Impact of NH₄OH treatment on the ion-exchange and pore characteristics of metakaolin-based geopolymer

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1. Variable-temperature ¹²⁹Xe spectra and fits



¹²⁹Xe spectra collected under various temperatures of four samples are shown in Fig. S1.

Figure S1. The ¹²⁹Xe spectra acquired under variable temperature of (a) N1, (b) N2, (c) N3 and (d) N4.

2. ¹²⁹Xe dynamic data and fits

The ¹²⁹Xe dynamic in site IP and BP were detected by measuring exchange rate (k), spin-lattice relaxation time (T_1) and spin-spin relaxation time (T_2). Selective-Inversion-Recovery (IR),¹ IR,² and Carr-Purcell-Meiboom-Gill (CPMG)³ experiments were performed to get these three values, respectively. All of these data were analysed according to the following theories in MATLAB R2017b (Mathworks, Natick, Massachusetts, United States of America).

Based on the previous studies, ^{1,4,5} when the exchange process takes place between two sites, IP and BP, the time dependence of their magnetizations under ¹²⁹Xe selective-IR experiment is given by,

$$\frac{\partial}{\partial t} \begin{pmatrix} M_{IP}(t) - M_{eq,IP} \\ M_{BP}(t) - M_{eq,BP} \end{pmatrix} = - \begin{pmatrix} R_{1,IP} + k_{IP-BP} & -\frac{M_{eq,IP}}{M_{eq,BP}} * k_{IP-BP} \\ -k_{IP-BP} & R_{1,BP} + \frac{M_{eq,IP}}{M_{eq,BP}} * k_{IP-BP} \end{pmatrix} \begin{pmatrix} M_{IP}(t) - M_{eq,IP} \\ M_{BP}(t) - M_{eq,BP} \end{pmatrix},$$
(S1)

where $M_{IP}(t)$ and $M_{BP}(t)$ are the magnetizations for two sites at time t, $M_{eq,IP}$ and $M_{eq,BP}$ are the equilibrium magnetizations, $R_{1,IP}$ and $R_{1,BP}$ are the spin-lattice relaxation rates ($1/T_1$) for two sites, k_{IP-BP} is the exchange rate between two sites.

Then our ¹²⁹Xe selective-IR data were fitted using the solution of Eq. S1, which is,

$$\binom{M_{IP}(t)}{M_{BP}(t)} = \binom{M_{eq,IP}}{M_{eq,BP}} + exp \left[-\binom{R_{1,IP} + k_{IP-BP}}{-k_{IP-BP}} - \frac{M_{eq,IP}}{M_{eq,BP}} * k_{IP-BP} + \frac{M_{eq,IP}}{M_{eq,BP}} * k_{IP-BP} \right] t \left[\binom{M_{IP}(0) - M_{eq,IP}}{M_{BP}(0) - M_{eq,BP}} \right],$$
(S2)

ere $M_{IP}(0)$ and $M_{BP}(0)$ are the magnetizations at t=0.

The ¹²⁹Xe *T*₁IR signals intensities of peak IP and BP were derived by Topspin software (Bruker, Rheinstetten, Germany) and then fitted by the following equation, respectively,

$$M(t) = M_{eq} * \left[1 - n * \exp\left(\frac{-t}{T_1}\right) \right], \tag{S3}$$

where M(t) is the magnetization at time t, M_{eq} are the magnetization at equilibrium-state, T_1 is the spin-lattice relaxation time and n is a free fitting parameter.

The fit equation for ¹²⁹Xe CPMG data is,

$$M(t) = M_{eq} * \exp\left(\frac{-t}{T_2}\right),\tag{S4}$$

where M(t) is the magnetization at time t, M_{eq} are the magnetization at equilibrium-state, T_2 is the spin-spin relaxation time.

The raw signals and fitted signals of three experiments are shown in Fig. S2. The detailed fit results of these signals are shown in Tables S1-3.



Figure S2. The raw signal (dots) and fitted signal (lines) of (a-c) 129 Xe selective IR, (d-f) T_1 IR and (g-i) CPMG experiments performed at room temperature of (a, d and g) N1, (b, e and h) N2 and (c, f and i) N3.

Table S1. The fit results of $^{\rm 129}{\rm Xe}$ selective-IR data.

SellR	M _{eq} (IP)	M _{eq} (BP)	<i>R</i> 1 (IP)	<i>R</i> ₁ (BP)	k _{IP-BP}	<i>M</i> ₀ (IP)	<i>M</i> ₀ (BP)	resnorm
N 1	0.99 ± 0.03	0.91 ±	1.33e-3 ±	1.39 ±	181.67 ± 30.81	-0.61 ±	0.63 ±	0.075
		0.03	4.79	5.25		0.03	0.03	
N 2	1.01 ± 0.03	0.73 ±	4.41e-3 ±	0.85 ±	239.77 ± 36.23	-0.49 ±	0.48 ±	0.037
		0.03	3.48	4.86		0.02	0.02	
N 3	1.02 ± 0.05	0.67 ±	4.84e-3 ±	0.87 ±	209.22 ± 40.75	-0.58 ±	0.45 ±	0.066
		0.04	3.57	5.46		0.03	0.03	

Table S2. The fit results of 129 Xe T_1 IR data.

<i>T</i> ₁IR	N 1		N	2	N 3	
	IP BP		IP	ВР	IP	BP
M _{eq}	1.01 ± 0.02	0.77 ± 0.02	1.06 ± 0.03	0.85 ± 0.04	1.07 ± 0.02	0.63 ± 0.02
<i>T</i> ₁ (s)	1.50 ± 0.04	1.60 ± 0.07	2.99 ± 0.10	3.18 ± 0.18	3.05 ± 0.07	3.15 ± 0.16
n	1.83 ± 0.02	1.70 ± 0.02	1.76 ± 0.02	1.71 ± 0.03	1.77 ± 0.02	1.67 ± 0.03
resnorm	0.004	0.005	0.003	0.006	0.002	0.002

Table S3. The fit results of $^{\rm 129}{\rm Xe}$ CPMG data.

CPMG	N 1		N	2	N 3	
	IP	BP	IP	BP	IP	BP
M _{eq}	1.11 ± 0.04	0.61 ± 0.05	1.10 ± 0.04	0.57 ± 0.03	1.12 ± 0.06	0.42 ± 0.05
T ₂ (ms)	3.20 ± 0.17	0.79 ± 0.08	2.88 ± 0.18	0.72 ± 0.04	2.89 ± 0.23	0.75 ± 0.10
resnorm	0.004	0.001	0.005	4e-4	0.009	0.001

3. ¹H cryoporometry data and fits

The signal intensity at each temperature step (S(X)) is dependent on the inverse temperature, X=1000/T. Their relationship agrees with the following equation,⁶

$$S(X) = \sum_{i=1}^{n} \frac{S_{0i}}{2} \left[1 - \operatorname{erf}\left\{ \frac{X - X_{ci}}{\sqrt{2}\sigma_i} \right\} \right],$$
(S5)

where *n* is the number of phase transitions, S_{0i} , X_{ci} and σ_i are the signal intensity, the inverse transition temperature and the width of the temperature distribution curve of phase *i*, respectively.

Our signal intensity data as a function of X are shown in Fig. S3. The data were fitted with Eq. S5, assumed with containing three components (n=3), S, B and V, by using CFTOOL installed in MATLAB R2017b (Mathworks, Natick, Massachusetts, United States of America). The detailed fit results are shown in Tab. S5.



Figure S3. The raw (dots) signal intensity at each temperature step and the fitted (lines) signal intensity as a function of 1000/Temperature of (a) N1, (b) N2, (c) N3 and (d) N4.

Table S4. Fit results of cryoporometry data.

		S ₀ /2	X _c	ν2σ	R ²
N1	S	0.15 ± 0.03	3.78 ± 0.01	0.09 ± 0.02	0.9997
	В	0.09 ± 0.25	3.50 ± 1.64	0.91 ± 0.73	
	ВР	0.31 ± 0.02	3.67 ± 1e12	0.003 ± 3e12	
N2	S	0.15 ± 0.04	3.79 ± 0.01	0.09 ± 0.03	0.9983
	В	0.07 ± 0.17	3.88 ± 1.45	0.73 ± 0.83	
	ВР	0.29 ± 0.01	3.67 ± 1e12	0.002 ± 7e12	
N3	S	0.15 ± 0.04	3.79 ± 0.02	0.09 ± 0.03	0.9983
	В	0.07 ± 0.16	3.89 ± 1.41	0.73 ± 0.81	
	ВР	0.29 ± 0.02	3.67 ± 4e11	0.006 ± 2e12	
N4	S	0.15 ± 0.04	3.79 ± 0.01	0.09 ± 0.03	0.9997
	В	0.07 ± 0.16	3.89 ± 1.40	0.73 ± 0.81	
	BP	0.29 ± 0.02	3.67 ± 2e12	0.0005 ± 7e12	

By plugging the fitted $S_0/2$, X_c and $\sqrt{2\sigma}$ into the following equation, the pore size distribution dS/da as a function of a were obtained,

$$\frac{dS}{da} = \frac{10^{3}k}{\sqrt{2\pi} (aT_{melting} - k)^{2}} \sum_{i=1}^{n} \frac{S_{0i}}{\sigma_{i}} \times \left[-\left\{ \frac{10^{3}a - X_{ci} (aT_{melting} - k)}{\sqrt{2}\sigma_{i} (aT_{melting} - k)} \right\}^{2} \right],$$
(S6)

where T_{melting} is the melting temperature of bulk water, which is 273 K in our cases, k is a constant, 89 K*nm is used here. The k has the same value as our pervious geopolymer sample⁷ we used to evaluate the K_0 in Section S3, and it also agrees with the k value used for silica gel from one study.⁸

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