

## **Batch and Continuous Packed-Bed Column Sorption of Metal Ions using Economically Derived Ca-MOF Immobilized Cellulose Porous Matrix**

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## Supplementary file

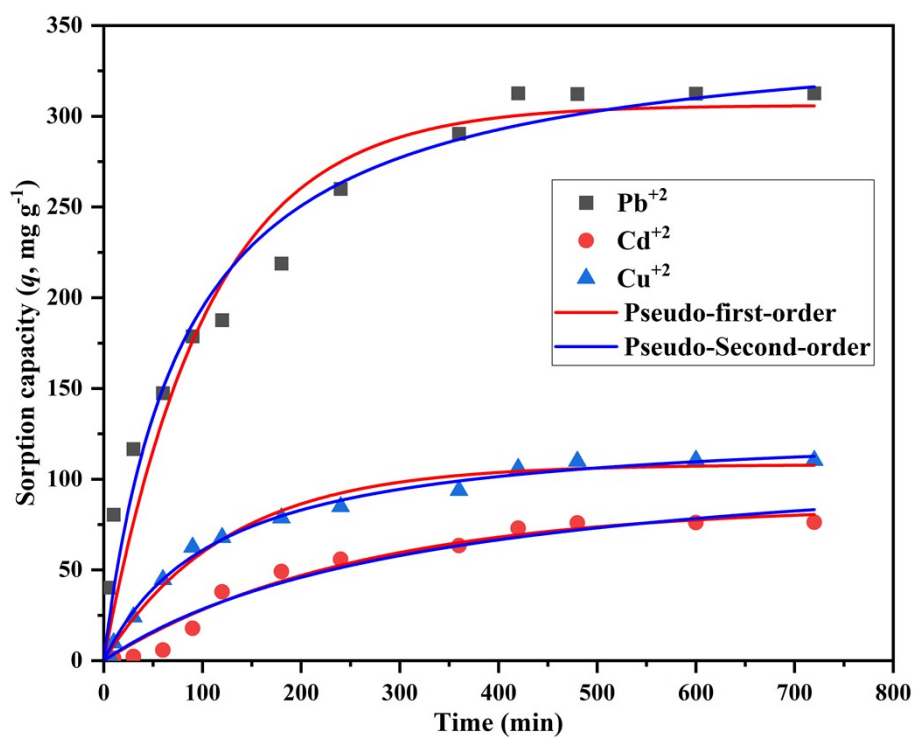
**Table S1** Different isotherms and kinetic models were used to fit the sorption equilibrium and kinetic data.

	Non-linear Equations	Model parameters	Other variables
Isotherm models			
Langmuir	$\theta = \frac{q_e}{q_m} = \frac{bC_e}{1 + bC_e}$	$q_m$ , monolayer sorption capacity mg g <sup>-1</sup> . $b$ , affinity of union sites.	$\theta$ , fractional coverage. $C_e$ , equilibrium concentration of solute in the solution mg L <sup>-1</sup> . $q_e$ , equilibrium sorption capacity mg g <sup>-1</sup> .  $R_L$ , is a separation factor $C_o$ , maximum concentration at equilibrium.
	<u>Sub Eq.</u> $R_L = \frac{1}{1 + bC_0}$		
Freundlich	$q_e = K_f C_e^{\frac{1}{n}}$	$K_f$ , sorption capacity related to bond energy (mg g <sup>-1</sup> ) (L mg <sup>-1</sup> ) <sup>1/n</sup> . $n$ , sorption intensity.	$q_e$ , equilibrium adsorption capacity mg g <sup>-1</sup> . $C_e$ , equilibrium concentration mg L <sup>-1</sup> .
Temkin	$q_e = \frac{RT}{b_T} \ln (A_T C_e)$	$A_T$ , equilibrium binding constant. $b_T$ , Temkin constant.	$T$ , absolute temperature K. $R$ , universal gas constant, 8.314 J mol <sup>-1</sup> K <sup>-1</sup> .  $B$ , constant related to heat of adsorption J mol <sup>-1</sup> .
	<u>Sub Eq.</u> $B = RT/b_T$		
D-R	$q_e = q_m \exp (-K\varepsilon^2)$  <u>Where;</u>	$K$ , D-R constant mol <sup>-2</sup> K <sup>-1</sup> J <sup>-2</sup> . $q_m$ , monolayer sorption capacity mg g <sup>-1</sup> .	$C_e$ , equilibrium concentration mg L <sup>-1</sup> . $T$ , absolute temperature K. $R$ , universal gas constant, 8.314 J mol <sup>-1</sup> K <sup>-1</sup> .

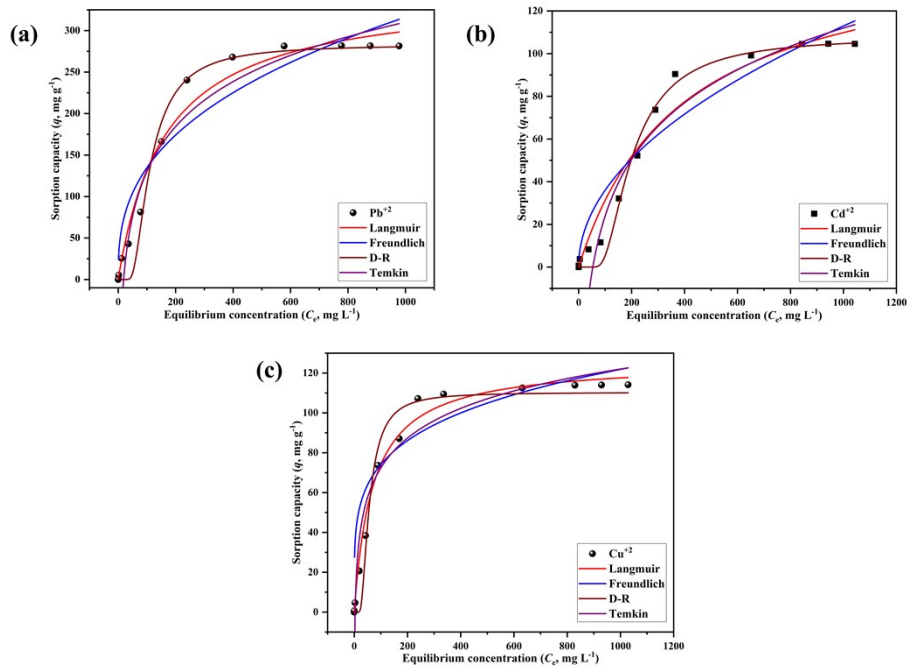
	$\varepsilon = RT * \ln \left( 1 + \frac{1}{C_e} \right)$		$E$ , mean free energy kJ mol <sup>-1</sup> .
	<u>Sub Eq.</u> $E = \frac{1}{(2K)^{\frac{1}{2}}}$		
<b>Kinetic models</b>			
Pseudo-first order	$q_t = q_e \left( 1 - e^{-k_1 t} \right)$	$q_e$ , equilibrium sorption capacity mg g <sup>-1</sup> . $k_1$ , pseudo-first-order rate constant min <sup>-1</sup> .	$q_t$ , sorption capacity at time 't' mg g <sup>-1</sup> .
Pseudo- second-order	$q_t = \frac{q_e^2 k_2 t}{1 + q_e k_2 t}$	$q_e$ , equilibrium sorption capacity mg g <sup>-1</sup> . $k_2$ , pseudo-second-order rate constant g mg <sup>-1</sup> min <sup>-1</sup> .	$q_t$ , sorption capacity at time 't' mg g <sup>-1</sup> .

**Table S2** Predicted breakthrough points from the constants of the BDST model for different influent concentrations ( $Q$ : 5 mL min<sup>-1</sup>,  $Z$ : 20 cm).

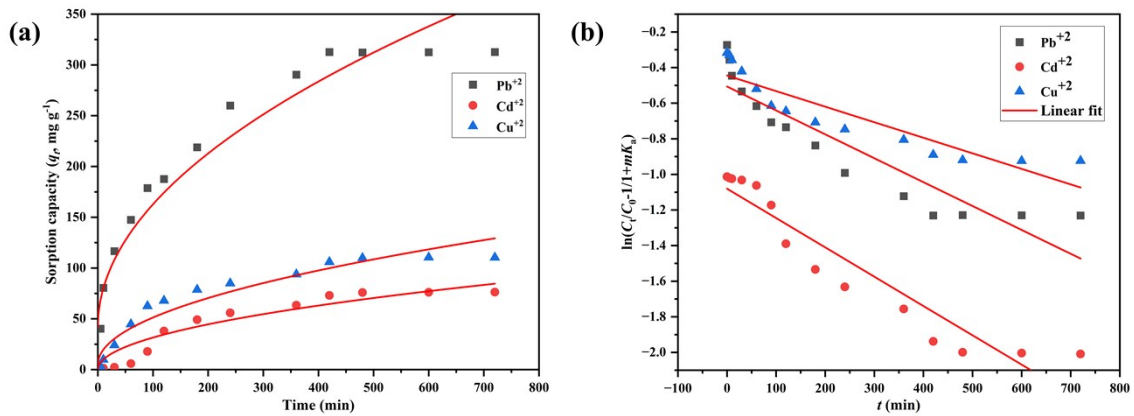
$C_i/C_0$	$a$ (min cm <sup>-1</sup> )	$b$ (min)	300 mg L <sup>-1</sup>				$E$ (%)
			$a'$ (min cm <sup>-1</sup> )	$b'$ (min)	$t_{\text{pred.}}$ (min)	$t_{\text{exp.}}$ (min)	
0.01	31	300	51.66	118.51	914.81	530	72.60
0.1	38	300	63.33	145.28	1121.38	1440	-22.12
0.5	60	270	100.00	229.39	1770.61	2400	-26.22
0.9	69	200	115.00	263.79	2036.20	3140	-35.15



**Fig. S1** Applicability of kinetic models for the sorption of (a) Pb<sup>2+</sup>, (b) Cd<sup>2+</sup>, and (c) Cu<sup>2+</sup> ions using Ca-MOF-CB.



**Fig. S2** Applicability of isotherm models for the sorption of (a) Pb<sup>2+</sup>, (b) Cd<sup>2+</sup>, and (c) Cu<sup>2+</sup> ions using Ca-MOF-CB.



**Fig. S3** Plots determining kinetic parameters of (a) intra-particle diffusion and (b) external film diffusion.

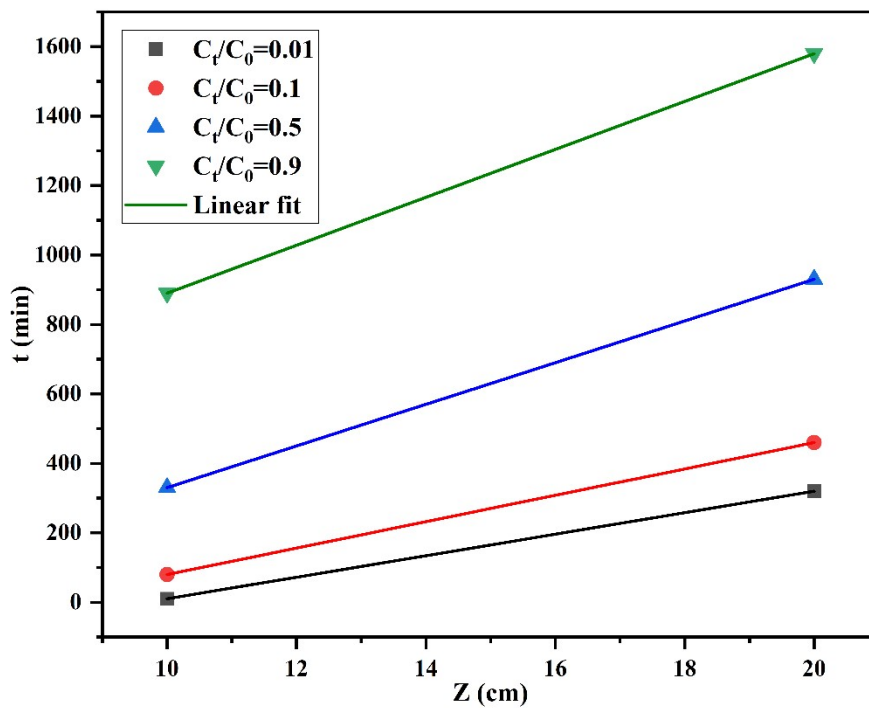


Fig. S4 Applicability of the BDST model to the experimental run.