B}_3\text{O}_4(\text{OH})_3)\cdot \text{H}_2\text{O}$	$P2_1$	5.67	7.20	$d_{22} = 0.15, d_{23} = -0.05$	0.028
10	171019	$\text{CaB}_8\text{O}_{11}(\text{OH})_4$	$P2_1$	5.56	6.71	$d_{22} = 0.65, d_{23} = -0.66$	0.091
11	250323	$\text{CaB}_8\text{O}_{11}(\text{OH})_4$	$P2_1$	5.59	6.81	$d_{14} = -0.07, d_{16} = 0.10,$ $d_{22} = 0.62, d_{23} = -0.64$	0.061
12	262502	$\text{Ba}_2(\text{B}_6\text{O}_9(\text{OH})_4)$	$P2_1$	5.22	7.14	$d_{16} = -0.43, d_{22} = 1.07$	0.037
13	415082	$\text{Ca}(\text{B}_8\text{O}_{11}(\text{OH})_4)$	$P2_1$	5.58	6.80	$d_{14} = -0.07, d_{16} = 0.12,$ $d_{22} = 0.63, d_{23} = -0.64$	0.091
14	432814	$\text{Ca}_2(\text{B}_5\text{O}_8(\text{OH}))_2\text{B}(\text{OH})_3\cdot \text{H}_2\text{O}$	$P2_1$	5.89	7.54	$d_{16} = -0.06, d_{22} = 0.13,$ $d_{23} = -0.08$	0.076
15	4228	$\text{Sr}(\text{B}_8\text{O}_{11}(\text{OH})_4)$	$P2_1$	5.06	6.45	$d_{16} = -0.88, d_{22} = 0.57,$ $d_{23} = 0.47$	0.076
16	20074	$\text{Sr}_2(\text{B}_5\text{O}_8(\text{OH}))_2\text{B}(\text{OH})_3\cdot \text{H}_2\text{O}$	$P2_1$	5.85	7.36	$d_{22} = 0.08, d_{23} = -0.07$	0.040
17	28014	$\text{Sr}_2(\text{B}_5\text{O}_8(\text{OH}))_2\text{B}(\text{OH})_3\cdot \text{H}_2\text{O}$	$P2_1$	5.35	6.77	$d_{22} = 0.21, d_{23} = -0.03$	0.050
18	100400	$(\text{NH}_4)_2(\text{B}_4\text{O}_5(\text{OH})_4)\cdot 2\text{H}_2\text{O}$	$P2_1$	4.97	6.30	$d_{14} = 0.18, d_{16} = 0.32,$ $d_{22} = -0.62, d_{23} = 0.25$	0.014
19	49364	$(\text{NH}_4)_2\text{B}_4\text{O}_5(\text{OH})_4\cdot 2\text{H}_2\text{O}$	$P2_1$	5.18	6.68	$d_{14} = -0.20, d_{16} = -0.37,$ $d_{22} = 0.80, d_{23} = -0.42$	0.016
20	49365	$(\text{NH}_4)_2\text{B}_4\text{O}_5(\text{OH})_4\cdot 2\text{H}_2\text{O}$	$P2_1$	5.17	6.47	$d_{14} = -0.10, d_{16} = -0.24,$ $d_{22} = 0.55, d_{23} = -0.28$	0.041
21	19922	$\text{Ba}_2(\text{B}_5\text{O}_8(\text{OH}))_2\text{B}(\text{OH})_3\cdot \text{H}_2\text{O}$	$P2_1$	5.83	6.76	$d_{16} = -0.07, d_{22} = -0.16,$ $d_{23} = 0.10$	0.070
22	141235	$\text{NaRb}_3\text{B}_6\text{O}_9(\text{OH})_3(\text{HCO}_3)$	$P2_1$	4.19	5.40	$d_{14} = 0.08, d_{16} = 0.06,$ $d_{22} = 0.11, d_{23} = 0.16$	0.017

No.	ICSD code	Compounds	Space group	Band gap (eV)		SHG coefficients (pm/V)	Δn at 1064 nm
				GGA	HSE06		
23	95447	$\text{Na}_2\text{Ba}_2(\text{B}_{10}\text{O}_{17}(\text{OH})_2)$	<i>C2</i>	4.70	6.12	$d_{16} = 0.38, d_{22} = -1.08$	0.027
24	403149	$\text{Ba}_3(\text{B}_{10}\text{O}_{17}(\text{OH})_2)$	<i>C2</i>	4.62	5.95	$d_{22} = 0.33, d_{23} = -0.18$	0.033
25	262542	$\text{Ba}_3\text{B}_6\text{O}_{11}(\text{OH})_2$	<i>Pc</i>	4.76	6.12	$d_{11} = -0.67, d_{33} = 0.33$	0.010
26	154523	$\text{Na}_4(\text{B}_{10}\text{O}_{16}(\text{OH})_2) \cdot 4\text{H}_2\text{O}$	<i>Pc</i>	4.79	6.42	$d_{11} = 0.65, d_{12} = -0.25,$ $d_{13} = -0.38, d_{15} = -0.08,$ $d_{33} = 0.21$	0.030
27	26380	$\text{NH}_4(\text{B}_5\text{O}_6(\text{OH})_4) \cdot 2\text{H}_2\text{O}$	<i>Pc</i>	4.98	6.47	$d_{11} = 0.29, d_{12} = -0.39,$ $d_{13} = 0.06, d_{15} = 0.10,$ $d_{33} = 0.07$	0.050
28	2942	$\text{Sr}_2(\text{B}_5\text{O}_8(\text{OH}))_2(\text{B}(\text{OH})_3) \cdot \text{H}_2\text{O}$	<i>Cc</i>	5.91	7.49	$d_{11} = 0.07, d_{13} = 0.06,$ $d_{24} = -0.08, d_{33} = 0.12$	0.005
29	260879	$\text{Na}_3(\text{B}_3\text{O}_4(\text{OH})_4)$	<i>Cc</i>	4.64	5.92	$d_{15} = 0.26, d_{24} = -0.34$	0.037
30	262913	$\text{La}(\text{B}_4\text{O}_6(\text{OH})_2\text{Cl})$	<i>Cc</i>	6.17	7.14	$d_{11} = -0.79, d_{12} = 0.77,$ $d_{13} = 0.34, d_{15} = -0.38,$ $d_{24} = -0.39, d_{33} = 0.93$	0.030
31	124040	$\text{Ba}_2\text{B}_{10}\text{O}_{16}(\text{OH})_2(\text{H}_3\text{BO}_3) \cdot \text{H}_2\text{O}$	<i>Cc</i>	5.48	7.29	$d_{24} = 0.10, d_{33} = -0.11$	0.069
32	34648	$\text{K}_2(\text{B}_4\text{O}_5(\text{OH})_4) \cdot 2\text{H}_2\text{O}$	<i>P2₁2₁2₁</i>	5.12	6.67	$d_{14} = -0.13$	0.008
33	57297	$\text{Ba}(\text{BO}_2(\text{OH}))$	<i>P2₁2₁2₁</i>	4.10	5.88	$d_{14} = 0.07$	0.082
34	13423	$\text{Li}_2\text{CsB}_7\text{O}_{10}(\text{OH})_4$	<i>C222</i>	5.20	7.26	$d_{14} = 0.70$	0.023
35	431106	$\text{Na}(\text{B}_5\text{O}_7(\text{OH})_2) \cdot \text{H}_2\text{O}$	<i>Pca2₁</i>	5.79	7.29	$d_{24} = -0.14, d_{33} = -0.09$	0.059
36	250215	$\text{CaLi}_4(\text{B}_5\text{O}_8(\text{OH})_2)_2$	<i>Pnc2</i>	5.08	6.75	$d_{24} = -0.11, d_{33} = 0.29$	0.033
37	36431	$\text{Li}_3(\text{B}_5\text{O}_8(\text{OH})_2)$	<i>Pnc2</i>	5.60	6.26	$d_{24} = -0.05$	0.037
38	22192	$\text{CaB}_3\text{O}_5(\text{OH})$	<i>Pna2₁</i>	5.50	6.36	$d_{15} = -0.65, d_{24} = 0.48,$ $d_{33} = 0.82$	0.043
39	23880	$\text{CaB}_3\text{O}_5(\text{OH})$	<i>Pna2₁</i>	5.50	6.96	$d_{15} = 0.41, d_{24} = -0.57,$ $d_{33} = 0.72$	0.040
40	1973	$(\text{Na}(\text{H}_2\text{O}))_2(\text{B}_5\text{O}_8(\text{OH}))$	<i>Pna2₁</i>	5.00	6.47	$d_{15} = 0.34, d_{24} = 0.33,$ $d_{33} = -0.68$	0.023
41	249876	$\text{Na}_2\text{B}_5\text{O}_8(\text{OH}) \cdot 2\text{H}_2\text{O}$	<i>Pna2₁</i>	5.00	6.62	$d_{15} = -0.35, d_{24} = -0.34,$ $d_{33} = 0.70$	0.023
42	252381	$\text{CaB}_3\text{O}_5(\text{OH})$	<i>Pna2₁</i>	5.74	7.15	$d_{15} = -0.50, d_{24} = 0.70,$ $d_{33} = -0.77$	0.037
43	253012	$\text{K}_3\text{B}_3\text{O}_4(\text{OH})_4 \cdot 2\text{H}_2\text{O}$	<i>Cmc2₁</i>	4.45	5.77	$d_{15} = 0.01, d_{24} = -0.39,$ $d_{33} = 0.33$	0.036
44	113334	$(\text{NH}_4)_2(\text{B}_4\text{O}_5(\text{OH})_4) \cdot 2\text{H}_2\text{O}$	<i>Cmc2₁</i>	5.19	6.71	$d_{15} = 0.61, d_{24} = -0.20,$ $d_{33} = -0.50$	0.016
45	6292	$\text{K}(\text{B}_5\text{O}_6(\text{OH})_4) \cdot 2\text{H}_2\text{O}$	<i>Aba2</i>	5.57	7.02	$d_{15} = 0.116, d_{24} = -0.085,$ $d_{33} = 0.082$	0.050
46	29406	$\text{RbB}_5\text{O}_6(\text{OH})_4 \cdot 2\text{H}_2\text{O}$	<i>Aba2</i>	5.50	7.22	$d_{15} = 0.08, d_{24} = -0.08,$ $d_{33} = 0.07$	0.050
47	90001	$(\text{NH}_4)(\text{B}_5\text{O}_6(\text{OH})_4) \cdot 2\text{H}_2\text{O}$	<i>Aba2</i>	5.58	6.91	$d_{15} = -0.18, d_{24} = 0.15,$ $d_{33} = 0.26$	0.049

No.	ICSD code	Compounds	Space group	Band gap (eV)		SHG coefficients (pm/V)	Δn at 1064 nm
				GGA	HSE06		
48	410811	$(\text{NH}_4)(\text{B}_5\text{O}_6(\text{OH})_4) \cdot 2\text{H}_2\text{O}$	<i>Aba2</i>	5.59	6.88	$d_{15} = -0.17, d_{24} = 0.13,$ $d_{33} = 0.26$	0.049
49	4481	$\text{K}_3\text{B}_5\text{O}_8(\text{OH})_2$	<i>Fdd2</i>	4.84	6.26	$d_{15} = 0.21, d_{24} = 0.26$	0.042
50	20662	$\text{Mg}(\text{B}_2\text{O}(\text{OH})_6)$	<i>P4₂</i>	5.44	7.15	0	0.004
51	24920	$\text{Mg}(\text{B}_2\text{O}(\text{OH})_6)$	<i>P4₂</i>	4.30	5.86	$d_{33} = -0.39$	0.002
52	20155	$\text{Li}_3(\text{B}_5\text{O}_8(\text{OH})_2)$	<i>P4_{12,2}</i>	6.37	7.82	0	0.004
53	20173	$\text{Li}_3(\text{B}_5\text{O}_8(\text{OH})_2)$	<i>P4_{12,2}</i>	5.97	7.53	0	0.004
54	418166	$\text{Li}_3(\text{B}_5\text{O}_8(\text{OH})_2)$	<i>P4_{32,2}</i>	5.96	7.81	0	0.004
55	431536	$\text{Ba}_2(\text{B}_4\text{O}_7(\text{OH})_2)$	<i>P3₁₂₁</i>	4.13	5.15	$d_{11} = 0.57, d_{12} = -0.57$	0.014
56	10266	$\text{Na}_2(\text{B}_4\text{O}_5(\text{OH})_4) \cdot 3\text{H}_2\text{O}$	<i>R32</i>	5.23	6.60	$d_{11} = 0.10, d_{12} = -0.10$	0.007
57	70998	$\text{NaRb}_6(\text{B}_4\text{O}_5(\text{OH})_4)_3(\text{BO}_2)$	<i>R32</i>	4.75	5.83	$d_{11} = 0.02, d_{12} = -0.02$	0.010
58	70999	$\text{NaRb}_6(\text{B}_4\text{O}_5(\text{OH})_4)_3(\text{BO}_2)$	<i>R32</i>	4.73	5.82	$d_{11} = 0.09, d_{12} = -0.09$	0.010
59	421260	$\text{Y}(\text{B}_2\text{O}_3(\text{OH}))_3$	<i>R3c</i>	6.25	7.60	$d_{21} = -0.78, d_{22} = 0.78,$ $d_{15} = 0.20, d_{24} = 0.20$	0.037
60	425207	$\text{Li}_3(\text{B}_8\text{O}_{12}(\text{OH})_3)$	<i>P$\bar{6}$2c</i>	5.72	6.84	$d_{16} = 0.20, d_{22} = -0.20$	0.036

Table S7 Calculated band gaps (E_g) by hybrid HSE06, the maximum SHG coefficients (d_{ij}), birefringence at 1064 nm (Δn), UV cutoff wavelengths (λ_{cutoff}), shortest phase-matching wavelengths (λ_{PM}), dimensionality of B–O/OH anionic framework, and ($A + \text{OH}$)/B ratio of screened hydroxyborate crystals.

No.	ICSD code	Compounds	Space group	E_g (eV)	d_{ij} (pm/V)	Δn	λ_{cutoff} (nm)	λ_{PM} (nm)	Dimension / Ration
1	42570	$\text{Ba}_2\text{B}_{13}\text{O}_{19}(\text{OH})_5 \cdot 5\text{H}_2\text{O}$	$P1$	6.58	$d_{23} = 0.65$	0.04	189	298	2/0.539
1a ¹			$P1$	> 6.2	$d_{\langle\text{powder}\rangle} \approx 1.0 \times \text{KDP}$	---	<200	---	
1b ¹			$P1$	5.41 GGA	$d_{23} = 0.87$	0.042	230	270	
2	171019	$\text{CaB}_8\text{O}_{11}(\text{OH})_4$	$P2_1$	6.71	$d_{23} = -0.66$	0.091	185	199	2/0.625
2a ²			$P2_1$	> 6.3	$d_{\langle\text{powder}\rangle} \approx 1.4 \times \text{KDP}$	---	<200	---	
2b ²			$P2_1$	7.43 PBE0	$d_{23} = -0.41$	0.093	165	174	
3	4228	$\text{Sr}(\text{B}_8\text{O}_{11}(\text{OH})_4)$	$P2_1$	6.45	$d_{16} = -0.88$	0.076	193	211	2/0.625
3a ²			$P2_1$	>6.30	$d_{\langle\text{powder}\rangle} \approx 1.4 \times \text{KDP}$	0.109	<200	---	
3b ²			$P2_1$	7.02 PBE0	$d_{16} = 0.39$	0.087	176	185	
4	13423	$\text{Li}_2\text{CsB}_7\text{O}_{10}(\text{OH})_4$	$C222$	7.26	$d_{14} = 0.70$	0.023	171	321	2/1
4a ³			$C222$	6.35	$d_{\langle\text{powder}\rangle} \approx 2.5 \times \text{KDP}$	---	196	---	
4b ³			$C222$	4.56 GGA	$d_{14} = -0.76$	---	273	---	
5	249876	$\text{Na}_2\text{B}_5\text{O}_8(\text{OH}) \cdot 2\text{H}_2\text{O}$	$Pna2_1$	6.62	$d_{33} = 0.70$	0.023	188	348	2/0.6
5a ⁴			$Pna2_1$	> 6.5	$d_{\langle\text{powder}\rangle} \approx 0.5 \times \text{KDP}$	---	<190	---	
6	253012	$\text{K}_3\text{B}_3\text{O}_4(\text{OH})_4 \cdot 2\text{H}_2\text{O}$	$Cmc2_1$	5.77	$d_{24} = -0.39$	0.036	216	295	0/2.333
6a ⁵			$Cmc2_1$	6.1	$d_{\langle\text{powder}\rangle} \approx 0.8 \times \text{KDP}$	---	204	---	
6b ⁵			$Cmc2_1$	4.8 GGA	$d_{24} = 0.37$	---	256	---	

^a Experimentally measured data in references. ^b Theoretically calculated data in references.

Table S8 Predicted band gaps (E_g) by hybrid HSE06, largest SHG coefficients (d_{ij}), birefringence at 1064 nm (Δn), UV cutoff wavelengths (λ_{cutoff}), shortest phase-matching wavelengths (λ_{PM}), dimensionality of B–O/OH anionic framework, and ($A + \text{OH}$)/B ratio of screened hydroxyborate crystals.

No.	ICSD code	Compounds	Space group	E_g (eV)	d_{ij} (pm/V)	Δn	λ_{cutoff} (nm)	λ_{PM} (nm)	Dimension / Ration
1	187776	$\text{KCa}_4(\text{B}_{22}\text{O}_{32})(\text{OH})_{10}\text{Cl}\cdot 4\text{H}_2\text{O}$	$P1$	7.08	$d_{12} = 0.59$	0.065	176	235	2/0.682
2	76888	$\text{Ca}_9\text{B}_{26}\text{O}_{34}(\text{OH})_{24}\text{Cl}_4\cdot 13\text{H}_2\text{O}$	$P1$	6.65	$d_{24} = -0.41$	0.031	187	336	3/1.269
3	95447	$\text{Na}_2\text{Ba}_2(\text{B}_{10}\text{O}_{17}(\text{OH})_2)$	$C2$	6.12	$d_{22} = -1.08$	0.027	203	368	2/0.6
4	154523	$\text{Na}_4(\text{B}_{10}\text{O}_{16}(\text{OH})_2)\cdot 4\text{H}_2\text{O}$	Pc	6.42	$d_{11} = 0.65$	0.03	194	318	2/0.6
5	1973	$(\text{Na}(\text{H}_2\text{O}))_2(\text{B}_5\text{O}_8(\text{OH}))$	$Pna2_1$	6.47	$d_{33} = -0.68$	0.023	192	346	2/0.6
6	134988	$\text{Ca}_2(\text{B}_5\text{O}_8(\text{OH}))_2\text{B}(\text{OH})_3\cdot \text{H}_2\text{O}$	$P1$	7.38	$d_{12} = -0.67$	0.071	170	229	2/0.636
6a ⁶			$P1$	>5.75	$d_{\langle\text{powder}\rangle} \approx 1.8 \times \text{KDP}$	---	<216	---	
7	262502	$\text{Ba}_2(\text{B}_6\text{O}_9(\text{OH})_4)$	$P2_1$	7.14	$d_{22} = 1.07$	0.037	174	302	2/1
7a ⁷			$P2_1$	>6.5	$d_{\langle\text{powder}\rangle} \approx 3 \times \text{KDP}$	---	<190	---	
8	26380	$\text{NH}_4(\text{B}_5\text{O}_6(\text{OH})_4)\cdot 2\text{H}_2\text{O}$	Pc	6.47	$d_{12} = -0.39$	0.05	192	240	0/1
8a ⁸			Pc	6.91	---	0.058	≈ 180	---	
9	252381	$\text{CaB}_3\text{O}_5(\text{OH})$	$Pna2_1$	7.15	$d_{33} = -0.77$	0.037	174	327	2/0.667
9a ⁹			$Pna2_1$	---	$d_{\langle\text{powder}\rangle} \approx 1 \times \text{KDP}$	---	---	---	

^a Experimentally measured data in references.

Table S9 The investigation of ratio $(A + OH)/B = 0.636$, dimensionality of B–O/OH anionic framework, birefringence at 1064 nm (cal.), and $[BO_3]$ & $[B(OH)_3]$ & $[BO_2(OH)]$ density among hydroxyborates involving the screened compounds.

No.	ICSD code	Compounds	Space group	Dimension	Number of $[BO_3]$ & $[B(OH)_3]$ & $[BO_2(OH)]$ in cell	Cell volume (\AA^3)	Birefringence at 1064 nm (cal.)	Density of $[BO_3]$ & $[B(OH)_3]$ & $[BO_2(OH)]$ groups(\AA^{-3})
1	420549	$Ca_2(B_5O_8(OH))_2B(OH)_3 \cdot H_2O-I$	<i>P1</i>	2D	6.5	386.3	0.06	0.0168
2	134988	$Ca_2(B_5O_8(OH))_2(B(OH)_3) \cdot H_2O-II$	<i>P1</i>	2D	7	385.7	0.071	0.0181
3	432814	$Ca_2(B_5O_8(OH))_2(B(OH)_3) \cdot H_2O-III$	<i>P2</i> ₁	2D	14	773.2	0.076	0.0181
4	20074	$Sr_2(B_5O_8(OH))_2(B(OH)_3) \cdot H_2O-I$	<i>P2</i> ₁	2D	13	802.5	0.040	0.0162
5	28014	$Sr_2(B_5O_8(OH))_2(B(OH)_3) \cdot H_2O-II$	<i>P2</i> ₁	2D	13	802.5	0.050	0.0162
6	2942	$Sr_2(B_5O_8(OH))_2(B(OH)_3) \cdot H_2O-III$	<i>Cc</i>	2D	18	1627.7	0.005	0.0111
7	19922	$Ba_2(B_5O_8(OH))_2(B(OH)_3) \cdot H_2O-I$	<i>P2</i> ₁	2D	14	857.1	0.070	0.0163
8	124040	$Ba_2B_{10}O_{16}(OH)_2(H_3BO_3) \cdot H_2O-II$	<i>Cc</i>	2D	30	1717.0	0.069	0.0174

Table S10 Bonding electron difference ($\Delta\rho$) and contribution percent w (%) of different units in $\text{KCa}_4(\text{B}_{22}\text{O}_{32}(\text{OH})_{10}\text{Cl})\cdot 4\text{H}_2\text{O}$ calculated by the REDA model.

Compounds	units	$\Delta\rho$	w (%)
$\text{KCa}_4(\text{B}_{22}\text{O}_{32}(\text{OH})_{10}\text{Cl})\cdot 4\text{H}_2\text{O}$	$[\text{BO}_3]$	0.0106	52.46
	$[\text{BO}_2(\text{OH})]$	0.0054	26.55
	$[\text{B}(\text{OH})_3]$	0.0029	14.28
	$[\text{BO}_4]$	0.0008	4.04
	$[\text{KO}_4]$	0.0001	0.73
	$[\text{CaO}_9]$	0.0003	1.45
	$[\text{CaO}_8\text{Cl}]$	0.0001	0.49

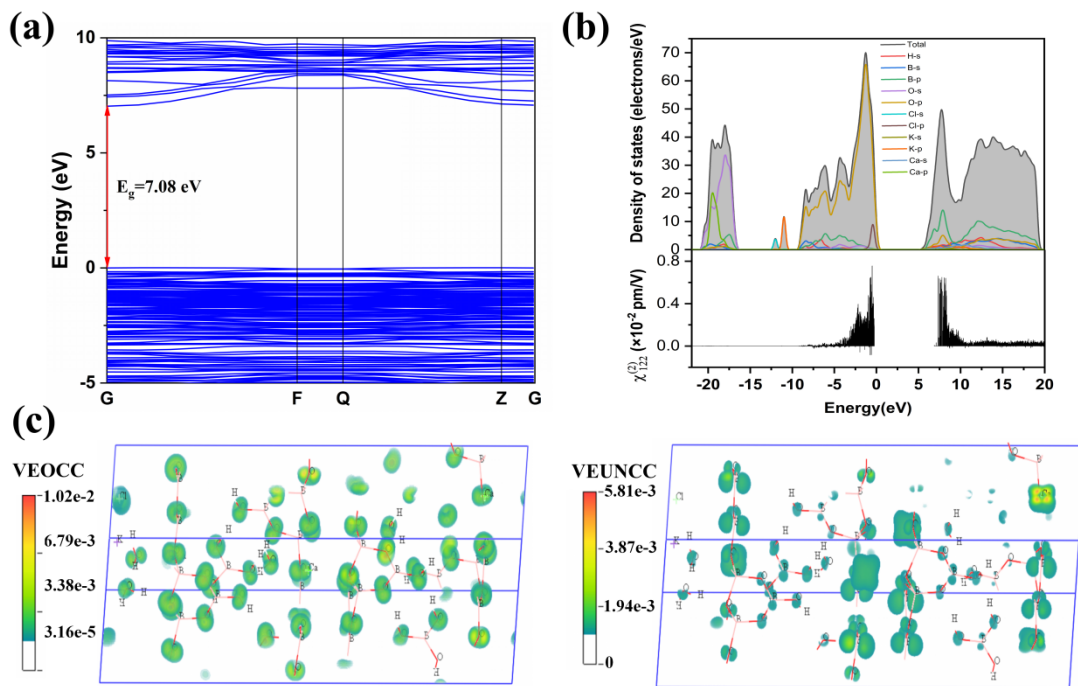


Figure S1. (a) Band structures by the HSE06 functional. (b) Total and partial density of states (PDOS) and band-resolved NLO coefficients. (c) SHG-weighted density of occupied and unoccupied states in virtual-electron (VE) progress of $\text{KCa}_4(\text{B}_{22}\text{O}_{32}(\text{OH})_{10}\text{Cl}) \cdot 4\text{H}_2\text{O}$. Here, $\chi_{122} = 2d_{12}$.

Notes and references

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